



Max-Planck-Institut
für Plasmaphysik

Effects of distribution functions in global gyrokinetic simulations of energetic particle driven Alfvénic and EGAM instabilities in ITER and ASDEX Upgrade

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EUROfusion

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Numerical model: the ORB5 Code
Background distribution functions

ASDEX Upgrade “NLED-AUG”

ITER 15MA scenario

ITER PFPO scenario (101006)

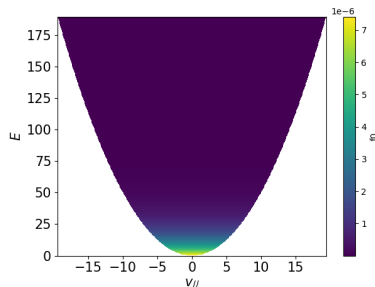
“ORB5: a global electromagnetic gyrokinetic code using the PIC approach in toroidal geometry”

- ▶ Filter applied in toroidal and poloidal mode numbers
 - ▶ $m(r) = nq(r) \pm \Delta m$
- ▶ Effectively mitigates with the so-called cancellation problem using the pullback scheme [Mishchenko 2019]
- ▶ These EM results all with kinetic (some w/ reduced mass ratio) electrons, (ES with adiabatic)
- ▶ Gyrokinetic or drift-kinetic ions (here: bulk gyro-, EPs drift- kinetic)
- ▶ Previously used for turbulence studies as well as EP physics
- ▶ International AE benchmarking activities:
 - ▶ e.g.: ITPA-TAE benchmark, DIII-D RSAE/TAE benchmark
 - ▶ benchmarking activities used local Maxwellian for EPs

¹for details, see Lanti+ CPC 2020

$$F_{0,f,Max.} = \frac{n_f(r)}{(2\pi v_{th}^2(r))^{3/2}} \exp(-E/v_{th}^2) \exp\left(-\frac{u_{||}}{2} (u_{||} - 2v_{||})/v_{th}^2\right)$$

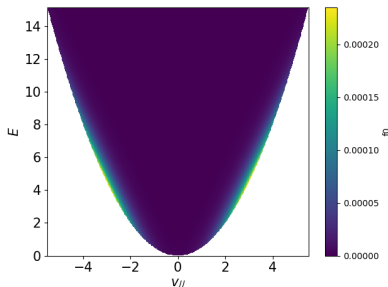
in absence of shift ($u_{||} \rightarrow 0$), reduces to function of Energy, radius



$$F_{0,f,\text{BoT}} = C \cdot n_f(r) \exp(-E \cdot m_f / T_f) \exp(-v_{\parallel,f}^2 / (2 T_f)) \cosh(v_{\parallel} v_{\parallel,f} / T_f)$$

function of Energy, radius, v_{\parallel}

- ▶ “Toy” distribution function with strong anisotropy (ideal to study EGAMs)
- ▶ Originally zero radial dependence, since extended to include $n(r)$



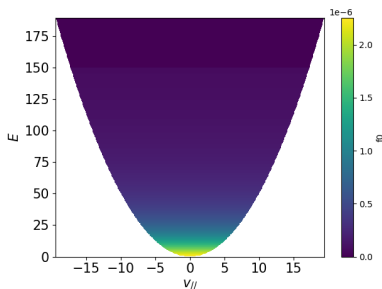
²Original version implemented for [Zarzoso+, NF, 2014], based on GYSELA work

$$F_{0,f,SD} = \frac{3n_f(r)}{4\pi} \frac{\Theta(v_0 - |v|)}{(v_c(r))^3 + |v|^3 \ln(1 + v_0/v_c(r))}$$

also function of Energy ($|v|$), radius

- ▶ Decent approximation for alpha particles

Apply to ITER 15MA scenario,
previously studied with Maxwellian
in [Hayward-Schneider+, NF2021]



³Vannini+, thesis+paper 2021+

$$F_{0,f,ASD} = F_{0,f,SD}(r, E) \cdot C \exp\left(-(\xi - \xi_0)^2 / (2\Delta\xi^2)\right)$$

where $\xi = v_{\parallel} / |v|$, \rightarrow function of Energy, radius, and parallel velocity

