



# Multivariable feedback control of radiative loss-processes using multi-spectral imaging

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\*See author list of S. Coda et al. 2019 Nucl. Fusion 59 112023



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## EUROfusion roadmap mission-2: Heat-exhaust systems

- capable of withstanding the large heat and particle fluxes of a fusion power plant;
- allow as high performance as possible from the core plasma.

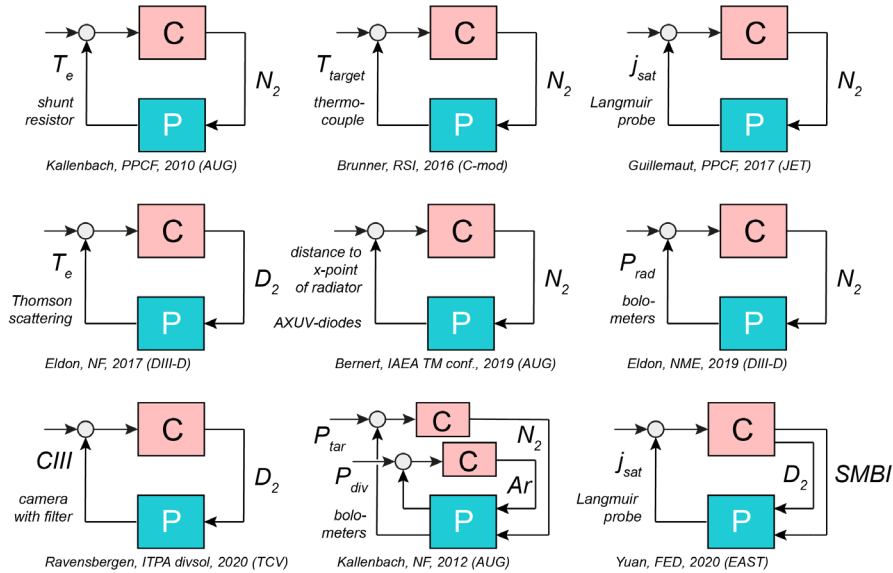
Foreseen to be achieved by producing ‘detached’ divertor conditions, maintained by an active control system.

Inherently a multi-input multi-output problem (multiple performance parameters and multiple actuators).

