

Saturation of fishbone modes by self-generated zonal flows and constants of motions EP distributions in tokamak plasmas

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⁶ École Polytechnique - CPHT

Outline

I) Interplay fishbone/zonal flows in gyrokinetic simulations

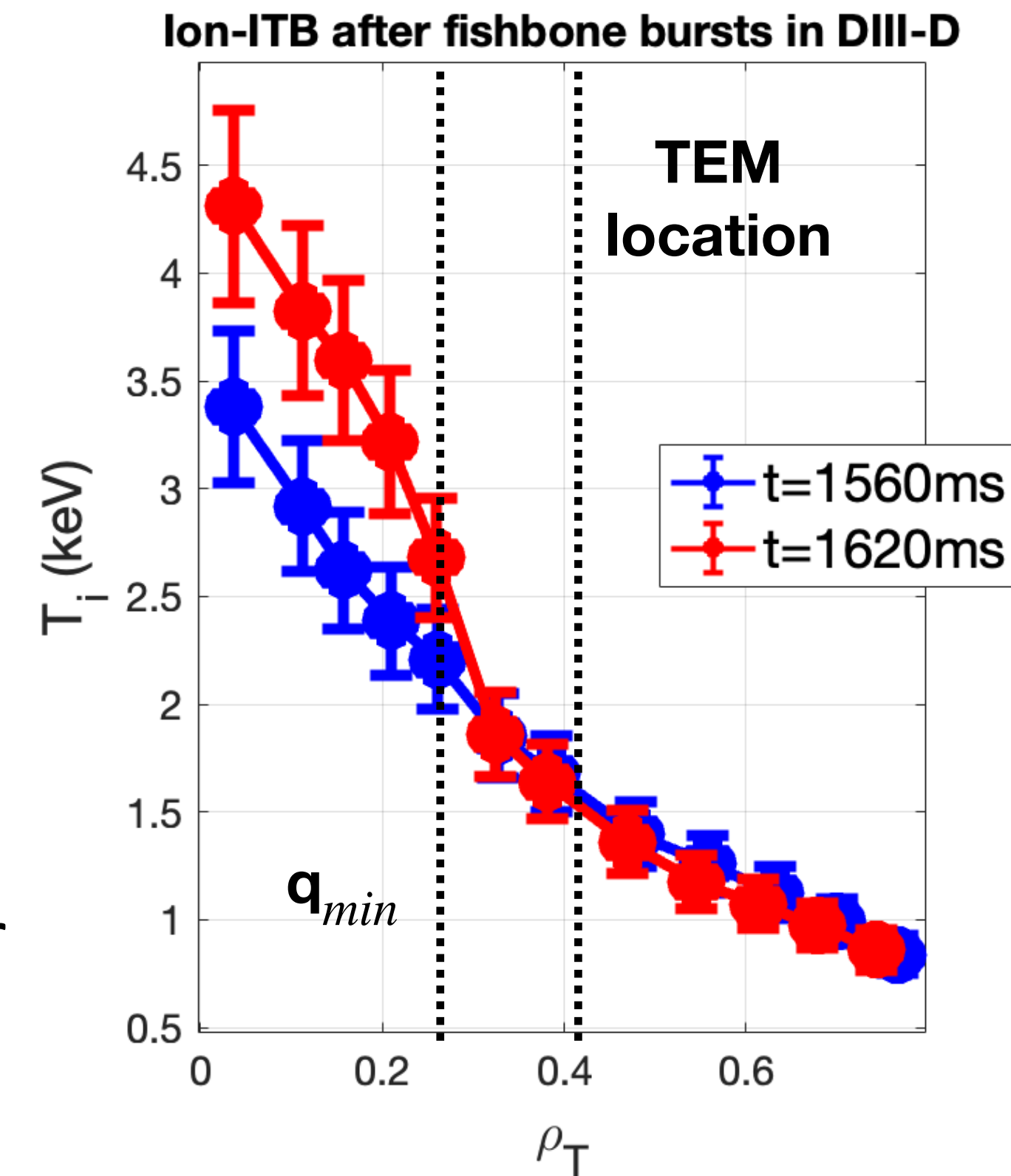
- A) Experimental fishbone validation on a DIII-D discharge
- B) Predicted fishbone dynamics in ITER PFPO-2 scenario

II) Computation of CoMs EP distribution in IMAS

- A) Versatile method for coordinate transformation
- B) Application for NBI and alpha distributions in a JET-DT pulse

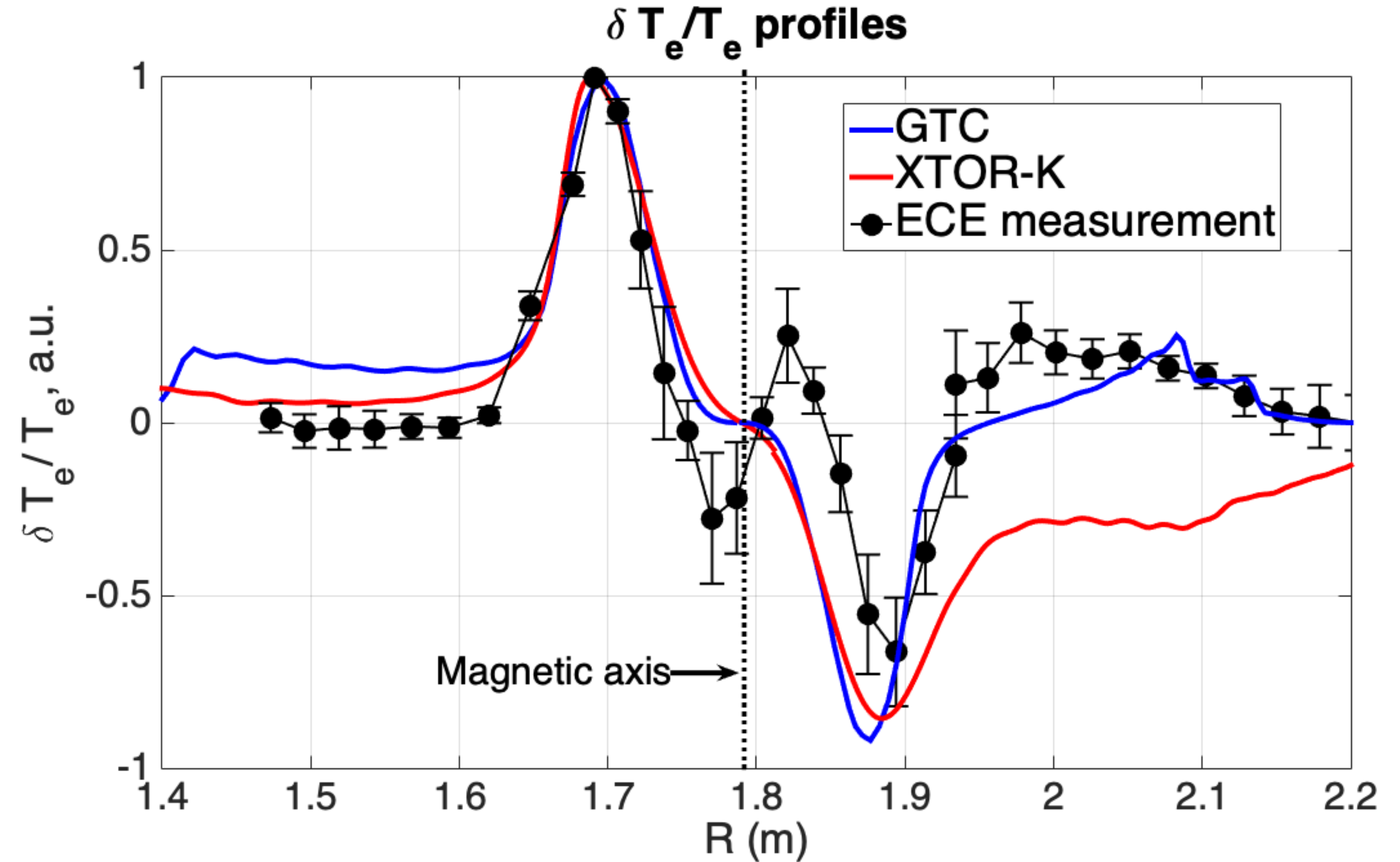
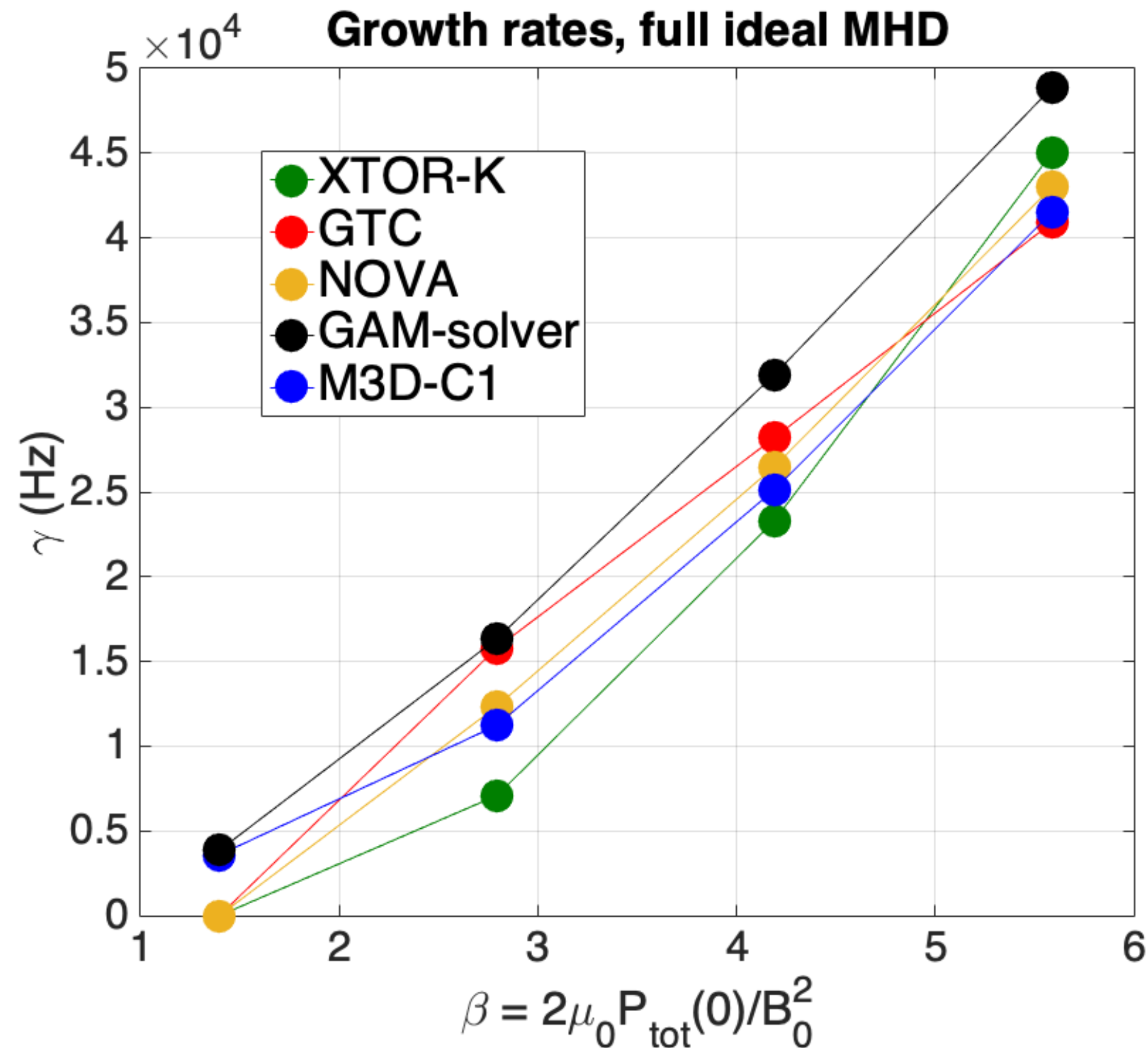
Importance of gyrokinetic simulations of fishbone modes for EP transport

- **Zonal flows (ZFs)** can impact significantly **thermal and EP transport** by **mitigating microturbulence** [1] and **AEs** [2] saturation amplitudes
- **Drift-waves modes** and **EP-driven AEs** can trigger **ZFs** respectively through **modulational instability** [3] and **EPs-induced polarisation** [4]
- **Fishbones** known to **trigger ITBs** in **ASDEX** [5], **MAST** [6], **HL-2A** [7], **EAST** [8] plasmas, and were observed to **destabilise strong zonal sheared flows** in **kinetic-MHD** simulations [9,10]
- A **gyrokinetic formalism** for **self-consistent ZFs evolution** is **crucial** to capture their **collisionless damping** [11], requiring **kinetic treatment of thermal ions**
- **GTC** is applied to study **self-consistently fishbone-induced EP transport** in **DIII-D** and **ITER**, as a **stepping stone** towards **upcoming cross-scale gyrokinetic simulations**



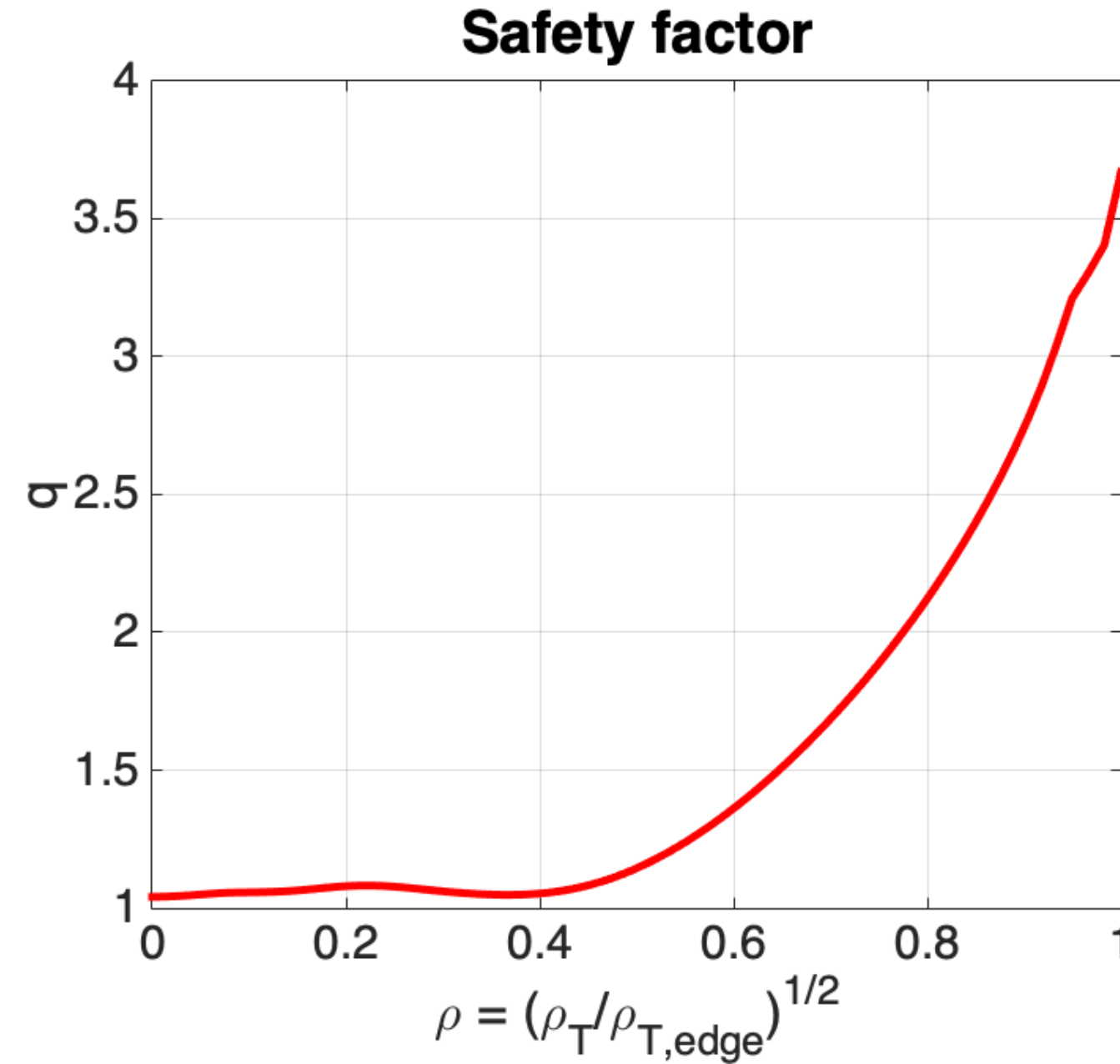
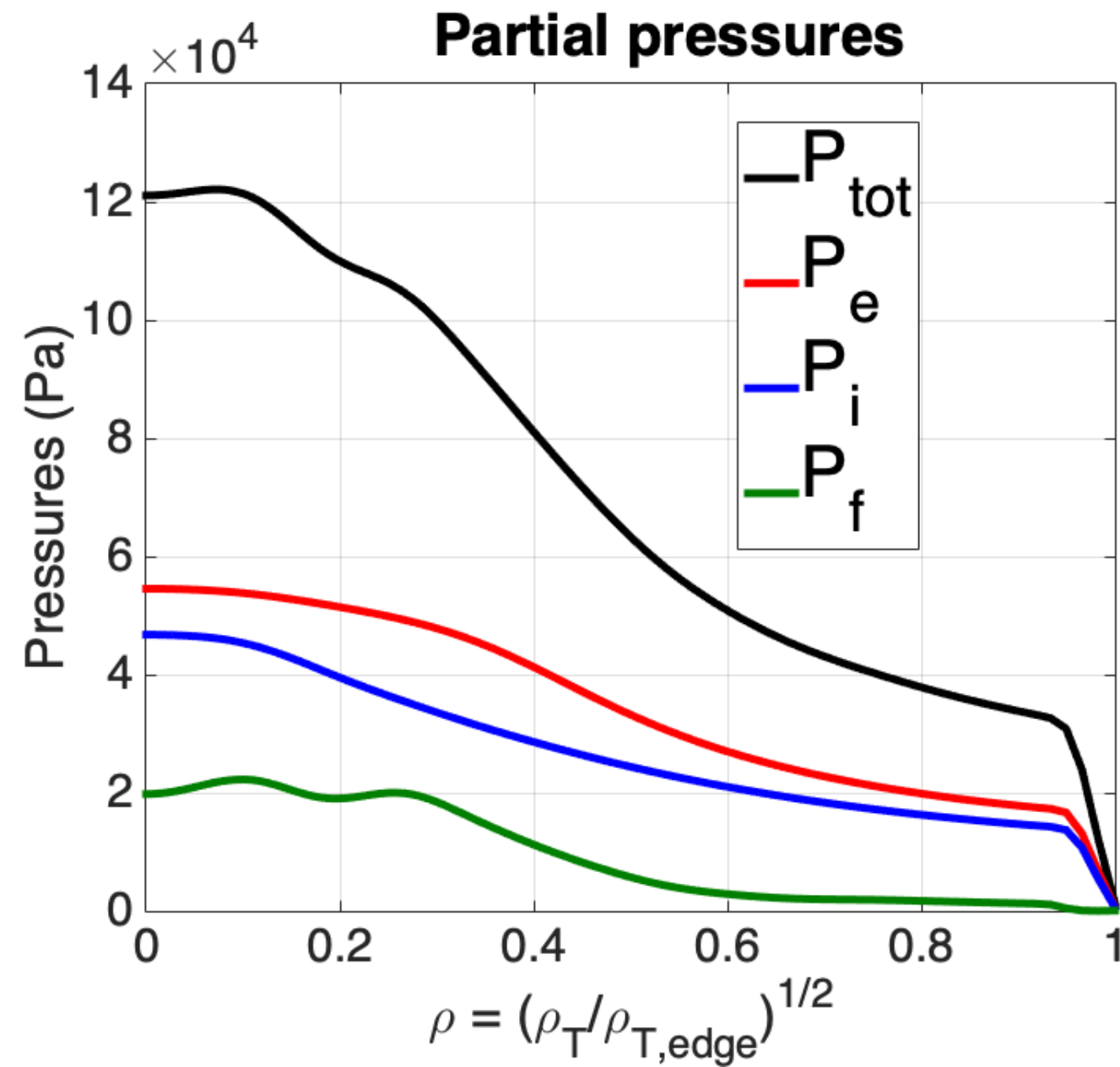
[1] Z. Lin et al. 1998, *Science* [4] Z. Qiu et al. 2016, *Phys. Plasmas* [7] W. Chen et al. 2016, *Nucl. Fusion* [10] G. Wanling et al. 2023, *Nucl. Fusion*
 [2] Y. Todo et al. 2012, *Nucl. Fusion* [5] S. Günter et al. 2001, *Nucl. Fusion* [8] X. Gao et al. 2018, *Phys. Lett. A* [11] M.N. Rosenbluth et al. 1998, *PRL*
 [3] L. Chen et al. 2000, *Phys. Plasmas* [6] A.R. Field et al. 2011, *Nucl. Fusion* [9] G. Brochard et al. 2020b, *Nucl. Fusion*

GTC capable of simulating macroscopic modes [1]

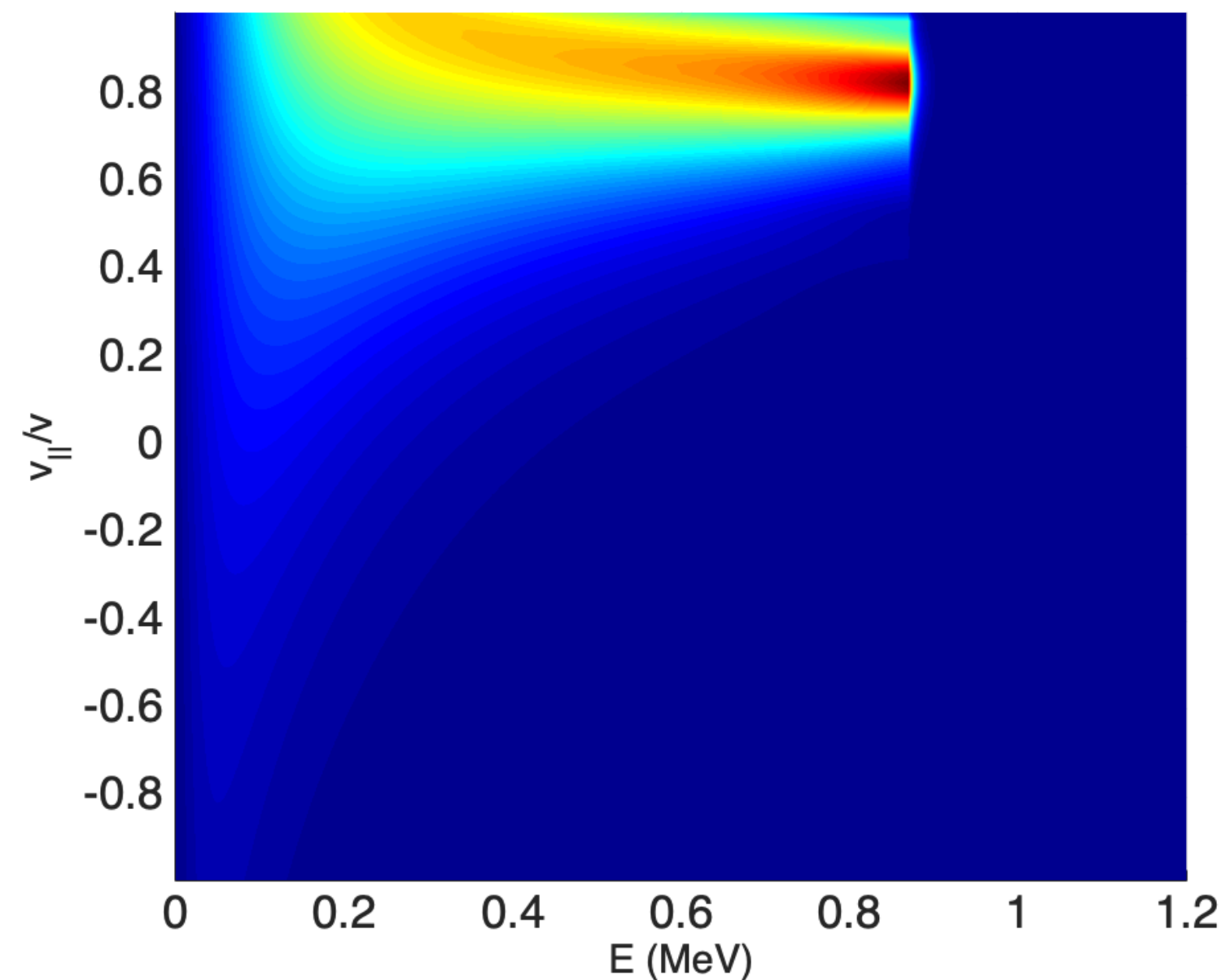


- **GTC** has been **verified** and **linearly validated** for **internal kink instability** in **DIII-D** plasmas
- **Successful benchmark** for **kink growth rate** in **ideal MHD** limit between **GTC** and **kinetic-MHD** codes
- **Linear validation** obtained between **ECE** and δT_e profiles in **GTC** and **XTOR-K** simulations

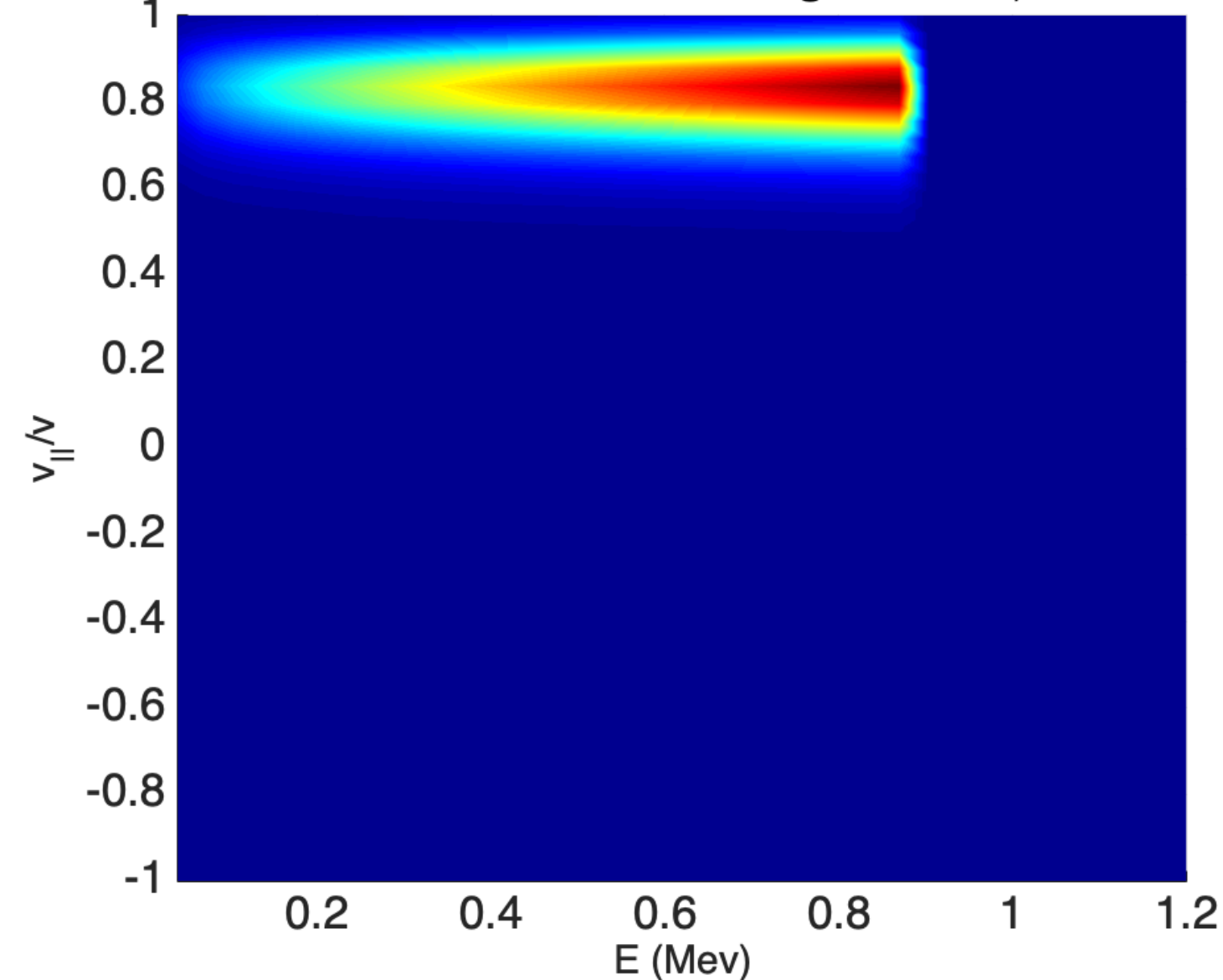
ITER baseline pre-fusion #101006



ASTRA NBI beam, averaged over ψ



GTC NBI beam, averaged over ψ

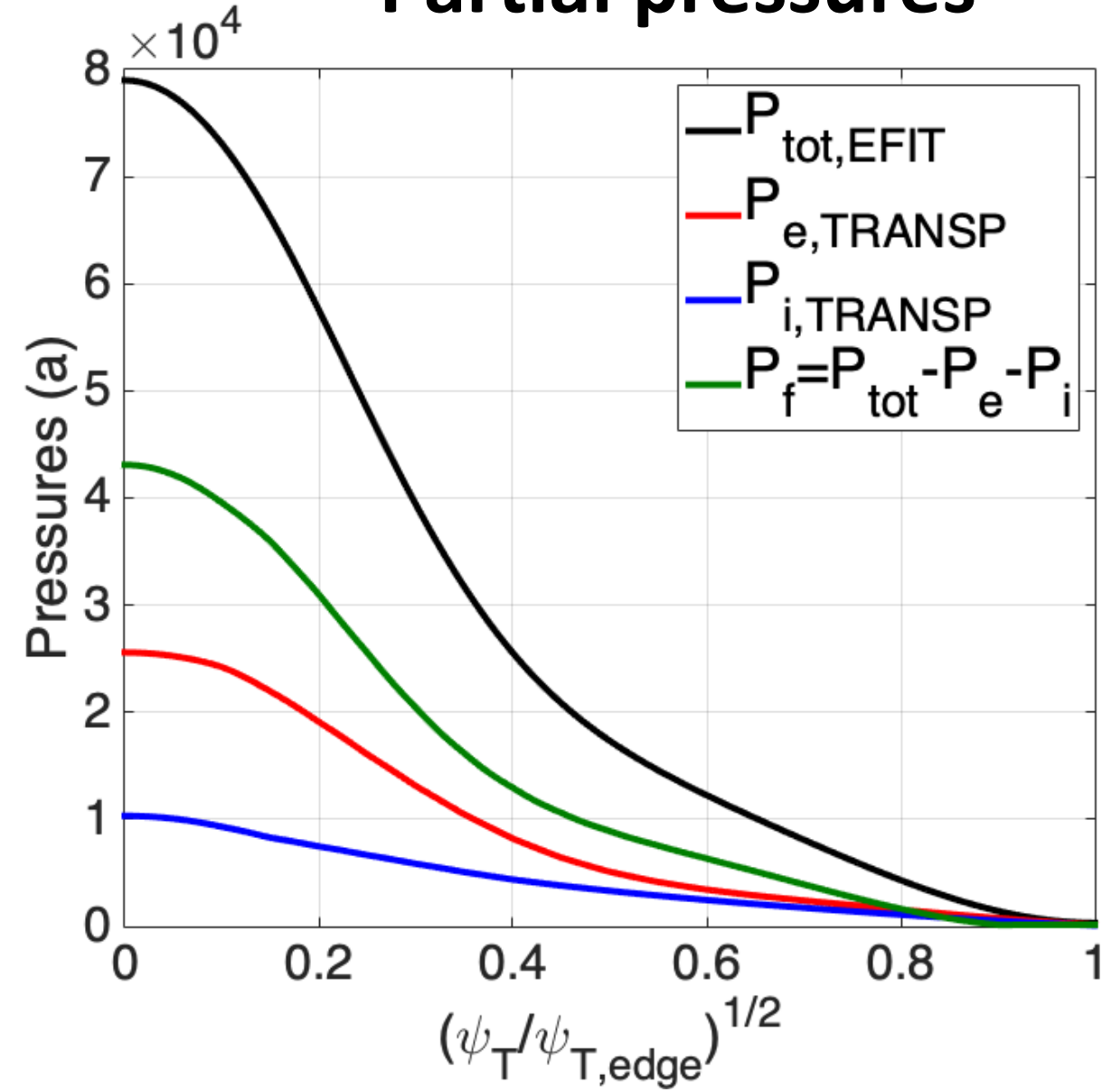


- Analysing **ITER scenarios** as part of **ITPA-EP 15** joint activity and **ISEP US DOE theory milestones 2022**
- **15 codes** from **Europe, US** and **Asia** used to **study EP transport** for **all scales**
- A **baseline pre-fusion** plasma is chosen by IO[1] for **macroscopic** simulations
- Scenario found **ideal MHD stable** [1], but **kinetic effects** need to be included
- **NBI** modeled in **GTC** with a co-passing **anisotropic slowing-down pdf**

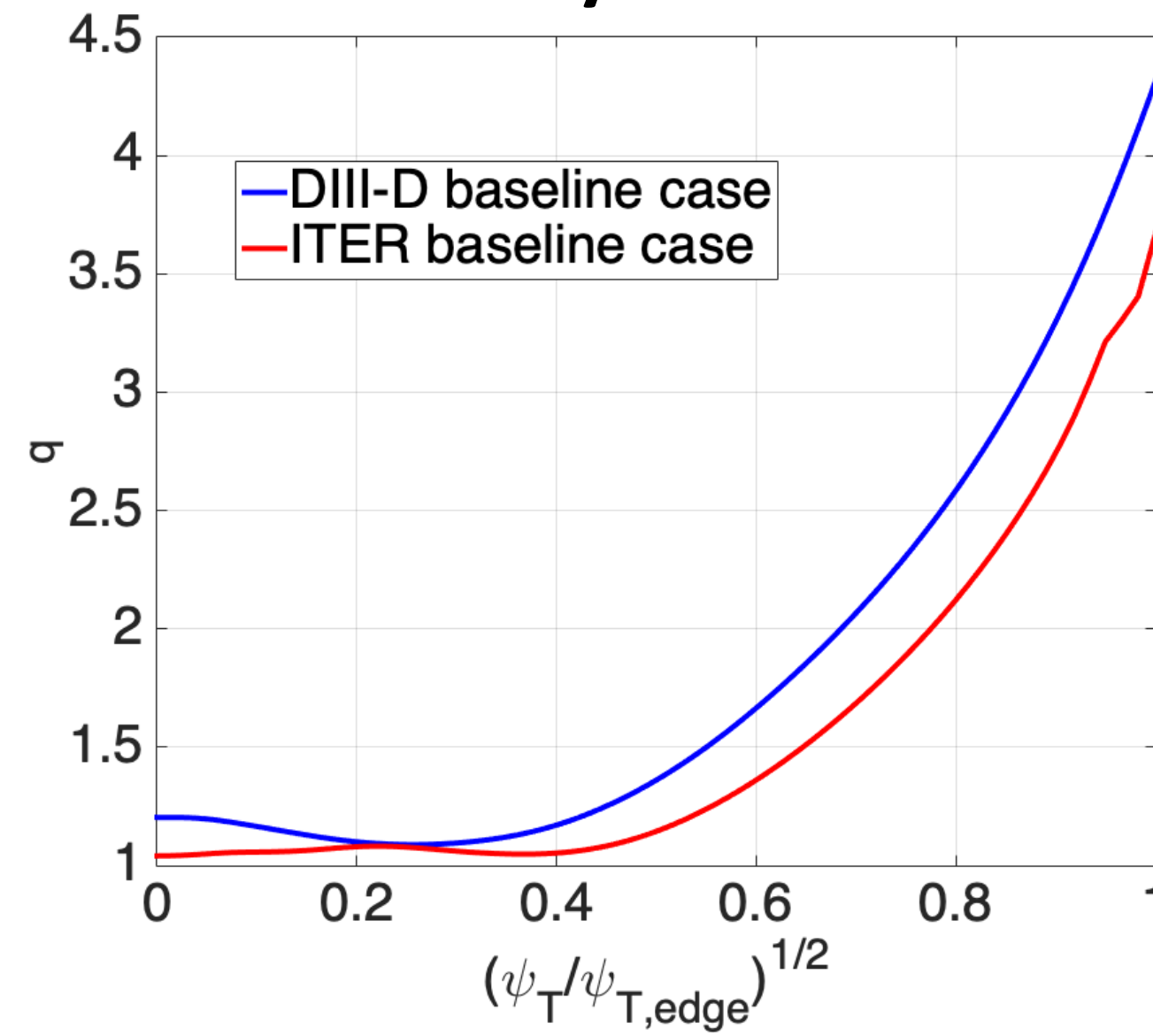
DIII-D discharge #178631 as ITER matching shot



