

TSVV13: Stellarator Turbulence Simulation

J. M. García Regaña (PI) on behalf of the TSVV13 Team

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	Physical Origin	Relevance for tokamaks	Relevance for stellarators
Classical transport	Collisions	Typically negligible	Typically negligible
Neoclassical Transport	Collisions + inhomogeneity of B	Small	Large in non-optimized stellarators
Turbulent transport	Collective fluctuations	Dominant	Relevant in neoclassically optimized stellarators

- **First** large **neoclassically optimized stellarator**, Wendelstein 7-X (W7-X), **in operation since 2015**.
- Before, only GENE [Jenko PoP'00] and EUTERPE [Kornilov PoP'04] regularly carried out gyrokinetic simulations in W7-X, mostly linear and electrostatic.
- □ W7-X began its **exploitation with a notable deficiency in resources** to thoroughly comprehend its microturbulence.
- □ The **TSVV13** has assembled these resources, incorporating new gyrokinetic codes, stella [Barnes JCP´19] and GENE-3D [Mauer JCP´20], along with developers and users.

Background

- □ The understanding of turbulence in stellarators is **limited** in comparison with tokamaks, due to
 - □ the **computational cost** of handling 3D magnetic geometries;
 - □ the **limitations** of the flux tube approach for stellarators.
- □ In particular, some aspects of turbulence remain (electromagnetic turbulence, interplay between neoclassical (NC) and gyrokinetic (GK) physics) remain **practically unexplored**.

Project

- □ 9 milestones and 15 SMART deliverables to cover by 2025 the 5 key deliverables:
- 1) Stellarator GK codes verified against each other and 2) validated against stellarator and 3D tokamak experiments, 3) able to address the interaction between NC and GK turbulence and 4) to assess relative weight of NC and turb. transport. 5) Develop reduced models.

Team (CIEMAT, CCFE, MPG, DIFFER)

- 9 leading experts in GK theory and simulation, developers and users of the main European stellarator GK codes + a NC code: stella, GENE, EUTERPE, GENE-3D, KNOSOS.
- □ J.M. García-Regaña (PI), E. Sánchez, J. L. Velasco (CIEMAT), M. Barnes, J. Omotani (CCFE/U. Oxford), A. Bañón Navarro, J. Riemann, A. Zocco (MPG), J. Proll (DIFFER) + External Experts: M. J. Pueschel (DIFFER), R. Kleiber (MPG) ... + PhD students.
- **Former members: F. I. Parra, D. St.-Onge (Oxford), J. Alcusón (MPG).**



TSVV#13: Stellarator Turbulence Simulation Verification (and code development)



- **stella**: δ f flux tube, electrostatic, collisionless, multispecies, gyrokinetic code for 3D geometry [Barnes JCP'19].
- □ Operator splitting and implicit treatment of parallel streaming term ⇒ efficient treatment of kinetic electrons (larger time-step allowed) in multispecies simulations.
- A set of stellarator test cases for cross-code verification à la Cyclone Base Case (CBC) delivered for the benchmark of stella against GENE. All data, incl. configuration and resolution details in [González-Jerez JPP'22].
- □ So far, **GENE**, **stella**, **GX** [Mandel submitted'23], **EUTERPE** have used some, if not all, of these test cases.



stella: δf flux tube, <u>full flux surface</u> (FFS), <u>electromagnetic (EM)</u>, collisional, gyrokinetic code for 3D geo., w/ neoclassical terms.

- Full flux Surface (FFS) or flux annulus version has been developed (fully functional but still doing nonlinear tests).
- Spectral in plane normal to mean magnetic field.



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Implicit

ITG

implementation

electromagnetic (EM) terms.