Semi-analytical: F_0 analytic, but compute $\partial F_0 / \partial X$ numerically

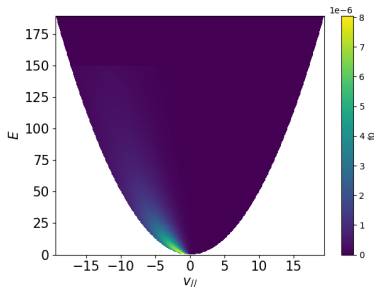
- Reasonable (parameterizable) approximation for NBI

Apply to NBI driven AEs and

EGAMs in ASDEX Upgrade

Apply to NBI driven AEs in ITER

PFPO



⁴Rettino+, paper 2021+

In principle, arbitrary function $F_0(r, v_{\parallel}, E)$ also now treated fully numerically in ORB5.

We “**just**” require F_0 on a mesh.

- ▶ To date, we can read in one of the previous analytical expressions, but also coupled to RABBIT.
- ▶ Work ongoing to couple to, e.g. ASTRA NBI module via IMAS

- ▶ RABBIT [Weiland+, NF, 2018+19]
 - ▶ real-time capable NBI code
- ▶ Describes NBI distribution function in experiment
- ▶ Non-Monte-Carlo method gives smooth function, good for derivatives
- ▶ We use RABBIT for ASDEX Upgrade (AUG) NBI F_0 (e.g. shot #31213 (NLED-AUG)) in the time-independent mode
- ▶ Coordinate mapping performed between RABBIT and ORB5

$$f_{-}(|v|, \xi) = \frac{1}{2\pi} \frac{\tau_s}{v^3 + v_c^3} \cdot \sum_{l=0}^{\infty} \left(l + \frac{1}{2} \right) P_l(\xi) S_l \cdot \left(\frac{v_0^3 + v_c^3}{v^3 + v_c^3} \frac{v^3}{v_0^3} \right)^{\frac{\beta}{3} l(l+1)}$$

$$\xi = v_{\parallel} / v$$

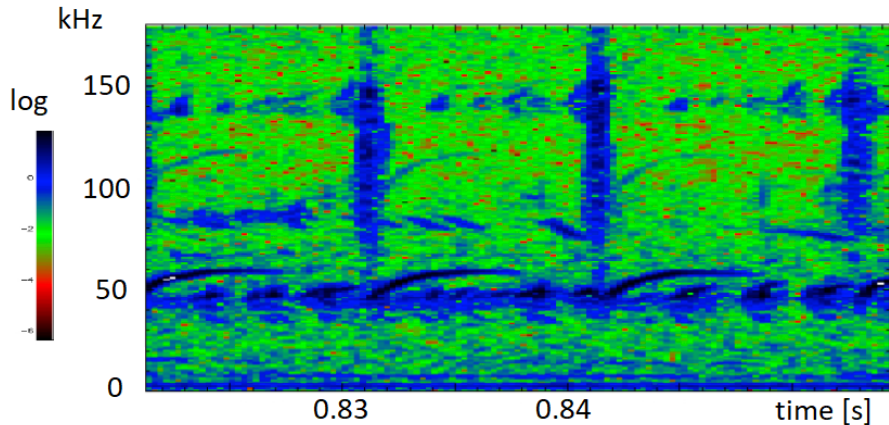
ASDEX Upgrade case with large EP to bulk plasma β ratio

- ▶ Off-axis NBI, NBI angle scan performed
- ▶ Bursts of TAEs/EPMs and EGAMs observed
- ▶ Previous works [Novikau, Di Siena, Vannini, Vlad, ...] modelled this case
 - ▶ EGAMs (bump on tail), TAE/EPM (Maxwellian), interaction of EGAMs & EPMs (bump on tail)
- ▶ Starting to become more realistic:
 - ▶ TAE/EPM with isotropic slowing down
 - ▶ EGAM with anisotropic slowing down
 - ▶ EGAM with RABBIT NBI