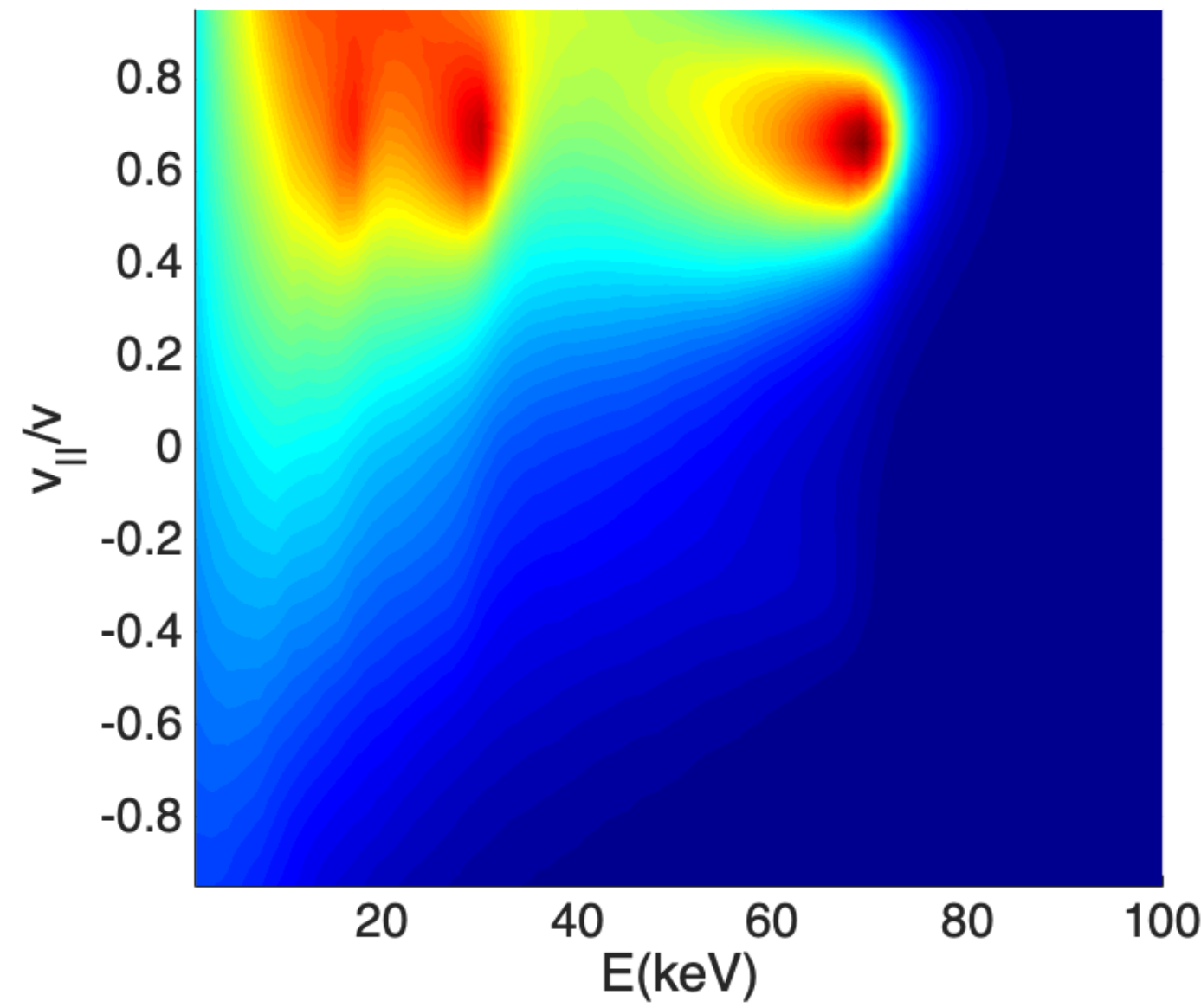
Partial pressures



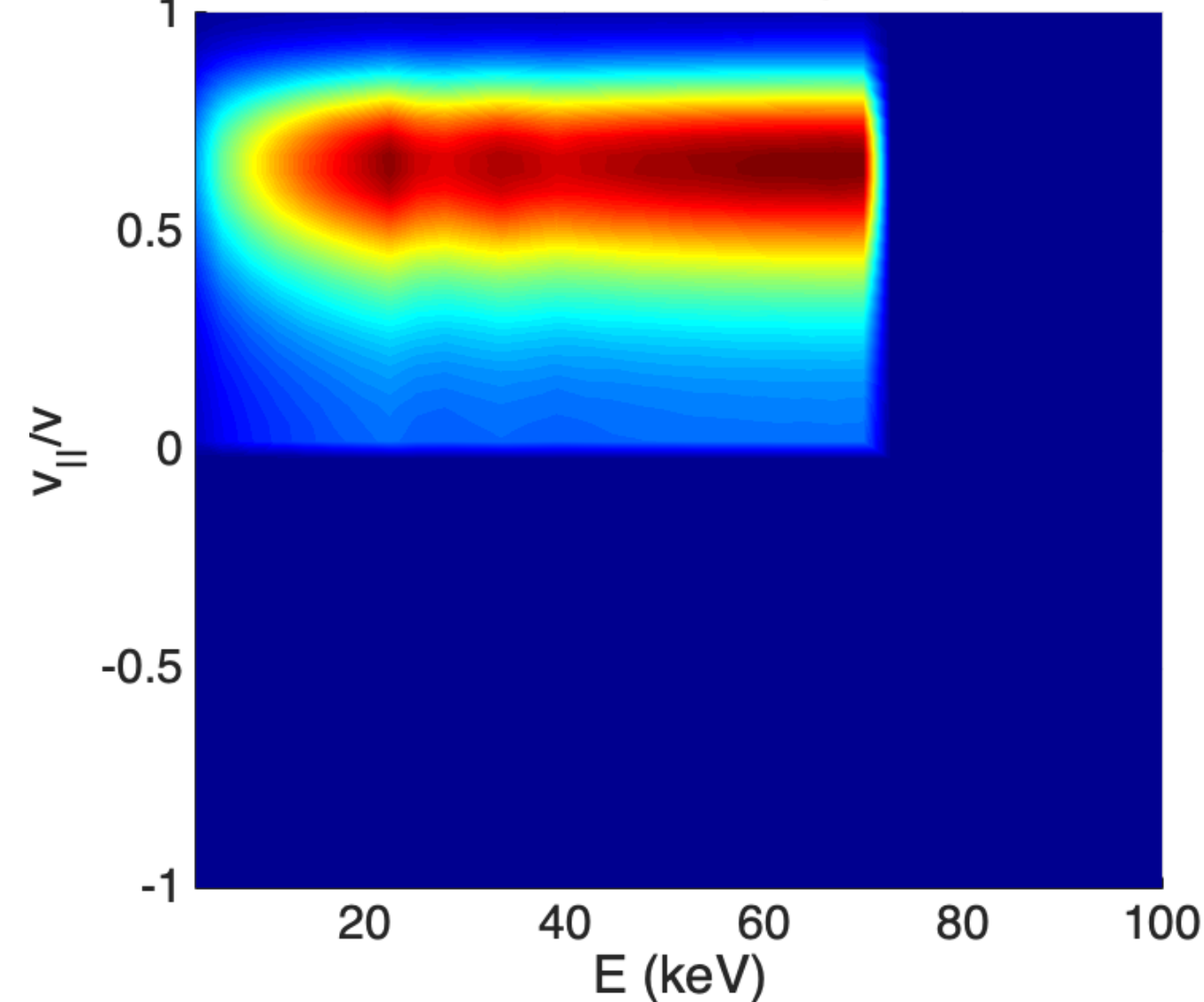
Safety factors



NUBEAM NBI beam, averaged over ψ



GTC NBI beam, averaged over ψ

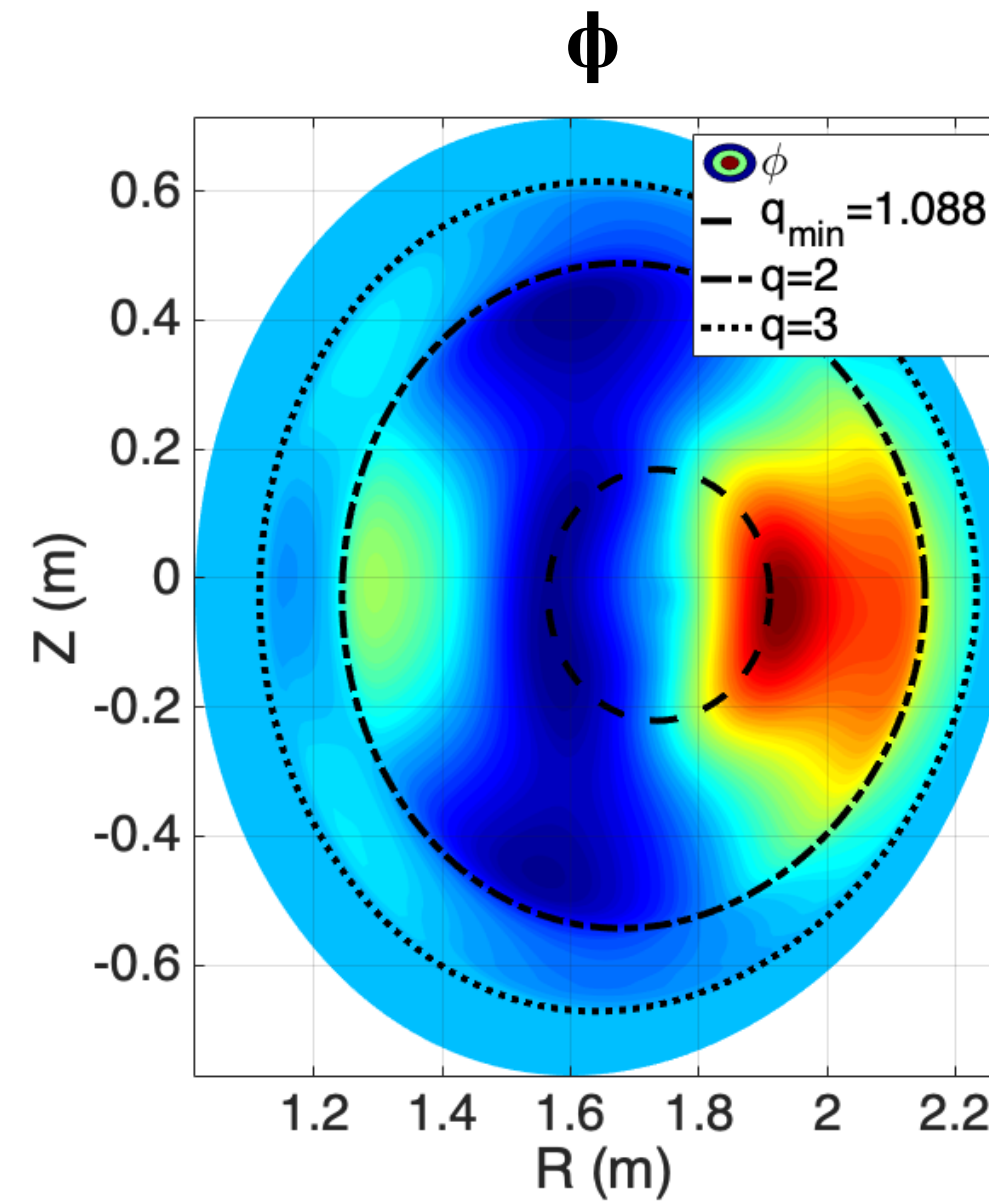
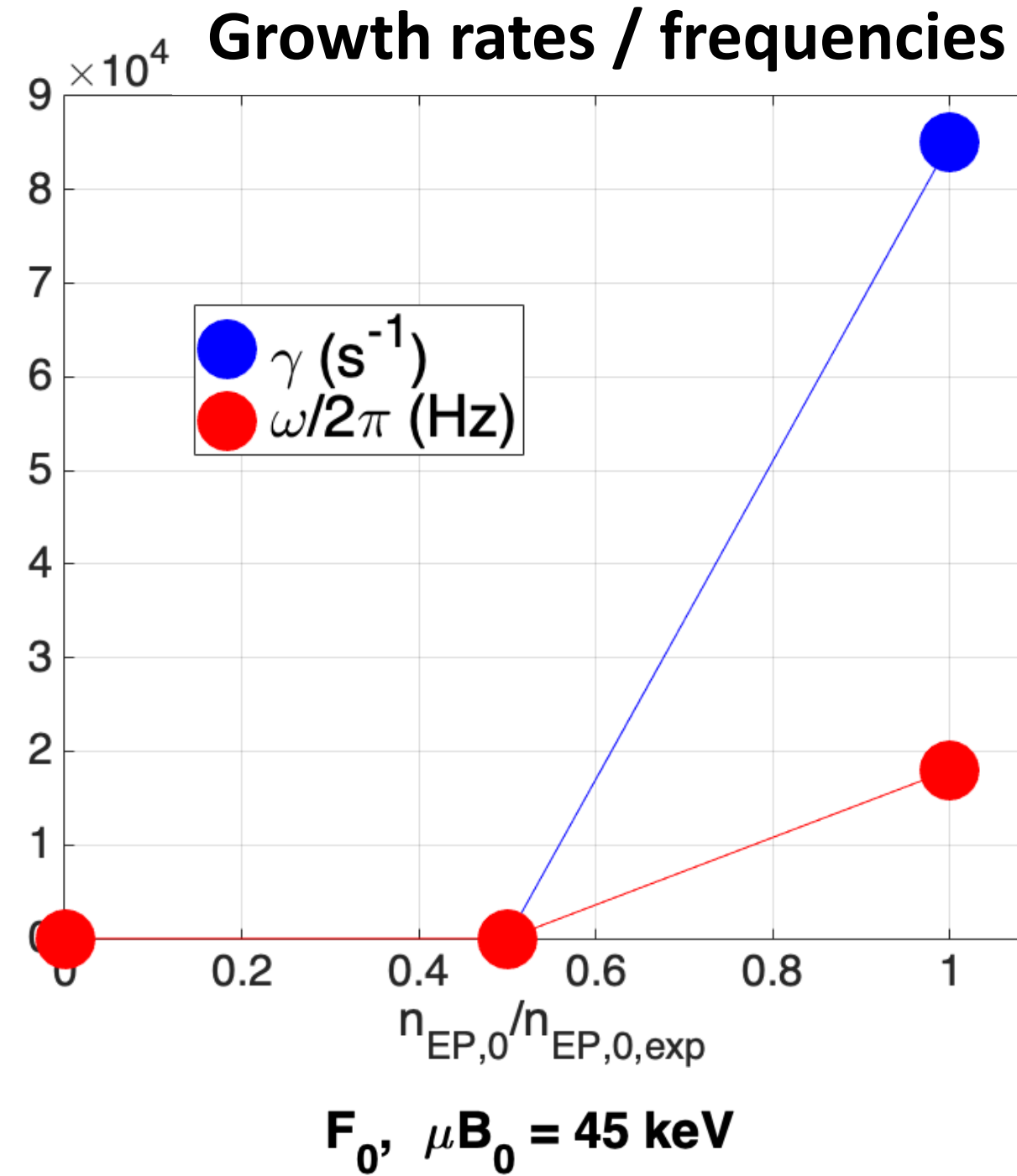


➤ A DIII-D discharge chosen for experimental validation with ITER pre-fusion baseline scenario (similar q , profile shapes and β_N)

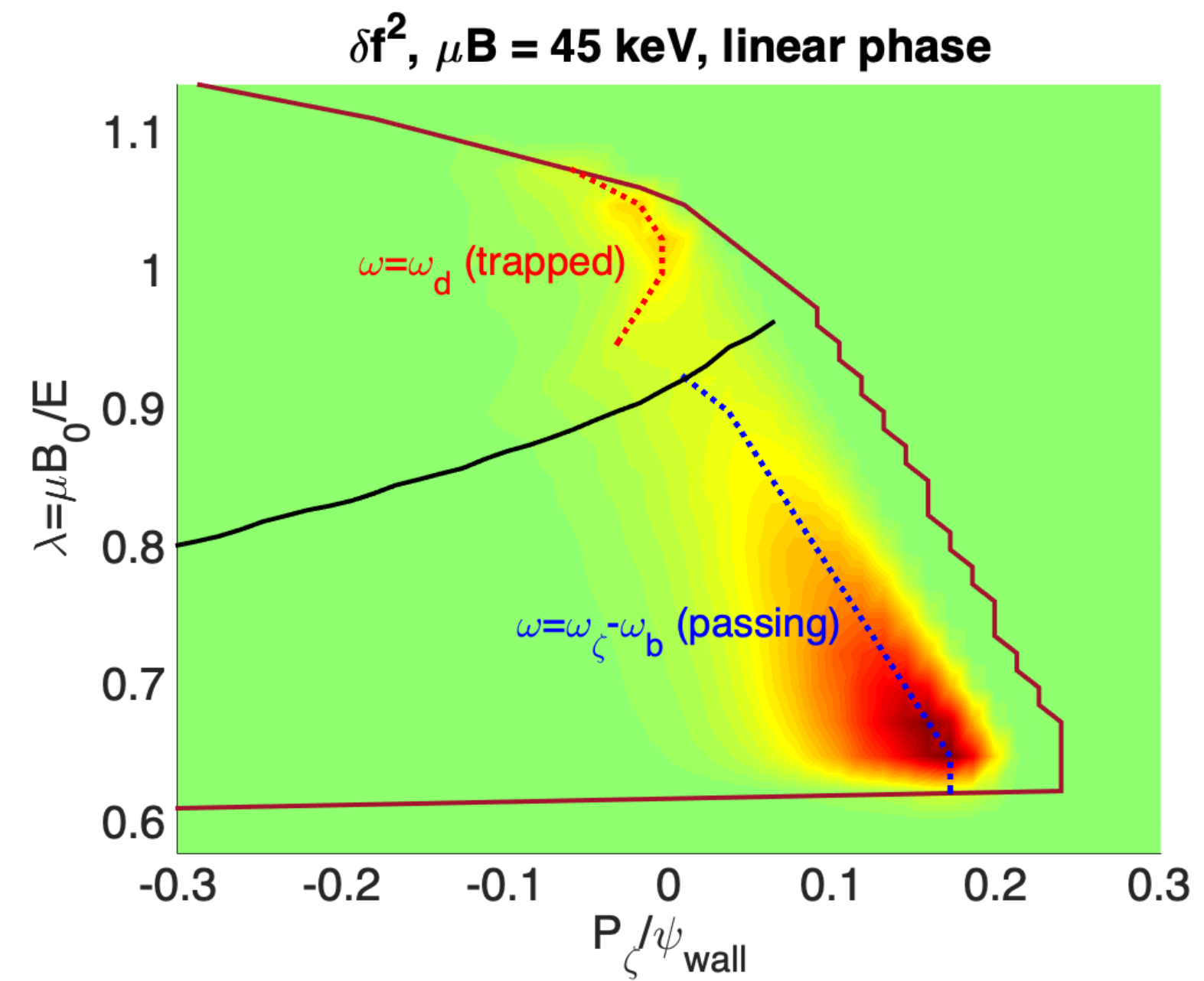
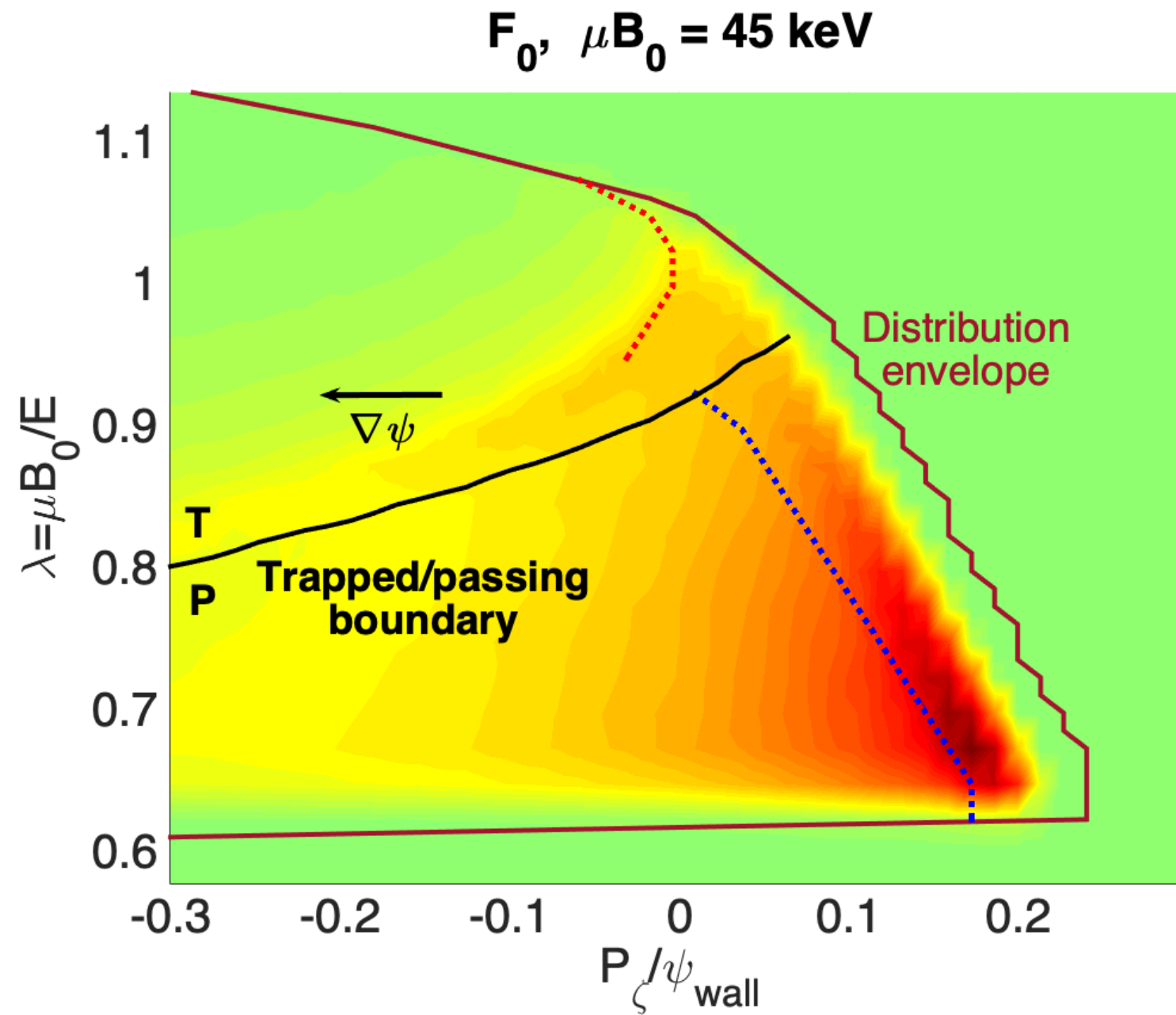
➤ N=1 fishbone modes experimentally observed, with frequencies of order 20kHz

➤ NBI also modeled with an anisotropic slowing-down pdf

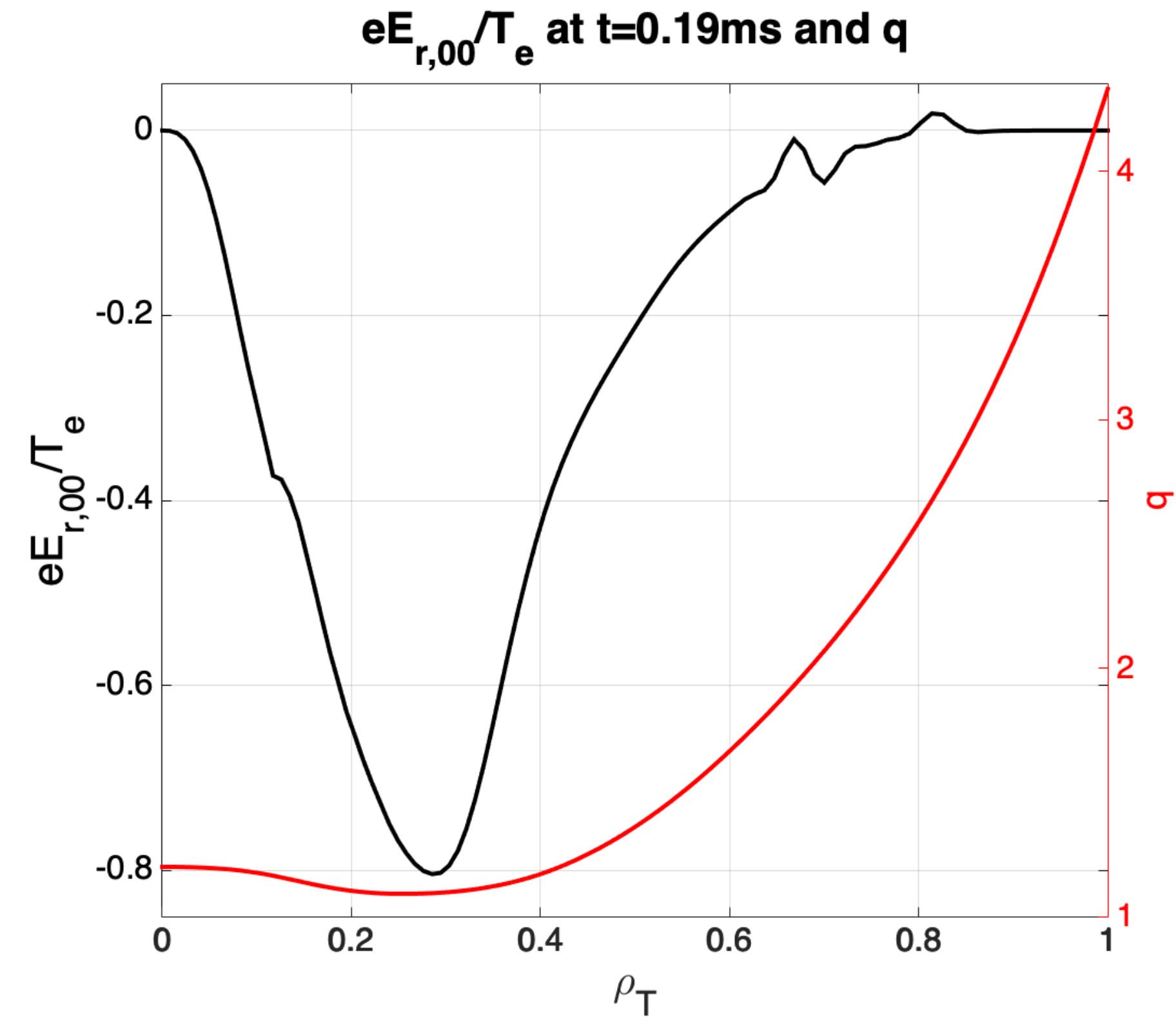
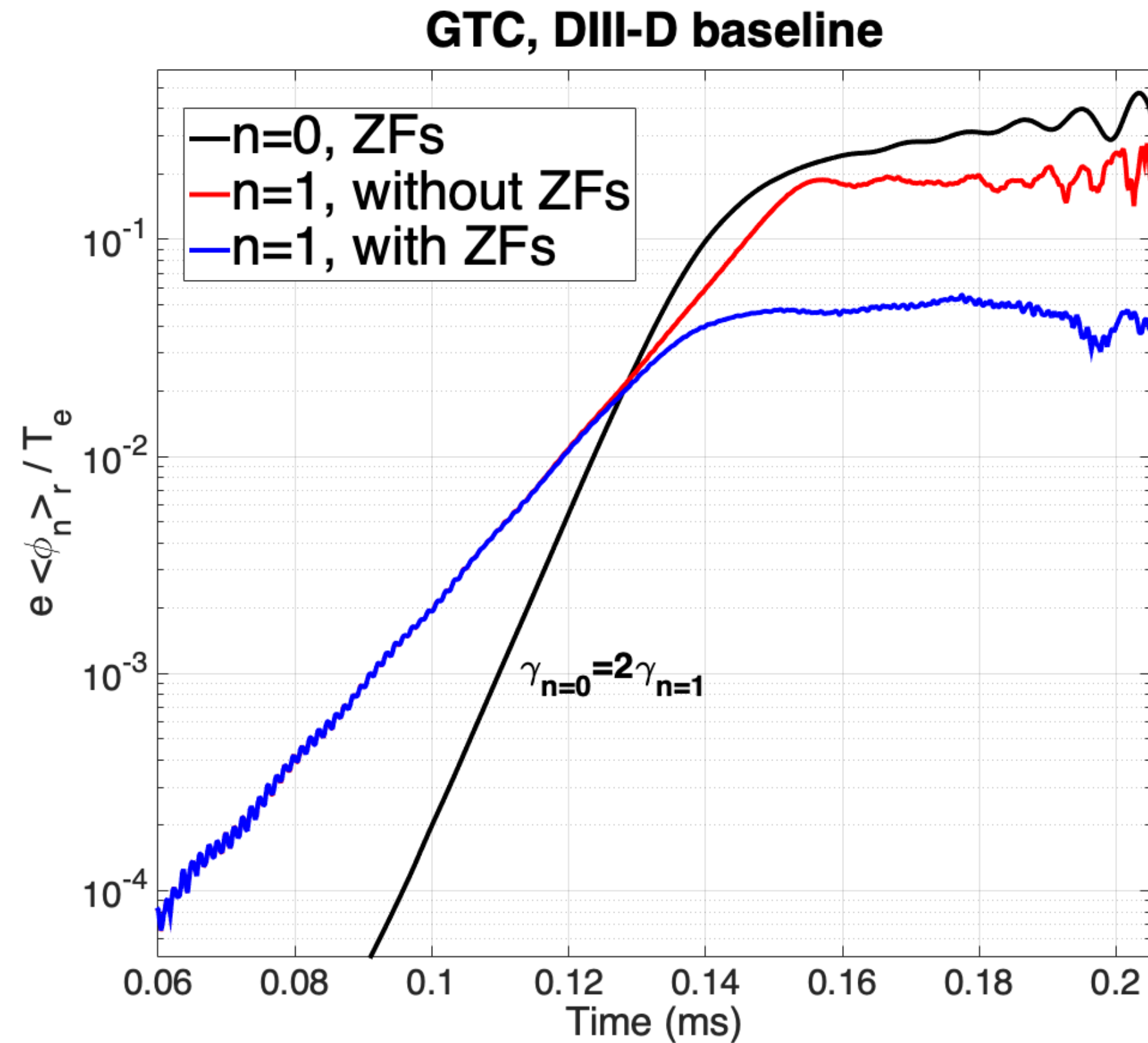
Fishbone unstable for DIII-D discharge



- Low n modes stable with maxwellian EP distributions
- Using realistic beam, a n=1 fishbone mode destabilised past a EP beta, close to marginal stability
- m=2 side-band is significant and extends mode structure close to plasma edge
- Both trapped and passing particles contribute to resonant interaction
- Resonant contribution from passing particles is dominant

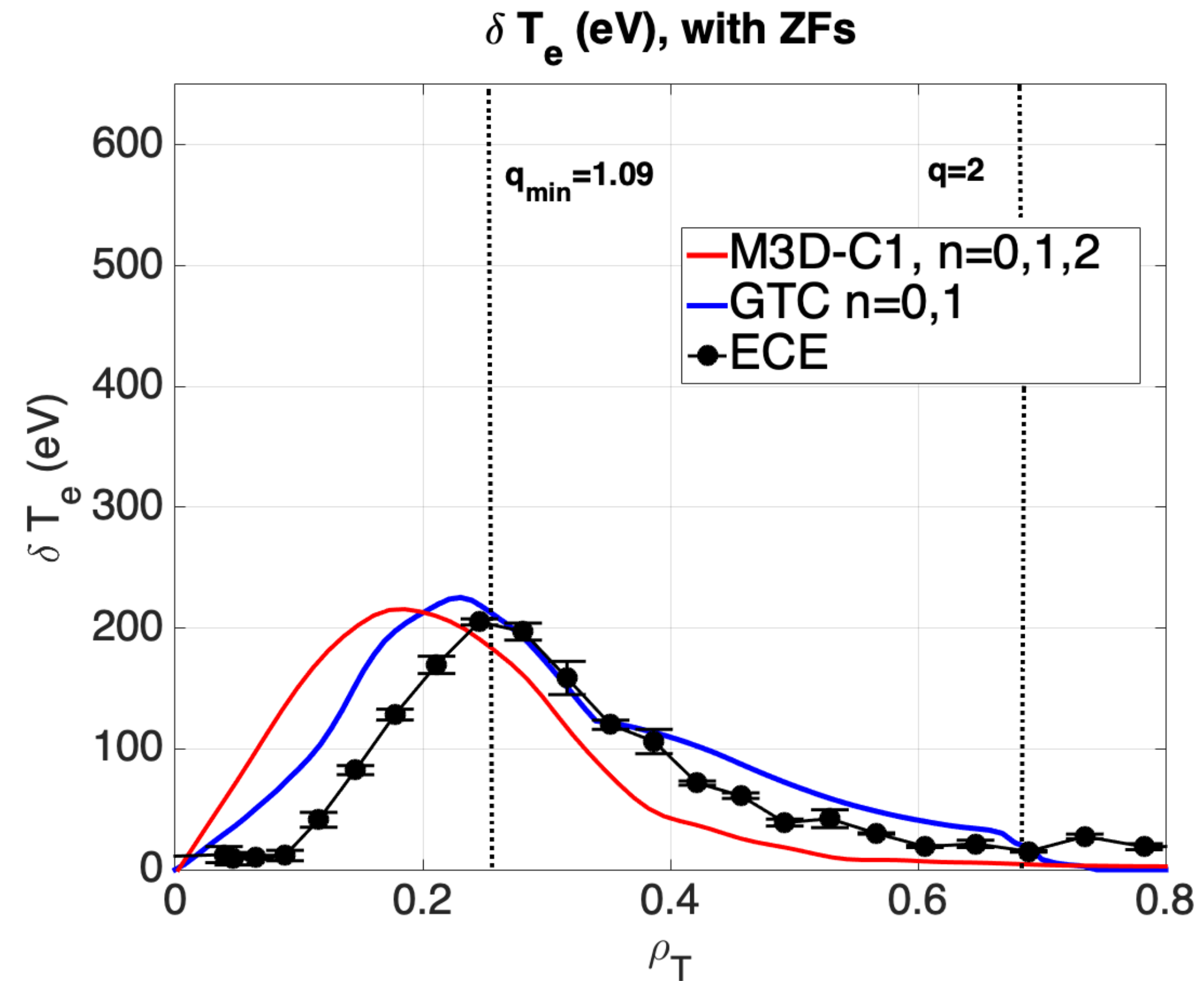
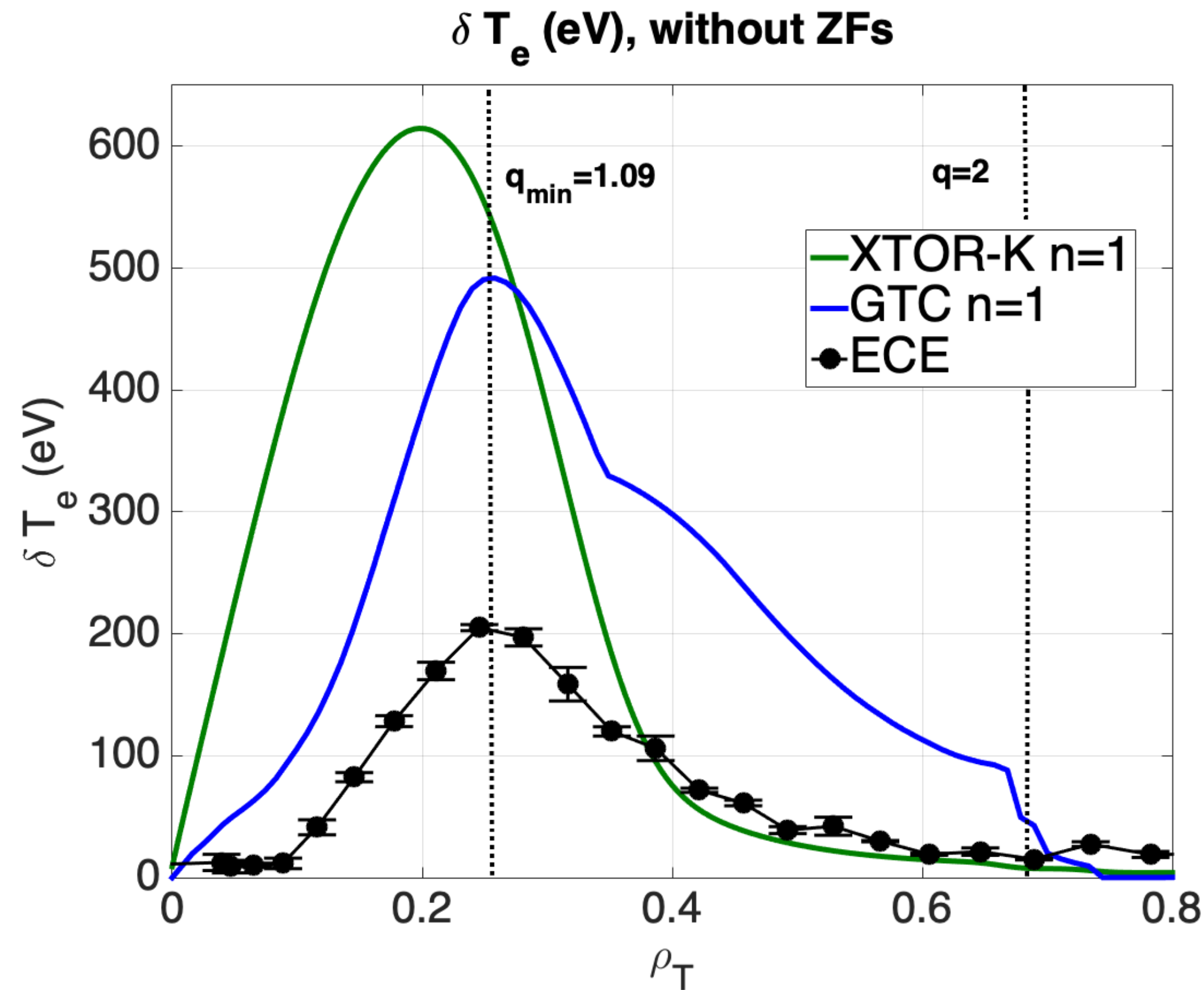


Zonal flows lower fishbone saturation amplitude



- Nonlinear GTC simulations performed keeping **only $n=1$ mode, with and without zonal flows**
- ZFs inclusion significantly **lowers saturation amplitude**, from $|\delta B/B_0| \sim 8 \times 10^{-3}$ to 2×10^{-3} at q_{min} , highlighting that **wave-particle trapping is not always the main saturation mechanism for fishbones**
- ZFs have a **growth rate twice of $n=1$ mode**, typical of force-driven ZFs generation [1]