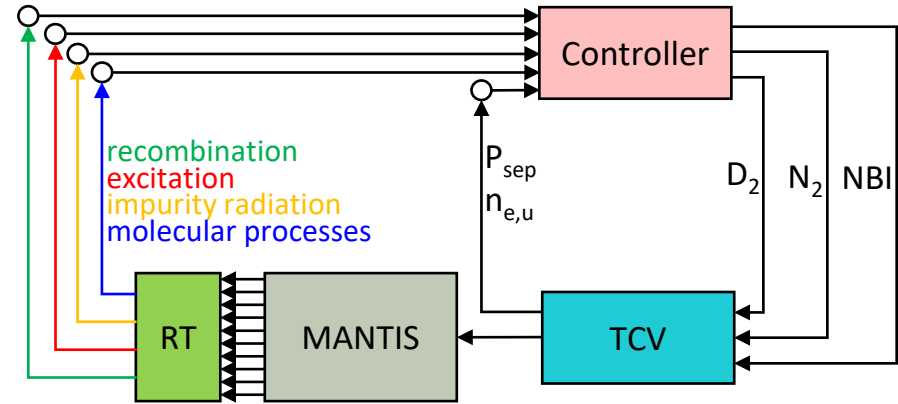
# Introduction



## Single-input single-output (SISO)



## Multiple-input multiple-output (MIMO)



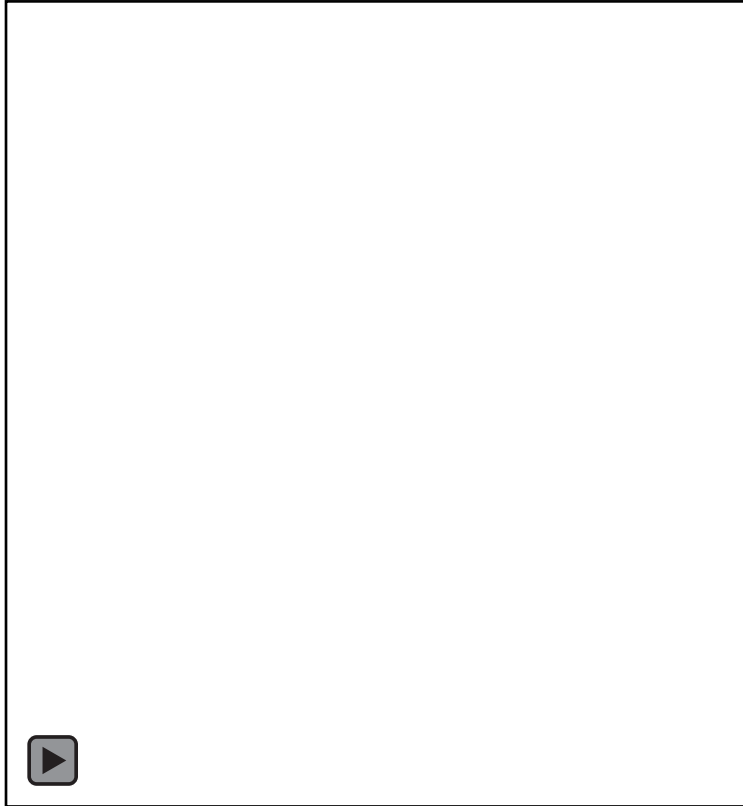
# Introduction



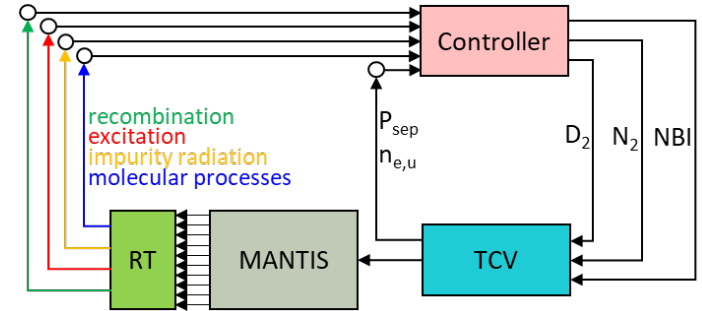
A. Perek et al., Rev. Sci. Instrum. **90**, 123514 (2019)



TCV view of divertor



## Multiple-input multiple-output (MIMO)



Other possible diagnostics for control (not RT-ready): DSS (spectroscopy), **RadCam (Soft-X, Bolometer, AXUV)**, Thomson, MANTISIIa, MANTISIIb mid/top-port views

# Introduction



MIMO control: Interaction is key

- Actuators affect multiple outputs

Stacking SISO controllers will lead to

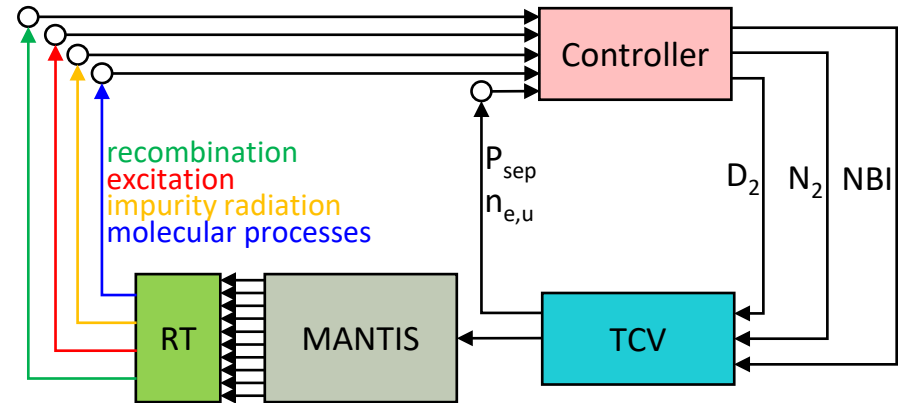
- other behavior than based on the individual SISO controllers

- extreme case: instability

Requires interaction analysis and MIMO controller design techniques

See: Skogestad and Postlethwaite.

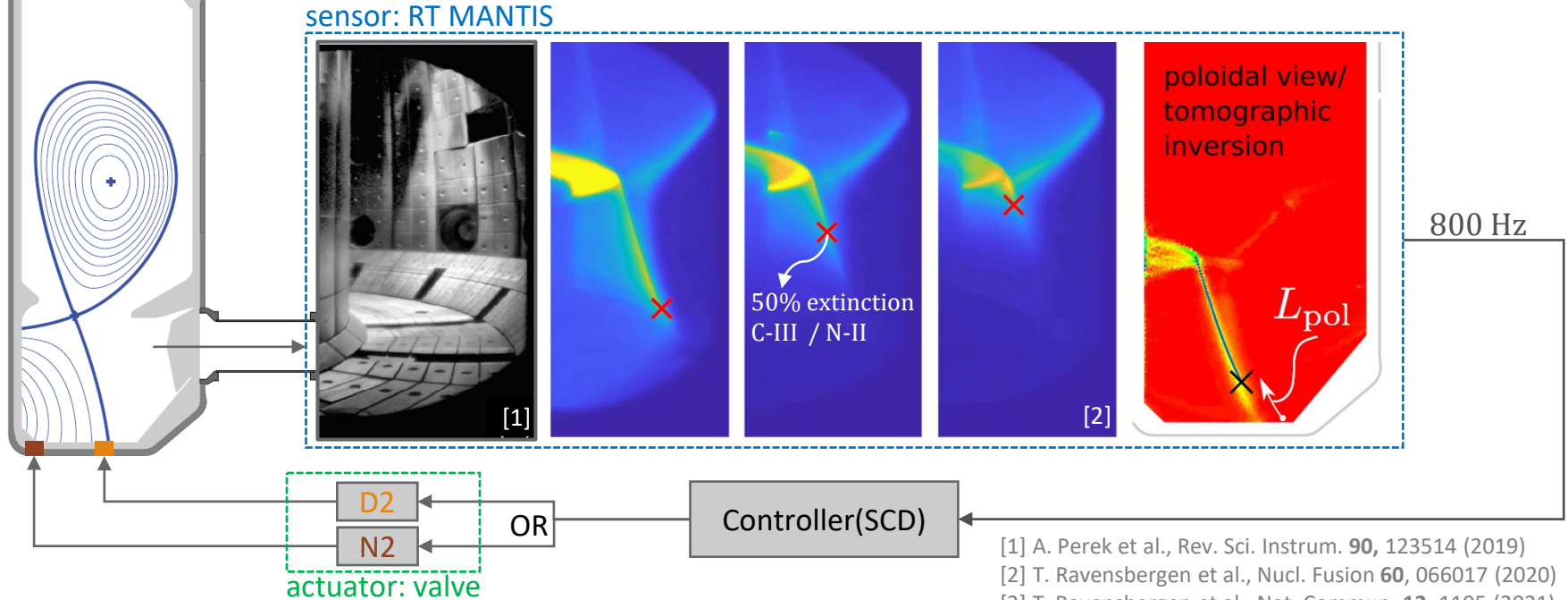
Multivariable Feedback Control, Analysis and Design (2007)