0.8

0.6 ĩЗ

0.4

stella: a mixed implicit-explicit δf gyrokinetic code for general geometry



of

0.04

collision

GS2 $(n_z = 32, n_{period} = 2)$ GS2 $(n_z = 64, n_{period} = 4)$

0.03

stella (implicit) ($n_z = 32$, $n_{period} = 2$)

stella (implicit) $(n_x = 64, n_{\text{option}} = 4)$

stella: a mixed implicit-explicit δf gyrokinetic code for general geometry



Full flux Surface (FFS) or flux annulus version has been developed (fully functional but still doing nonlinear tests).

0.2

0.15

0.1

0.05

0

0 0.5 flux tube

3

flux annulus

 $1 \quad 1.5 \quad 2 \quad 2.5$

 $k_y \rho_{\mathrm{ref}}$

 $\gamma(a/v_{\rm th,ref})$

Spectral in plane normal to mean magnetic field.

flux tube

3

3.5 4

flux annulus

 $1.5 \ 2 \ 2.5$

 $k_y \rho_{\text{ref}}$

W7-X, $\rho = 0.5$, kin.e⁻

0.8

0.7

0.6

0.50.4

0.3

0.2

0.1

0

0

1 0.5

 $\omega(a/v_{\rm th,ref})$

- Tokamak extension to allow radial profile variation following [Parra&Barnes PPCF'15].
- Local flux tubes determine boundary conditions of main (global) flux tube.





stella: a mixed implicit-explicit δf gyrokinetic code for general geometry





GENE-3D: a global gyrokinetic code for stellarators



- GENE-3D [Maurer JCP'20]: Eulerian, field-aligned coordinates, δf , EM, collisional, multispecies, it handles fully 3D geometries (coupled to GVEC).
- It can run in flux tube, full flux suface (FFS) and radially global domains (RG).
- RG version benchmarked against the radially global version of GENE for tokamak geometry, both linearly and nonlinearly [Wilms JPP'21]:



RG version benchmarked for linear and nonlinear simulations against EUTERPE in stellarator geometry [Sánchez NF'22].



- Good agreement between codes.
- Weaker turbulence localization in nonlinear simulations than in linear simulations.
- Weak effect of the neoclassical radial electric field (E_r) on heat fluxes and turbulent fluctuations localization.

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 - Next steps:

1.0

1.5

B[%]

1.4

1.2

 $\gamma [c_{\rm s}/R_0]$

0.4

0.2-

0.0 0.5

Implementation of $B_{||}$.

2.0

2.5

0.5

1.0

1.5

β[%]

version benchmarked for RG linear and nonlinear simulations against **EUTERPE** in stellarator geometry [Sánchez NF'22].



2.0

2.5

Weak effect of the neoclassical radial electric **field** (E_r) on heat fluxes and turbulent fluctuations localization.

impact of the domain considered in linear simulations.

0.25

 Comparison of all gyrokinetic codes with participation in the TSVV13: stella, GENE (run in FT and FFS domains), GENE-3D (run in FFS and RG domains) and EUTERPE (run in RG domain)

Verification of codes beyond flux tube geometry and

- Linear simulations of ITG instabilities (adiabatic electrons) and zonal flow relaxation, in the LHD and W7-X stellarators.
- □ FT results converge to each other and to FFS and RG simulations with increasing FT length (dependence on configuration).

GENE/GENE-3D/stella/EUTERPE cross code comparison for linear simulations







TSVV#13: Stellarator Turbulence Simulation Theory and Simulation

Cross-device comparison of electrostatic instabilities and turbulence





W7-X and NCSX benefit from the increase of the density gradient to access low turbulent heat levels. Linear simulations do not correlate well, in general, with nonlinear fluxes.



Next steps:

- Including new optimized stellarators.
- Exploring various functional forms dependent on linear parameters to predict nonlinear heat fluxes from linear information.

