CONSTITUTE OF PLASMA PHYSICS

BOUNDARY CONDITIONS IN THE GBS SIMULATION OF THE COMPASS TOKAMAK

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OUTLINE

- Boundary condition types
- BCs used in COMPASS simulation and simulation domain
- An impact of BCs on turbulence
- Impact of BCs on electron velocities and vertical electric field
- Conclusion

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GBS CODE

GLOBAL BRAGINSKII SOLVER

- First principle, 3D, flux-driven, global, turbulence code for plasma edge simulations based on Braginskii equations [1].
- Full plasma volume, Divertor geometry, electromagnetic effects, kinetic neutrals, ion temperature dynamics, self-consistent turbulence evolution.
- High computational requirements (~2000 cores, ~5-10 M CPU hours).
- Validation on COMPASS tokamak first validation of full-size simulation after TCV.
- Validation on COMPASS will include electron temperature and plasma potential fluctuations.

GBS - EQUATIONS

EQUATIONS

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- Braginskii equations are solved, Boussinesq approximation is not used.
- 7 fields are evolved during each step:
	- Density, electron and ion parallel velocity, vorticity, electron and ion temperature, and psi (if electromagnetic effects are enabled).
- If kinetic neutrals are included:
	- Neutral density, and neutral parallel velocity.

$$
\nabla \cdot (n \nabla_{\perp} \phi) = \Omega - \frac{\nabla_{\perp}^2 p_i}{e},
$$

$$
\left(\nabla_{\perp}^2 - \frac{e^2 \mu_0}{m_e} n\right) v_{\parallel e} = \nabla_{\perp}^2 U_{\parallel e} - \frac{e^2 \mu_0}{m_e} n v_{\parallel i} + \frac{e^2 \mu_0}{m_e} \vec{j}_{\parallel}.
$$

$$
U_{\parallel e} = v_{\parallel e} + e \psi / m_e
$$

Particle $\frac{\partial n}{\partial t} = -\frac{1}{B}[\phi,n] + \frac{2}{eB}\Big[C(p_e) - nC(\phi)\Big] - \nabla_{\parallel}(n v_{\parallel e}) + D_n \nabla_{\perp}^2 n + s_n + v_{iz}n_n - v_{\text{rec}}n,$ (1) $\frac{\partial \Omega}{\partial t} = -\frac{1}{R} \nabla \cdot [\phi, \omega] - \nabla \cdot (v_{\parallel i} \nabla_{\parallel} \omega) + \frac{B \Omega_{ci}}{g} \nabla_{\parallel} j_{\parallel} + \frac{2 \Omega_{ci}}{g} C (p_e + p_i)$ Vorticity $+\frac{\Omega_{ci}}{3\rho}C(G_i)+D_{\Omega}\nabla_{\perp}^2\Omega-\frac{n_{\rm n}}{n}v_{\rm cx}\Omega,$ (2) $\frac{\partial U_{\parallel e}}{\partial t} = -\frac{1}{B}[\phi, v_{\parallel e}] - v_{\parallel e}\nabla_{\parallel}v_{\parallel e} + \frac{e}{m_e}\left(\frac{j_{\parallel}}{\sigma_{\parallel}} + \nabla_{\parallel}\phi - \frac{1}{en}\nabla_{\parallel}p_e - \frac{0.71}{e}\nabla_{\parallel}T_e - \frac{2}{3en}\nabla_{\parallel}G_e\right)$ Electron inertia $+D_{v||e} \nabla_{\perp}^2 v_{||e} + \frac{n_{\rm n}}{n} (v_{\rm en} + 2v_{\rm iz}) (v_{||n} - v_{||e}),$ (3) $\frac{\partial v_{\|i}}{\partial t} = -\frac{1}{B}[\phi, v_{\|i}] - v_{\|i}\nabla_{\|}v_{\|i} - \frac{1}{m!}\nabla_{\|}(p_e + p_i) - \frac{2}{3mn}\nabla_{\|}G_i$ ion inertia $+D_{v_{||i}}\nabla_{\perp}^{2}v_{||i}+\frac{n_{\rm n}}{n}(v_{iz}+v_{\rm cx})(v_{||n}-v_{||i}),$ (4) electron $\frac{\partial T_e}{\partial t} = -\frac{1}{B}[\phi, T_e] - \nu_{\parallel e} \nabla_{\parallel} T_e + \frac{2}{3} T_e \left[0.71 \frac{\nabla_{\parallel} j_{\parallel}}{e n} - \nabla_{\parallel} \nu_{\parallel e} \right] + \frac{4}{3} \frac{T_e}{e B} \left[\frac{7}{2} C(T_e) + \frac{T_e}{n} C(n) - e C(\phi) \right]$ energy confinement $+ \nabla_{\parallel} (\chi_{\parallel e} \nabla_{\parallel} T_e) + D_{T_e} \nabla_{\perp}^2 T_e + s_{T_e} - \frac{n_{\rm n}}{n} v_{\rm en} m_e \frac{2}{3} v_{\parallel e} (v_{\parallel n} - v_{\parallel e})$ $-2\frac{m_e}{m_i}\frac{1}{\tau_e}(T_e-T_i)+\frac{n_n}{n}v_{iz}\left[-\frac{2}{3}E_{iz}-T_e+m_e v_{||e}\left(v_{||e}-\frac{4}{3}v_{||n}\right)\right],$ (5) ion $\frac{\partial T_i}{\partial t} = -\frac{1}{B}[\phi, T_i] - \nu_{\parallel i} \nabla_{\parallel} T_i + \frac{4}{3} \frac{T_i}{e B} \Big[C(T_e) + \frac{T_e}{r} C(n) - e C(\phi) \Big] - \frac{10}{3} \frac{T_i}{e B} C(T_i)$ energy confinement $+\frac{2}{3}T_{i}\left[(v_{\|i}-v_{\|e})\frac{\nabla_{\|}n}{n}-\nabla_{\|}v_{\|e}\right]+\nabla_{\|}(\chi_{\|i}\nabla_{\|}T_{i})+D_{T_{i}}\nabla^{2}_{\perp}T_{i}+s_{T_{i}}$