# Introduction



- Real-time detection of emission fronts with multi-spectral imaging (MANTIS)
- Impurity emission fronts (C-III, N-II) strongly related to local temperature
- Actuation of front position by D2 fueling or N2 seeding



- [1] A. Perek et al., Rev. Sci. Instrum. **90**, 123514 (2019)  
[2] T. Ravensbergen et al., Nucl. Fusion **60**, 066017 (2020)  
[3] T. Ravensbergen et al., Nat. Commun. **12**, 1105 (2021)  
[4] J.T.W. Koenders et al., 47th EPS on Plasma Physics, P1.1058



## Main goal: setting up for MIMO control with different MANTIS camera's

Delayed: main (full-time) person is missing and will start 1st March!

- **RT-image processing (based on past experiments):** Improve and make current algorithms real-time (not in the control system yet) for nitrogen and Balmer lines to determine recombination and excitation regions.
- **Qualitative RT-image processing:** Qualitative real-time algorithms for the observation of nitrogen, recombination and excitation (ionization) based on camera images only (based on ~ 5 cameras).

Hence, shifted focus to:

- **Simple-MIMO identification demonstration:** Demonstrate MIMO system identification algorithms developed in this proposal for the simplified case of D2 and N2. (initial testing RT-*alg.*)

Ongoing process:

- **Selection of control targets:** Scenario selection and determination on control targets is performed, ongoing process.
- **Integration DCS:** Integration of algorithms into the digital control system TCV and verify real-time algorithms.

# ENR WPs overview and progress



**Main goal: setting up for MIMO control (P6) with different MANTIS camera's**

Progress	Project
P1	MANTIS development to determine loss-processes in 2D
P2	Detachment analysis, scenario selection, setting control requirements
P3	Conversion from off-line to real-time camera analysis (incl. machine learning)
P4	MIMO system identification
P5	Dynamic modelling for MIMO-control
P6	MIMO feed-back control (and integration)

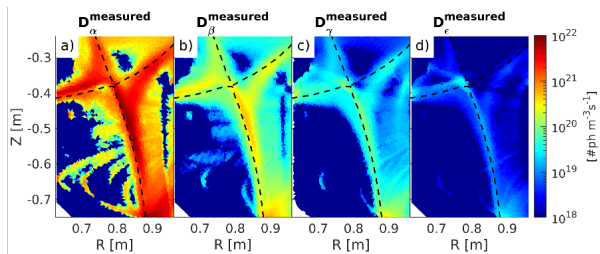


# WP1 – Determine loss-processes in 2D



## Spectroscopic emissivity analysis

Emissivity of 4 Deuterium lines



ADAS Collisional-Radiative model

Hydrogen Analysis

$n_e, T_e, n_0, I_{rate}, R_{rate}, CX_{rate}, P_{exc}, P_{rec}$

$$B_{n \rightarrow 2} = n_e^2 PEC_{n \rightarrow 2}^{rec}(n_e, T_e) + n_e n_0 PEC_{n \rightarrow 2}^{exc}(n_e, T_e)$$

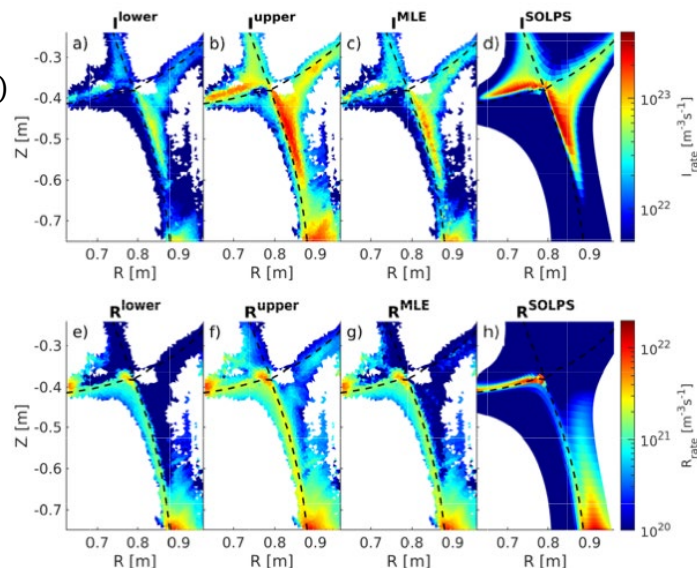
$$P_{n \rightarrow 2}(n_e, T_e, n_0) \propto e^{-\left(\frac{B_{n \rightarrow 2}^{model} - B_{n \rightarrow 2}^{measured}}{B_{n \rightarrow 2}^{err}}\right)^2}$$