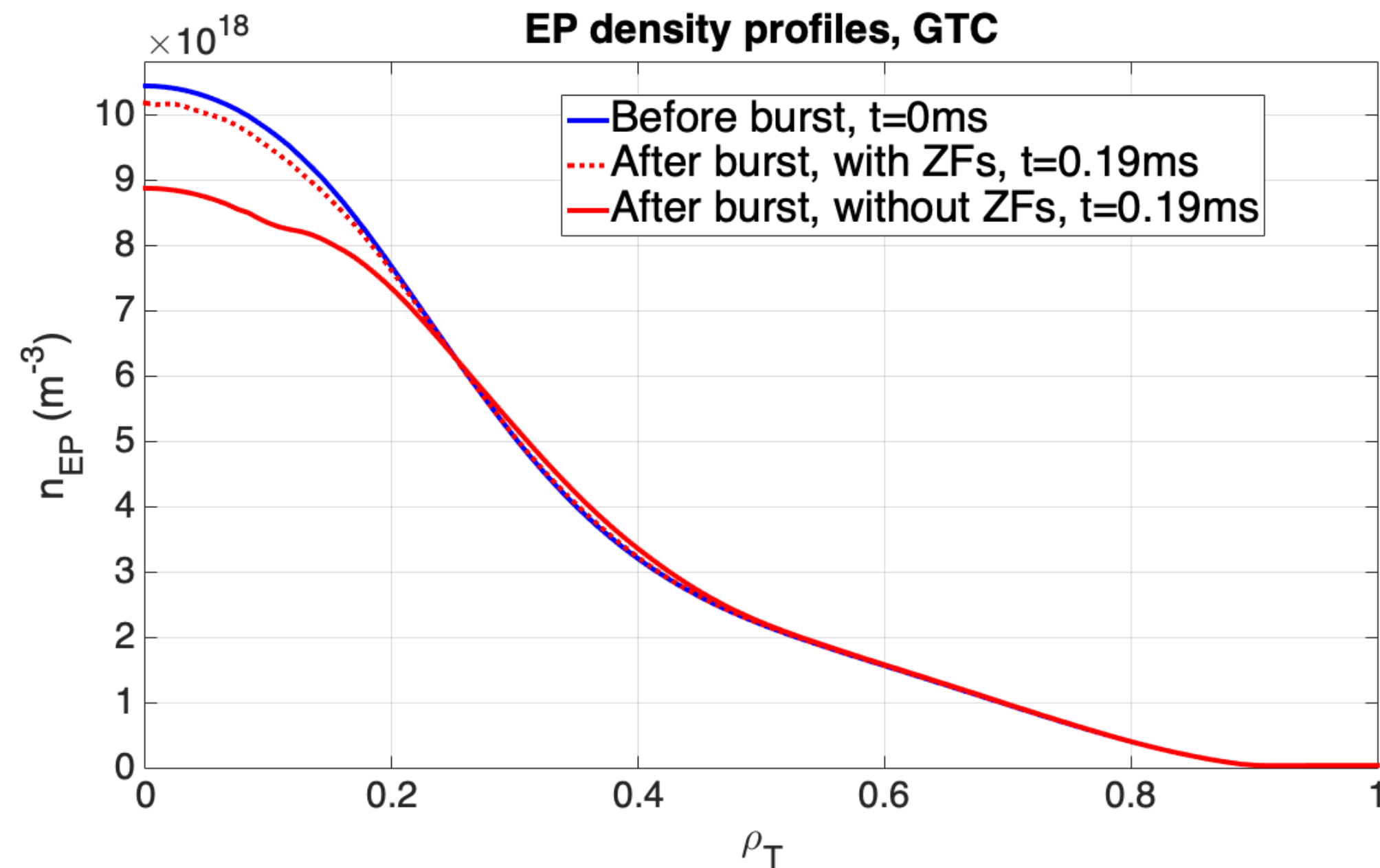
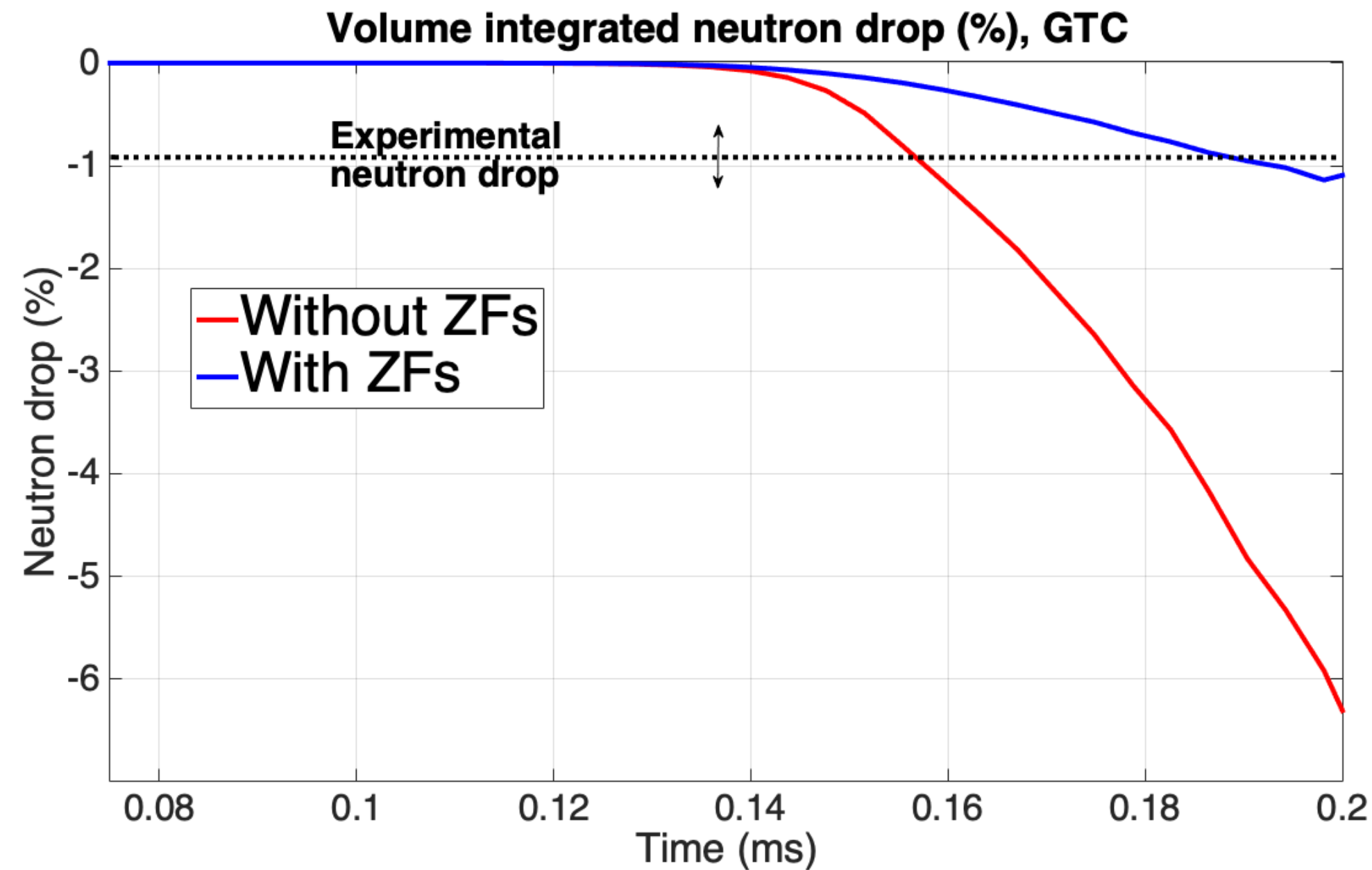
Nonlinear validation against ECE measurements



- Zonal flows inclusion allow GTC and M3D-C1 to obtain saturation amplitudes comparable with ECE [1]
- The significant $m=2$ side-band allows GTC to obtain a quantitative agreement with the ECE
- Validation to be completed with cross-scales GTC simulation for more realistic zonal flows levels

[1] G. Brochard et al. 2022, to be submitted to *Phys. Rev. Lett.*

Outward EP transport and neutron drop

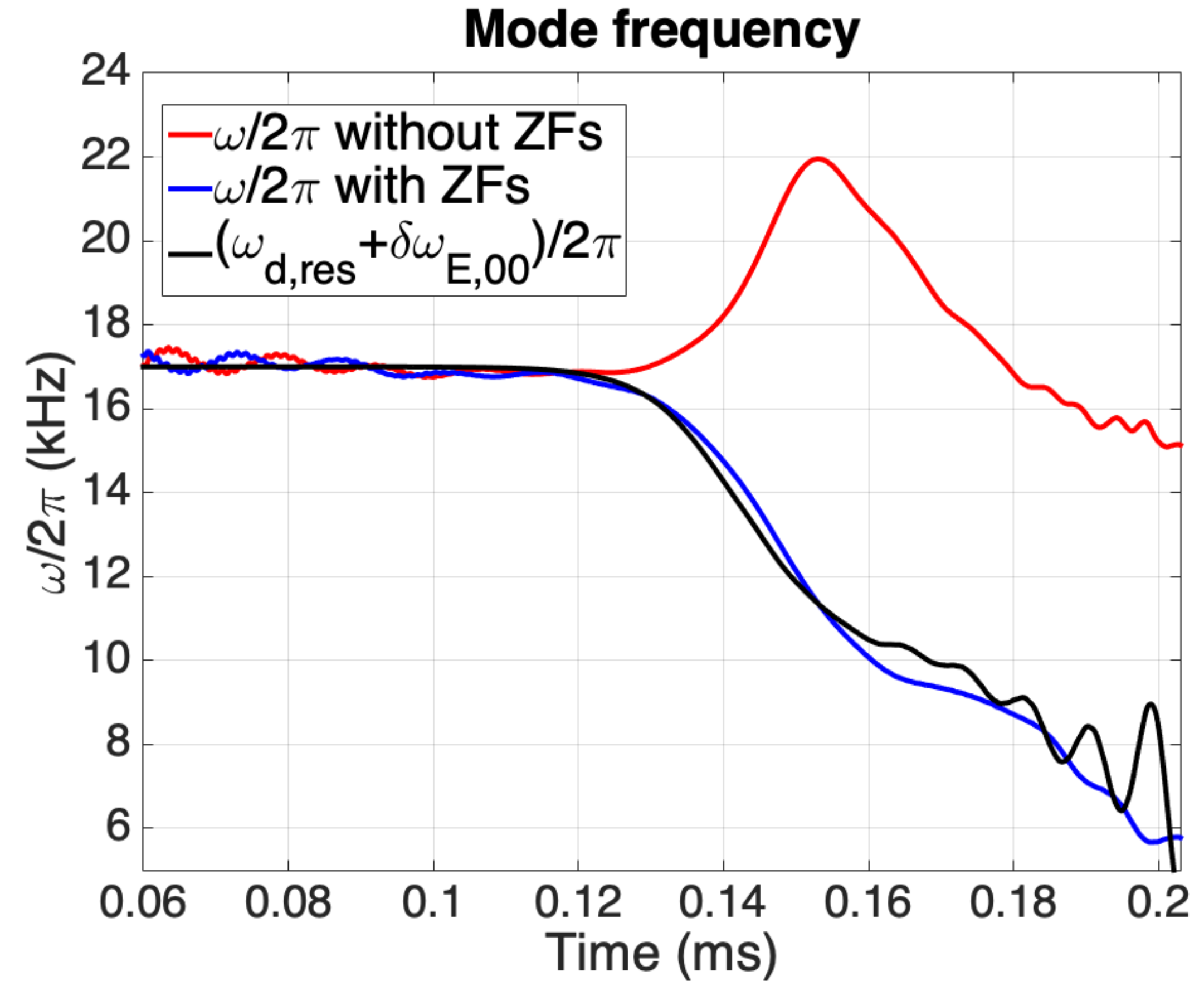
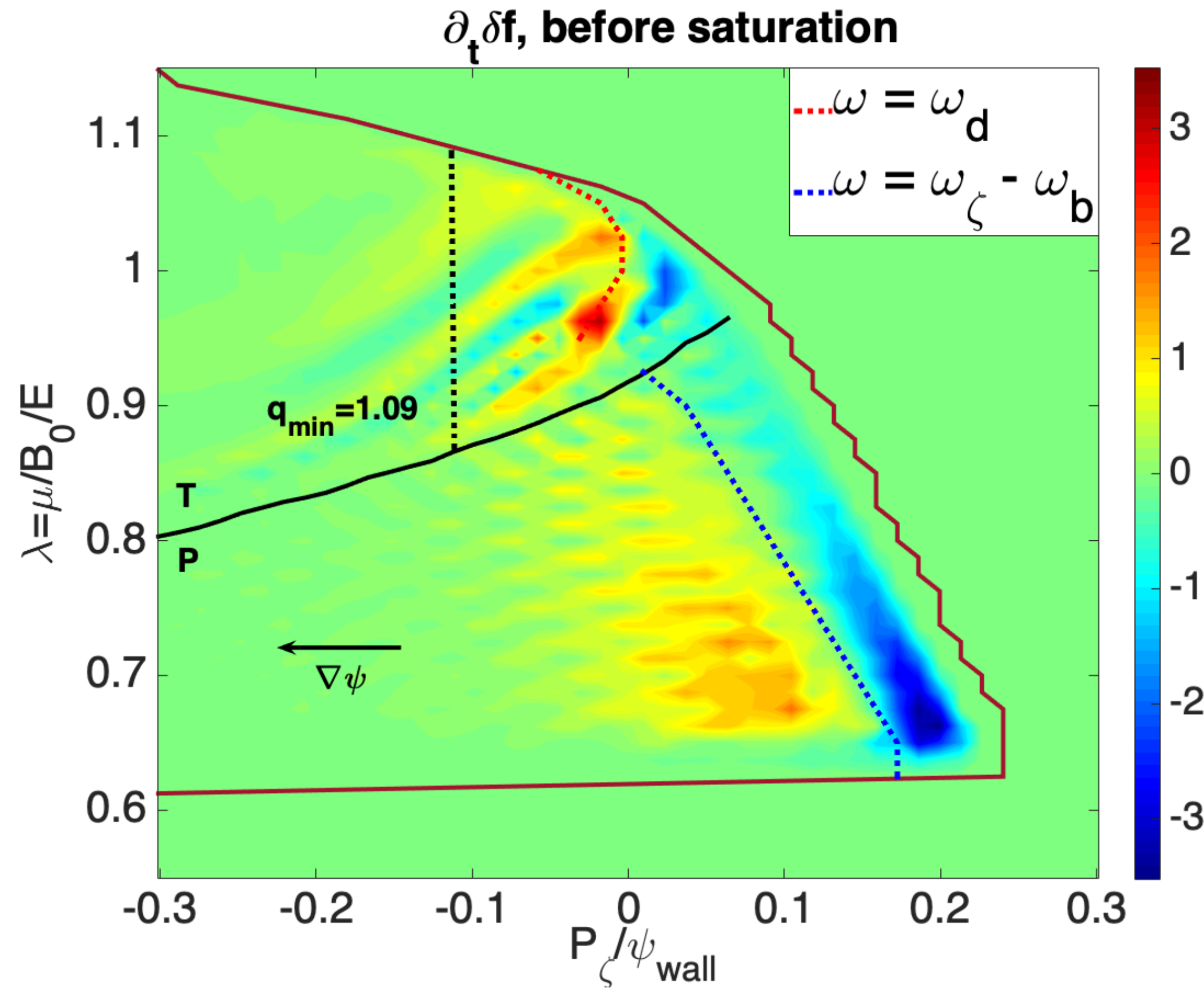


➤ Zonal flows also lowers the simulated neutron drop, providing a quantitative agreement with the experimental one, further validating GTC for fishbone simulations

➤ The EP density profile is flattened due to resonant transport ($|\delta n_{EP}/n_{EP}| \sim 15\%$ inside q_{min} without zonal flows)

➤ Zonal flows inclusion lead to weaker EP transport ($|\delta n_{EP}/n_{EP}| \sim 3\%$ inside q_{min})

Zonal flows generate additional drift for EPs

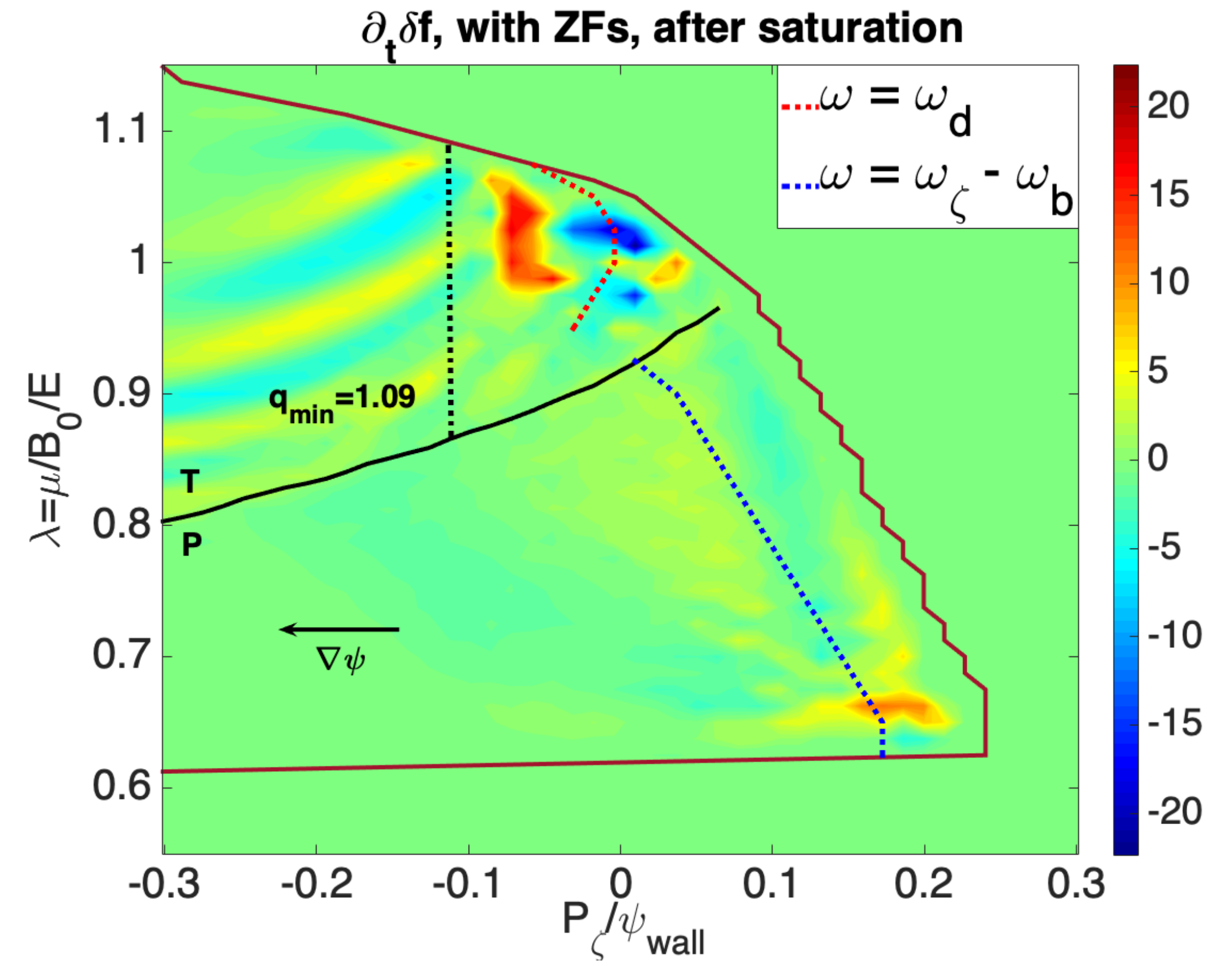
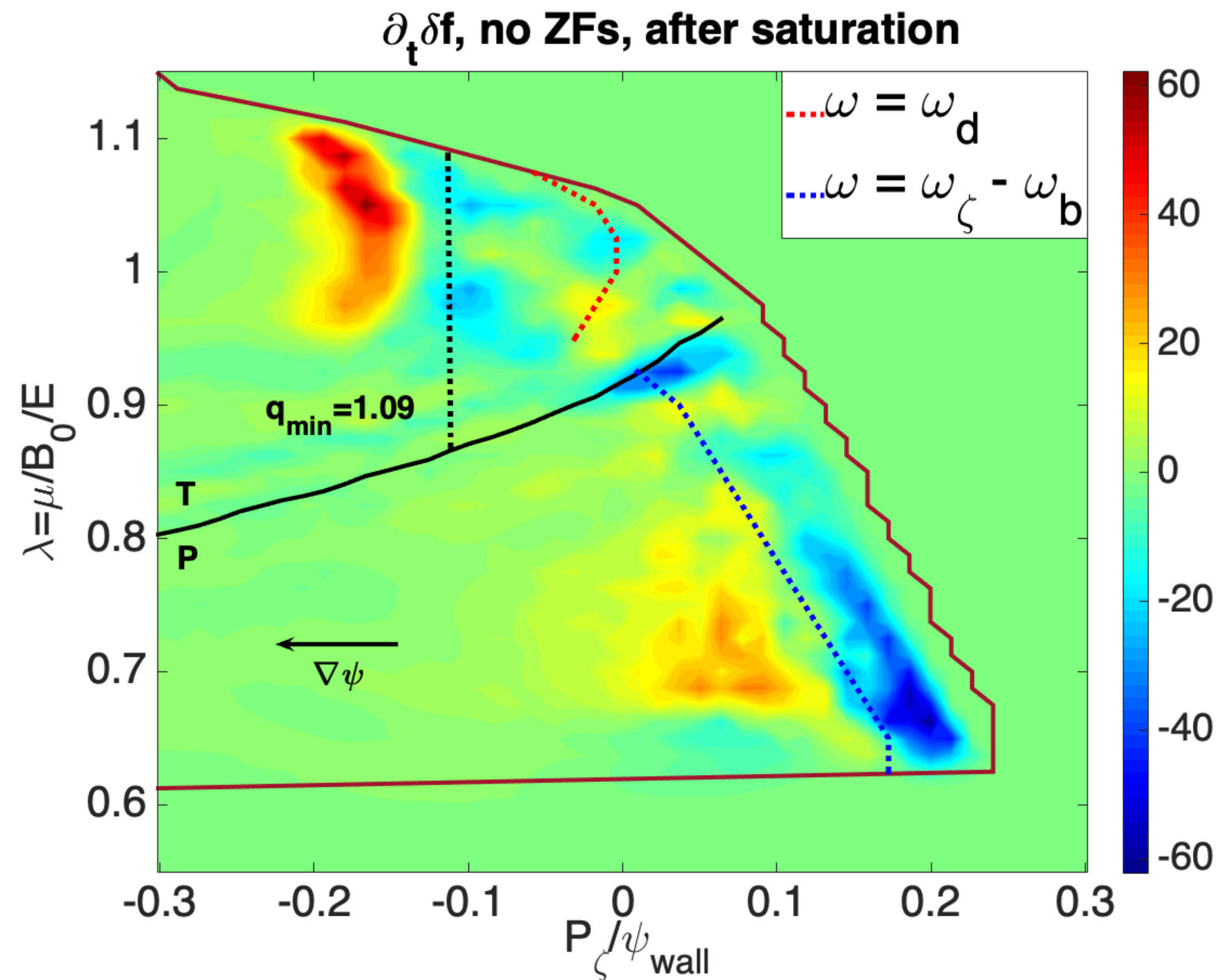


➤ **Hole and clump** structures appear around both **trapped** and **passing resonances**

➤ Fishbone frequencies chirp down at saturation with and without ZFs

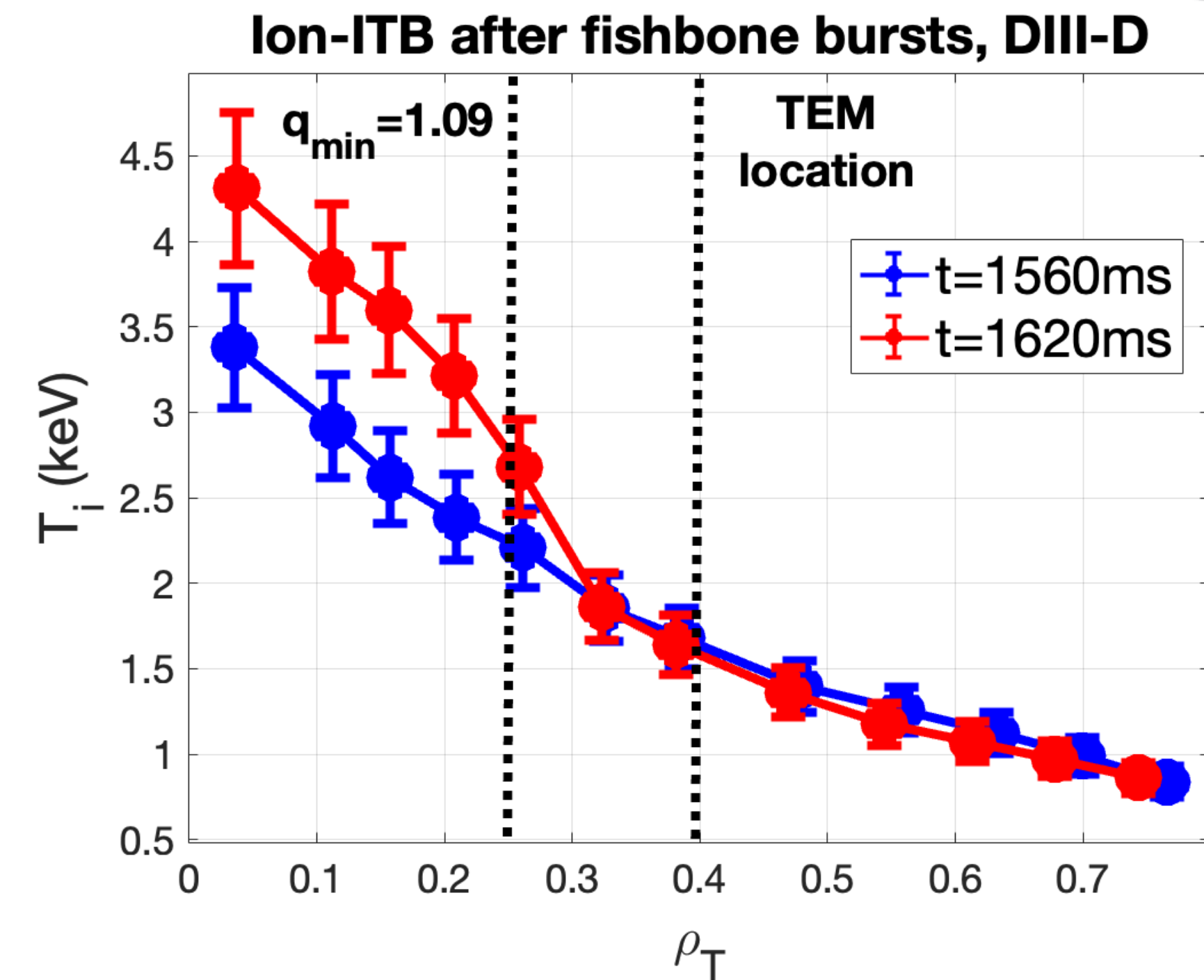
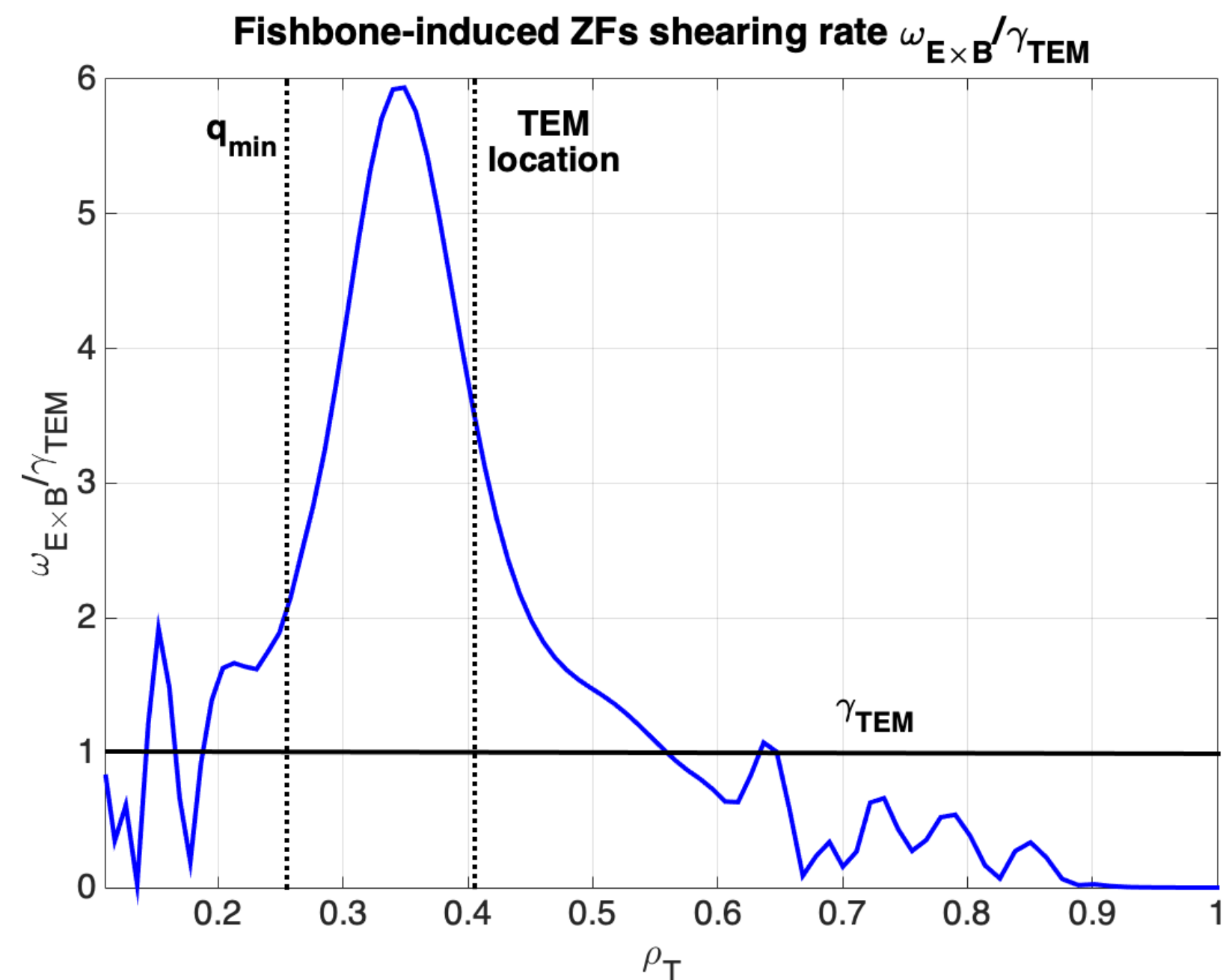
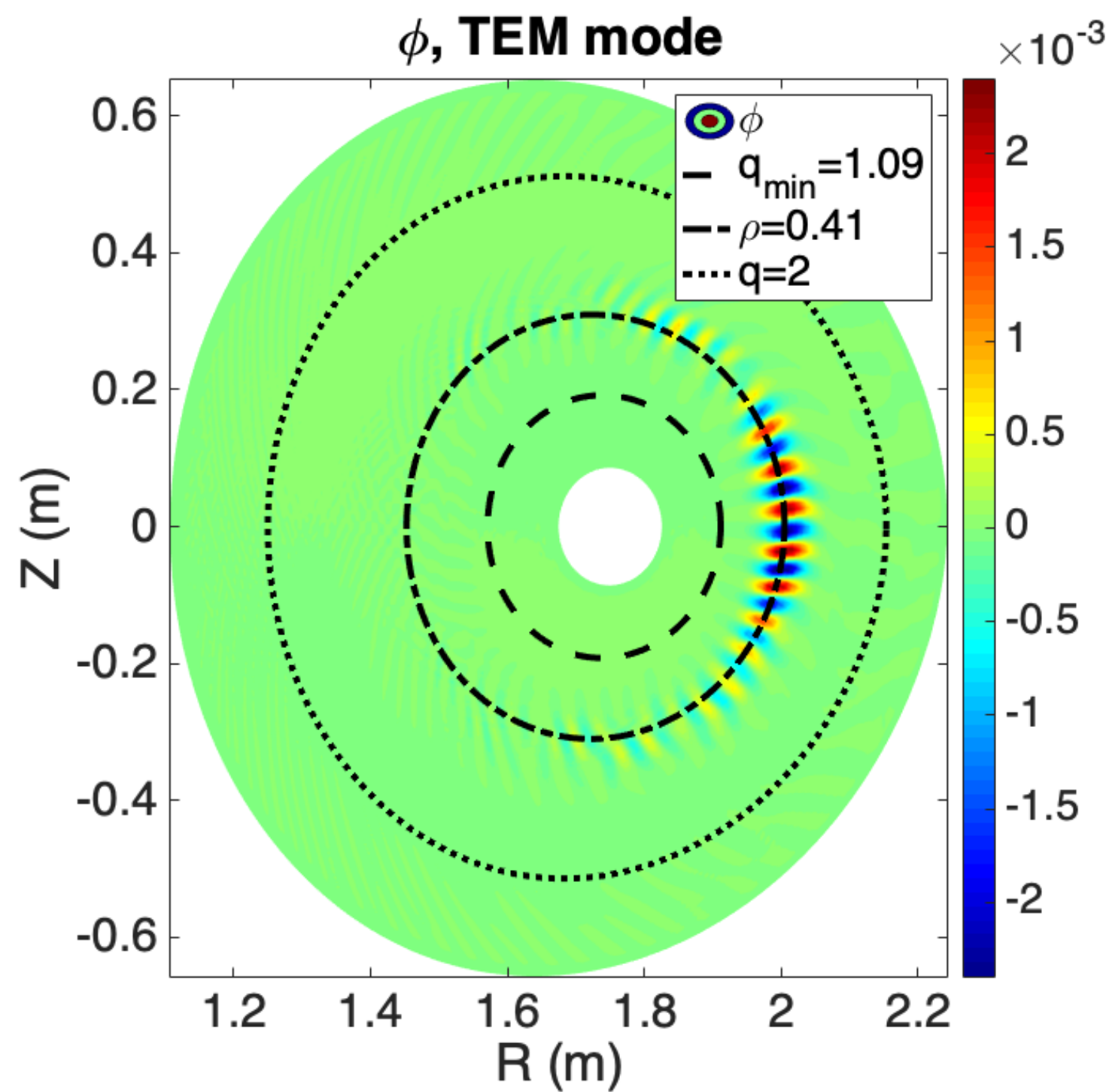
➤ ZFs provide an additional drift frequency $\delta\omega_{E,00} = -\partial_\psi\phi_{00}$, locking linearly resonant EPs

Zonal flows prevent more EPs to become resonant



- Precessional hole and clump stays indeed static with zonal flows, reducing
- Resonant passing EPs are detuned by ZFs, potentially due to ZFs effects on transit frequency
- ZFs prevent phase space structures from affecting new EPs, explaining fishbone mitigation by ZFs

Fishbone-induced ZFs can lead to ion-ITB



- GTC electrostatic simulations find an **unstable TEM mode** at $\rho = 0.41$ with $\gamma_{TEM} = 1.38 \times 10^5 s^{-1}$
- Fishbone-induced $\omega_{E \times B}$ much larger at saturation than γ_{TEM} , which can lead to **turbulence suppression**
- Ion-ITB observed in **DIII-D** after **fishbone bursts** occurring at $t \in [1580, 1620]$ ms, as in ASDEX [1], MAST [2], HL-2A [3], EAST [4]
- **Cross-scales** GTC simulations with $n \in [0, 50]$ required to confirm **fishbone-induced ITB**