⁵Lauber+, IAEA FEC 2018

"NLED-AUG": ASDEX Upgrade #31213

TAE \rightarrow EGAM bursts observed in experiment

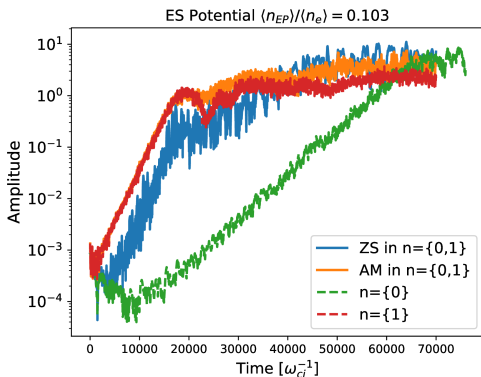


Interaction of EPM & EGAM⁶

$n=0$ & $n=1$ different from $n=\{0,1\}$

- ▶ High EP density, $n = 0$ enhanced
- ▶ Low EP density, $n = 1$ enhanced

$n=1$ mode also studied with isotropic slowing down⁷



high-EP density

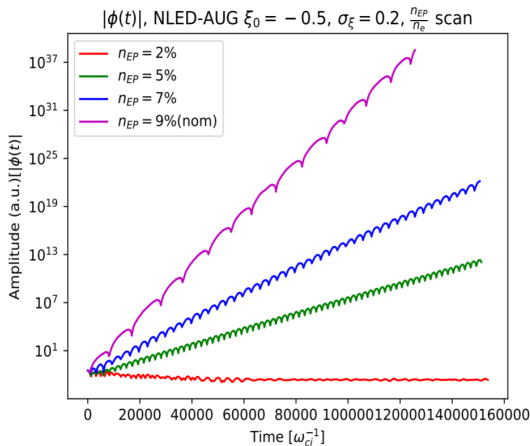
⁶Details in Vannini+ PoP 2021

⁷Vannini+ 2021+

Study with ES Simulations of
 $n=0$ EGAM⁸

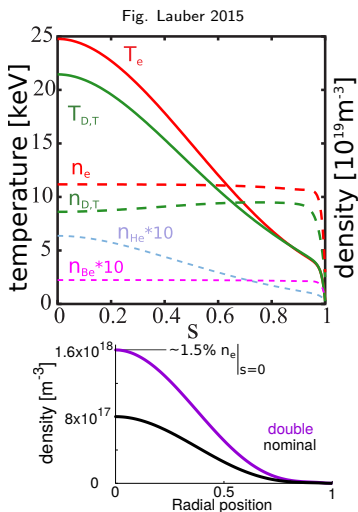
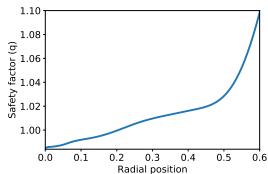
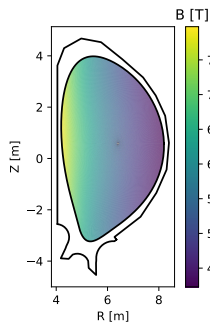
- ▶ Anisotropic slowing down
- ▶ RABBIT NBI distribution⁸

EM simulations with $n=1$
EPM also underway



Anisotropic slowing down driven EGAM

⁸Rettino+ 2021+



⁹Polevoi+ 2002; ITPA; similar to IMAS #131018 (slightly different q -profile)

Simplifying the problem

- ▶ Remove density/temperature pedestal gradients
- ▶ Fast ions: 3.5MeV **Slowing down** & 900keV Maxwellian
- ▶ Neglect impurity species (He, Be)
- ▶ Hybrid isotope: 50% ^2D + 50% ^3T \rightarrow 100% $^{2.5}\text{DT}$
- ▶ Increase electron mass: m_i/m_e : 4550 \rightarrow 200
- ▶ Neglect gyroaverage in fast ions
- ▶ Double EP density

All the isotope effects & m_e studied separately, not reported here

Summary of previous results

Summary of Hayward-Schneider+ NF 2021, EPPI 2019, ...