Global simulations of electrostatic stability in W7-X

- **Stability** studies with **global simulations** (EUTERPE) for W7-X requires full profiles.
- **Pressure preserving scheme** has scanned $\eta = T'/n'$ in the range [0.33, 0.3] considering experimentally achievable profiles and consistent VMEC equilibria.
- **Local maxima of** γ found for $k_{\perp}\rho_i \approx 2$ found for a broad regions of the parameter space.
- Diagnostics to characterize the source of the instabilities in phase space.



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Next steps: axima of γ found for $k_{\perp}\rho_i \approx 2$ found for a broad regions of the parameter space.

- Including effect of E_r , obtained from RG neoclassical simulation (new in EUTERPE), i-e root transition.
- Enhancing performance using multigrid solver (2023/24 ACH task, carried out by **ACH-MPG**)





What is the impact of the domain choice in nonlinear simulations? [Wilms JPP'23]



- □ Full-flux-surface simulations confirm the stabilisation of turbulence in Wendelstein 7-X through a/L_n by local simulations [Alcusón PPCF'21].
- Significant differences between flux-tube and full-flux-surface results for some parameters



■ Turbulence is only weakly localised on surface → extended nature could ease experimental measurements of fluctuation levels.



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Next step:

Investigate when **global effects** are important.

Electrostatic turbulence close to marginality in Wendelstein 7-X



- Electrostatic ITG turbulence with moderate to **nearly marginal temperature gradient**, $a/L_T = \{0.9, 2.0\}$, critical gradients has been studied.
- Close to marginality, extended linearly unstable modes are dominant, even in the presence of kinetic electrons.
- No observed Dimits shift, as turbulence becomes more radially localized and less prone to zonal EXB shearing stabilization.







$\Box \quad How \text{ does high } \beta \text{ modify electrostatic picture?}$

Linear GENE simulations

- **Dominant** (solid lines) and **sub-dominant** (dashed lines) instabilities have been characterized for a β scan at different wavelengths (k_{γ}).
- GENE eigenvalue solver reveals many subdominant unstable modes with $\gamma < \gamma_{max}$ at each wavenumber.
- **Given Subdominant KBM (stKBM) threshold revealed:** $\beta_{crit}^{stKBM} \approx 1\%$.
- **stKBM** unstable far **below MHD** ballooning **limit** ($\beta_{crit}^{MHD} \approx 3\%$).





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Nonlinear GENE simulations

- □ Heat fluxes decrease slightly for $0 < \beta < 1\%$.
- **Q** Rapid heat-flux increase for $\beta \ge \beta_{crit}^{stKBM} \approx 1\%$
- stKBM is highly excited in turbulence (NL projections) [Mulholland submitted'23].







Assessment of turbulent impurity transport under different turbulence type and comparison across devices.



ITG (resp. TEM) turbulence yield curvature pinch (resp. anti-pinch) convective contribution. Both turbulence type yield inward thermo-diffusive contributions. Weak dependency on the device observed for ordinary difussion.

Impurity transport and turbulence in the presence of impurities



- Assessment of turbulent impurity transport under different turbulence type and comparison across devices.
- W7-X (ITG) Fe¹⁶⁺, r/a = 0.75, $a/L_{n_i} = 0$ 15 $- D_{Z1}$ (bean) $\rightarrow D_{Z1}$ (tri.) D¢ ¢. V + 6 D_{Z2} (bean) D_{Z2} (tri.) $D_{Z1}, D_{Z2} \ [\text{m}^{2\text{s}-1}], \ C_{Z} \ [\text{m} \ \text{s}^{-1}]$ o c c 0 C_{Z} (bean) C_Z (tri.) 4 $[\Gamma_{\mathrm{gB},i}a/n_i]$ $V \left[\Gamma_{\mathrm{gB},i}/n_i \right]$ m 2Ð. 0 \Box -2 -4 (b) W7-X TJ-II LHD NCSX W¹⁶⁺ Ar^{16+} W44+ Device [García-Regaña JPP'21]. [García-Regaña NF²¹].
- ITG (resp. TEM) turbulence yield curvature pinch (resp. anti-pinch) convective contribution. Both turbulence type yield inward thermo-diffusive contributions. Weak dependency on the device observed for ordinary difussion.