[1] S. Günter et al. *Nucl. Fusion*, 2001

[2] A. R. Field et al., *Nucl. Fusion* 2011

[3] W. Chen et al. *Nucl. Fusion*, 2016

[4] X. Gao et al. *Physics Letters A* 2018

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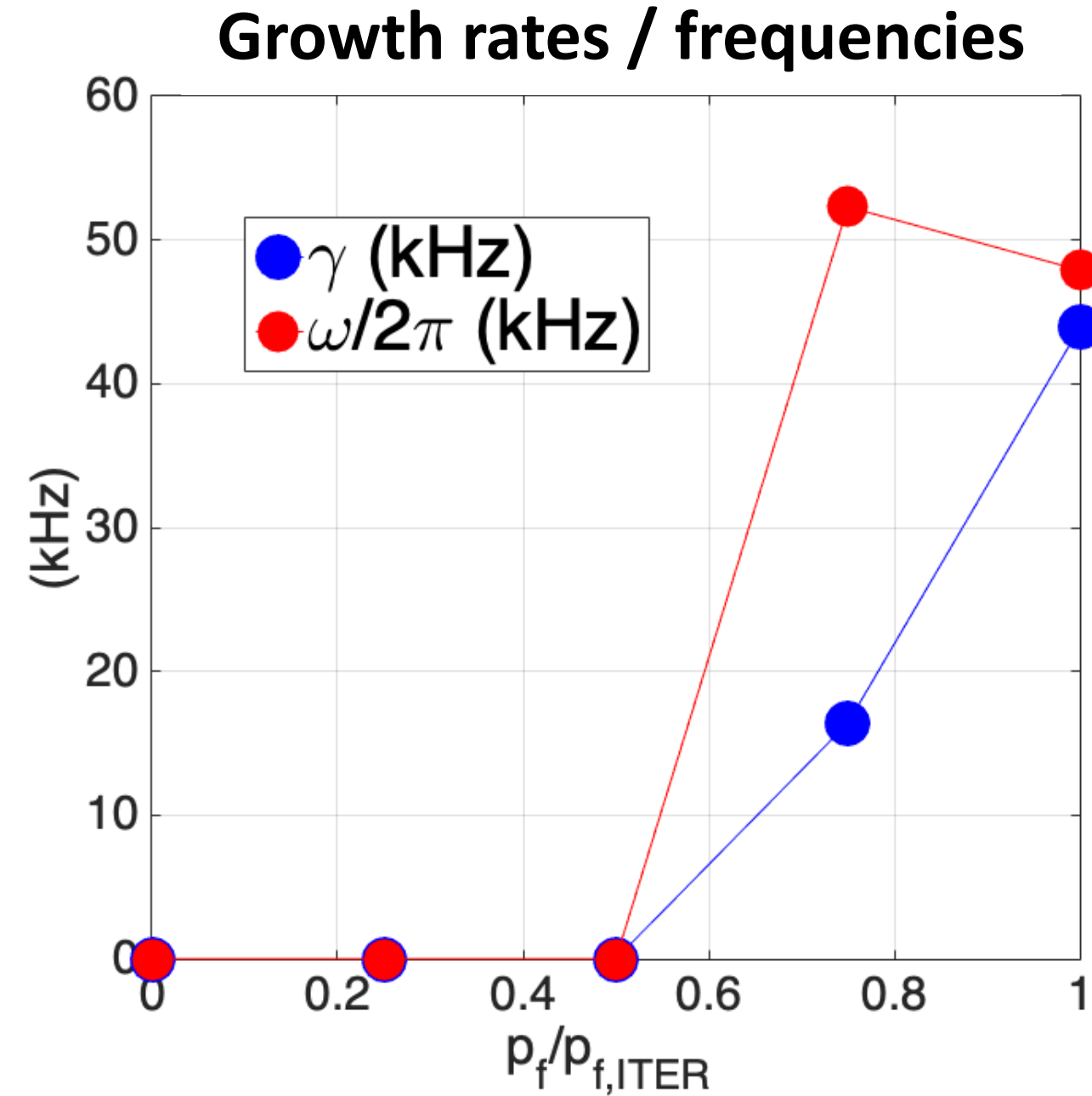
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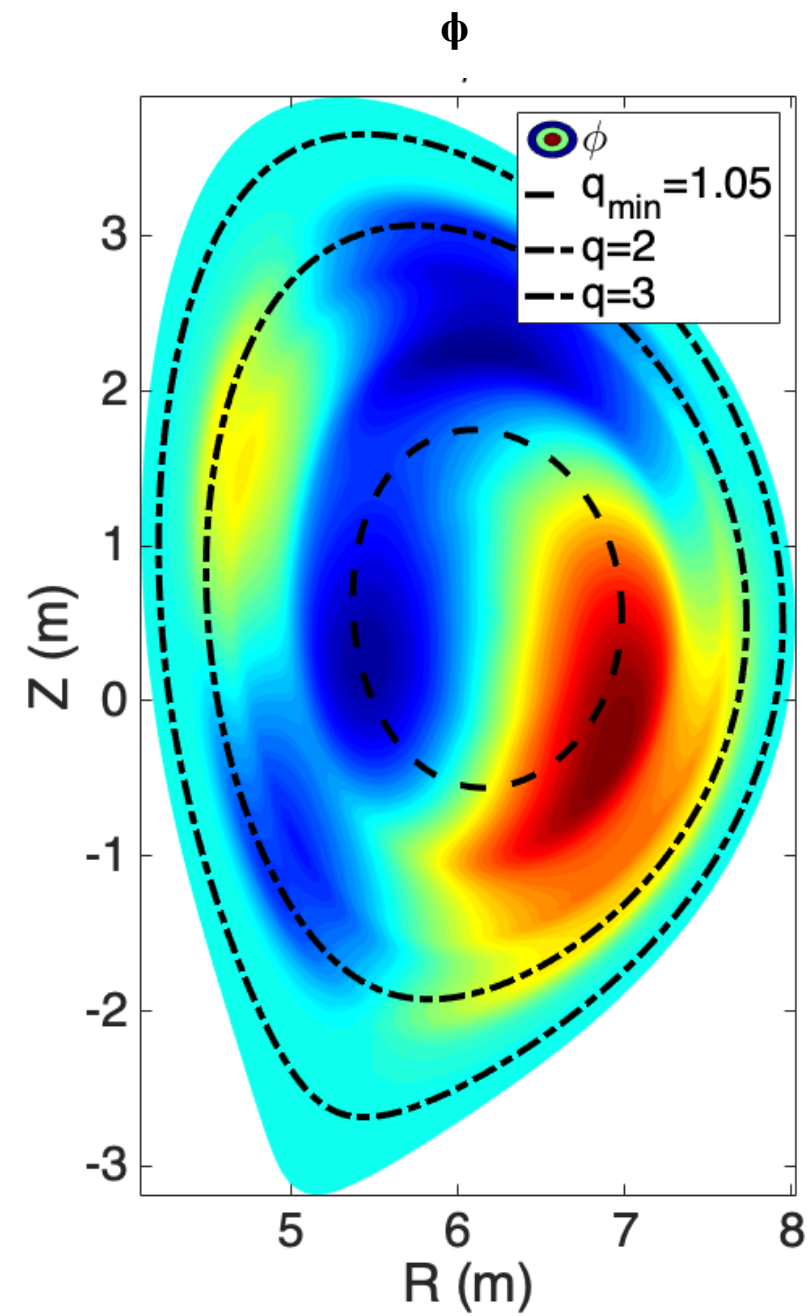
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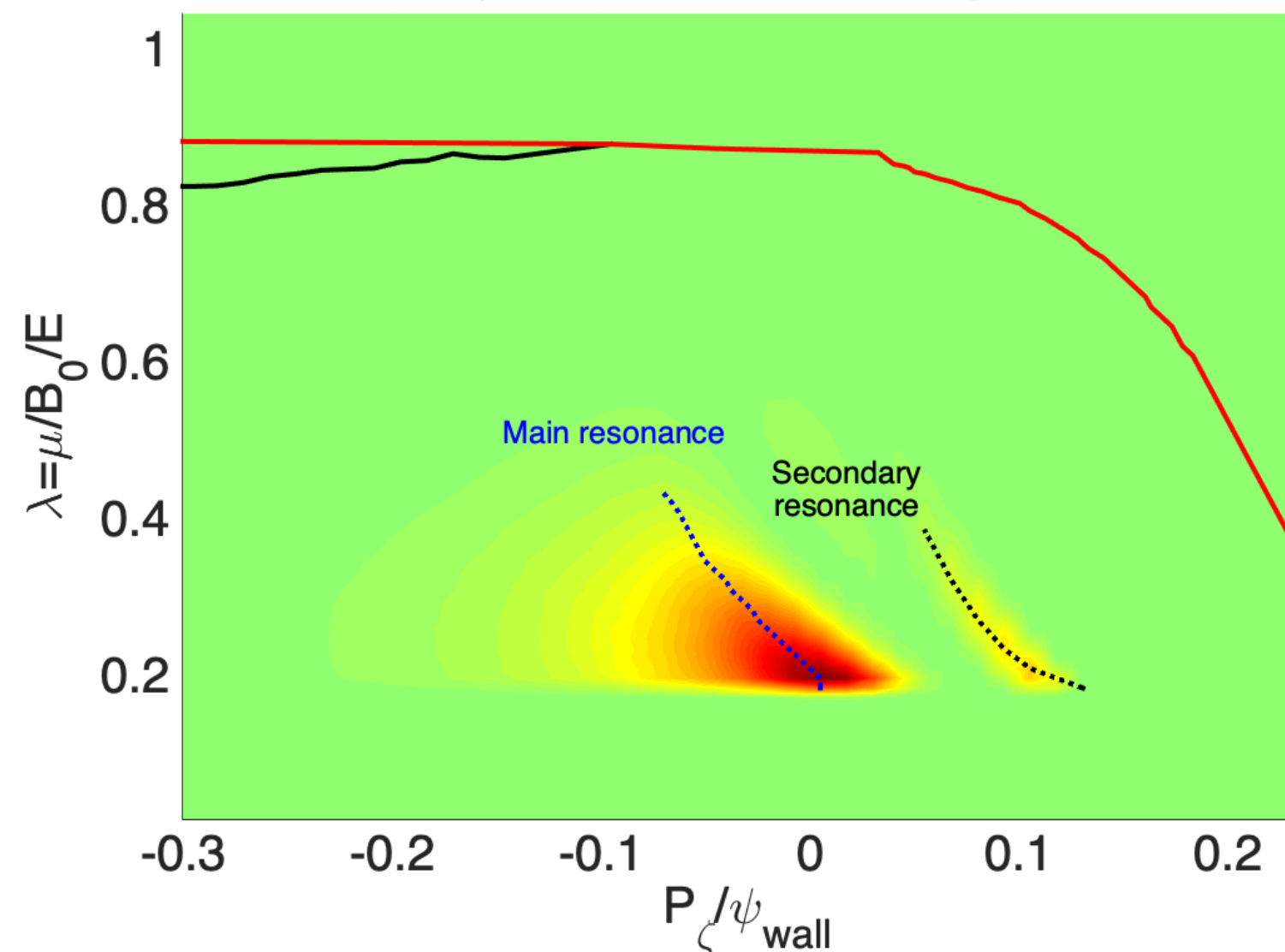
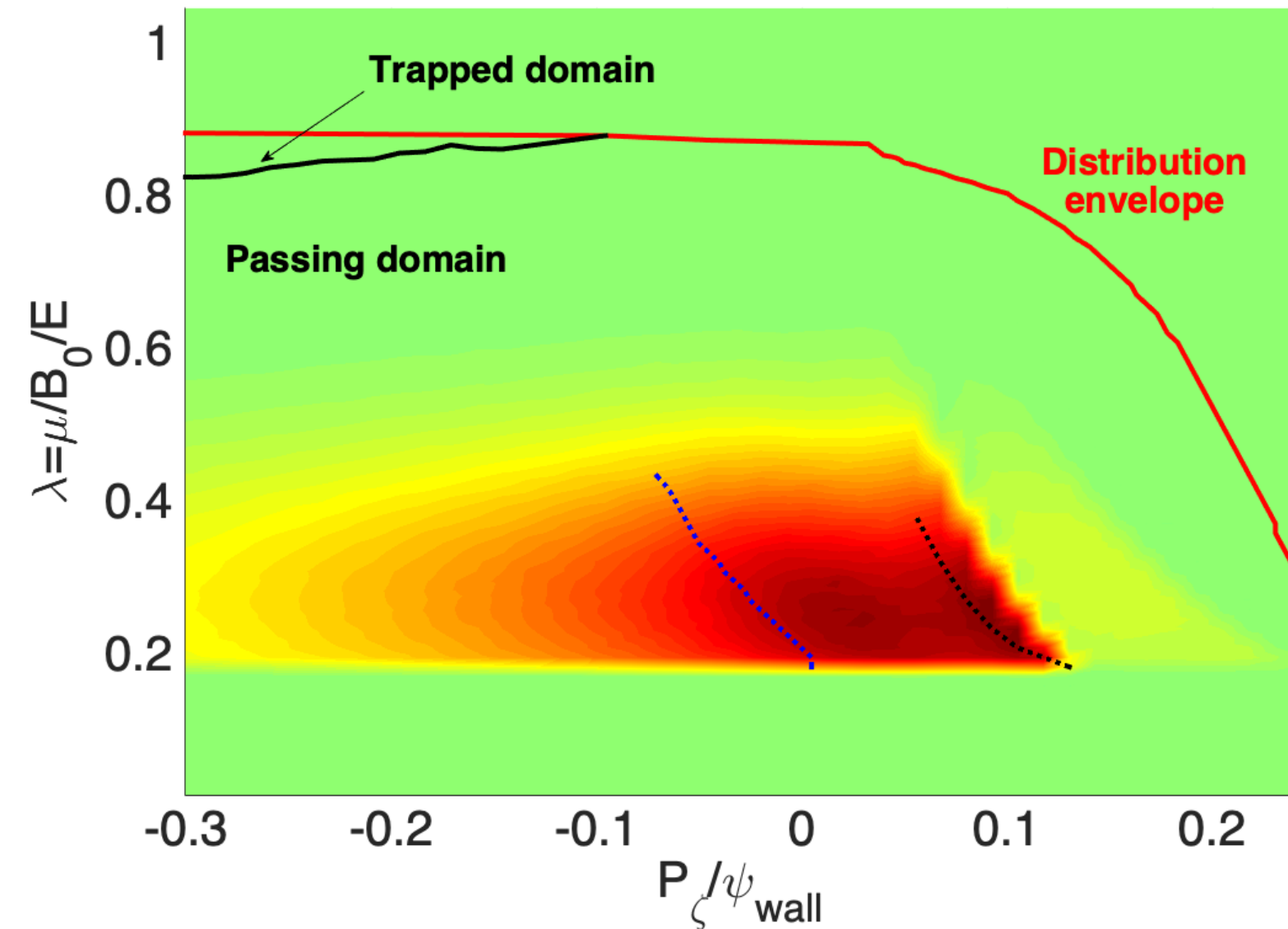
Fishbone unstable with realistic beam in ITER



$F_0, \mu B = 160$ keV

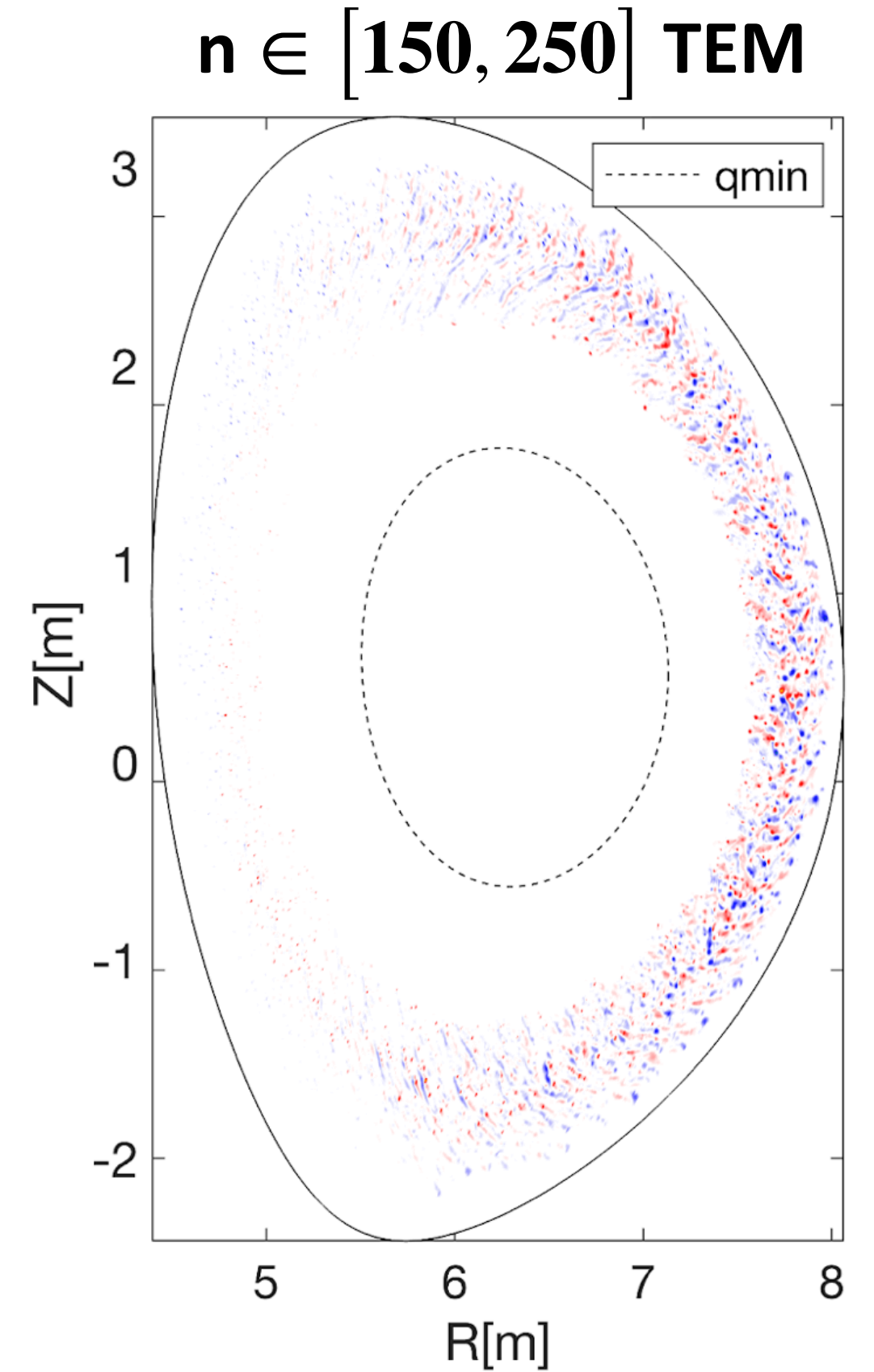
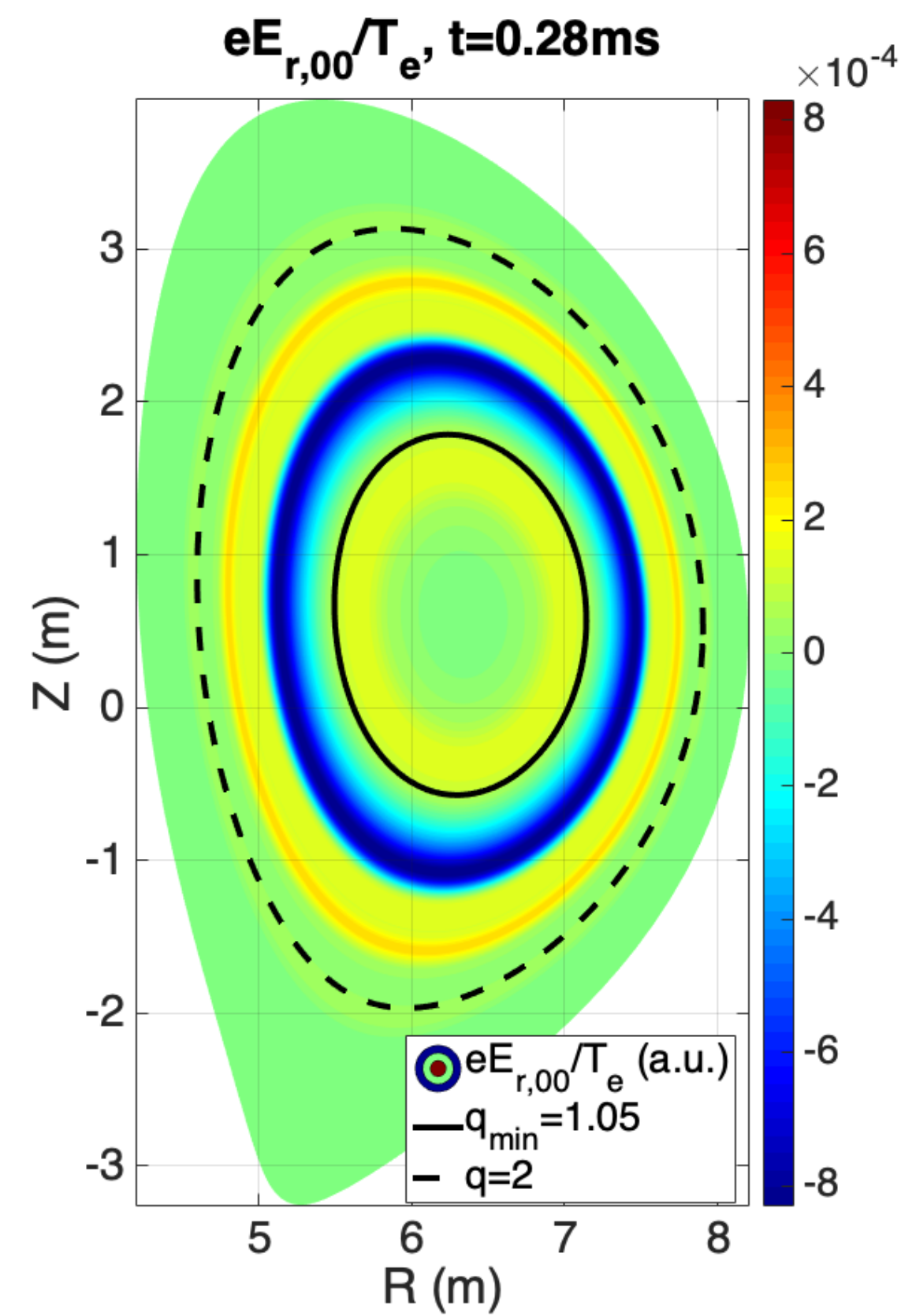
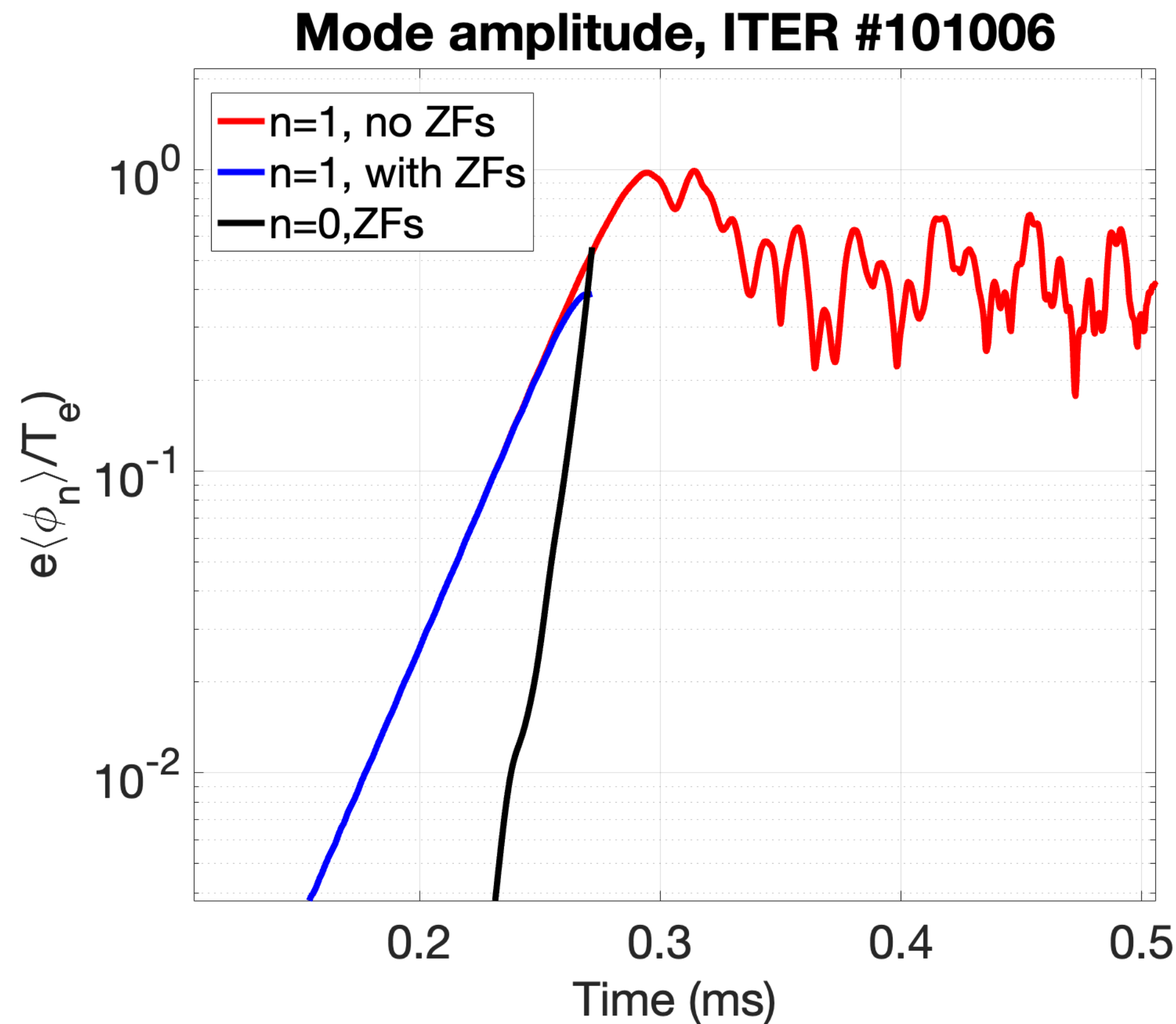


$\delta f^2, \mu B = 160$ keV, linear phase



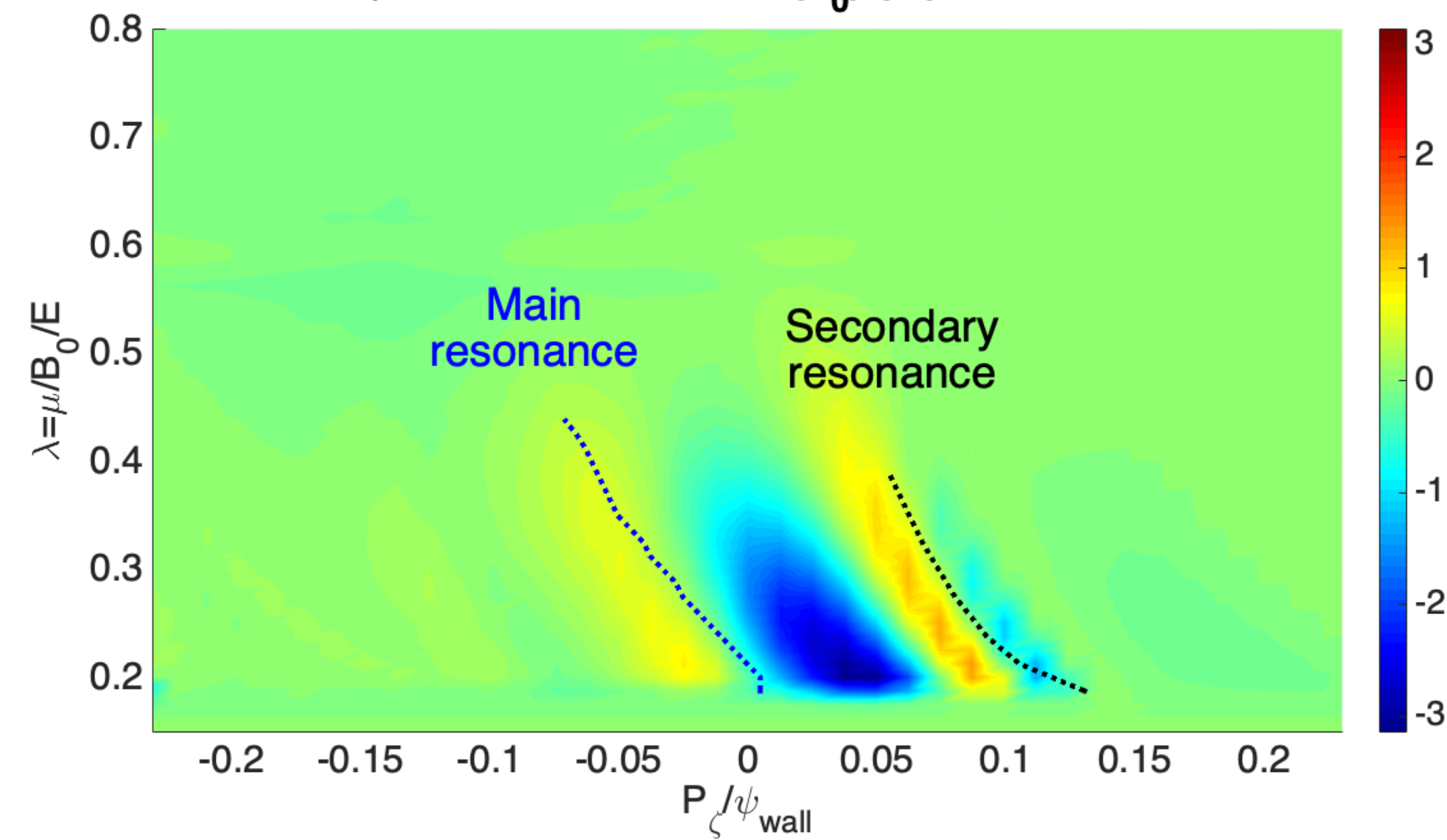
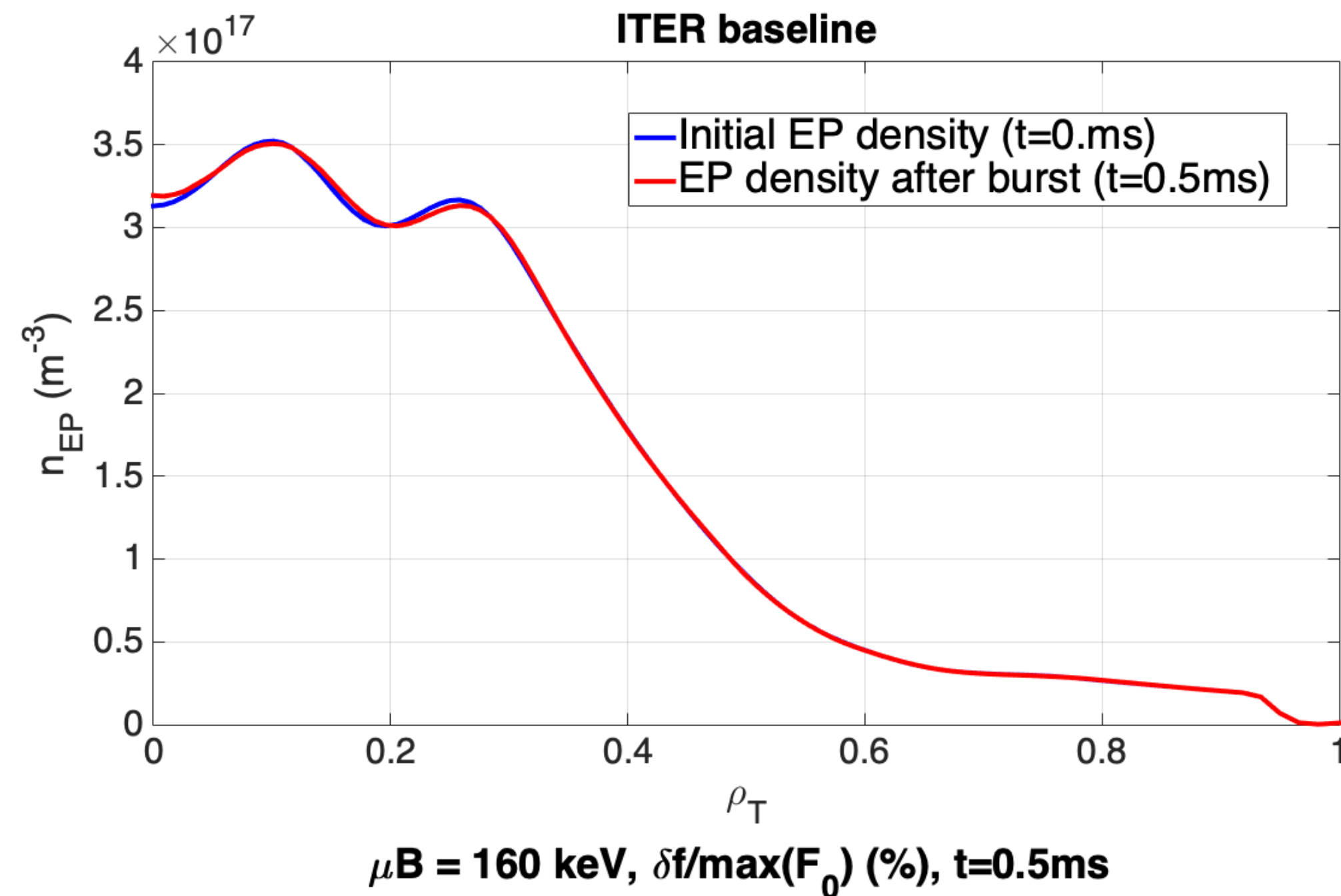
- Low n modes also **stable** with **maxwellian fast ion** kinetic effects
- With **anisotropic slowing-down pdf** for **fast ions**, a dominant $n=m=1$ fishbone mode is **destabilized**
- Similarly to the **DIII-D discharge**, the mode has a **significant $m=2$ side-band**
- **Fishbone mode driven by passing particles through two drift-transit resonances [1]**

Zonal flows also impact the ITER scenario



- **Nonlinear GTC simulations performed again keeping only $n=1$ mode, with and without zonal flows**
- **ZFs inclusion again lowers saturation amplitude, from $|\delta B / B_0| \sim 4 \times 10^{-4}$ to 1×10^{-4} at q_{\min}**
- **Fishbone-induced $\omega_{E \times B} / \gamma_{TEM} \sim 3$ at saturation, could lead to ITB formation in this ITER scenario**
- **Long time simulation with zonal flows and fishbone to be performed with GTC**

Marginal EP transport in ITER scenario



- Inward and outward EP fluxes exist due to positive and negative pressure gradients
- EP redistribution is marginal, up to 2% of initial density profile [1] without zonal flows. Similar levels were found for the alpha-fishbone in ITER 15 MA DT scenarios [2]
- NBI pressure drive too low to cause large redistribution
- Hole and clump structures form in phase space, but saturate at low amplitude

[1] G. Brochard et al. 2022, to be submitted to *Phys. Rev. Lett.*

[2] G. Brochard et al. 2020b, *Nucl. Fusion*

Conclusions and perspectives

- **Zonal flows** can be force-driven by **fishbone modes** and **dominate their saturation**
- Simulated **fishbone saturation levels** in **quantitative agreement** with **ECE** and **neutron drop** measurements on **DIII-D with zonal flows**
- **Zonal flows reduce** available **resonant EPs**, providing the **mechanism** for **fishbone saturation**
- **Fishbone-induced zonal flows** may lead to **microturbulence suppression**, supported by **ion-ITB formation** after fishbone bursts in **DIII-D**
- **Cross-scales** simulations on **DIII-D** and **ITER required** to confirm **fishbone-induced ITBs causality**
- **High performance scenarios** could be developed in **ITER** by **triggering benign fishbones**

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Versatile method for CoM distribution construction

I) Construction of **CoM Jacobian** on a **cartesian** $(E, \lambda = \mu B_0 / E, P_\varphi)$ grid

II) Inputs from **Fokker-Planck codes** or **experimental measurements**

III) **3D C^2 spline function** of the CoM distribution $F((E, \lambda, P_\varphi, \sigma=-1,1))$

Full-F codes

δF codes

3D Monte-Carlo sampling based on spline CoM distribution

IV) **C^1 first order derivatives** along CoM ∂_i $F((E, \lambda, P_\varphi, \sigma))$

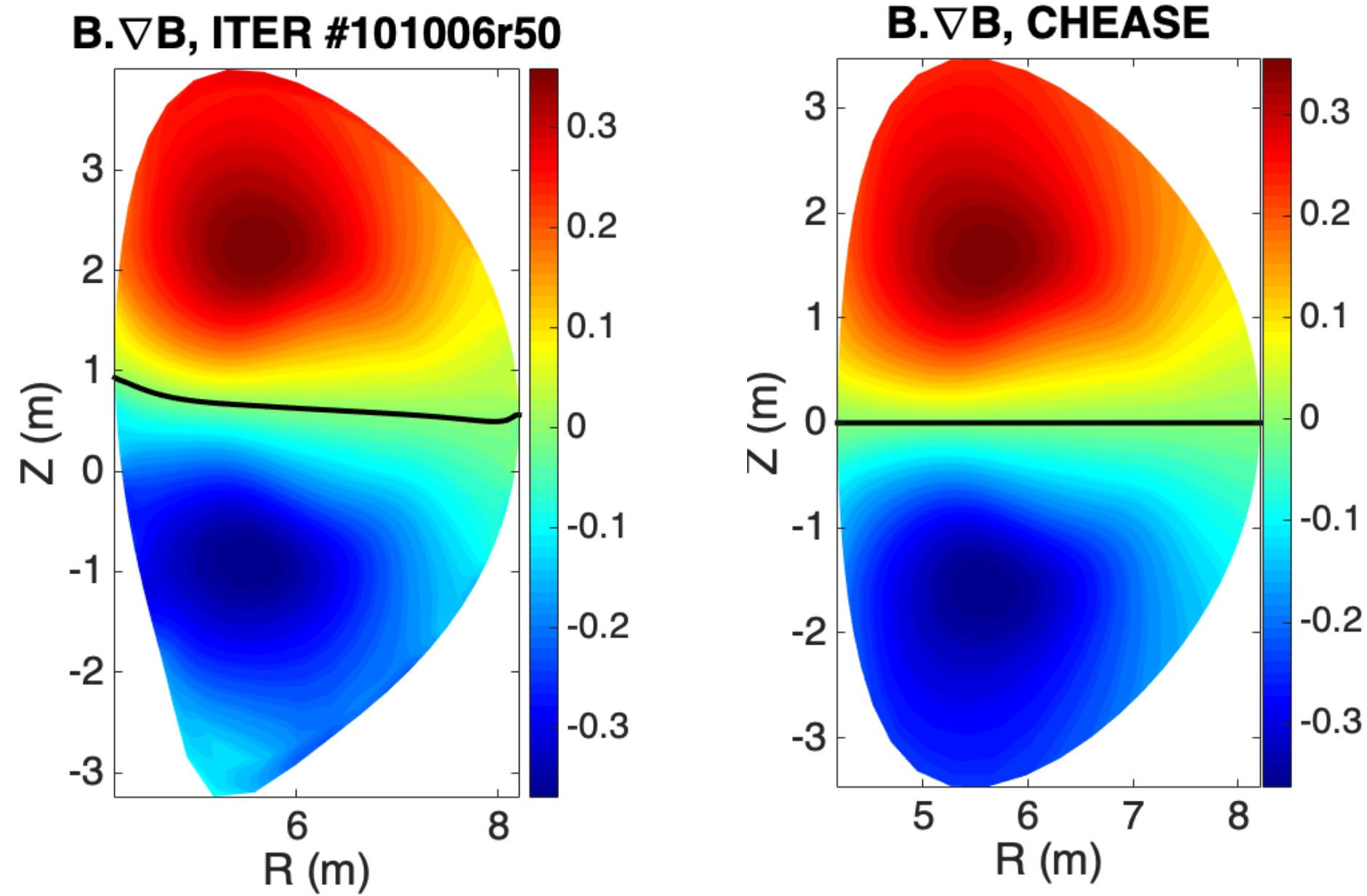
Backward transformation in 5D/6D cartesian/Boozer coordinates

IV) **Chain rule operations** to obtain $C^1 \nabla F|_{\mu, v_{||}}$ and $\partial_{v_{||}} F|_{\mu, X}$

- A **cartesian CoM grid** is first built to determine **orbits' nature** and J_{CoM}
- **Distributions/markers** in « regular » (E, p, R, Z) coordinates are loaded from **FK codes** or **experimental measurements**
- A **C^2 spline** of the **3D CoM distribution** is defined to ensure **good numerical properties** for both **full-F** and **δf codes**
- A **backward** $(E, \lambda, P_\varphi, \sigma) \rightarrow (E, p, R, Z)$ transformation is used to **load markers uniformly along orbits** for **full-F codes**
- For **δf codes**, the **weigh equation** can be fully defined by using **C^1 first-order CoM derivatives** (using a **chain rule**)

Construction of a smooth CoM jacobian

Generalised midplane



$(E, \lambda, P_\varphi) \rightarrow (E, \frac{v_{\parallel}}{v}, R_{mid})$ transformation

$$v_{\parallel}(R_{mid}) = \frac{P_\varphi + Ze\psi(R_{mid})}{mB(R_{mid})/B^\varphi(R_{mid})}$$

$$\lambda(R_{mid}) = \left(1 - \frac{v_{\parallel}^2(R_{mid})}{v^2}\right) \frac{B_0}{B(R_{mid})}$$

exactly correct in 6D for the gyroangle such as $v_\theta = 0$

➤ A method based on a cartesian CoM grid (E, λ, P_φ) avoid some singularities on J_{CoM} and ΔV_{CoM} observed in [1]

➤ $J_{CoM} \propto \sum_{\sigma} \tau_b(E, \lambda, P_\varphi)$, orbit tracing necessary to obtain τ_b in 3D, requiring a backward transformation to initialise markers in 5D/6D space on each (E, λ, P_φ) vertice