 $+2\frac{m_e}{m}\frac{1}{\tau}(T_e-T_i)+\frac{n_n}{n}(v_{iz}+v_{cx})\left[T_n-T_i+\frac{1}{3}(v_{\|n}-v_{\|i})^2\right],$

 (6)

GBS – BOUNDARY CONDITIONS

BOUNDARY CONDITIONS

- BCs play an important role in the simulation.
- Applied at the magnetic presheath.
- There are specific sets of BCs for plasma potential and for other fields.
- Plasma potential uses multiple conditions:
	- **Man** Dirichlet, Neumann fixing all fields.
	- **pAT** fixing potential to ΛT_e , other fields Man.
	- **Tar** fixing potential to ΛT_e , others Mag
	- **Rob**in allowing potential to vary from Λ T_e.
	- **Mag**netic full conductive condition.

 $v_{\parallel i} = \pm c_s \sqrt{1 + \frac{T_i}{T_e}},$

 $v_{\parallel} = \pm c_{\parallel} \sqrt{1 + \frac{T_i}{r}} \exp(\Delta - \frac{e\phi}{r}).$

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 $\partial_y \phi(x, z) = -\frac{\partial_x \psi(x, z)}{\sqrt{1 + \tau \frac{T_1(x, z)}{T_1(x, z)}}} \partial_y v_{\parallel} (x, z),$

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 $v_{\parallel i} = \pm c_s \sqrt{1 + \frac{T_i}{T_e}},$

 $v_{\text{u}} = +c \sqrt{1 + \frac{T_i}{r}} \exp(\Lambda - \frac{e\phi}{r})$

 $\partial_{u}\phi$

Mag

$$
(x,z)=-\frac{\frac{\partial_x\Psi}{|\partial_x\Psi|}c_{\rm s}(x,z)}{\sqrt{1+\tau\frac{T_{\rm i}(x,z)}{T_{\rm e}(x,z)}}}\partial_yv_{\parallel{\rm i}}(x,z),
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$$

 $v_{\parallel i} = \pm c_s \sqrt{1 + \frac{T_i}{T_e}},$
 $v_{\parallel i} = \pm c_s \sqrt{1 + \frac{T_i}{T_e}} \exp(\Delta - e\phi).$

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 $v_{\parallel i} = \pm c_s \sqrt{1 + \frac{T_i}{T_e}},$