Investigation of the impact of impurities on turbulent transport characterized in W7-X.



Impurities can substantially enhance or reduce turbulent heat losses. Optimal content of impurities found [García-Regaña submitted'23].



TSVV#13: Stellarator Turbulence Simulation Validation



First principles multiple-time scale approach: it simulates turbulence and transport only on their natural time scales.



- → KNOSOS [Velasco JCP'21] → neoclassical fluxes
- GENE/GENE-3D/Models → turbulent fluxes.

- Applied to standard ERCH W7-X scenarios [Banón Navarro NF'23].
- \Box Different ion heating result in **the same on-axis** T_i .
- □ The model **reproduces** the experimentally observed T_i clamping [Beurkens NF'21].





First principles multiple-time scale approach: it simulates turbulence and transport only on their natural time scales.

 $\overline{Q}_{s}(i) = \overline{Q}_{s}(i)^{\text{turb.}} + \overline{Q}_{s}(i)^{\text{neo.}}$

- Applied to standard ERCH W7-X scenarios [Banón Navarro NF'23].
- \Box Different ion heating result in the same on-axis T_i .
- □ The model reproduces the experimentally observed T_i clamping [Beurkens NF'21].

Next steps: Improving performance of Tango. Including GVEC calculation in the loop for consistency between magnetic equilibria and p profile. Developing quasi-linear models and neural network surrogates. Validating other W7-X scenarios (incl. impurity and particle transport) and studying confinement properties of new optimized stellarator designs. ho_{tor} $\rho_{\rm tor}$ $p_{s}(i+1)$ (iv) (a) Case 1 Case 2 Τ_{i,0} [keV] δ **KNOSOS** [Velasco JCP²1] → neoclassical fluxes GENE/GENE-3D/Models \rightarrow turbulent 5 10 fluxes. $\int P_i dV [MW]$

2.01

Turbulent particle transport in stellarators



- In neoclassically dominated plasmas, theory predics strongly hollow density profiles in stellarators, that are, in general, not observed.
- Particle transport studied for W7-X combining gyrokinetic stella simulations, KNOSOS neoclassical simulations and 1D neutral model [Thienpondt PRR'23].
- □ Turbulence driven by finite a/L_{T_e} and a/L_{T_i} produces a particle pinch. In W7-X, that pinch \Rightarrow absence of core density depletion.





The **parametric dependence** has been characterized in detail.

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- The parametric dependence has been characterized in detail.
- The presence of the turbulent pinch, is found in all devices analyzed so far.

Comparison between stella simulations and Doppler Reflectometry measurements



□ Confidence on our gyrokinetic codes is essential for the planning of experiments and their interpretation ⇒ careful translation of our code output into measurable data.



- stella-Doppler Reflectometry (DR) comparison (δn)² of OP1 plasmas for low and high density ECRH standard discharges [González-Jerez submitted'23].
- Agreement between experimental and simulations, and DR/PCI differences are explained by the measurement position in wavenumber space.

Frequency spectra of the density fluctuations measured by the DR have been obtained.



Frequency spectra of the zonal flow components has been brought forward for future comparison with dual DR system, run during past campaign.



Comparison between stella simulations and Doppler Reflectometry measurements



 $r_0/a = 0.9$

 $10^0 \ 10^1 \ 10^2 \ 10^3 \ 10^4$

 $\omega/2\pi$ [kHz]

sity fluctuations

 $10^{0} \ 10^{1} \ 10^{2} \ 10^{3} \ 10^{4}$

al flow components

 $\omega/2\pi$ [kHz]

n obtained.