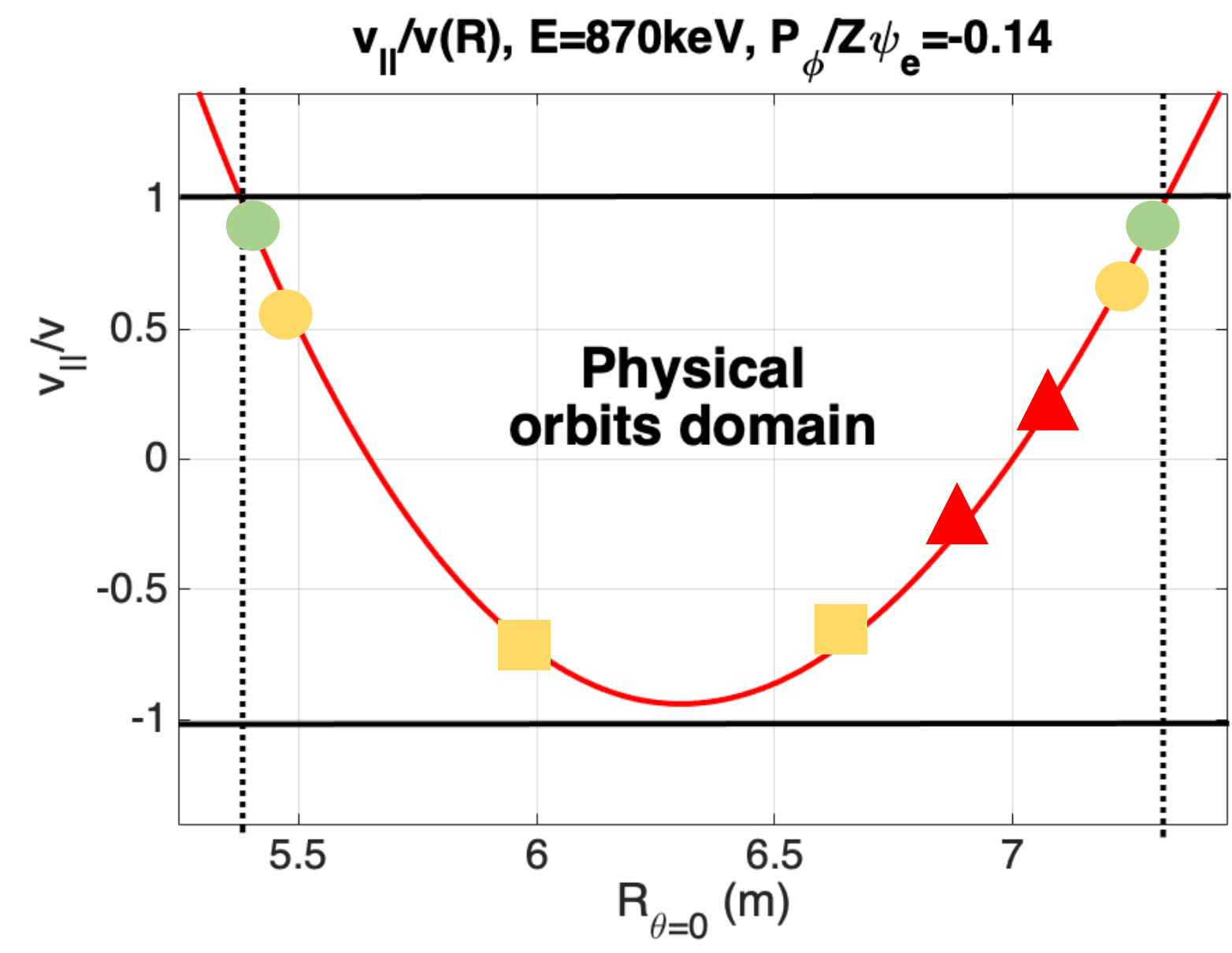
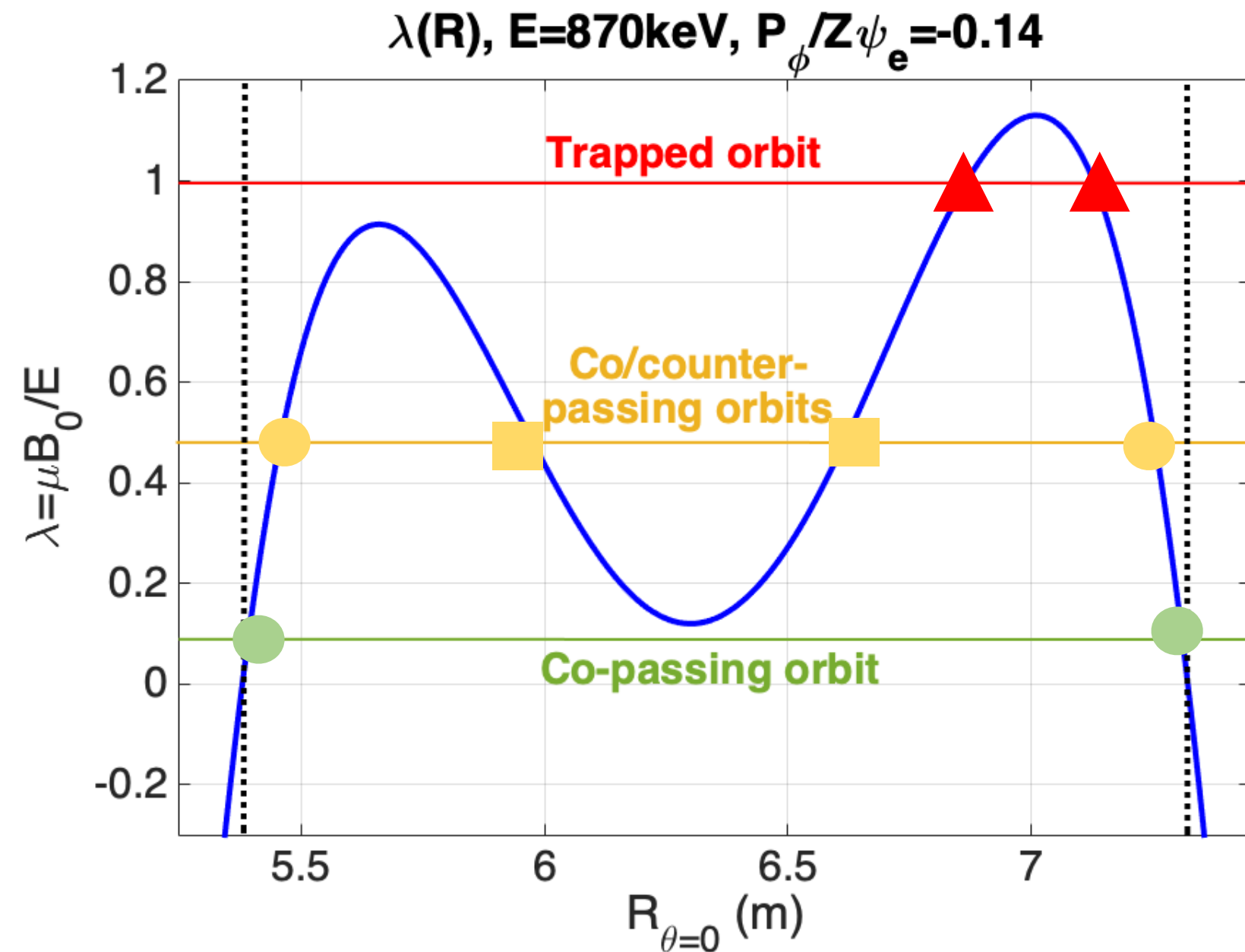
➤ Transformation is performed on midplane

$R_{mid} \equiv B \cdot \nabla B = \mathbf{0}$, intersected by all EPs orbits [1]

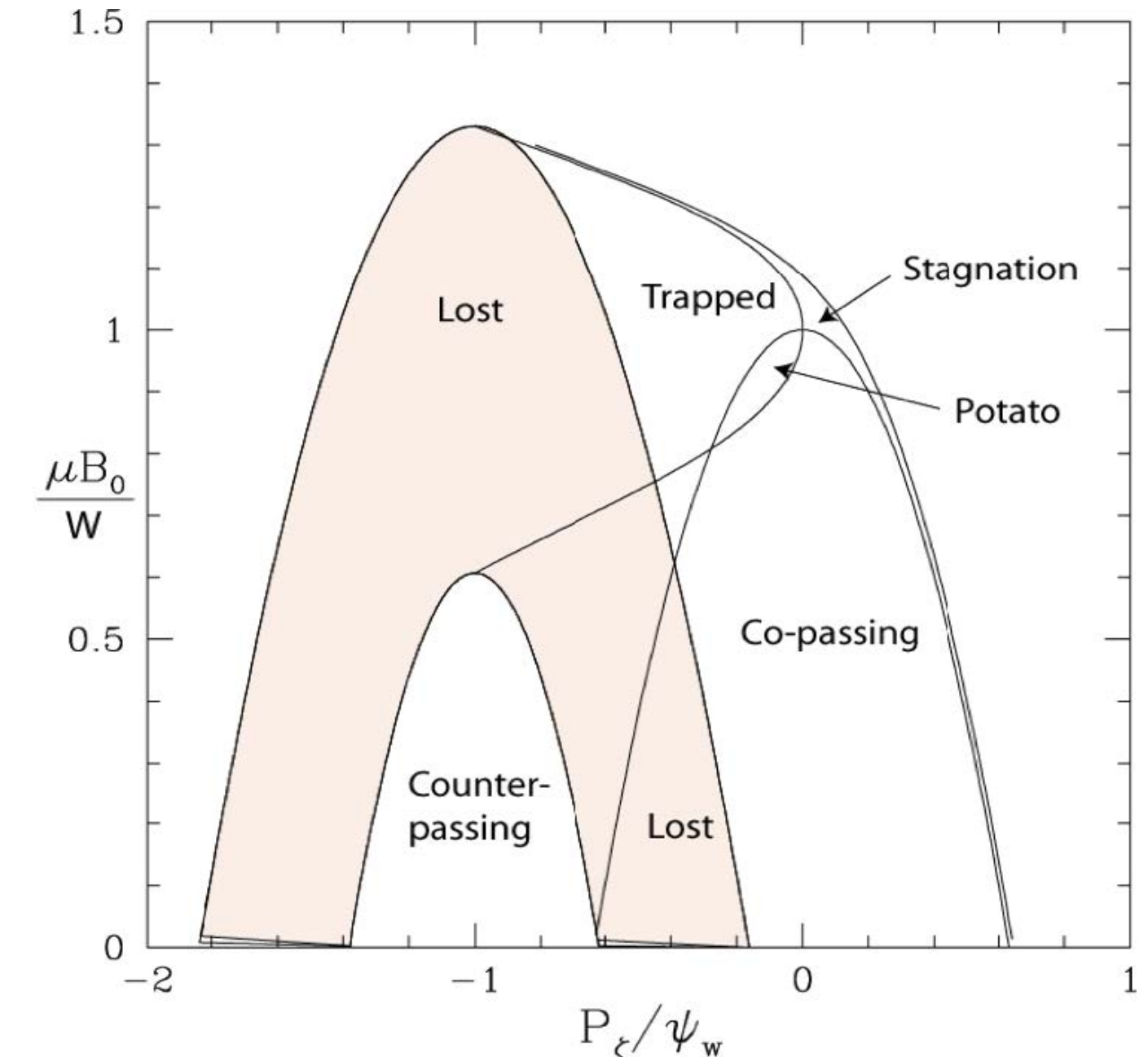
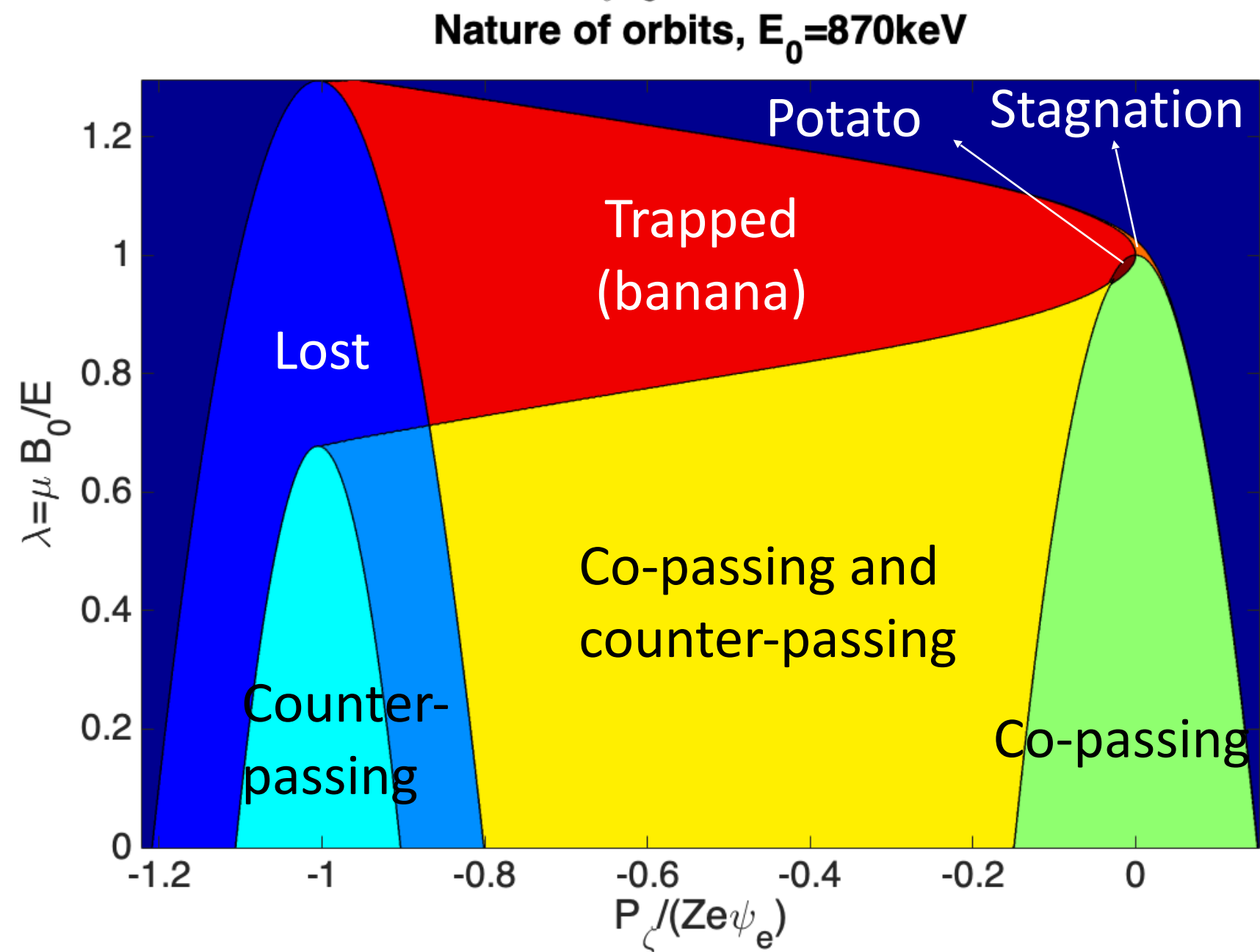
➤ For a given vertice on cartesian CoM grid $(E_i, \lambda_j, P_{\varphi,k})$, the coupled set of equations on (v_{\parallel}, λ) implicit in R_{mid} is solved to obtain $(\frac{v_{\parallel}}{v}, R_{mid})$

➤ This backward transformation on the generalized midplane does not require orbit tracing

Backward transformation and orbit classification

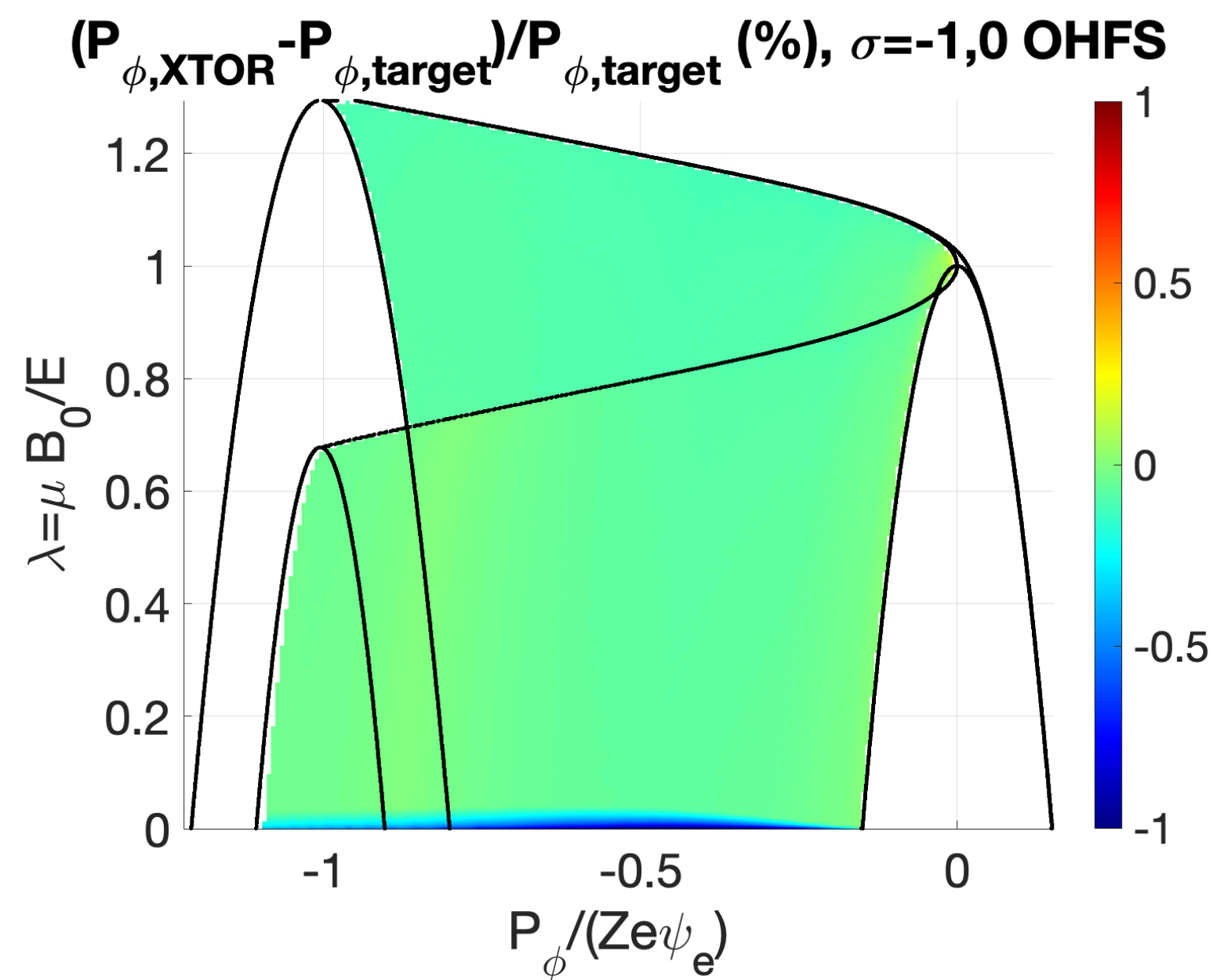
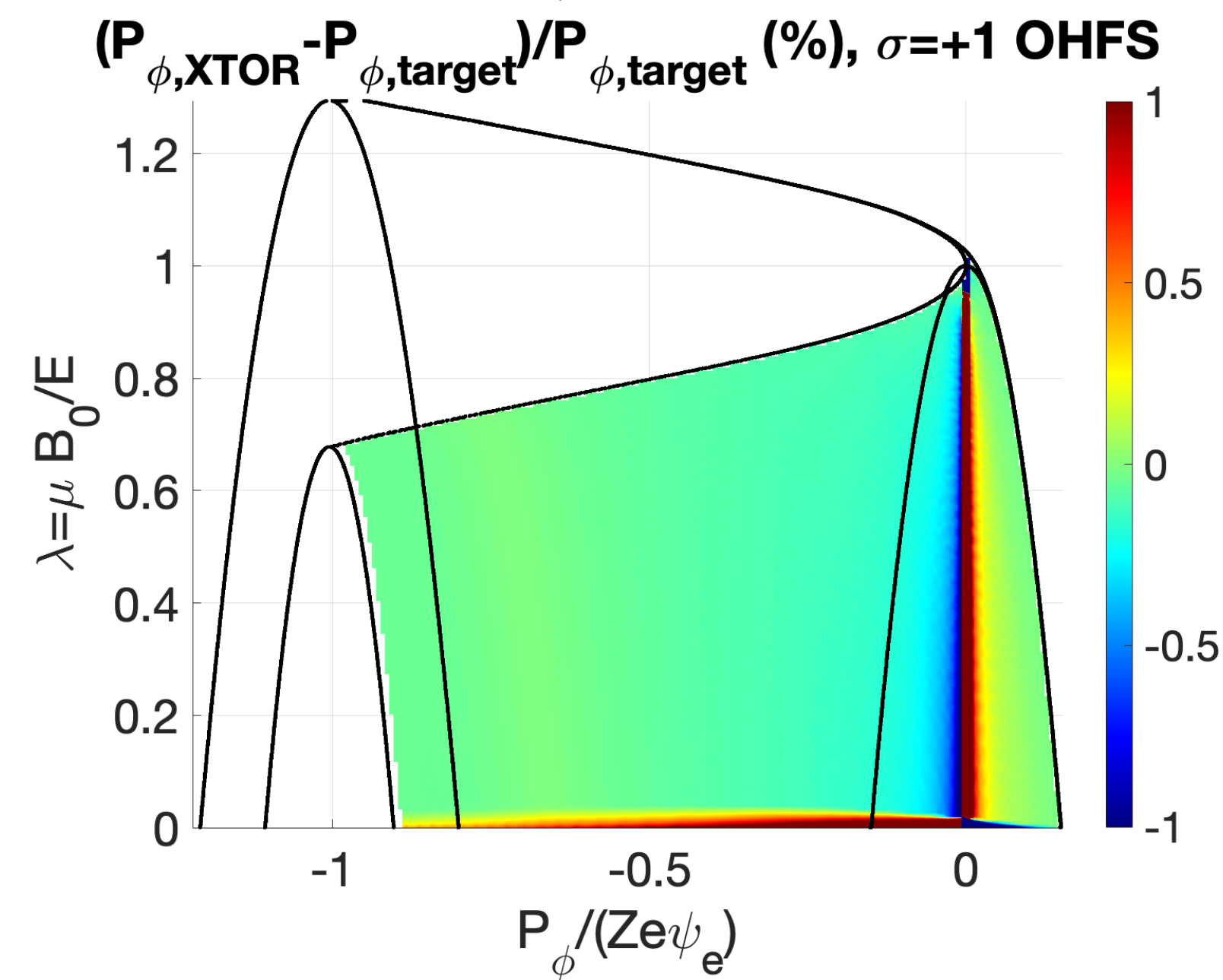
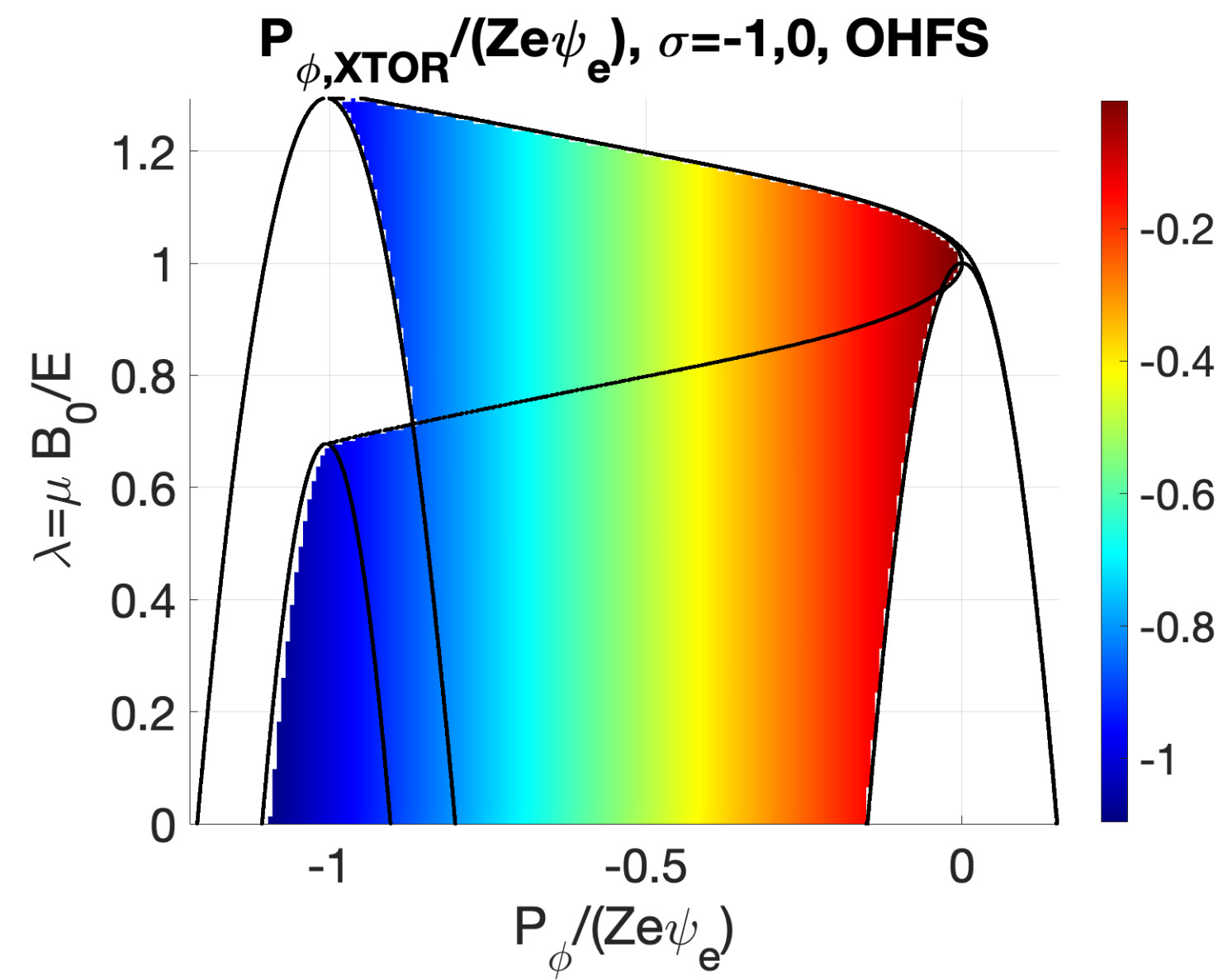
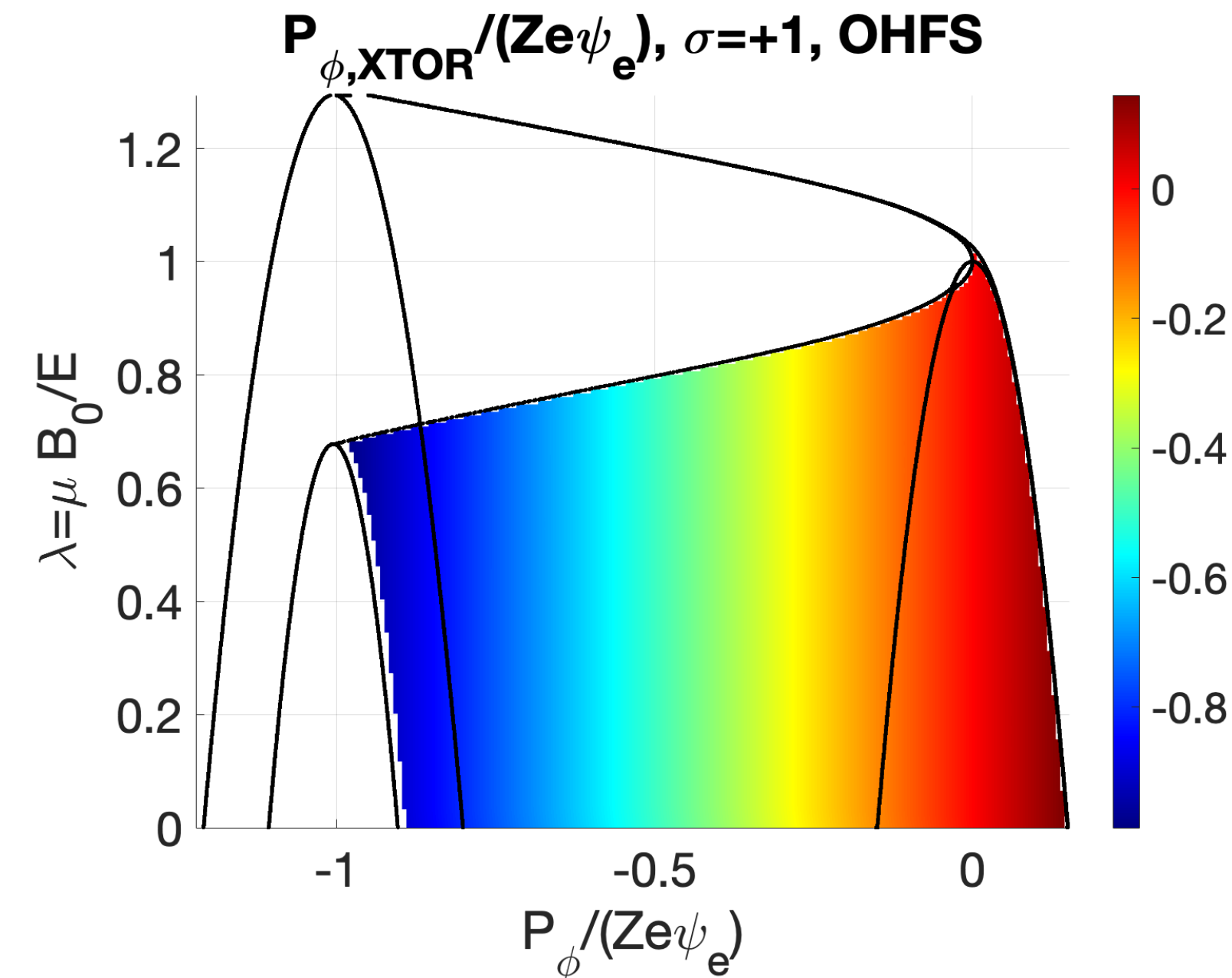


- The solutions of $\lambda[R_{mid}, v_{\parallel}(R_{mid}, P_{\phi,k})] = \lambda_j$ are obtained numerically by scanning R_{mid} , for $v_{\parallel} \in [-v_i, v_i]$
- For each orbit, the algorithm finds two solutions, on the LFS and HFS of the $B \cdot \nabla B = 0$ midplane



- 8 types of orbits are identified based on the values for (R_{mid}, v_{\parallel}) on the OLFS and OHFS
- In the (P_{ϕ}, λ) phase space at fixed energy, the topology is identical to White's. A 2000x2000 grid was used

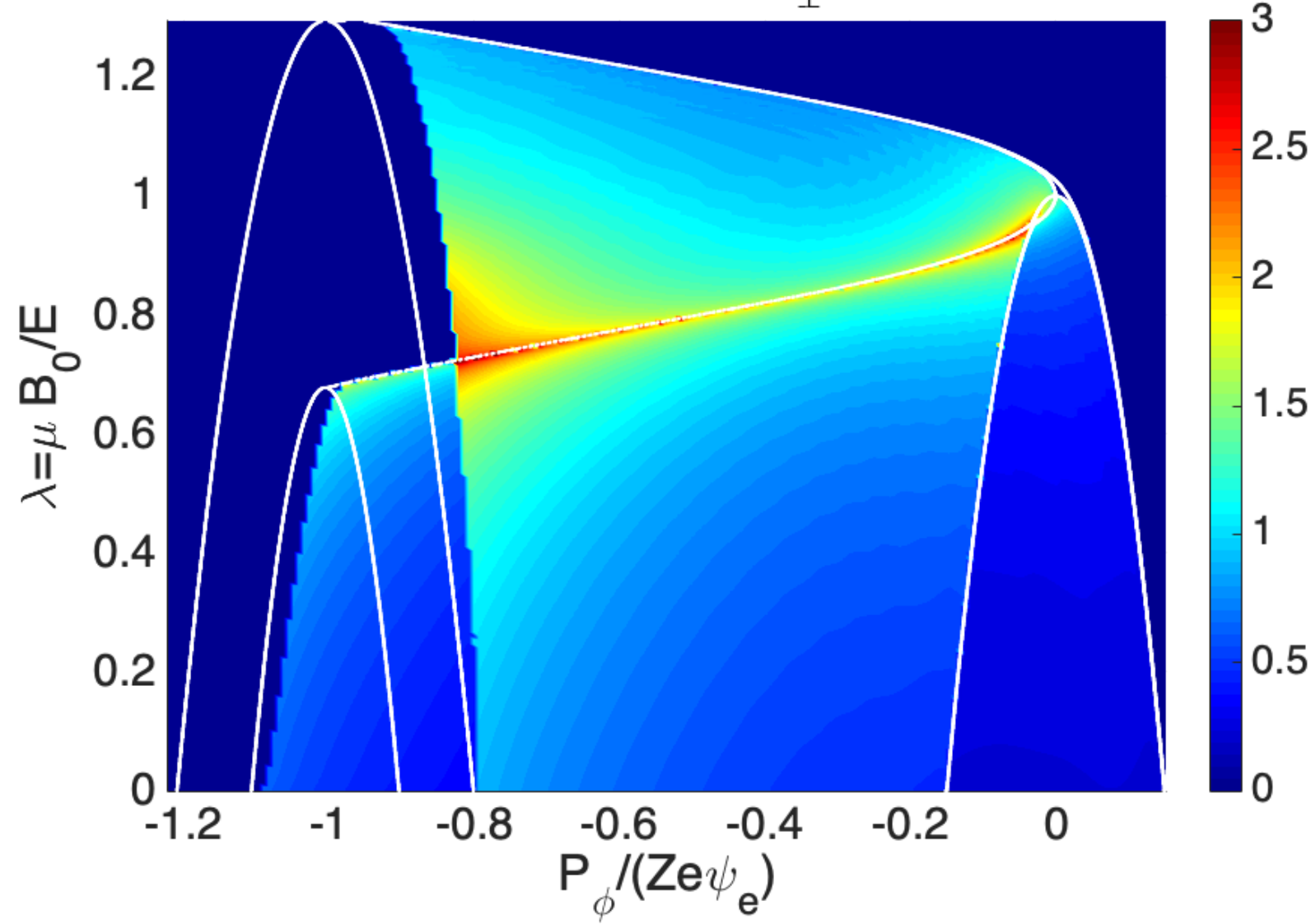
Accuracy of the backward transformation



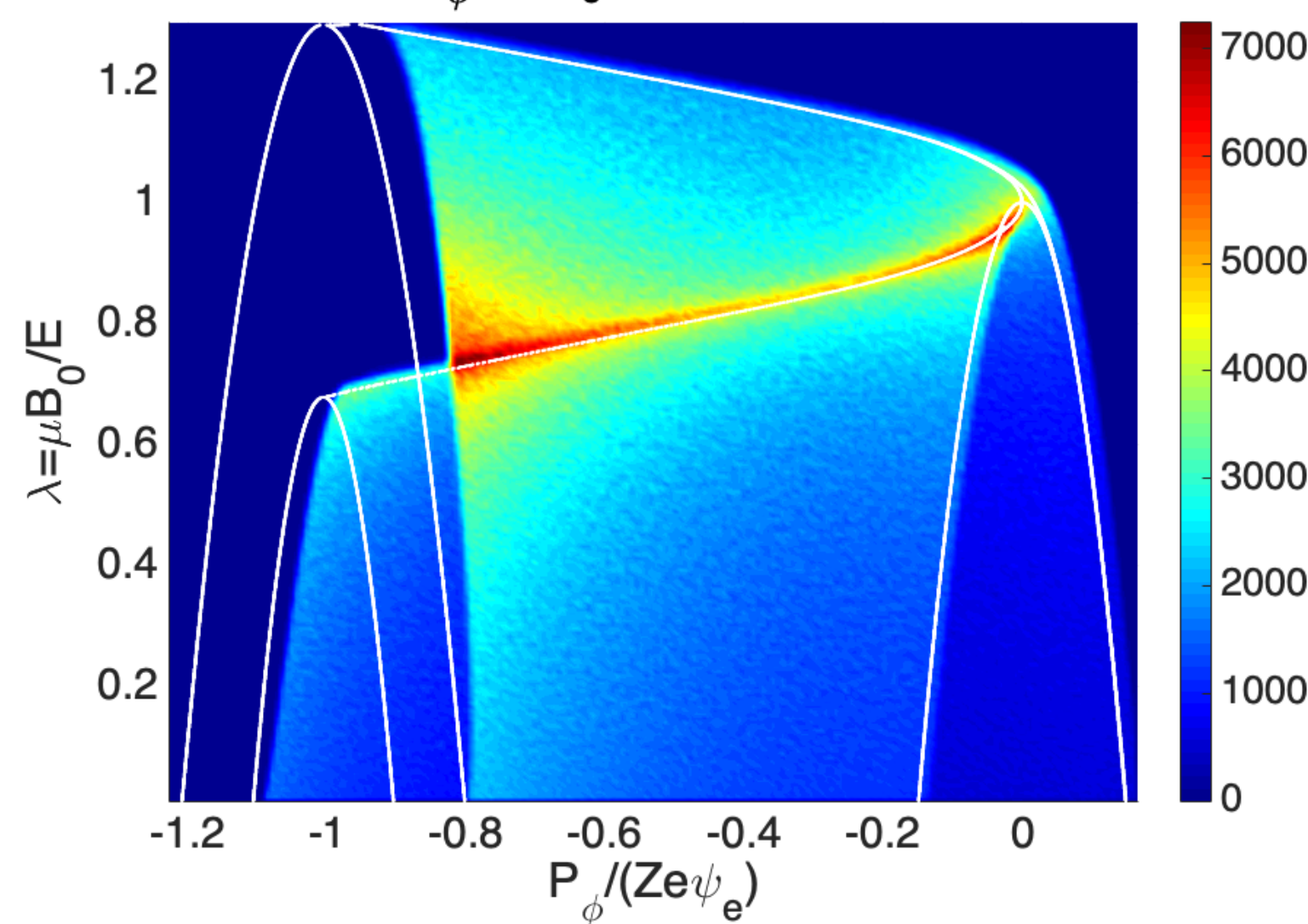
- The backward transformation is tested with the **XTOR-K 6D pusher** on a **200x200 (P_ϕ, λ) grid** at fixed energy
- For each target $(P_{\phi, i}, \lambda_j)$, the corresponding $(R_{mid}, v_{||})$ are identified on the **OHFS**
- P_ϕ is re-computed from the markers **6D position**
- The error on P_ϕ is under 1%, showing **good numerical accuracy** of the backward transformation
- **Similar results** are obtained for λ

« Analytic » construction of CoM jacobian

$$J_{CoM} = (2\pi)^2 E / (ZeB_0) \sum_{\sigma} \tau_b \text{ (keV.s}^{-1}\text{)}$$



$$J \times F(P_\phi, \lambda), E_0 = 870 \text{ keV, XTOR-K}$$



➤ J_{CoM} is theoretically defined as

$$J_{CoM} = \frac{(2\pi)^2 E}{ZemB_0} \sum_{\sigma=\pm 1} \tau_B(E, \lambda, P_\phi)$$

➤ J_{CoM} can be obtained on the (E, λ, P_ϕ) grid from the bounce time for each orbit