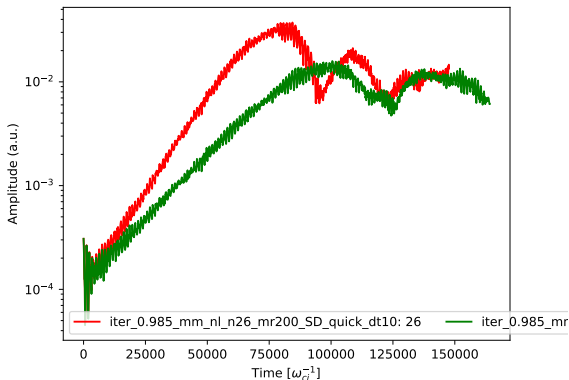
- ▶ low- n (e.g. 12) TAEs have radially global mode structures
- ▶ w/o EP FLR, γ peak around $n = 30$
- ▶ w/ EP FLR, γ for $n > 20$ reduced \rightarrow peak $20 < n < 25$
- ▶ Single modes cause negligible EP redistribution
- ▶ Multi (e.g. [20...30]) modes cause significant EP redistribution¹⁰
 - ▶ Subdominant edge TAEs nonlinear dominant
- ▶ Effects of Zonal physics as-yet unstudied

¹⁰At double EP density

Slowing down

Replacing 900 keV
Maxwellian with more
realistic 3.5 MeV isotropic
slowing down

TAE drive increased



(low resolution runs)

Slowing down

$n=26$

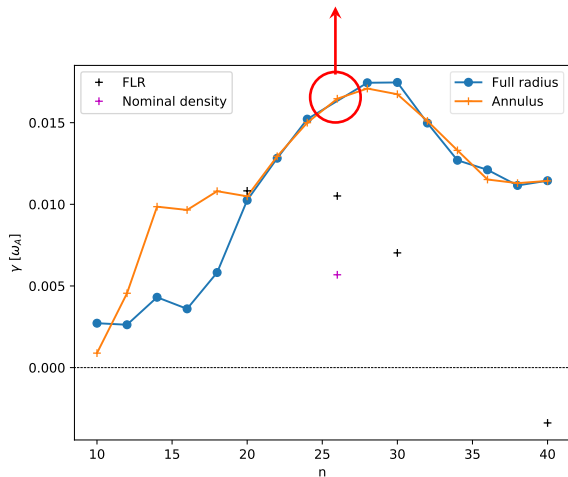
$\gamma = 0.0218 \omega_A$

(high resolution run)

c.f. $\approx 0.016 \omega_A$ for
Maxwellian

Previous Maxwellian
underestimated growth
rate.

Next: realistic
distribution \rightarrow nominal
density + EP FLR



Black: with EP FLR (bulk ion FLR always kept)

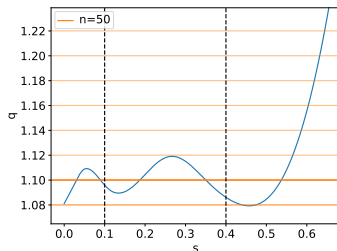
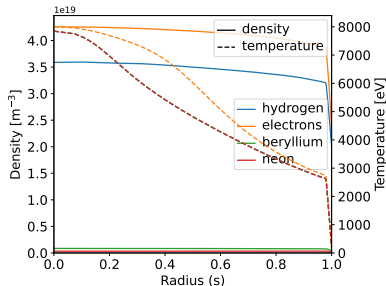
Pre-fusion-power-operation
(PFPO).

Half current.

Half field.

ITER wants to know:

- ▶ Will (NBI) EPs drive AEs unstable?
- ▶ If so: enough EP transport to need to take action?