Probability that multiple measured lines are observed:

$$P(n_e, T_e, n_0) = P_{3 \rightarrow 2} P_{4 \rightarrow 2} P_{5 \rightarrow 2}$$

$$P(n_e, T_e, n_0) \rightarrow P(I_{rate}), P(R_{rate})$$

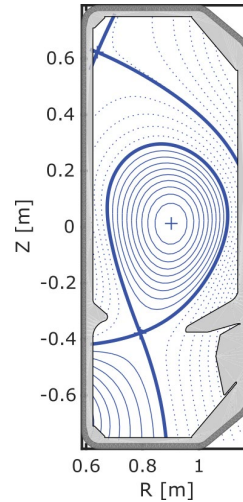
A. Perek et al. A spectroscopic inference and SOLPS-ITER comparison of flux-resolved edge plasma parameters in detachment experiments on TCV, submitted to Nuclear Fusion.





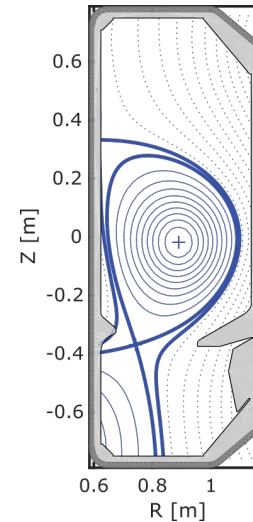
- L-mode

- PEX 250kA
- PEX 320 kA



- H-mode

- Small-Elms, 1MW NBH (+ ECRH later)
- Elmy 170kA, 1.3MW NBH (+ ECRH later)
- Elmy 170kA, 1.3MW NBH (+ ECRH later)



- Possible extension to more complex shapes / higher  $I_{\text{plasma}}$



- Actuators
    - Gas fueling and/or impurity seeding with weakly ( $N_2$ ) and strongly (Ne, Ar, ..) recycling species
    - Input power (NBH, possibly ECRH)
  - Performance variables
    - Neutral compression (baffles)
    - Location of CIII/NII impurity emission front (inter-Elm)
    - Ionization / recombination in the divertor
    - Upstream conditions, e.g.  $\langle n_e \rangle$ ,  $P_{\text{seperatrix}}$
- Ideally go for robust control approach (weight functions)



## Simultaneous (MIMO) control upstream density and detachment

- detachment control (using MANTIS)
- upstream density control (more complicated no direct sensor)
  - using FIR in observer to determine density profile (upstream density)
  - model based synthesis of upstream density control

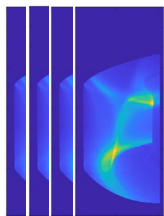
Addressing this:

- dynamics multiple valves with both core and exhaust tasks
- observer development (RAPTOR-RAPDENS) to RT-reconstruct density profile (together with RT-04 Thomas Bosman, Federico Felici)

# WP3 – Conversion to RT (neural networks)

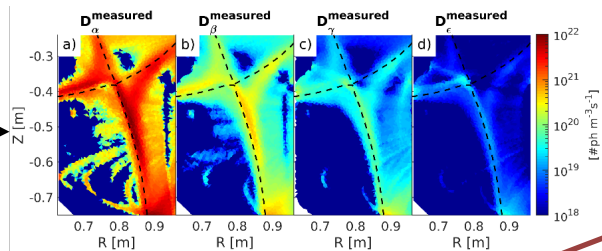


Filtered camera images of  
the Balmer line emission



Tomographic  
inversion  
~10s per  
frame per  
camera

Emissivity of the Balmer series



Bayesian inference  
using ADAS model  
~5000s per frame

Those two steps combined must be speed up by at least 6 orders of magnitude for real-time use. This will be attempted using Machine Learning:

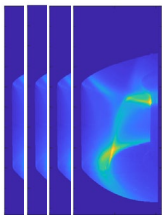
- Tomographic inversion — proposal submitted for Marconi.
- Bayesian inference — convolutional neural networks.

$n_e, T_e, n_o, I_{rate}, R_{rate}, CX_{rate}, P_{exc}, P_{rec}$

# WP3 – Conversion to RT (neural networks)

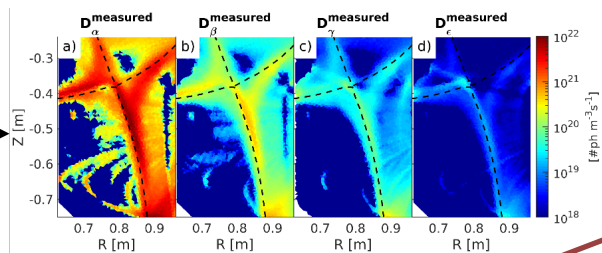


Filtered camera images of the Balmer line emission



Tomographic inversion  
~10s per frame per camera

Emissivity of the Balmer series



Bayesian inference using ADAS model  
~5000s per frame

Approximation of the electron temperature using convolutional neural networks and the ADAS model

$n_e, T_e, n_o, I_{rate}, R_{rate}, CX_{rate}, P_{exc}, P_{rec}$

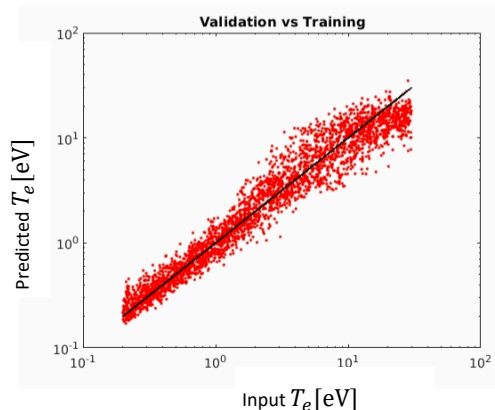
3000 samples of random combinations of plasma parameters within the ranges below were used to generate training and validation Balmer line emissivities using the ADAS model.