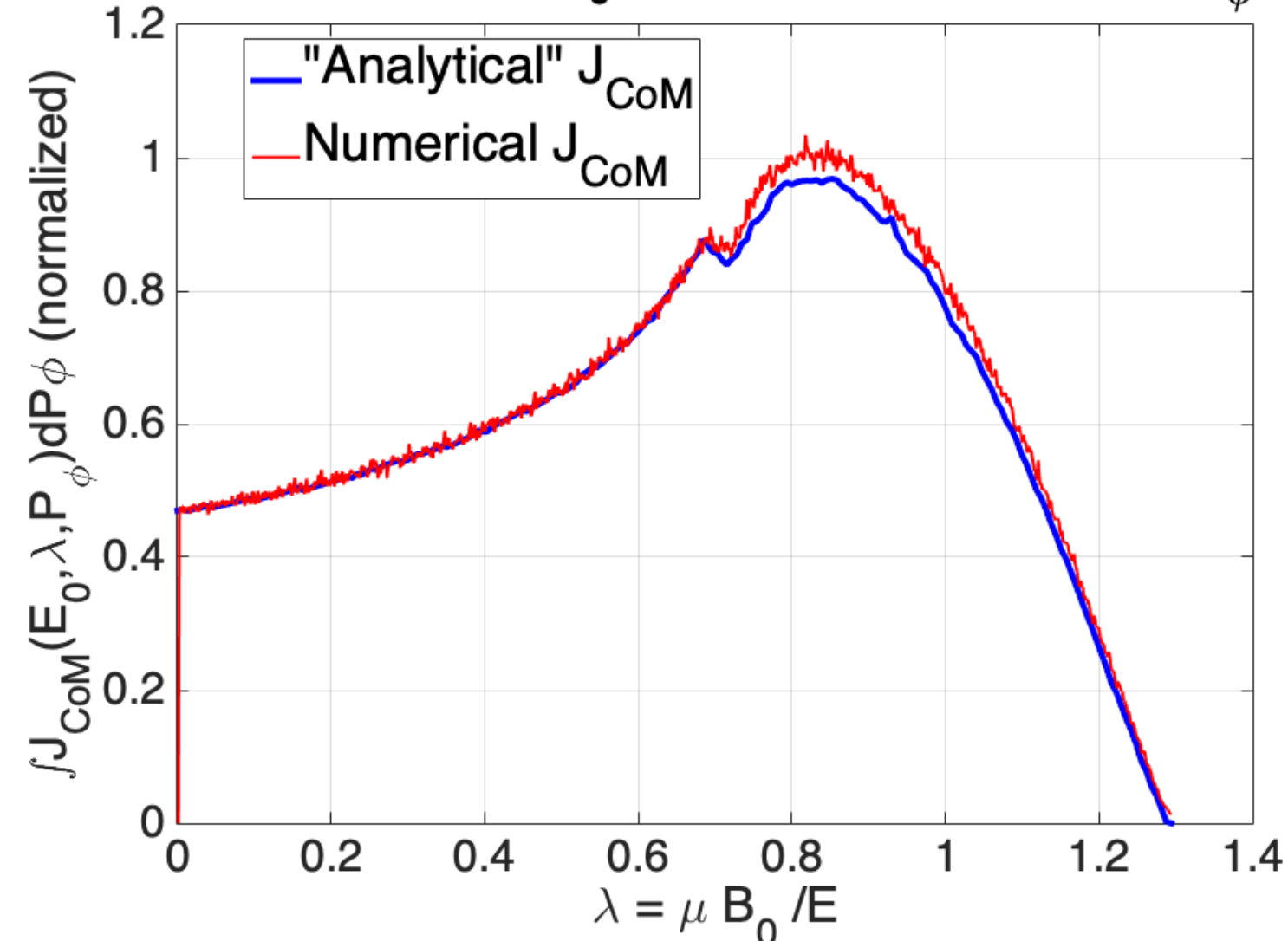
➤ J_{CoM} is successfully compared with the histogram of a flat, isotropic and monoenergetic distribution as

$$H_{CoM} = F_{CoM} \times J_{CoM}$$

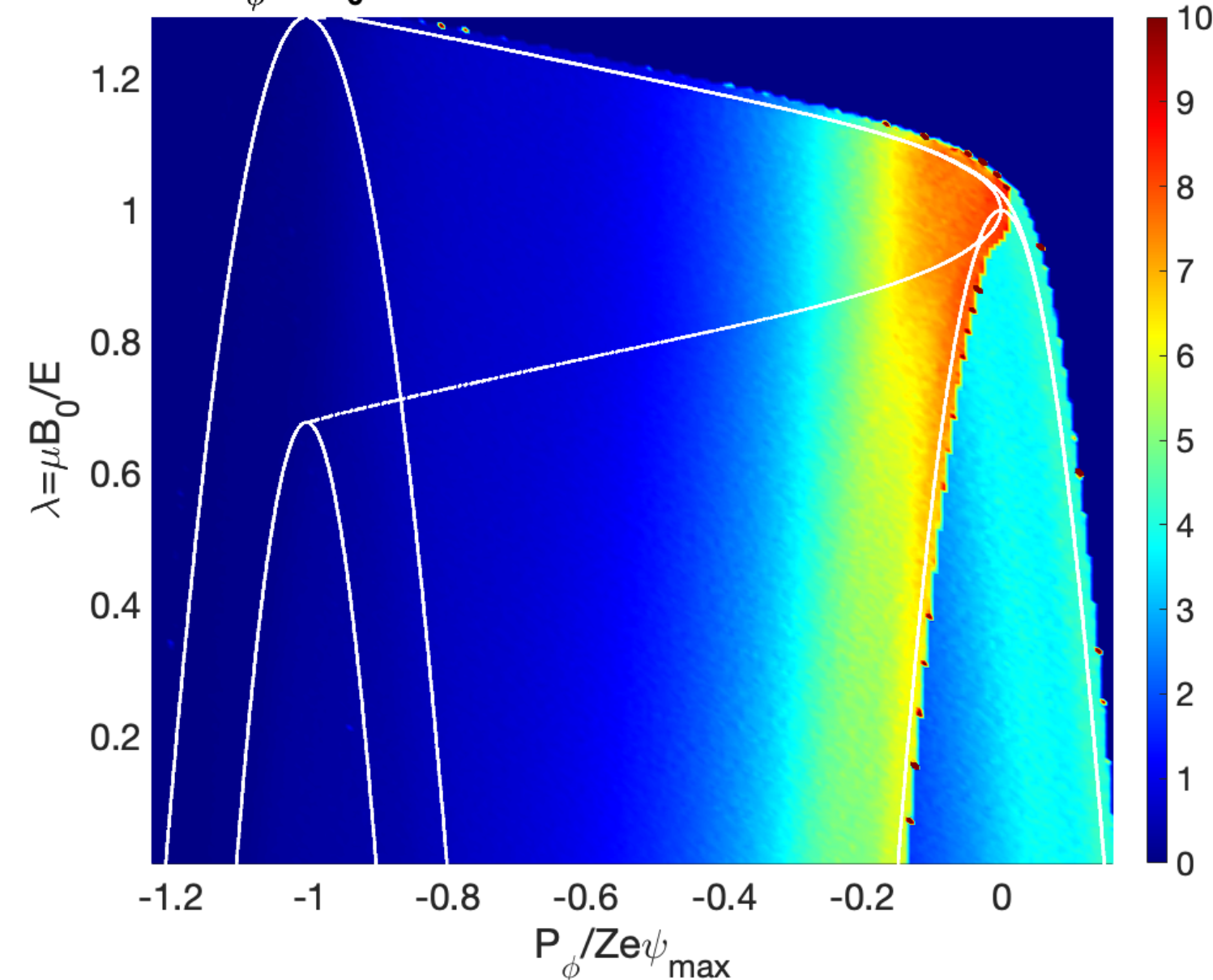
➤ Small inaccuracies remain near the trapped-passing boundary

➤ With a realistic density profile, most particles are located near topological boundaries of the (P_ϕ, λ) grid

CoM jacobian at $E_0 = 870 \text{ keV}$ integrated over P_ϕ



$F(P_\phi, \lambda), E_0 = 870 \text{ MeV, isotropic, \#101006r50, } \sigma = -1, +1$



Outline

I) Interplay fishbone/zonal flows in gyrokinetic simulations

A) Experimental fishbone validation on a DIII-D discharge

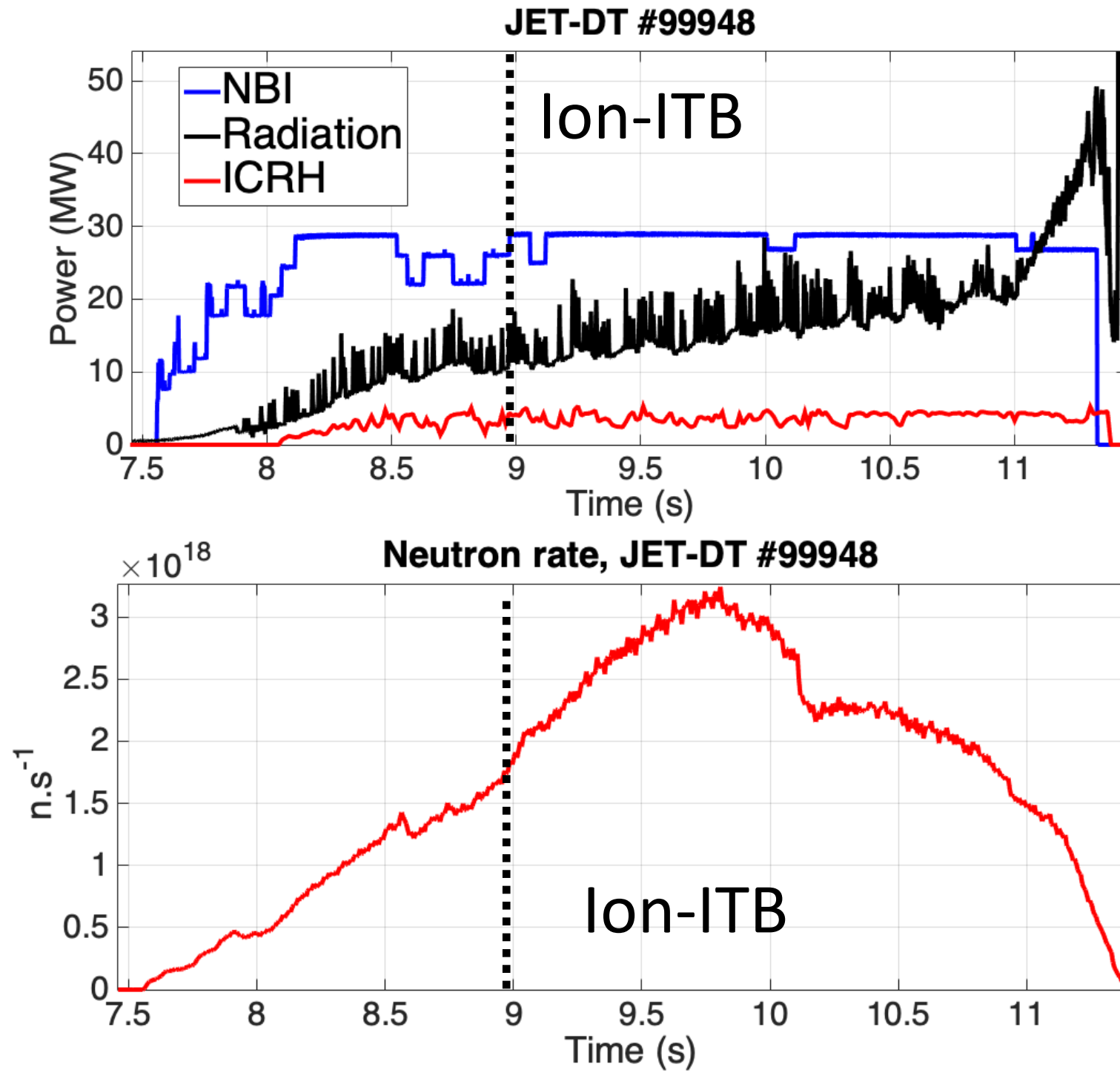
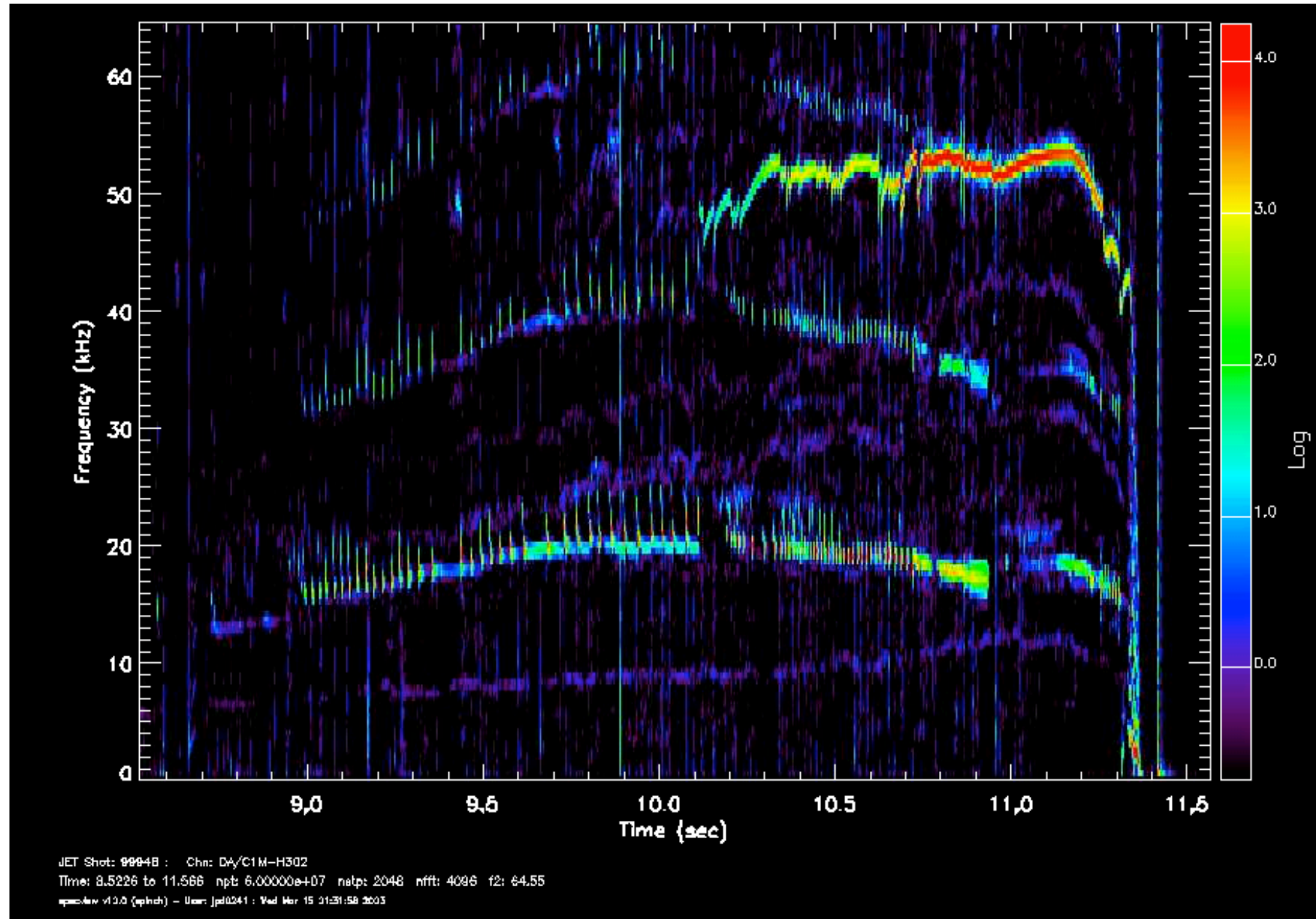
B) Predicted fishbone dynamics in ITER PFPO-2 scenario

II) Computation of CoMs EP distribution in IMAS

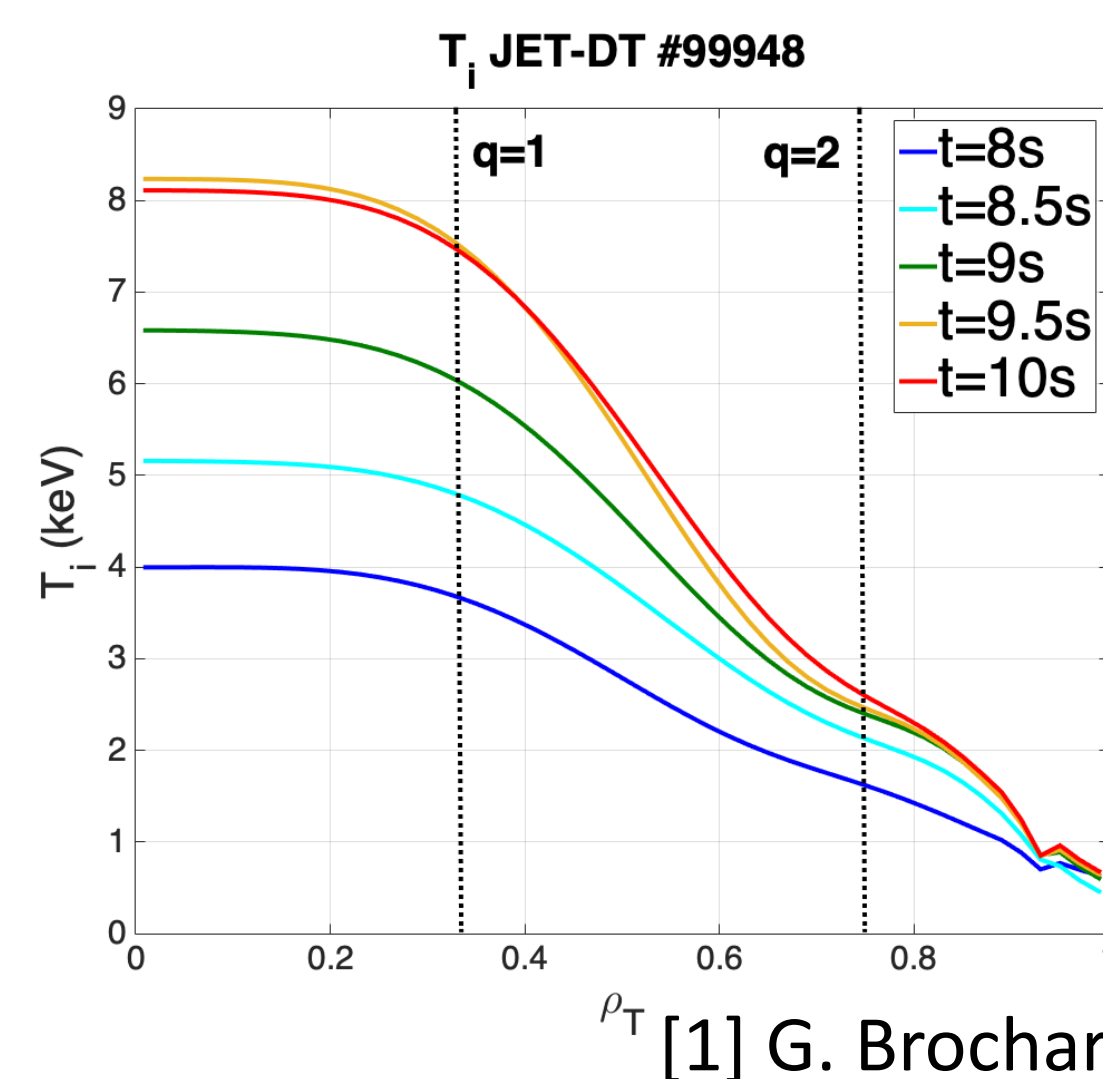
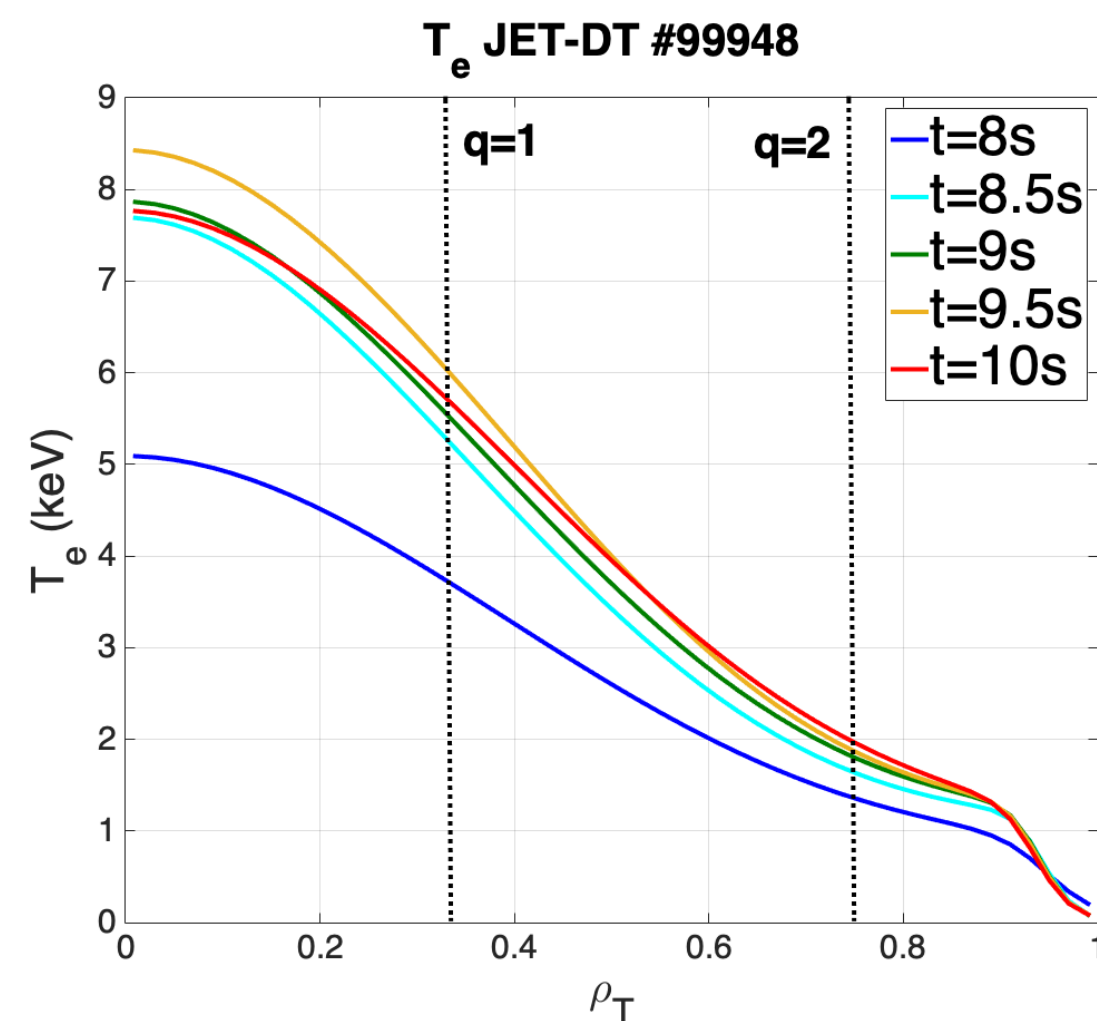
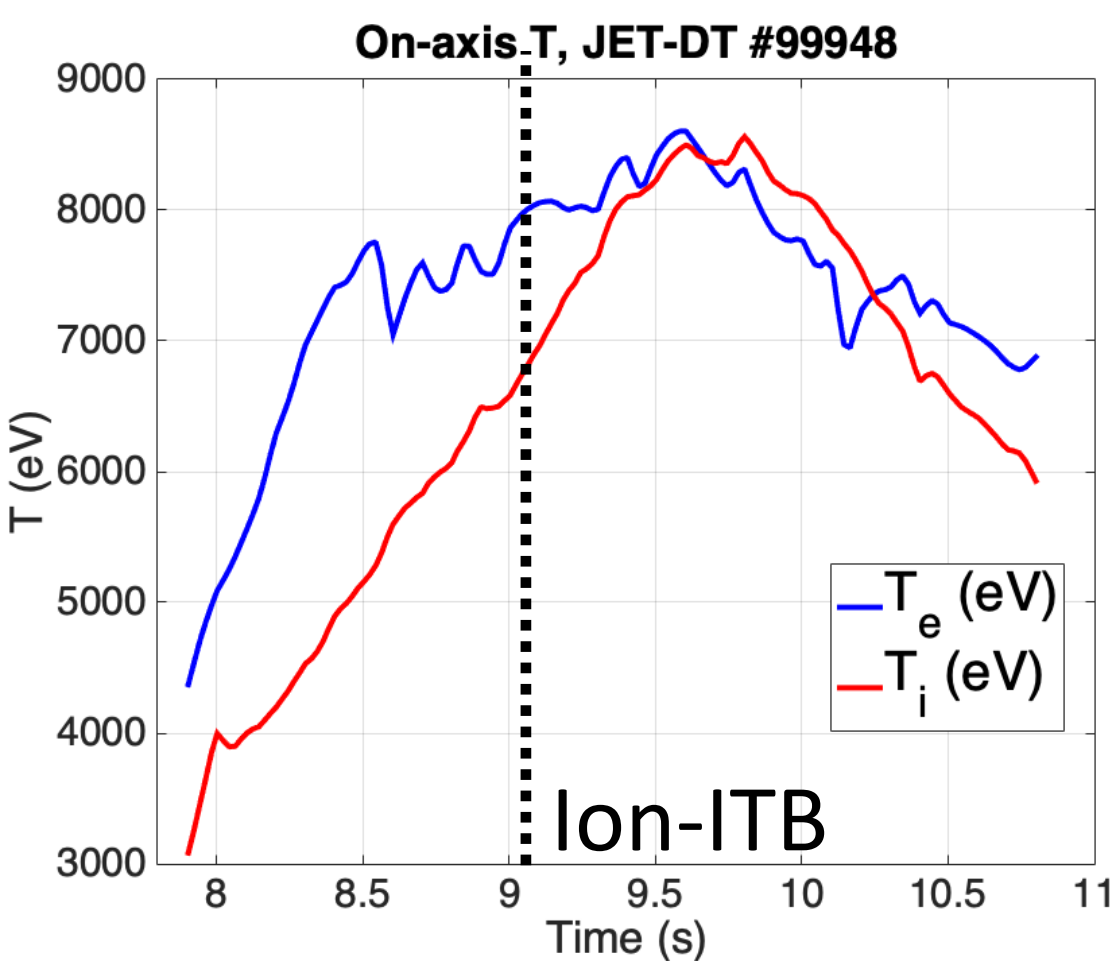
A) Versatile method for coordinate transformation

B) Application for NBI and alpha distributions in a JET-DT pulse

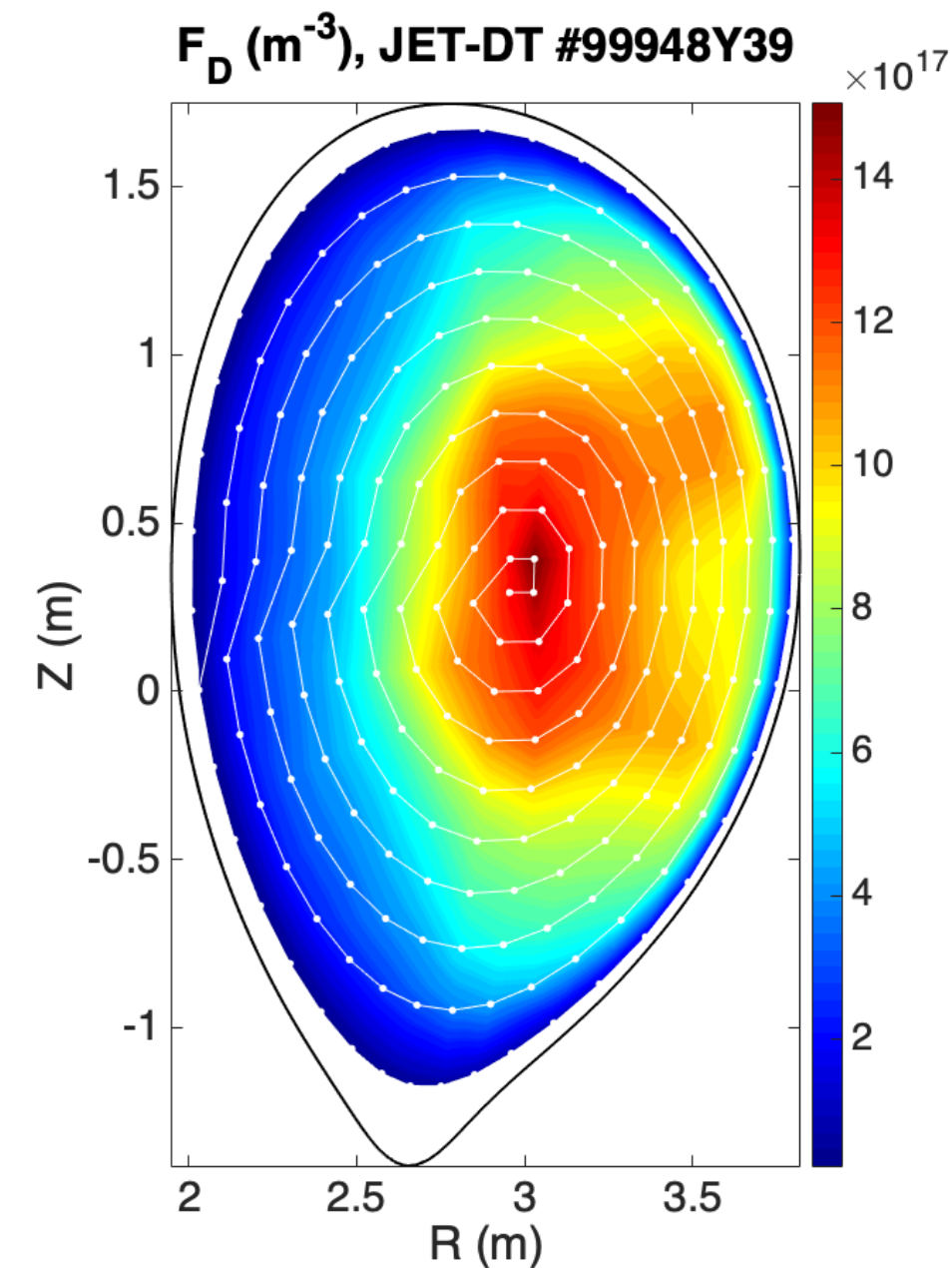
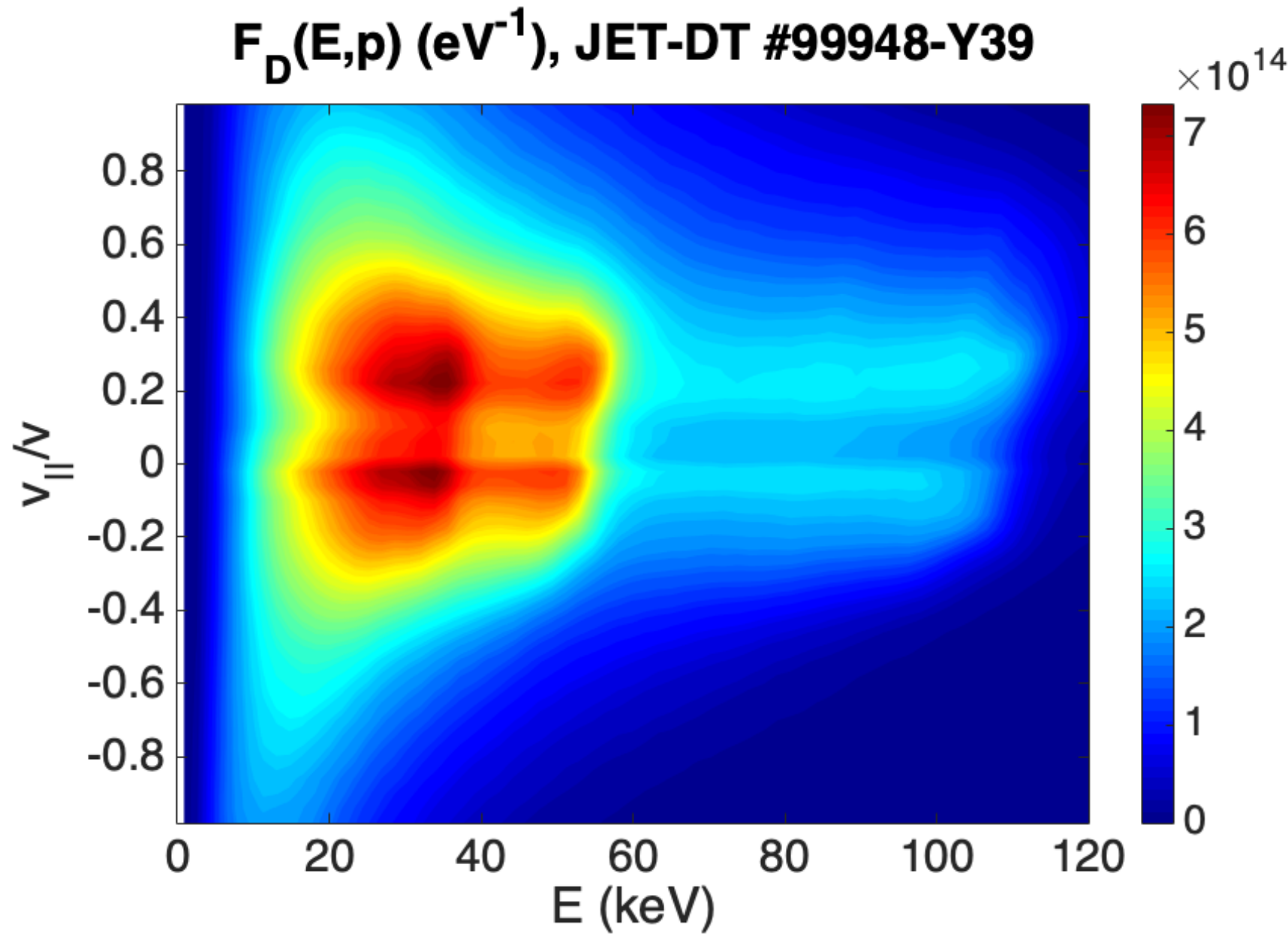
Fishbone-induced ion ITBs in JET-DT



- JET DT pulse #99948 experienced a 2x increased fusion gain with $Q=0.32$ after onset of fishbone bursts
- Ion-ITB formation is visible after $t=9s$ at $q=2$, no electron ITB identified
- There is a possible causality between fishbone starting at $t=9s$ and the ion-ITB, similar to [1] on DIII-D
- Nonlinear gyrokinetic and kinetic-MHD need to be performed with realistic CoM pds to verify this causality



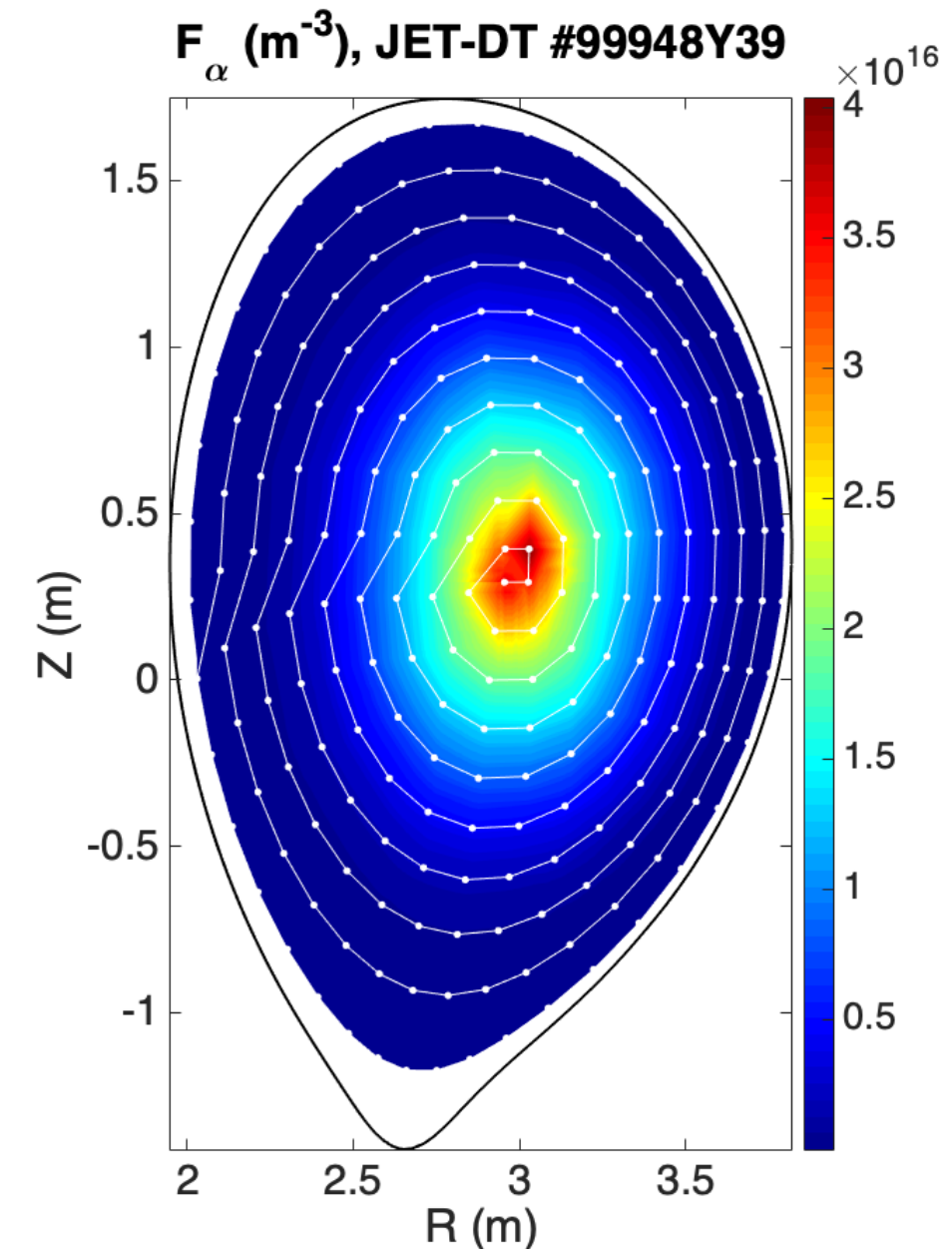
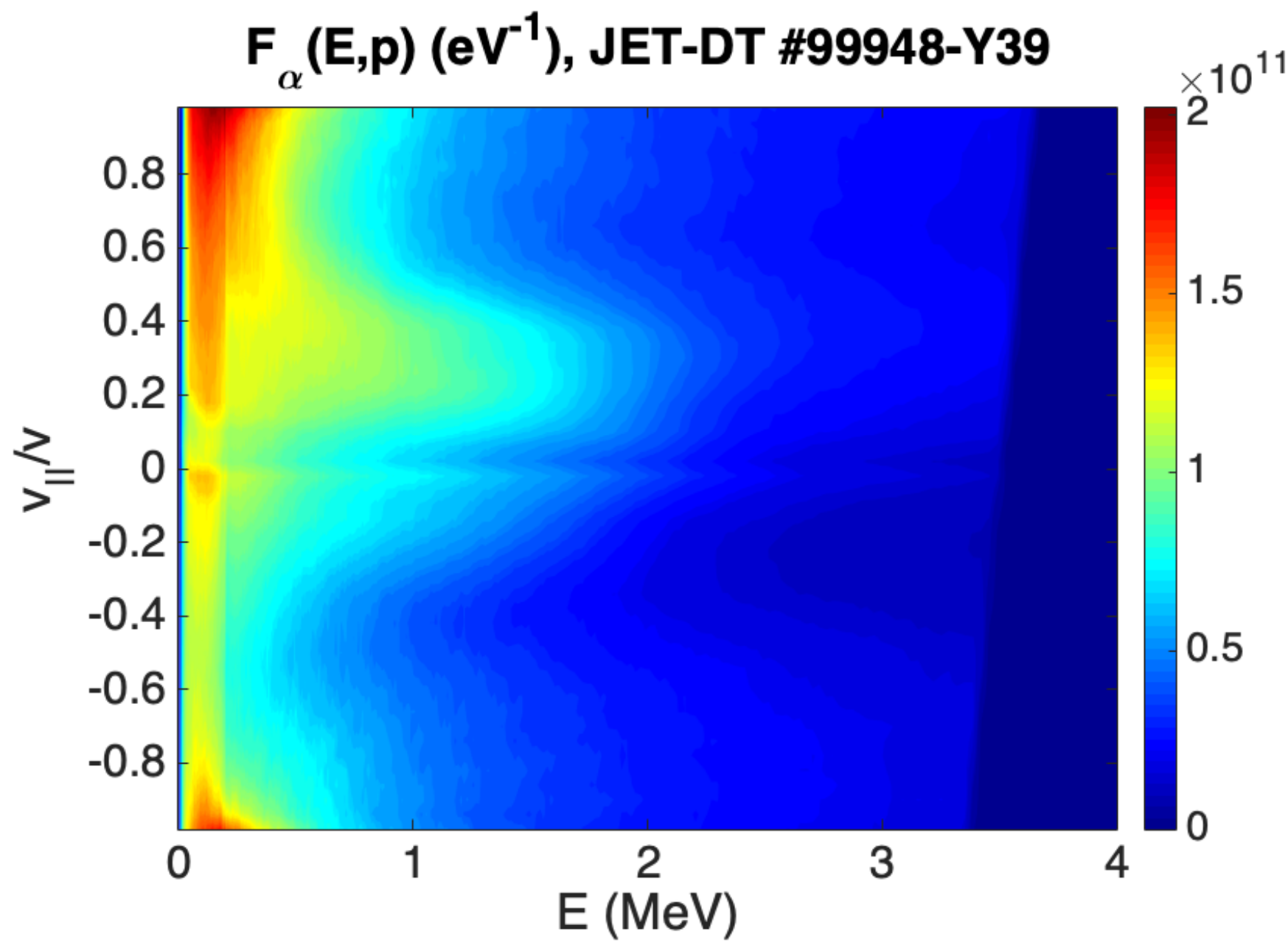
JET-DT #99948 : Fast-ion distributions