¹¹Polevoi+ 2021; ITPA B.11.12

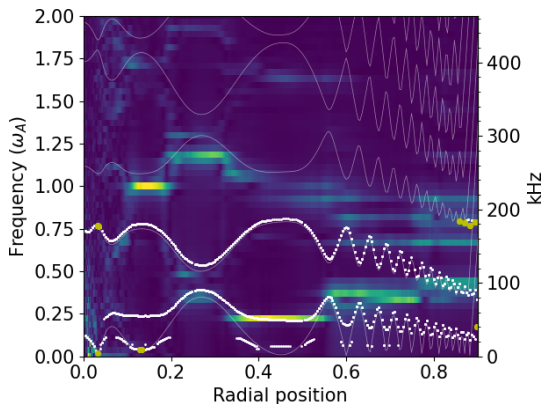
Preliminary results

AEs in the absence of EPs

(stable, weakly damped)

TAEs, EAEs, lower frequency

(RSAE and/or BAE)

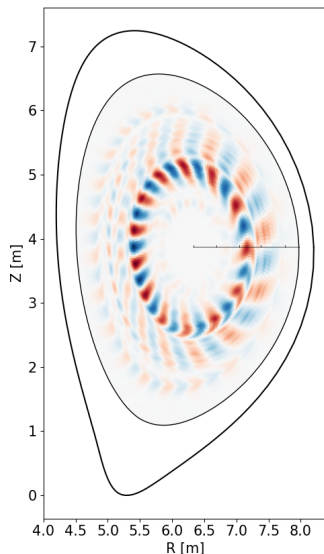


$n=12$

Alfvén continuum from ligka (thick: kinetic)

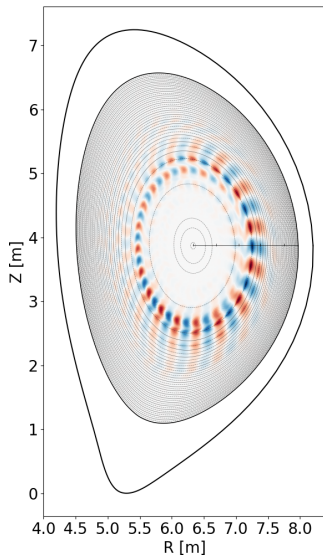
AEs in the absence of EPs
(stable, weakly damped)
TAEs, EAEs, lower frequency
(RSAE and/or BAE)

$n=12$



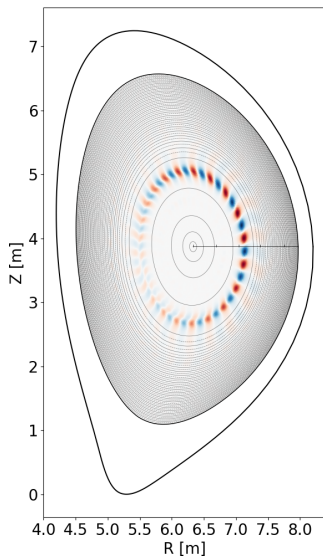
AEs in the absence of EPs
(stable, weakly damped)
TAEs, EAEs, lower frequency
(RSAE and/or BAE)

$n=16$



AEs in the absence of EPs
(stable, weakly damped)
TAEs, EAEs, lower frequency
(RSAE and/or BAE)

$n=20$



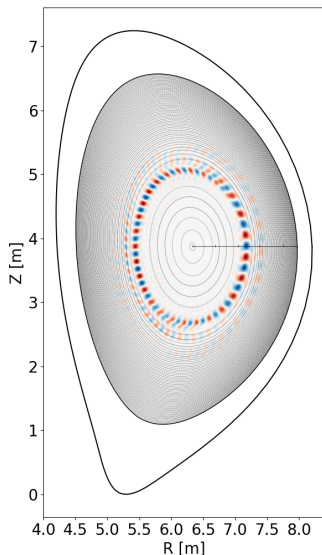
AEs in the absence of EPs

(stable, weakly damped)