 $r_0/a = 0.8$





 $r_0/a = 0.5$

 $r_0/a = 0.6$ $r_0/a = 0.7$

 $r_0/a = 0.8$

 $r_0/a = 0.9$

3

2 $k_u \rho_i$

- stella-Doppler Reflectometry (DR) comparison $(\delta n)^2$ of OP1 plasmas for low and high density ECRH standard discharges [González-Jerez submitted'23].
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Next steps on validation and the TSVV13 presence in the W7-X OP2 campaign



Proposal name	Author	Title
ksena_006	<u>P. Mulholland</u>	Stabilisation of KBMs with increasing magnetic shear
rjose_002	J. M. García-Regaña	Turbulent (de)stabilization driven by non-trace impurities
rjose_003	J. M. García-Regaña	Assessment of the relative weight of the different transport channels (i.e. neoclassical and turbulent) on particle transport
dinklage_013	A. Dinklage	Database for the TSVV code validation
edis_003	<u>E. Sánchez</u>	Experimental validation of theoretical expectations of ZF properties
gawe_020	G. Weir	Shear stabilization of ion-scale drift wave turbulence
gawe_021	G. Weir	Matching physics parameters and fluxes to nonlinear gyrokinetic calculations at the ion-scale
tere_003	T. Estrada	Systematic searching for zonal flows using dual V-band DR
dacar_006	D. Carralero	Full characterization of turbulence during suppressed turbulence scenarios
Etc.	Etc.	Etc.



- It has addressed numerous challenges, in the areas of code development, code verification and validation along with theory.
- The codes are in **continous development** and cross-**verification**.
- The **stability** properties in stellarators, in all their diversity of configurations, is **much better characterized** (sinergy with TSVV#12).
- Impact of the choice of reduced **domains**, w.r.t RG simulations, is much better **understood**.
- Bulk and impurity **particle transport** questions have been for the first time been **satisfactorily addressed**.
- **Transport simulations,** evolving profiles iteratively, have been **enabled**.
- **Electromagnetic simulations** have become routine (linked to TSVV#10 work).
- Etc.



Deliverable name	Short description	Progress
D-REF-CASES	Definition of a reference case for code verification and validation in stellarator geometry	100 %
D-TURB-ZTRANSP	Initial assessment of turbulent transport of impurities	100%
D-TURB-BULKTRANSP	Turbulent transport of the main ions and electrons in W7-X	In continuous progress
D-TURB-ZNONTRACE	Role of impurities in the turbulent heat losses	100 %
D-KBM-BASIC	Linear KBM simulations in W7-X equilibria	100%
D-TURB-WEIGHT	Assessment of the relative weight between turbulent and neoclassical transport	100 %
D-TURB-DOMAIN	Assessment of the effect of the spatial domain (global vs FFS) on turbulence	75 %
D-ADJ-THEORY	Development of time-dependent method for linear gyrokinetics	100 %
D-NUM-DIAG	Development of synthetic diagnostics	75 %
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Milestone name	Short description	Progress
M-GENE-3D-EM	Development of an electromagnetic version of GENE-3D	100 %
M-BENCHMARK-ES-GLOB	Benchmark between GENE-3D and EUTERPE for electrostatic turbulence with adiabatic electrons	100%
M-TRANSPORT-SUITE	Development of a transport suite that enables, with input from neoclassical and gyrokinetic codes, profile prediction and validation.	100 %
M-STELLA-COLL	Implementation of the full linearized collision operator in stella.	100%
M-STELLA-FFS	Development of a full-flux-surface (FFS) version of stella	75%
M-STELLA-EM	Development of an electromagnetic version of stella	75 %



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More than 90 % of Marconi quota consumed in 5th and 6th cycles (\approx 50% of 7th cycle) \Rightarrow **180 M CPUhours**, approximately, spent by the TSVV#13.