10% noise was added.

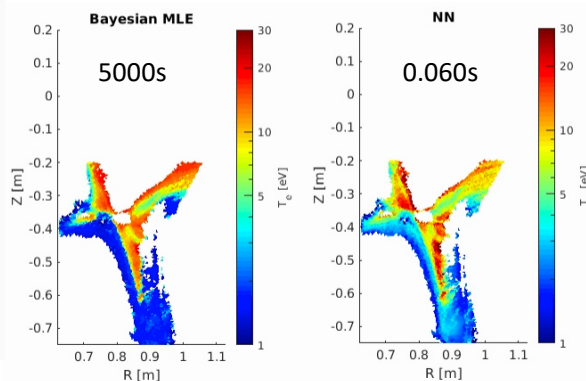
$$T_e = (0.2, 30)[eV]$$

$$n_e = (5e18, 2e20)[m^{-3}]$$

$$n_o = (5e16, 5e18)[m^{-3}]$$



Application to the experimental data





MIMO control: system identification experiment with periodic perturbation. Design controller on resulting FRF Matrix.

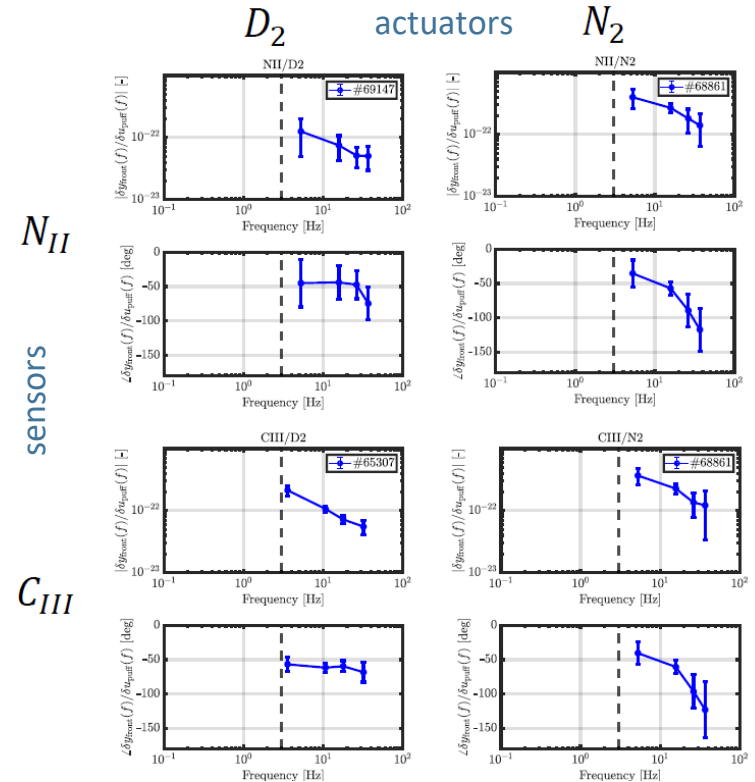
Filling the matrix with SISO identification:

- Requires (at least) 1 experiment per actuator

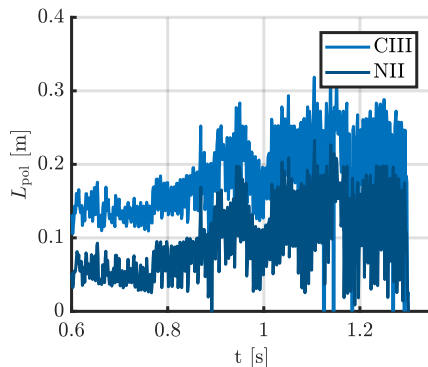
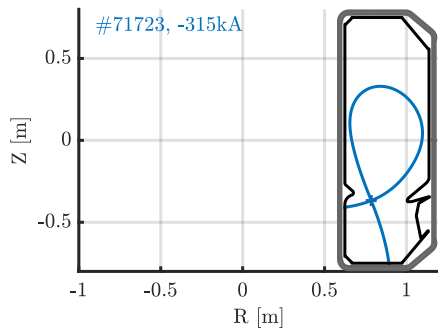
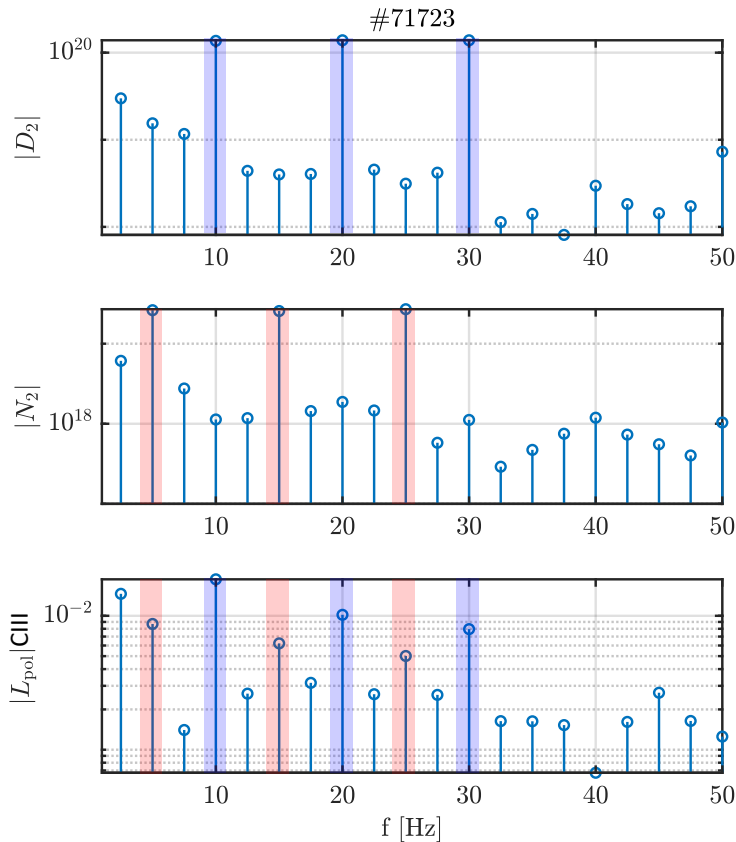
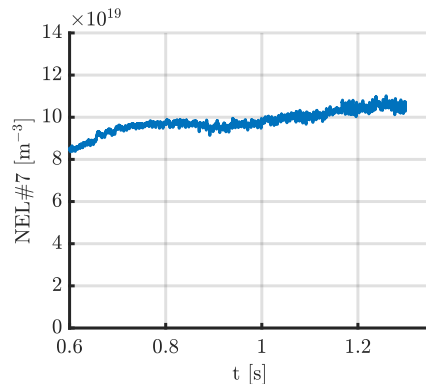
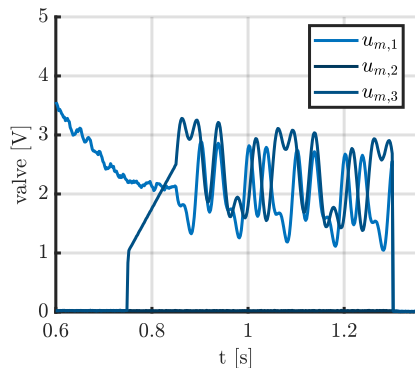
Filling the matrix with tailored MIMO identification:

- Requires only 1 experiment in total
  - Note, trade-off in quality is present

Multiple-input multiple-output (MIMO)