TAEs, EAEs, lower frequency

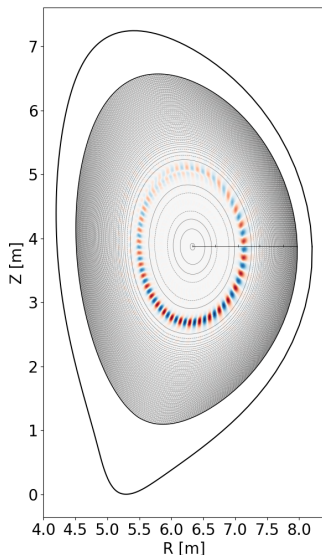
(RSAE and/or BAE)

$n=26$



AEs in the absence of EPs
(stable, weakly damped)
TAEs, EAEs, lower frequency
(RSAE and/or BAE)

$n=32$



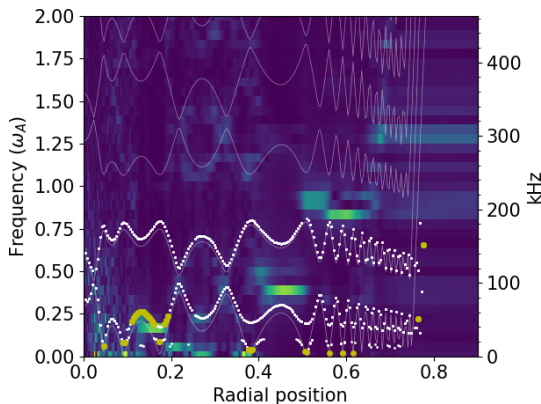
AEs in the absence of EPs

(stable, weakly damped)

TAEs, EAEs, lower frequency

(RSAE and/or BAE)

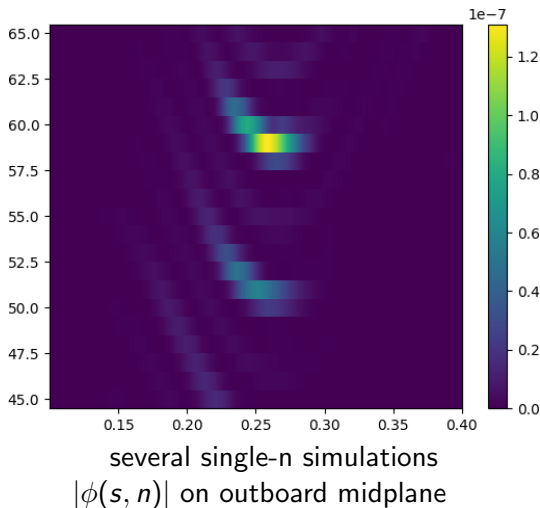
Now ready for NBI data from
ITER/IMAS



$n=32$

Alfvén continuum from ligka (thick: kinetic)

Higher- n core BAEs/AITGs in the absence of EPs (driven **unstable** by **bulk** plasma¹²)
Low frequency: in range $40 < n < 70$ (γ depends on distance between rational and q -extrema)

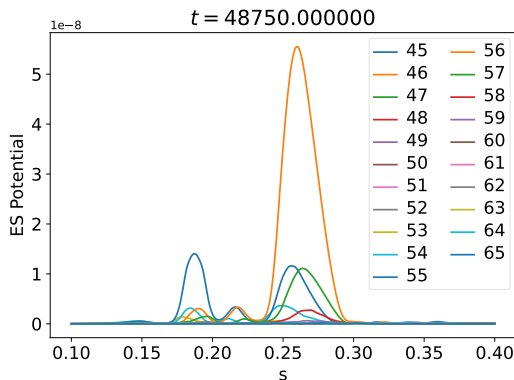


¹²Zonca+ 1996; 1998

Higher-n core BAEs/AITGs in the absence of EPs (driven **unstable** by **bulk** plasma¹²)

Low frequency: in range $40 < n < 70$ (γ depends on distance between rational and q-extrema)