➤ Distributions in the $(E, \frac{v_{\parallel}}{v}, R, Z)$ phase space are provided from TRANSP-NUBEAM for alphas and NBI

➤ 256k markers are used for both alphas and NBI to reproduced distributions

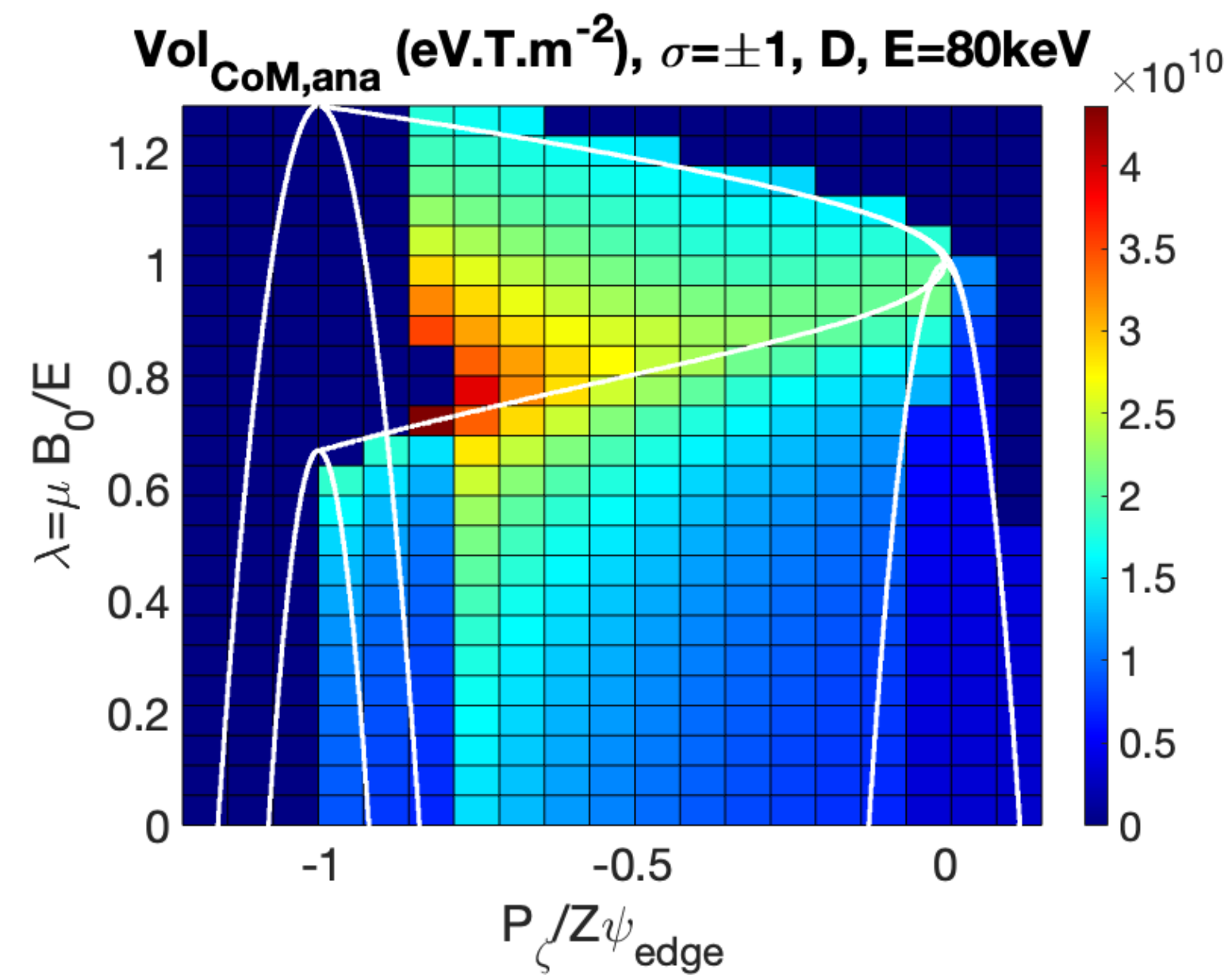
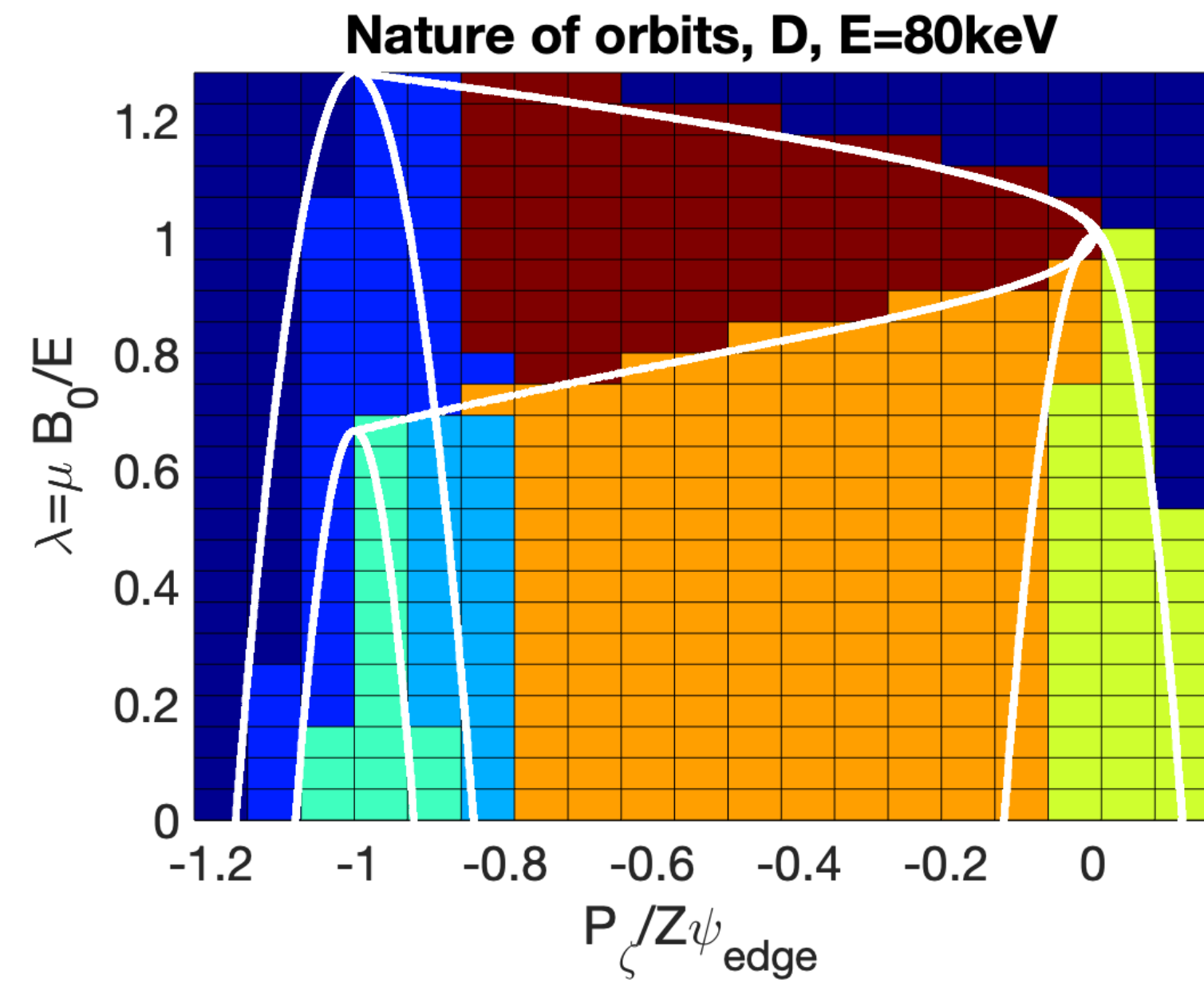
➤ Resolution in the $(E, \frac{v_{\parallel}}{v})$ space is relatively ok : $N_E = 70$ (NBI) – 340(α), $N_{v_{\parallel}} = 50$.



➤ A low spatial resolution is used : 220 grid points on ~10 flux surfaces. It restricts heavily P_{ϕ} resolution in CoM space. A 2D cartesian re-mapping with a 18x18 grid is performed

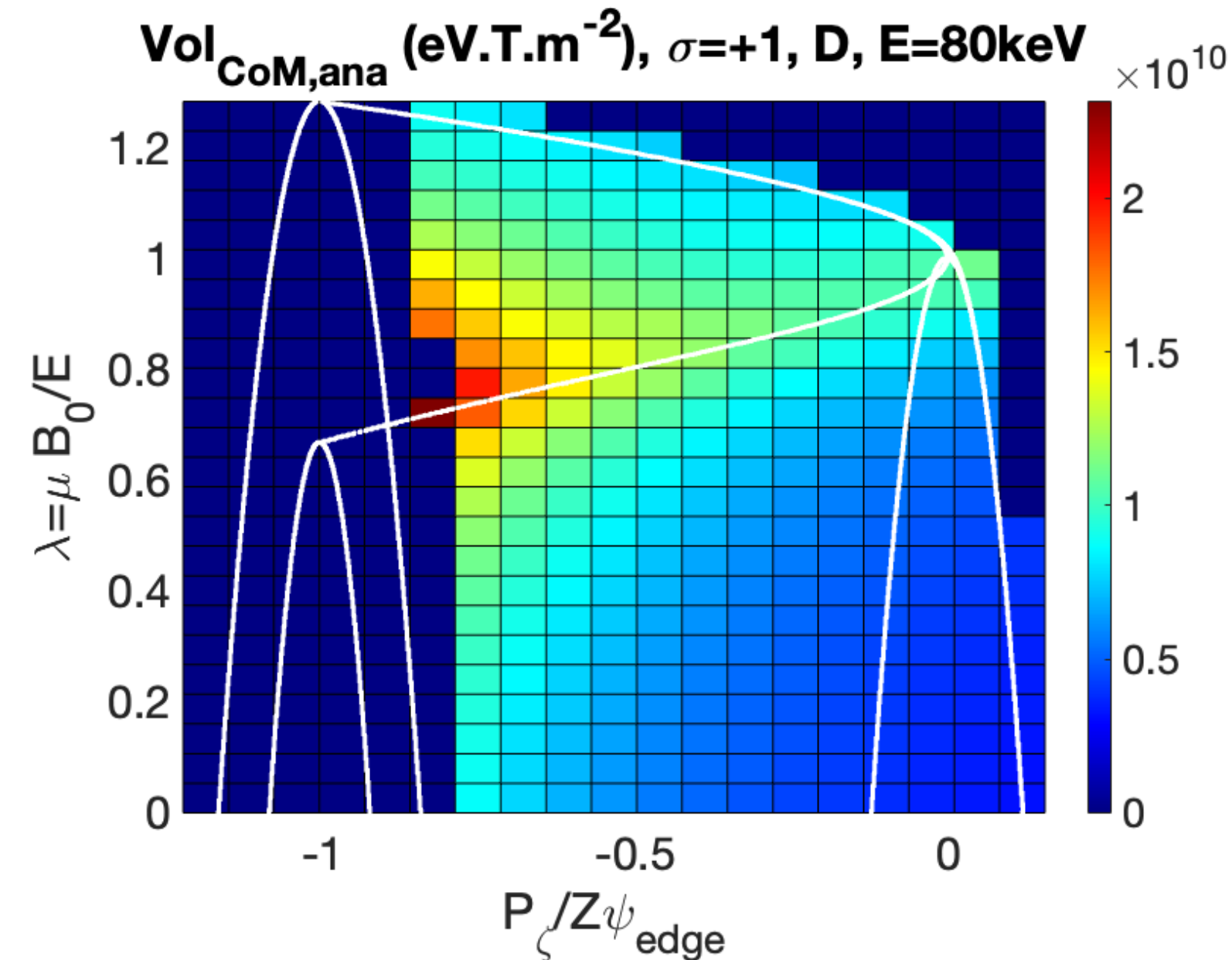
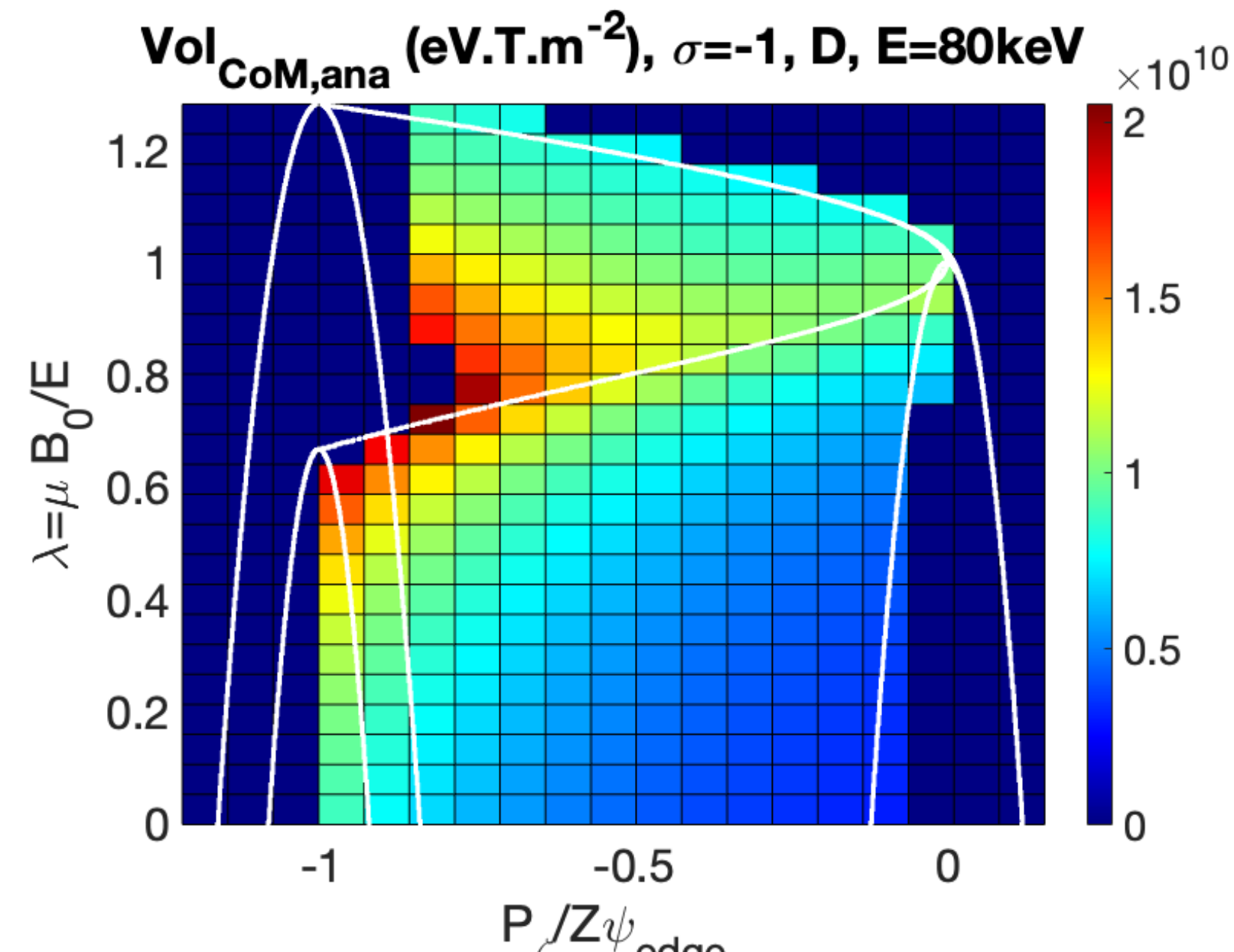
➤ A H-minority heated by ICRH is also present, but not modelled by NUBEAM

Jacobian construction on CoM grid



➤ The CoM grid used has the resolution : $(N_E=50, N_\lambda=25, N_{P_\varphi}=20)$

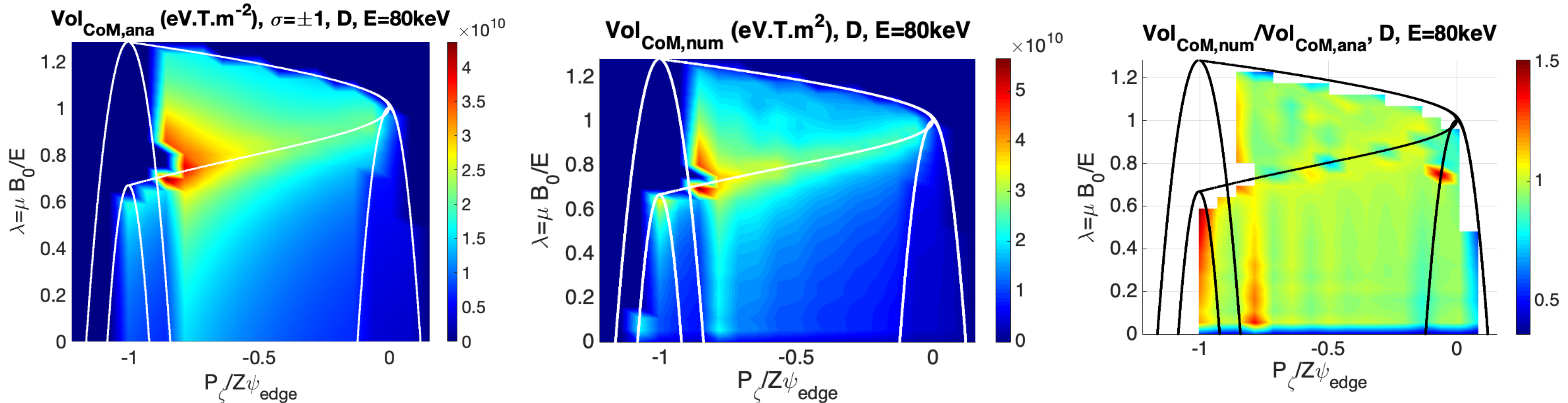
➤ $\Delta V_{CoM} = J_{CoM} \Delta E \Delta \lambda \Delta P_\varphi$ is rather smooth on the CoM grid



➤ Co-passing and counter-passing orbits treated separately when they both exist on CoM grid (degeneracy)

➤ Trapped orbits contribution split in two to ensure J_{CoM} continuity over trapped-passing boundary

Alternative Jacobian construction



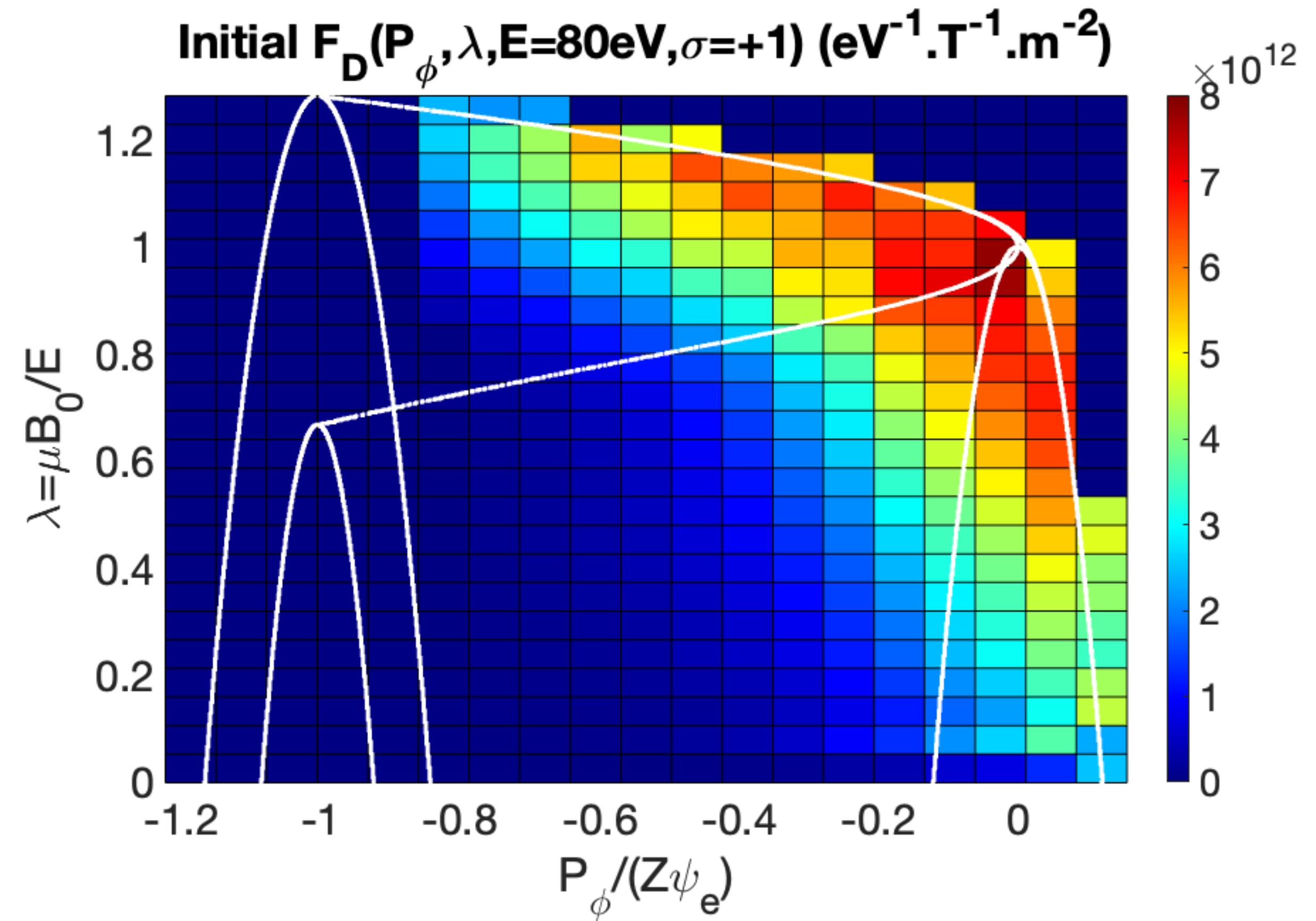
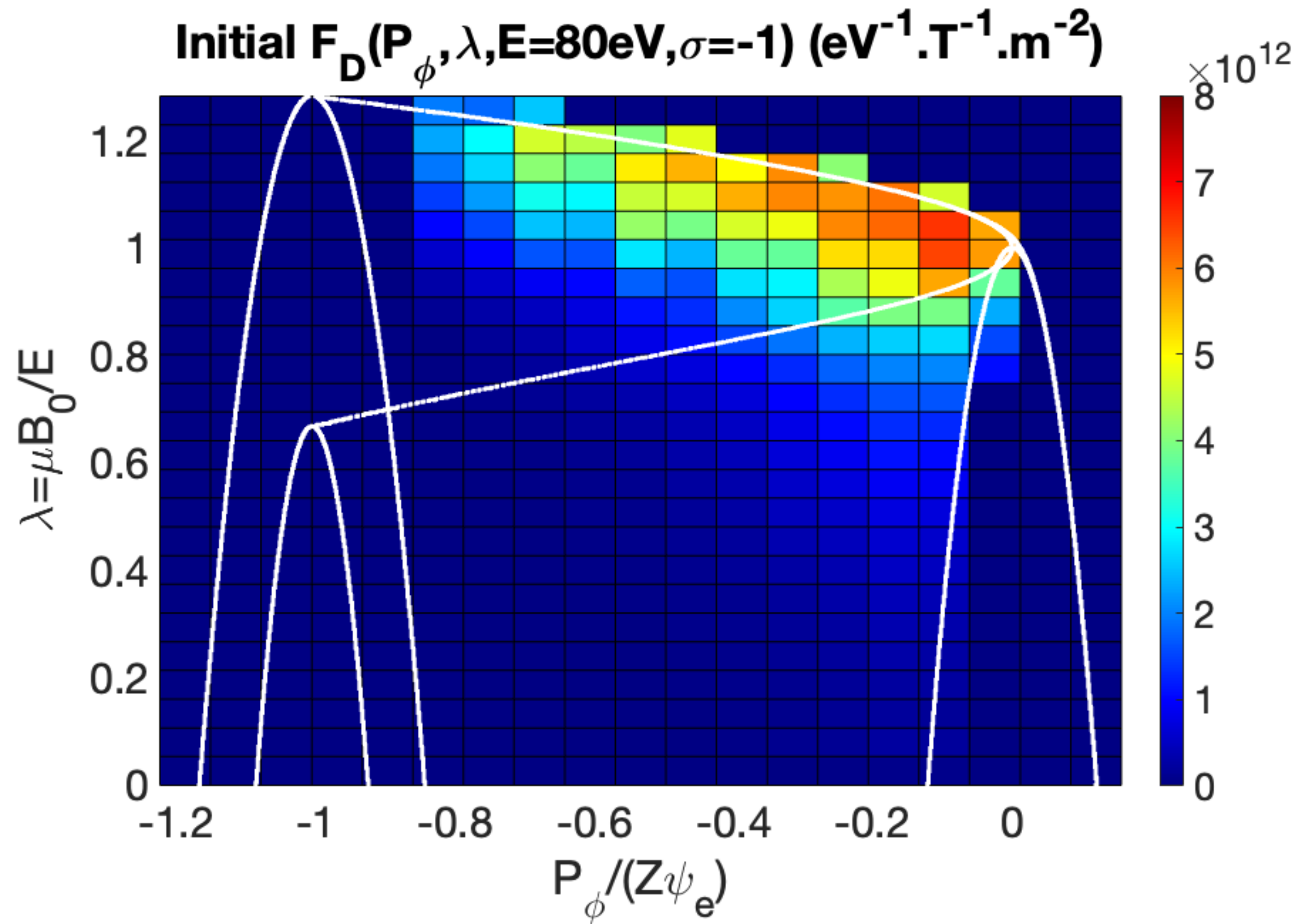
➤ ΔV_{CoM} can also be computed numerically using the $(E,p,R,Z)\rightarrow\text{CoM}$ coordinate transform as

$$\Delta V_{\text{CoM}}(E, \lambda, P_\varphi, \sigma) = \sum_i^{N_{\text{EpRZ}}} \delta_3(X_{\text{EpRZ},i} - X_{\text{CoM}}) \Delta E \Delta \lambda \Delta P_\varphi$$

➤ The two methods compare well, except at the domain edge due to the 3rd order interpolation

➤ Both Jacobian methods can be used to compute CoM distributions

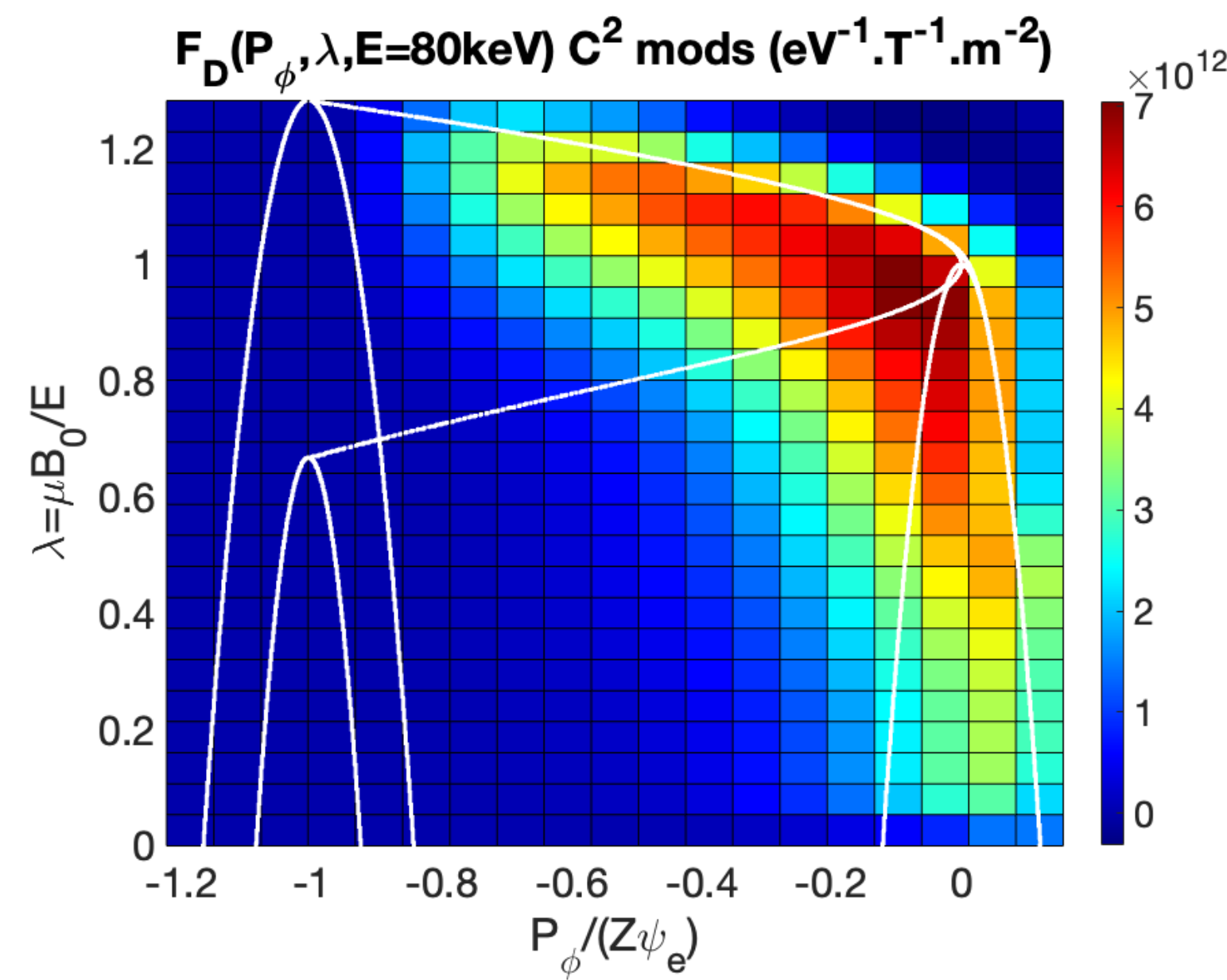
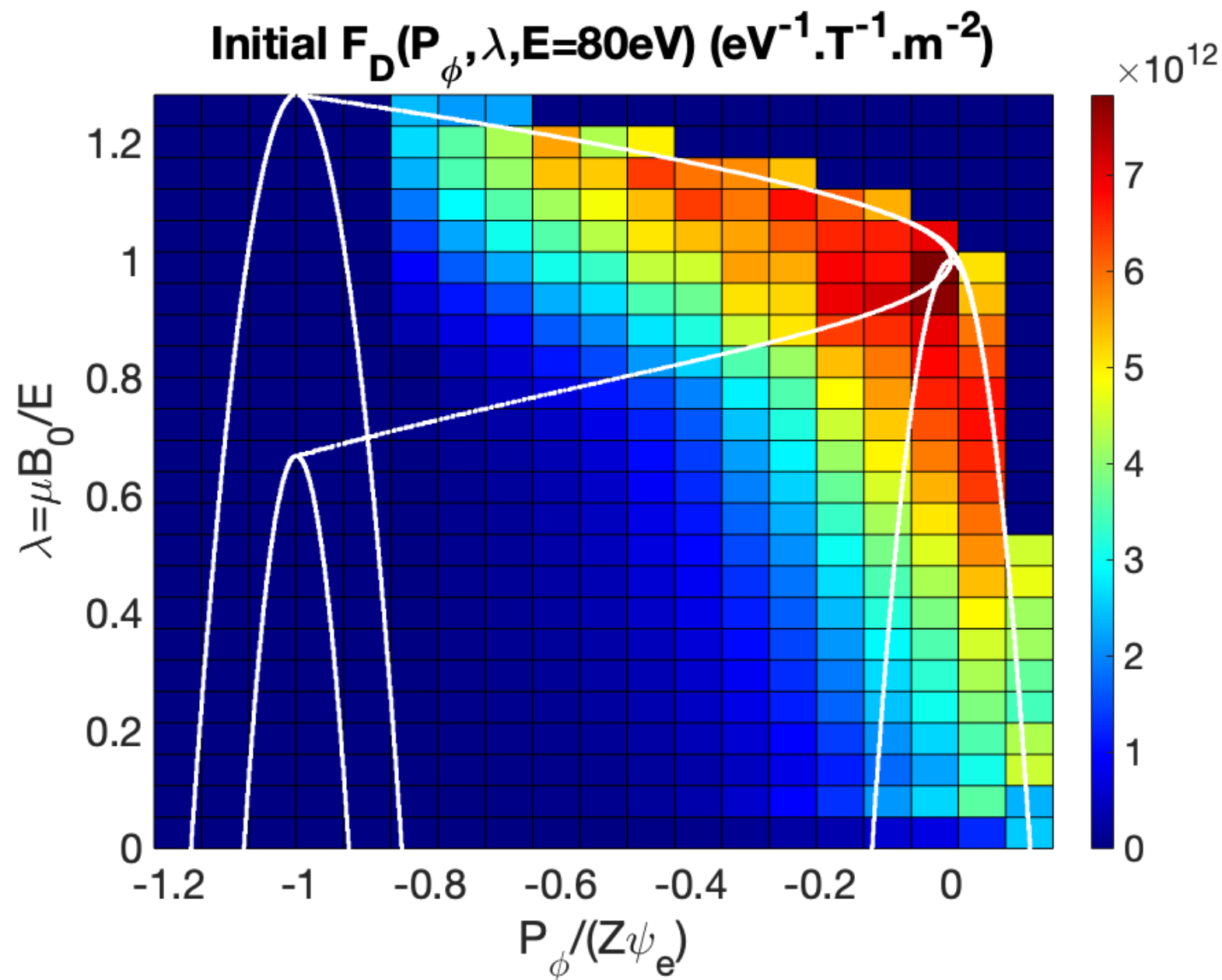
Interpolation between (E,p,R,Z)-> CoM distribution



➤ The **CoM D beam distribution** is computed as
$$F_D(E, \lambda, P_\phi, \sigma) = \sum_i^{N_{EpRZ}} \delta_3(\mathbf{X}_{EpRZ,i} - \mathbf{X}_{CoM}) F_D(E, p, R, Z) \frac{\Delta V_{EpRZ}}{\Delta V_{CoM}}$$

➤ $F_{D,CoM}$ needs also to be **separated** in two between **co-going** and **counter-going orbits** ($\sigma = \pm 1$)