 $\overline{I_i}$ $\overline{I_i}$ $\cos(\Lambda e^{\phi})$

ROBIN BOUNDARY CONDITION

 $v_{\parallel i} = \pm c_s \sqrt{1 + \frac{T_i}{T_e}},$

 $v_{\parallel e} = \pm c_s \sqrt{1 + \frac{T_i}{T_c}} \exp\left(\Lambda - \frac{e\phi}{T_c}\right),$

BOUNDARY CONDITIONS

$$
\phi(x, z) = \Lambda(x, z) T_e(x, z)
$$

- $R_{\text{fac}}(x) \partial_x \Psi(x) B_{\text{sign}}(x) T_e(x, z) (\partial_y n(x, z) + 1.71 \partial_y T_e(x, z)),$

where

$$
R_{\text{fac}}(x) = \sum_{z} \frac{T_{\text{e}}(x, z)}{c_{\text{s}}(x)\sqrt{1 + \tau \frac{T_{\text{i}}(x, z)}{T_{\text{e}}(x, z)}}} \mu \mu_{\text{spitzer}}(x) F_{\text{fac}},
$$

\n• **Tar** - fixing potential to AT_e, others Mag
\n• **Rohin** - allowing potential to your from AT_e
\n• **Rohin** - allowing potential to your from AT_e

Mag

- **Tar** fixing potential to Λ T_e, others Mag
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COMPASS SET OF BCS

- In the case of COMPASS simulation, all the **Tar**, **Rob**, and **Mag**netic BC were applied on the bottom boundary - the divertor position.
- **Tar** condition (potential fixed to λT_e) used at left and top boundary.
- **Dirichlet** and **Neumann** conditions are set on right boundary for all fields.
- It was shown, turbulent structures disappear before touching the right boundary.
- Influence of the Dirichlet boundary is therefore not propagating inside plasma.

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AN IMPACT OF BCs ON TURBULENCE

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ROBIN VS MAG BC

- Similar blob shapes and amplitudes are observed for both the **Rob** and **Mag**.
- A bit lower amplitudes of negative structures for the **Rob** BC.
- Both **Rob** and **Mag** should be equivalent to each other.
- Usage of **Mag** is however prefered, **Rob** used for transition from **Tar**.
- Furthermore, problem with Poisson solver and **Rob** BC in COMPASS simulation leading to code slowening.

ELECTRON PARALLEL VELOCITIES IN MAG

Electron parallel velocity Electron parallel velocity Zoomed on FPR

700

- Significantly higher values (~3x)of vpare for **Mag** BC.
- Sign represents direction with respect to magnetic field lines alignment.
- The 1D profile is smoothed by Tanh function in ghost cells where mag. Field is tangent to surface.
- Electron and ion parallel velocity set to 0 between the two regions (plus zero derivative of vpari).

1D profile of electron parallel velocity at the bottom boundary

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VERTICAL ELECTRIC FIELD AT BC

BOUNDARY PLOTS

 $\overline{5}$

• The crash in electron parallel velocities, caused by vertical electric field, was threatened by adjusting the mass ratio and the sheath drop Λ .

 10

 $5\overline{5}$

 $\overline{0}$

 -5

 -10

- The mechanism of positive vertical electric field formation is however still not well understood.
- Already appeared several times using **Mag** BC in past.
- Since now, the problem did not appear again.

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SUMMARY

- COMPASS simulation showed significant impact of BCs on simulation:
	- **Tar** condition caused huge amplitudes in potential, exceeding 2 000 V leading to crash.
	- Both **Rob**in and **Mag**netic BCs showed similar turbulence properties.
- Problems with Poisson solver combined with **Robin** boundary condition were observed.
- **Mag**netic boundary condition performed best, however, problems with vertical electric field were observed:
	- Increasing Ez caused acceleration of electrons and simulation crash.
	- The problem however fixed itself after enough simulation time and mass ratio adjustment.
	- This mechanism must be further investigated.
	- Since now, the problem with the bottom boundary did not happen again.

- 1. M. Giacomin et al J. Comput. Phys. 463 (2022) 111294 (The GBS code for the self-consistent simulation of plasma turbulence and kinetic neutral dynamics in the tokamak boundary)
- 2. M. Giacomin *et al* 2021 *Nucl. Fusion* **61** 076002 (Theory-based scaling laws of near and far scrape-off layer widths in single-null L-mode discharges)

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