Key deliverables:

- 1) Verified set of gyrokinetic stellarator codes that self-consistently treat multiple particle species (enabling, in particular, studies of turbulent impurity transport) and whose simulation domains cover an entire flux surface or a fully global domain. Assessment on the minimal simulation domain needed to correctly calculate turbulent fluxes and zonal flow dynamics in stellarators. Synergies with the tokamak community are to be sought.
- 2) Inclusion in (at least some of) these codes of the capability to use the **neoclassical equilibrium as background distribution for turbulence calculations**. Quantification of the modification of linear and nonlinear turbulence properties due to the neoclassical equilibrium.
- 3) Study of the **relative weight of the neoclassical and turbulent branches of radial transport in multispecies stellarator plasmas**, as a function of the species and the collisionality regime.
- 4) Validation of the codes for the calculation of turbulent fluxes in multispecies stellarator plasmas and in tokamaks with broken axisymmetry. In stellarators, explicit comparisons should be provided between the total transport experimentally measured and the sum of the simulated neoclassical and turbulent components.
- 5) Development of efficient reduced models (suitable for integration into stellarator optimization codes, see TSVV Task 12) capable of reliably predicting stellarator turbulent fluxes.

Substantial contributions / To be prioritized until 2025





Backup slides

Status of the code progress towards the EUROfusion standard software



	τςν// сонтаст		Progress towards EUROfusion Standard Software																
	ISVV CONTACT		SOFTWARE ENGINEERING			INTERFACES			ννυα			DISSEMINATION		DOCUMENTATION		USER SUPPORT			
CODE J	TSVV No 🔽 Contact Person 🖤	ACH support started	1. Version control implemented	2. Software engineering standards	3. Coding standards established	 Performance optimization on HPC systems 	1. User-friendly interface	2. Post- processing and visualisation tools	3. Interface to the IMAS Data Dictionary	1. Specific plans for code verification	2. Code verification studies	 Inter-code benchmarking accomplished 	4. Code validation studies accomplished	 Up-to-date Up-to-date release version on the Gateway 	2. Trainings provided to code users	1. High-quality technical documentation	2. User manual available for download	1. Responsive support team	 Tools for managing support requests
GENE	1 Tobias Görler	Started	Completed	Completed	Completed	In Progress	In Progress	In Progress	Not started	In Progress	Completed	Completed	In Progress	In Progress	Not started	In Progress	Completed	Completed	In Progress
EUTERPE	10 Ralf Kleiber	Started	Completed	In Progress	In Progress	Not started	In Progress	Completed	In Progress	In Progress	In Progress	In Progress	Completed	In Progress	Completed	In Progress	In Progress	Completed	Completed
KNOSOS	12 José Luis Velasco	Started	Completed	In Progress	Not started	In Progress	Not started	In Progress	Not started	Completed	In Progress	Completed	In Progress	Not started	Not started	In Progress	In Progress	Completed	Not started
GENE-3D	13 Alejandro Bañón-Navarro	Started	Completed	In Progress	In Progress	Not started	Not started	Completed	Not started	Not started	Completed	Not started	In Progress	Not started	Completed	In Progress	In Progress	Completed	Completed
STELLA	13 Michael Barnes	Started	Completed	In Progress	In Progress	In Progress	In Progress	In Progress	Not started	Completed	Completed	In Progress	In Progress	Not started	Completed	Completed	In Progress	Completed	Not started

Differences between flux tubes in a stellarator







FIGURE 3. Normalized geometric quantities in the range $\zeta - \zeta_0 = [-2\pi, 2\pi]$ for the surface $r_0/a = 0.8$ along the field lines $\alpha_0 = 0$ (solid black line) and $\alpha_0 = -\iota\pi/5$ (dashed green line). The magnetic field strength is represented in (*a*); the projections of $\hat{b} \times \nabla B$ and $B \times \kappa$ along the binormal direction are represented in (*b,c*), respectively; the projections of $\hat{b} \times \nabla B$ and $B \times \kappa$ along the radial direction are represented in (*d,e*), respectively.