$n=50$, frequency: -37.4 kHz
 $\gamma/\omega = 5.5\%$



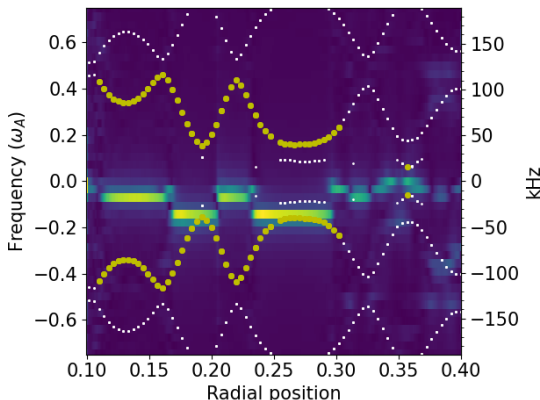
¹²Zonca+ 1996; 1998

Higher-n core BAEs/AITGs in the absence of EPs (driven **unstable** by **bulk** plasma¹²)

Low frequency: in range $40 < n < 70$ (γ depends on distance between rational and q-extrema)

$n=50$, frequency: -37.4 kHz

$\gamma/\omega = 5.5\%$



$n=50$, w/ kinetic spectrum from ligka in white/yellow dots ($\text{Im}(\omega) < 0, > 0$)

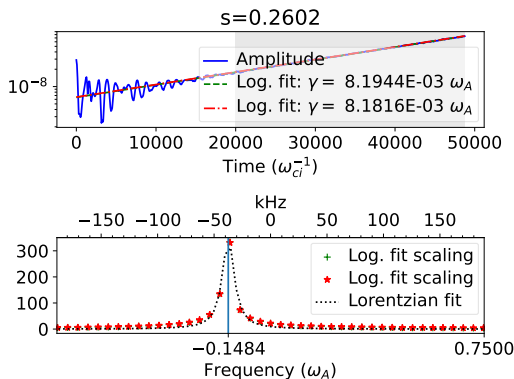
n.b. fig amplitude does not imply mode amplitude

¹²Zonca+ 1996; 1998

Higher-n core BAEs/AITGs in the absence of EPs (driven **unstable** by **bulk** plasma¹²)

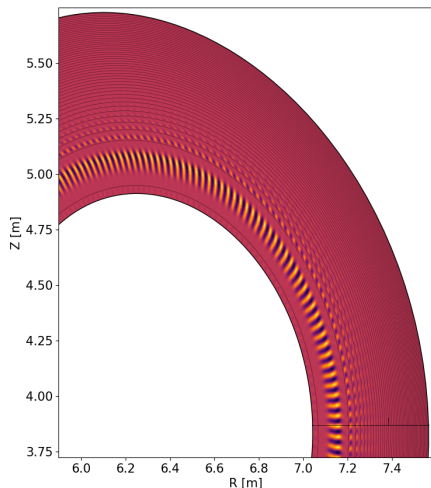
Low frequency: in range $40 < n < 70$ (γ depends on distance between rational and q-extrema)

$n=50$, frequency: -37.4 kHz
 $\gamma/\omega = 5.5\%$



¹²Zonca+ 1996; 1998

- ▶ Search high n (100–480)
- ▶ Found instability near q -min ($s \approx 0.45$)
- ▶ Electromagnetic simulations
- ▶ Peak growth $n \sim 150$ -200



$$n=180, \delta n_e$$

Numerics:

- ▶ Distribution functions added to ORB5
- ▶ Coupled to NBI code RABBIT

ASDEX Upgrade #31213:

- ▶ $n=0$ enhanced in coupled simulation – qual. similar to experiment
- ▶ EGAM & TAE/EPM with realistic NBI F_0 started

ITER 15MA Scenario

- ▶ 3.5 MeV slowing down: $\gamma \uparrow$
- ▶ Nominal study underway

ITER PFPO (101006)

- ▶ Multi scale problem
 - ▶ (Stable) TAE/EAE/RSAE/BAE in low- n (ready to add 1 MeV NBI)
 - ▶ Unstable BAEs in meso- n (bulk plasma ω^*)
 - ▶ High- n linear turbulent instabilities found