# WP4 – MIMO System Identification

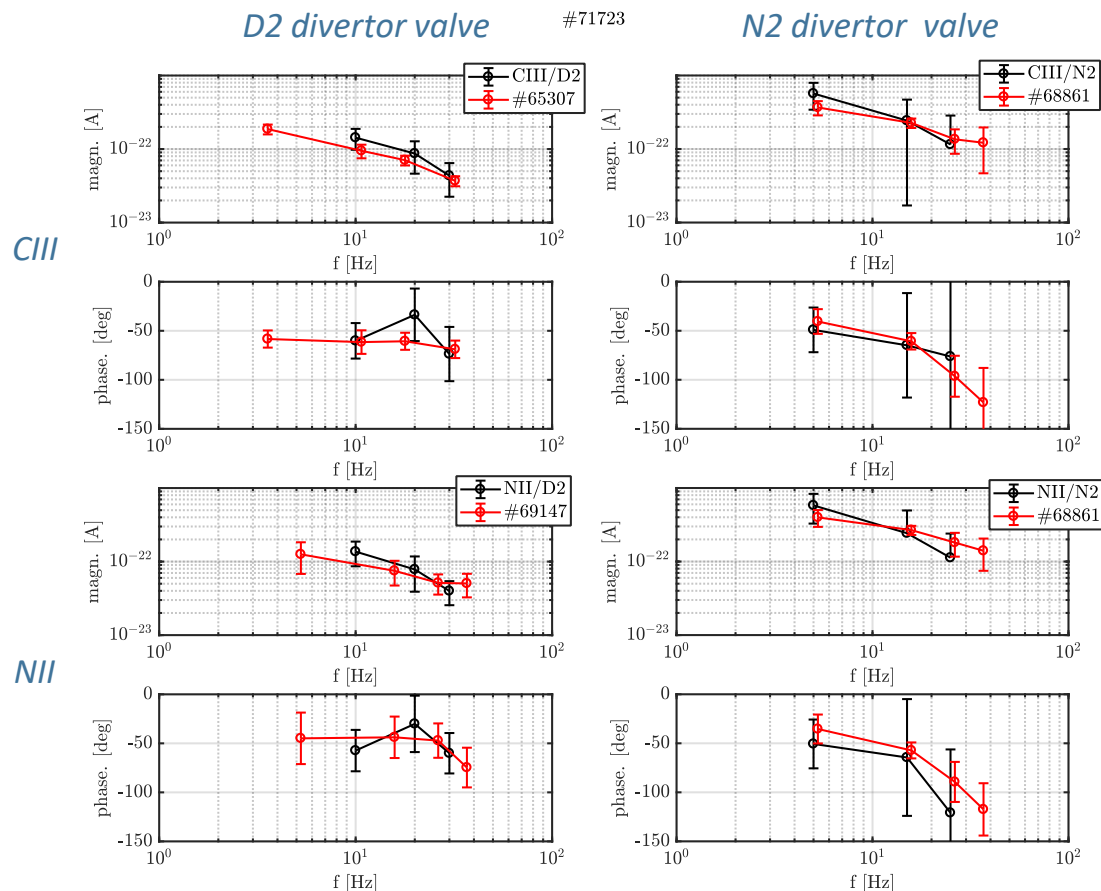




# WP4 – MIMO System Identification



- First results of MIMO system identification experiments
- 2x3 5 Hz zippered multisine
- ML in agreement with previous SISO results (red), but trade-off of single experiment means larger uncertainties
- Next step: continue analysis of interaction and actuator / sensor directions + start investigation of MIMO controller design



# WP5 – Dynamic modelling for control (+ENR-SW)

A one dimensional code to model divertor plasma dynamics from X-point to divertor target

## Basic equations [1,2,3]

- particle balance

$$\frac{\partial n}{\partial t} = -\frac{\partial}{\partial x}\Gamma_n + S_n, \quad \Gamma_n = nv_{\parallel}$$

- momentum balance

$$\frac{\partial nmv_{\parallel}}{\partial t} = -\frac{\partial}{\partial x}(nmv_{\parallel}^2 + p) + S_{\text{mom}},$$

- energy balance

$$\frac{\partial 3neT}{\partial t} = -\frac{\partial}{\partial x}q_{\parallel} + v\frac{\partial}{\partial x}p + Q,$$

$$q_{\parallel} = 5neTv_{\parallel} - \kappa_{\parallel}\frac{\partial T}{\partial x},$$

- neutral particle balance

$$\frac{\partial n_n}{\partial t} = \frac{\partial}{\partial x}D\frac{\partial}{\partial x}n_n - S_n,$$

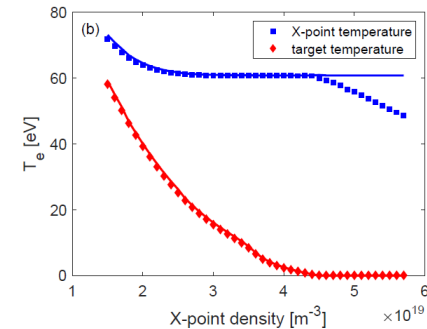
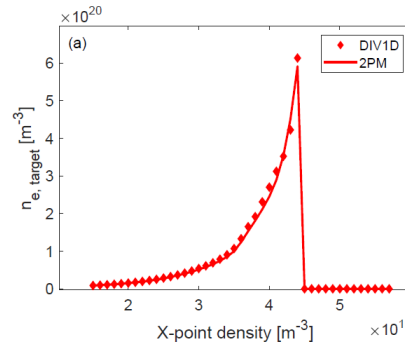
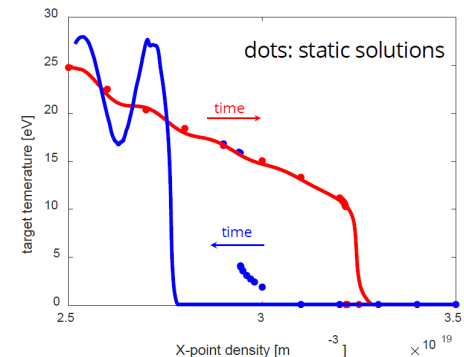


Figure 1: Results of an X-point density scan with a 1% Carbon impurity fraction. (a) Target density (diamonds) as a function of X-point density. (b) X-point (squares) and target (diamonds) temperatures. Corresponding results of the two-point model are shown as full lines.

## Bifurcation in dynamic simulations of X-point density ramp-up and ramp-down

- 5% Carbon
- 10 ms density ramp @  $\pm 10^{21} \text{ m}^{-3}$

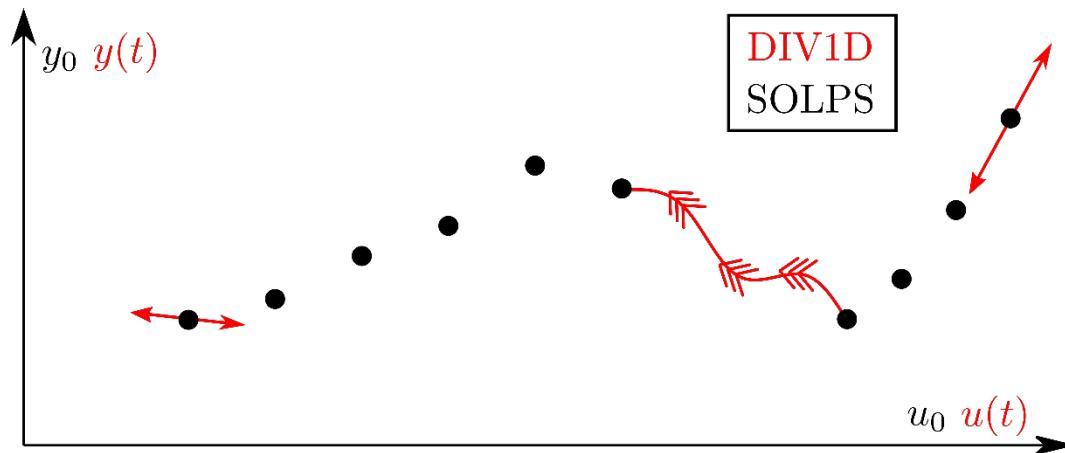


# WP5 – Dynamic modelling for control



- Complementing SOLPS with DIV1D:
  - Fit on SOLPS
  - Transition between points
  - Describe Measured Dynamics

- Requires Methods
  - F: mapping 2D to 1D
  - H: DIV1D input policy



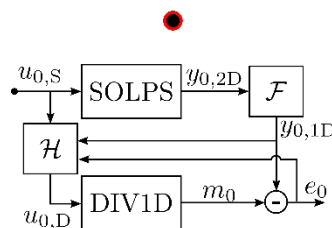
- State of Validation DIV1D
  - Reasonable agreement
  - Sensitive in density ramp (WIP)
  - Dynamics are too fast for control

- Outlook

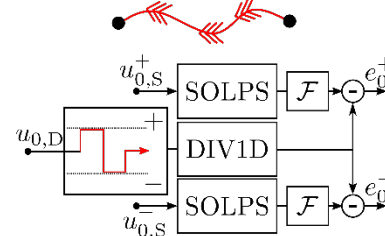
DIV1D → semi-heuristic transfer function models



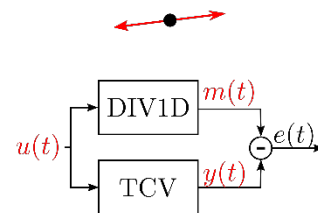
(1) Static Fit on SOLPS



(2) Transition Between SOLPS

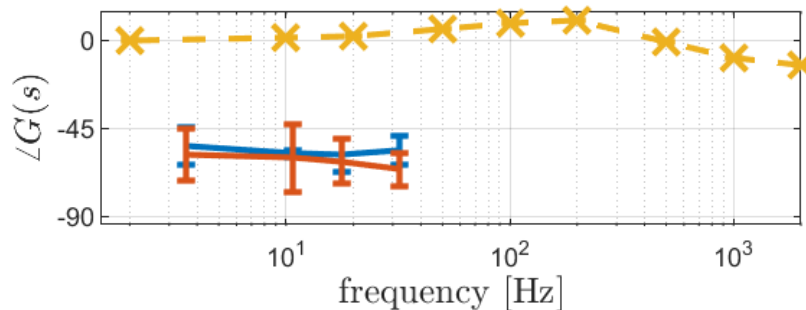
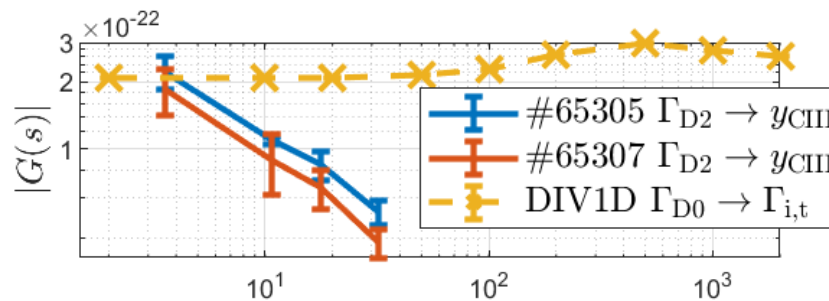
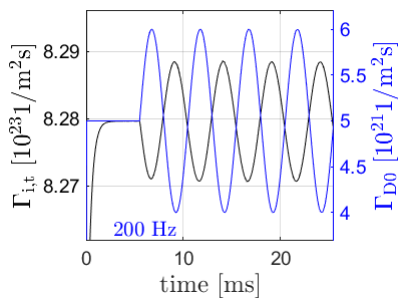
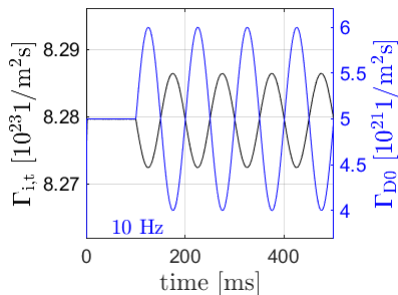


(3) Local Dynamics





(3) Local Dynamics





## Made deliverables:

- **Simple-MIMO identification demonstration:** Demonstrate MIMO system identification algorithms developed in this proposal for the simplified case of D2 and N2. (initial testing RT-alg.).

## Intermediate conclusion:

- Strong coupling between (NII/CIII) fronts necessitates MIMO-control (multiple valves) but limits independent control

## Next year:

Main (full-time) person is missing and will start 1<sup>st</sup> of march:

- **RT-image processing (based on past experiments):** Improve and make current algorithms real-time (not in the control system yet) for nitrogen and Balmer lines to determine recombination and excitation regions.
- **Qualitative RT-image processing:** Qualitative real-time algorithms for the observation of nitrogen, recombination and excitation (ionization) based on camera images only (based on ~ 5 cameras).

Ongoing process:

- **Selection of control targets:** Scenario selection and determination on control targets is performed, ongoing process.
- **Integration DCS:** Integration of algorithms into the digital control system TCV and verify real-time algorithms.

## First MIMO control experiments!



**DIFFER**

**EPFL**



University of  
**Strathclyde**  
Glasgow

**TU/e**