Spline construction, D beam

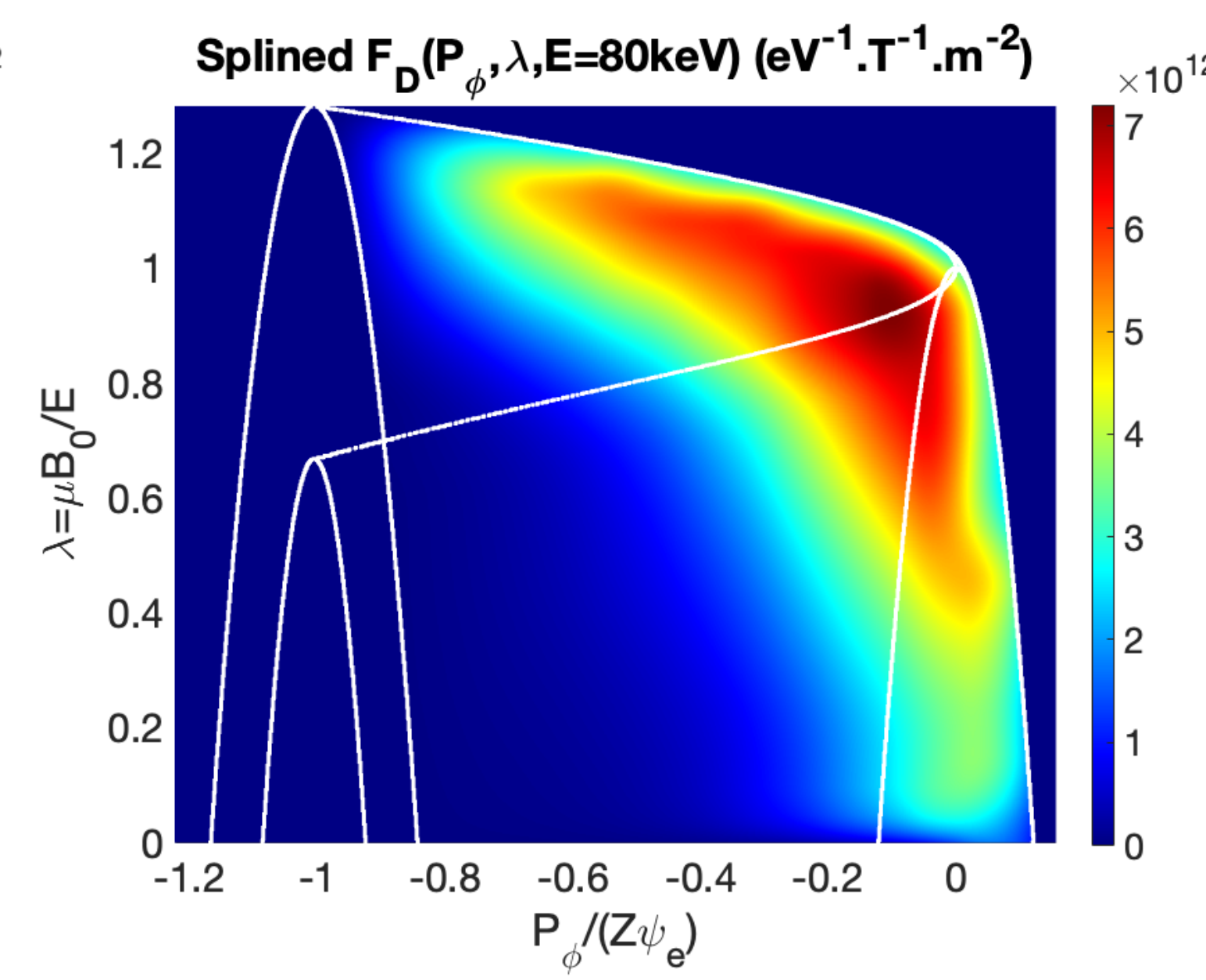
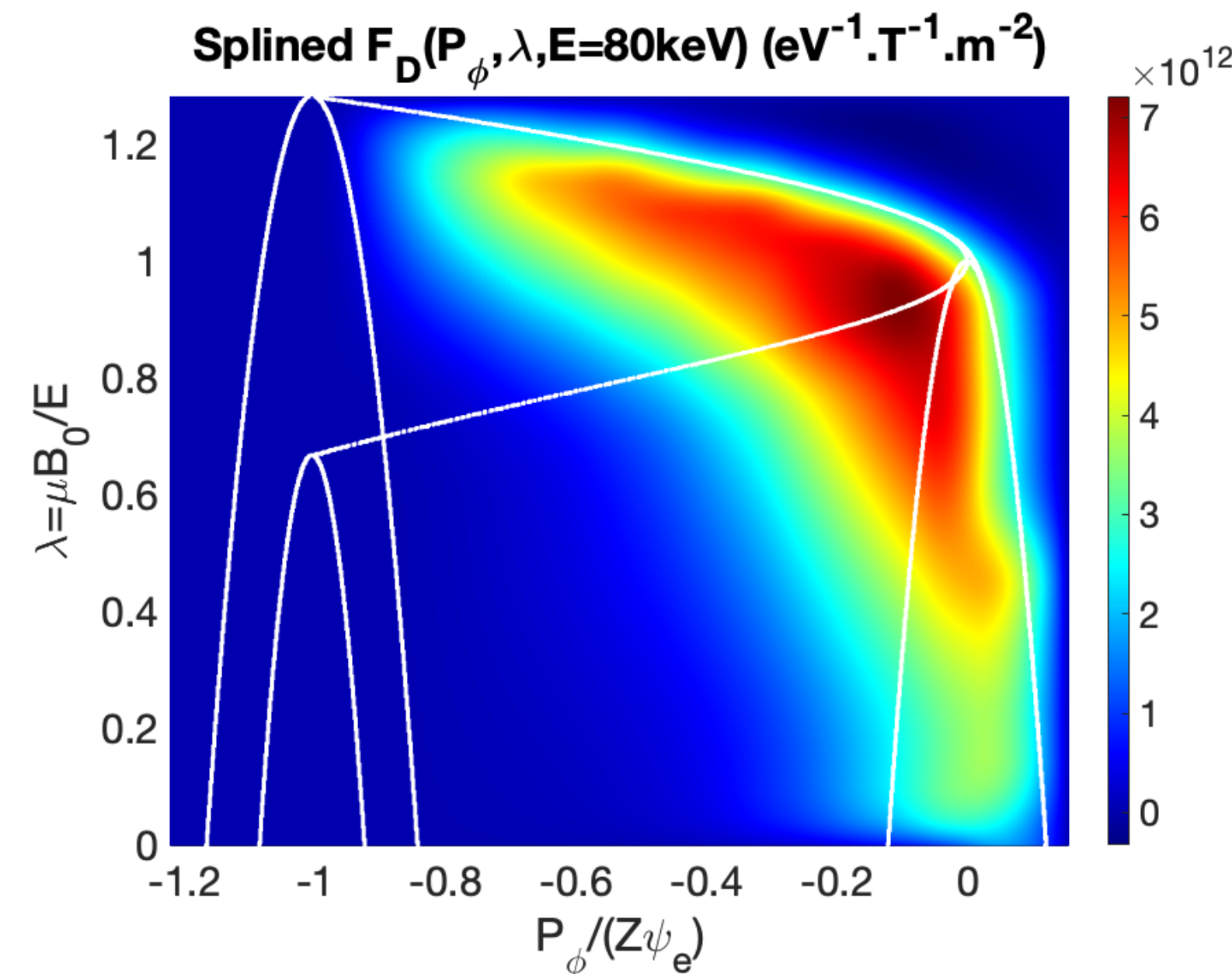


➤ C^2 CoM distribution defined with 2nd order 3D B-spline :

$$F_{D,s}(E, \lambda, P_\phi) = \sum_{i=0}^2 \sum_{j=0}^2 \sum_{k=0}^2 a_{ijk} x_E^i x_\lambda^j x_{P_\phi}^k, \quad x \in [0, 1]$$

➤ Distribution on CoM grid slightly adjusted to satisfy C^2 condition

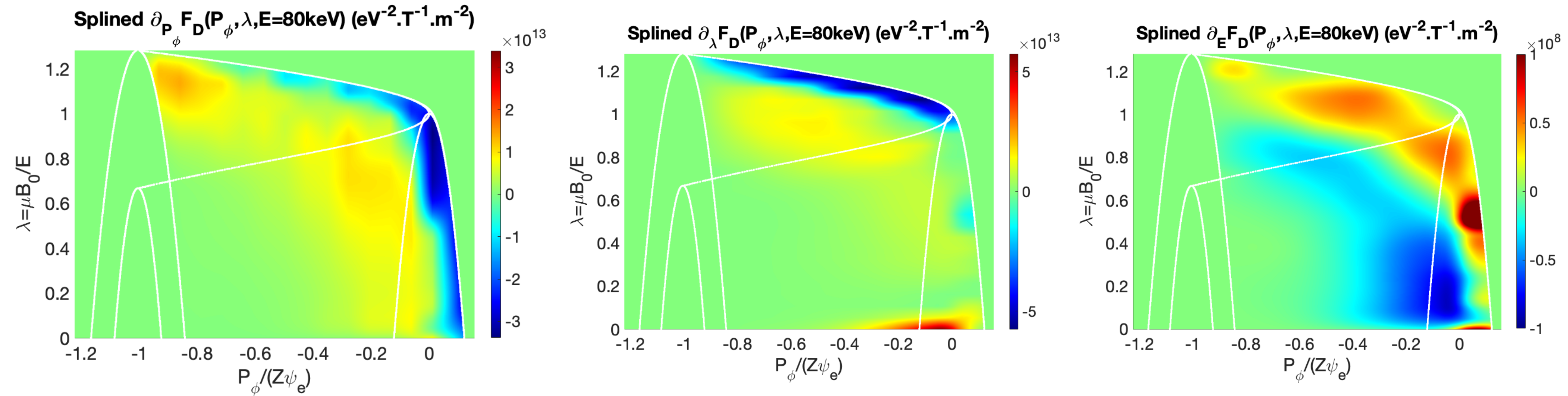
$$F(x_{i+1}) = \frac{3}{4}F(x_i) + \frac{1}{2}F'(x_i) + \frac{1}{4}F(x_{i+2})$$



➤ Samples out of topological boundaries removed via backward CoM \rightarrow (E,p,R,Z) transformation

➤ Markers in 5D/6D full-F codes (cylindrical/Boozer coordinates) initialised via backward transformation

1st order derivatives in CoM space



➤ **First order C^1 derivatives of the CoM distribution directly obtained from the 3D spline**

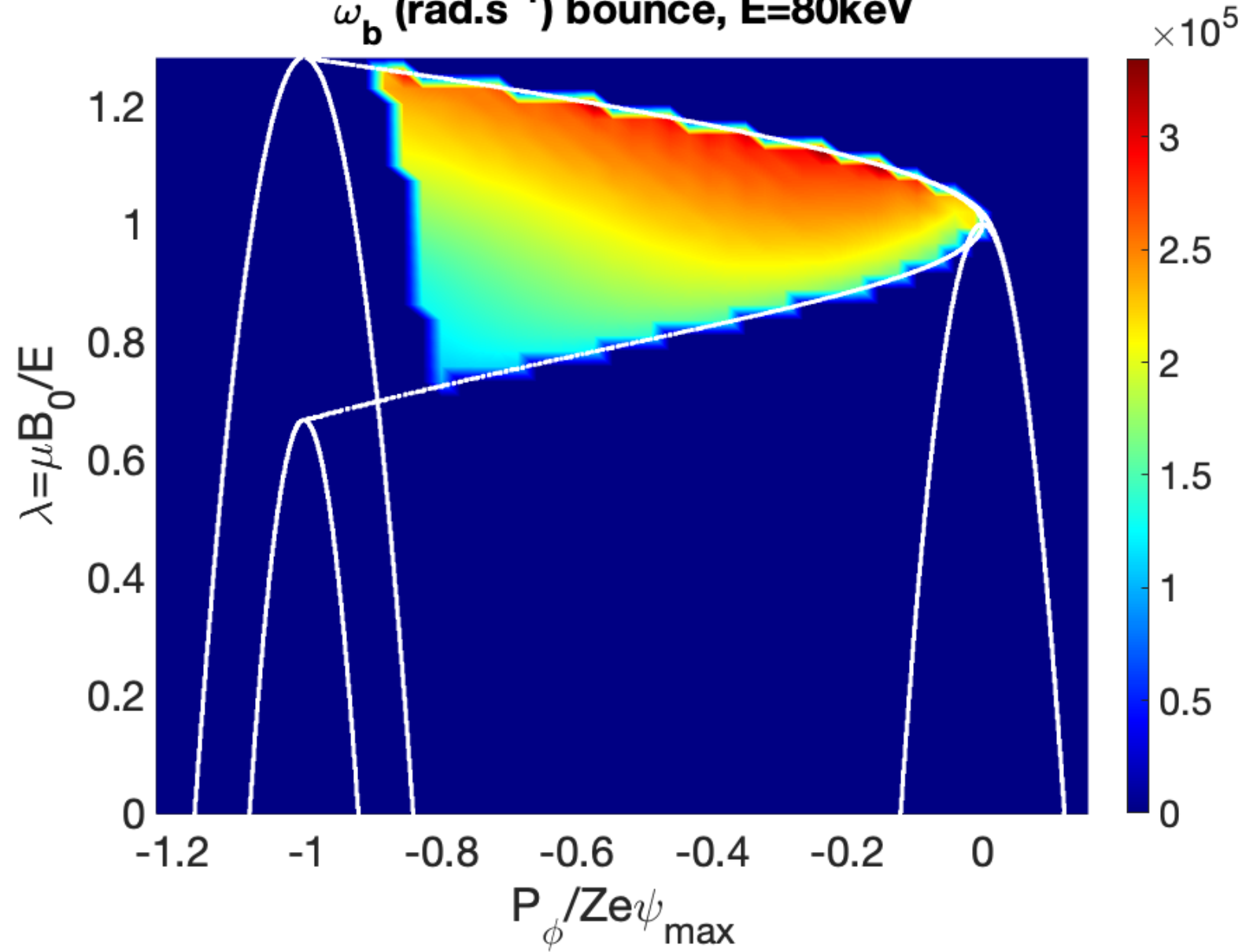
➤ **In δF codes, the derivatives used in the weight equation can be computed through the chain rule**

$$\nabla F|_{\mu, v_{\parallel}} = \nabla E|_{\mu, v_{\parallel}} \frac{\partial F}{\partial E} + \nabla \lambda|_{\mu, v_{\parallel}} \frac{\partial F}{\partial \lambda} + \nabla P_\phi|_{\mu, v_{\parallel}} \frac{\partial F}{\partial P_\phi} \quad \frac{\partial F}{\partial v_{\parallel}}|_{\mu, X} = \frac{\partial E}{\partial v_{\parallel}}|_{\mu, X} \frac{\partial F}{\partial E} + \frac{\partial \lambda}{\partial v_{\parallel}}|_{\mu, X} \frac{\partial F}{\partial \lambda} + \frac{\partial P_\phi}{\partial v_{\parallel}}|_{\mu, X} \frac{\partial F}{\partial P_\phi}$$

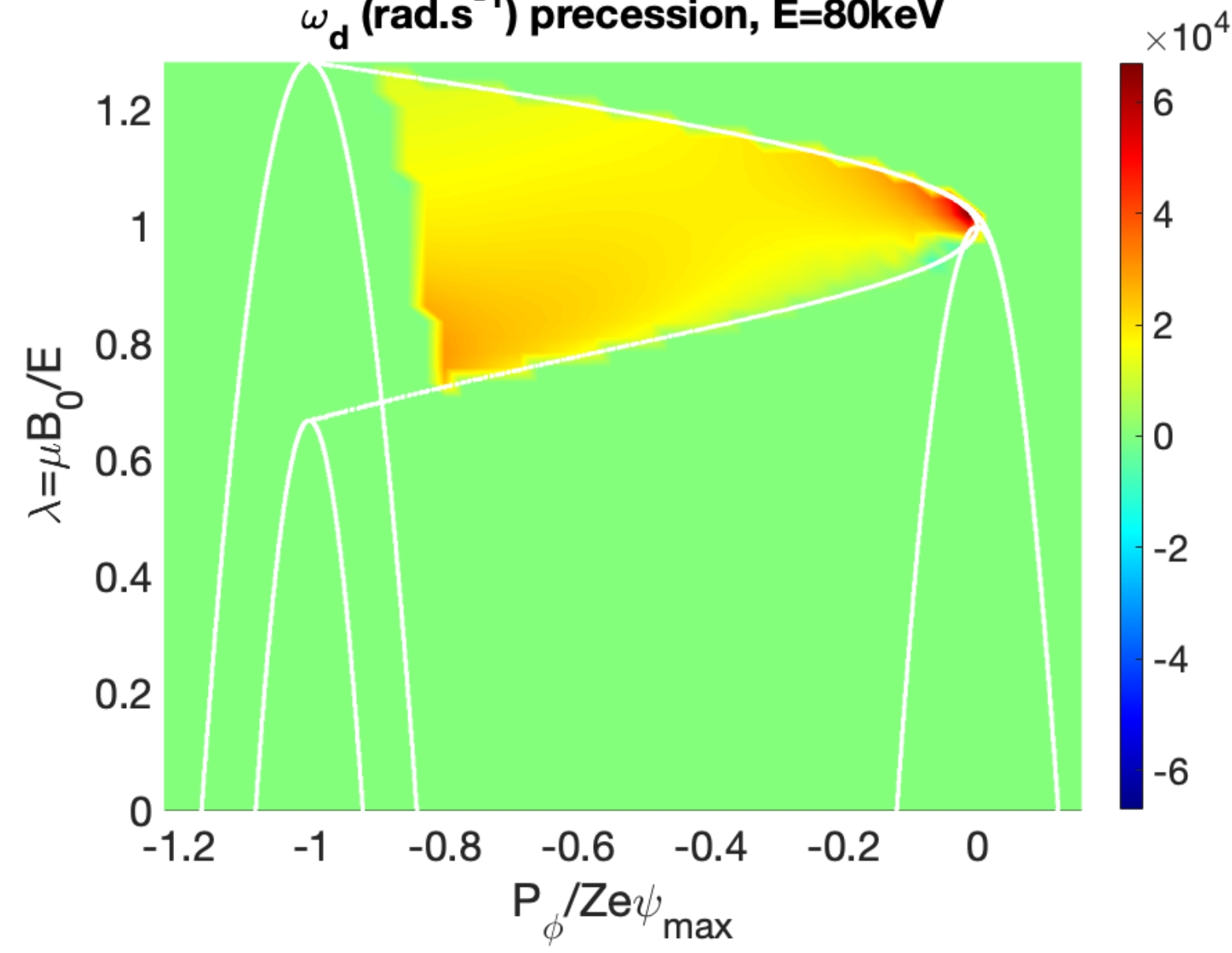
➤ **The forward transformation $(E, p, R, Z) \rightarrow \text{CoM}$ can be used for each marker to determine which of the splined CoM distributions to use (co-going or counter-going)**

EP frequencies in CoM space

ω_b (rad.s⁻¹) bounce, E=80keV

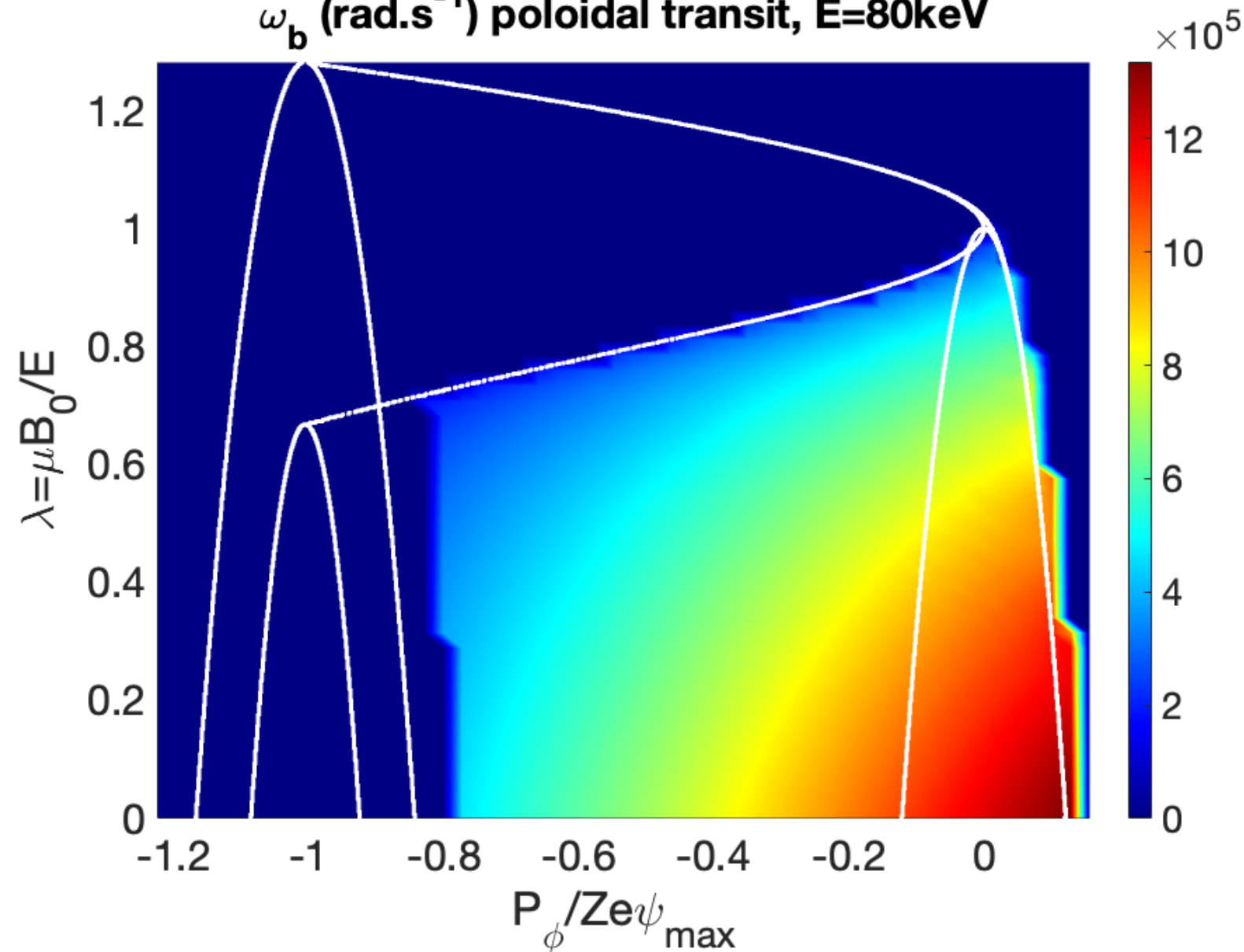


ω_d (rad.s⁻¹) precession, E=80keV

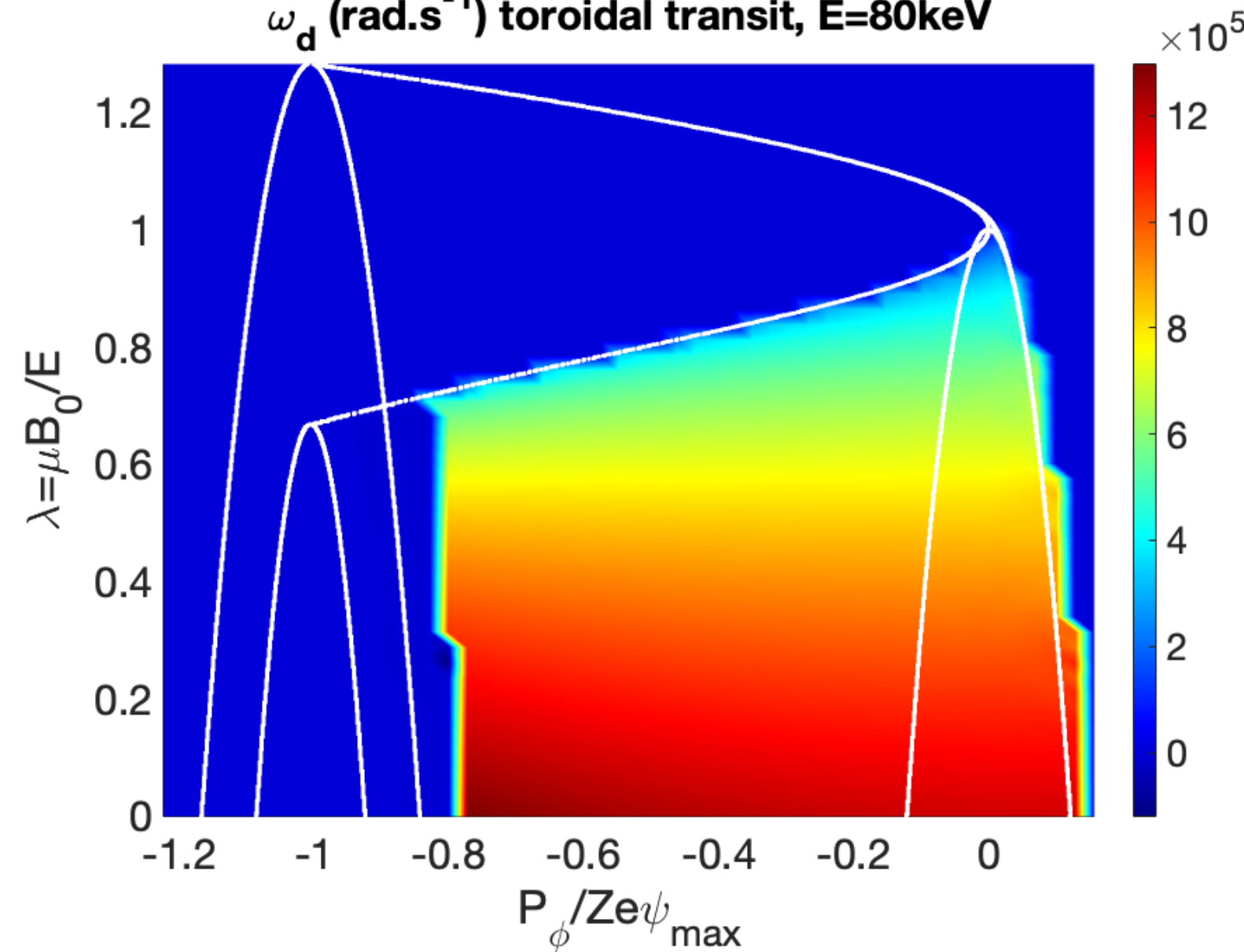


➤ EP frequencies (ω_b, ω_d) can be obtained in the **CoM spaces** through **orbit analysis** ($\theta(t), \varphi(t)$ traces)

ω_b (rad.s⁻¹) poloidal transit, E=80keV



ω_d (rad.s⁻¹) toroidal transit, E=80keV



➤ These mappings enable **identification of resonant plans** for a given mode frequency

➤ **IDS** will be created to store these informations for a given scenario

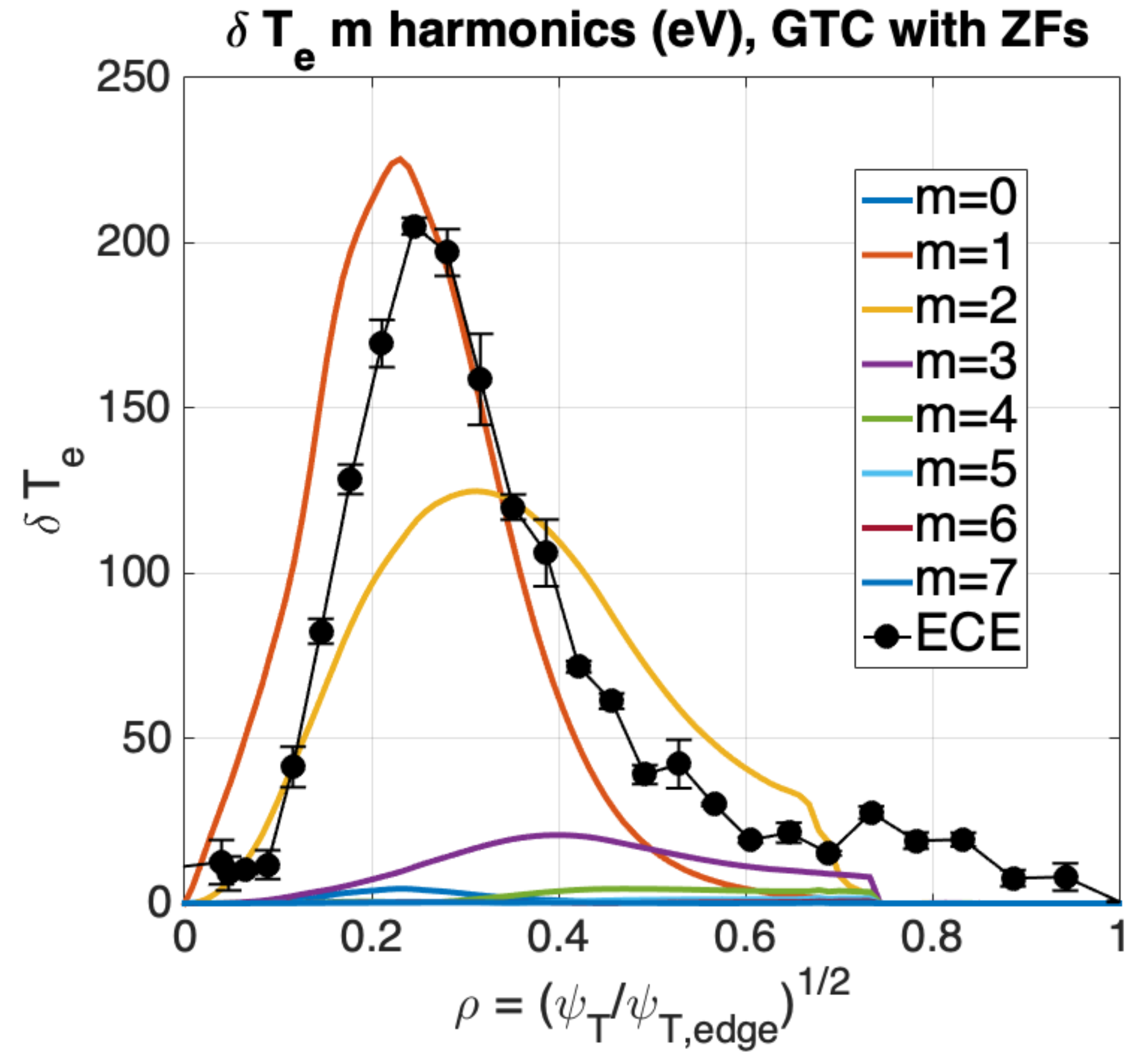
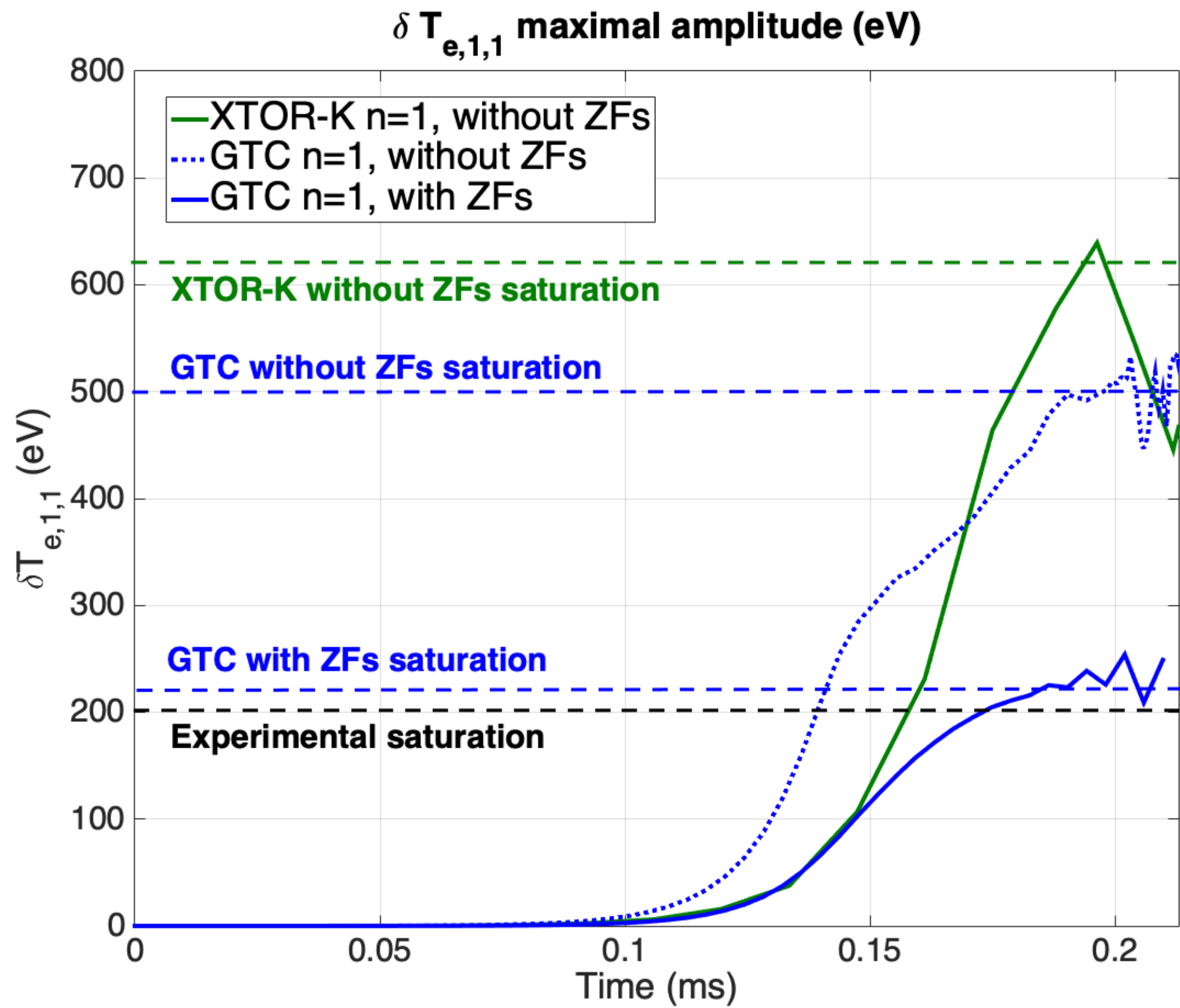
Conclusions

- A **versatile** method to initialise **CoM distributions** in **full-F** and δF codes from **experimental** and **Fokker-Planck inputs** was presented
- An **analytical backward CoM \rightarrow (E,p,R,Z) transformation** was successfully created, allowing **precise orbit characterisation** in CoM space
- Using XTOR-K's particle pusher, the **CoM Jacobian** is **accurately computed** on a **cartesian CoM grid**
- A **JET-DT pulse** with **potential fishbone-induced microturbulence stabilisation** is used to test the CoM distribution transformation method
- The **NUBEAM (E,p,R,Z) distribution** is transformed into a **CoM distribution**, separating CoM space between **co-going** and **counter-going topological regions**
- **3D B-spline** are used to define C^2 **CoM distributions** and their C^1 **first-order derivatives**. The **backward transformation** is used to **enforce the CoM space topological boundaries**

Perspectives

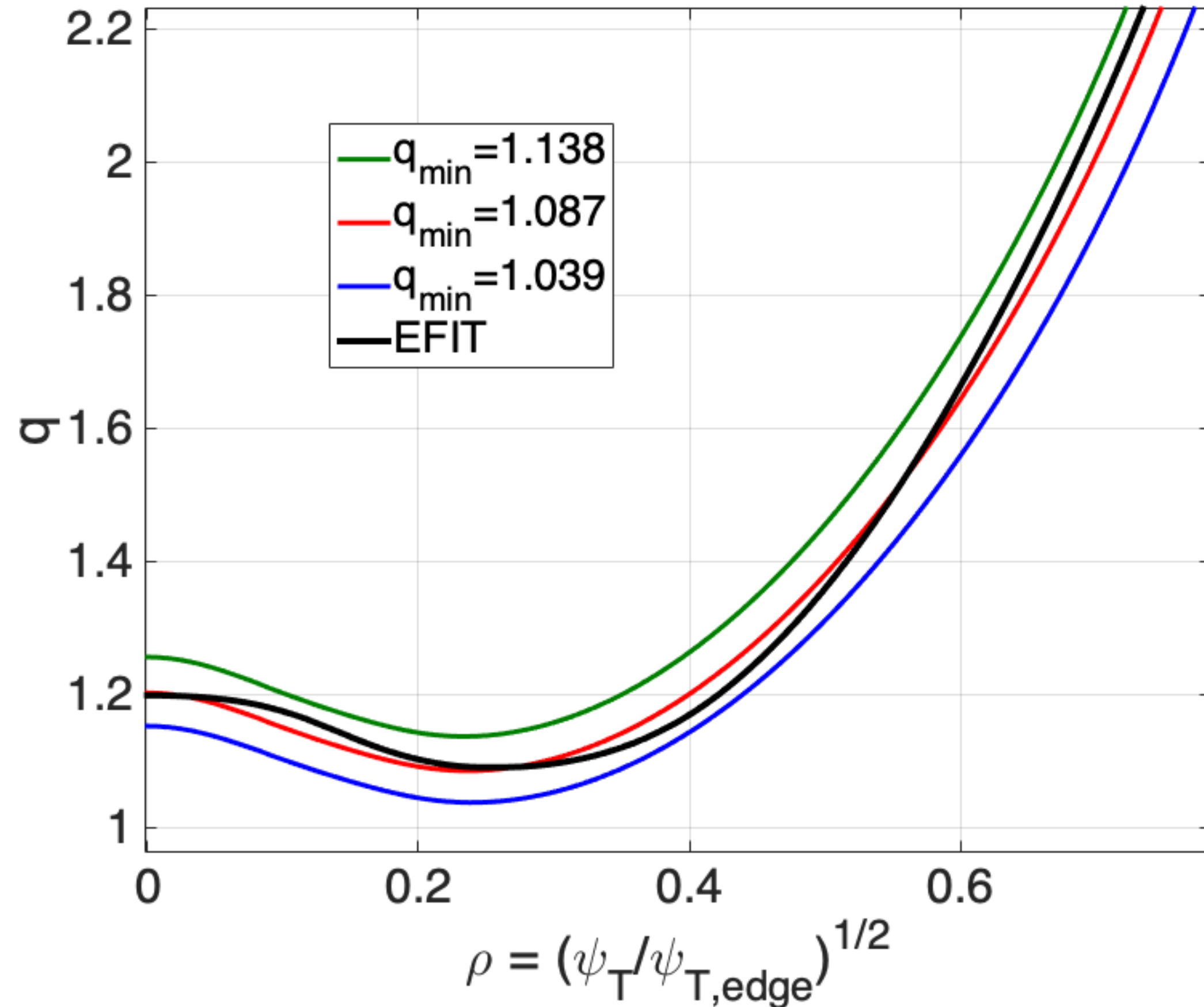
- **Re-process** the D-T beam and alpha distributions with **NUBEAM** input using **finer resolution**
- Perform loop **forward** $(E, p, R, Z) \rightarrow (E, \lambda, P_\phi, \sigma)$ and **backward** $(E, \lambda, P_\phi, \sigma) \rightarrow (E, p, R, Z)$ **transformations** to **quantity errors made** during distribution conversion
- **Test the CoM initialisation** in **first principles codes** such as **XTOR-K** (full-F) and **GTC** (δF)
- **Implement** the method in **IMAS** as to be compatible with the **EP stability workflow**
- **Accommodate IMAS** outputs for all EP codes across the **EP community**
- Perform **nonlinear kinetic-MHD** and **gyrokinetic** simulations to study **fishbone-microturbulence** interaction for the **JET-DT pulse #99948**

Nonlinear validation against ECE measurements

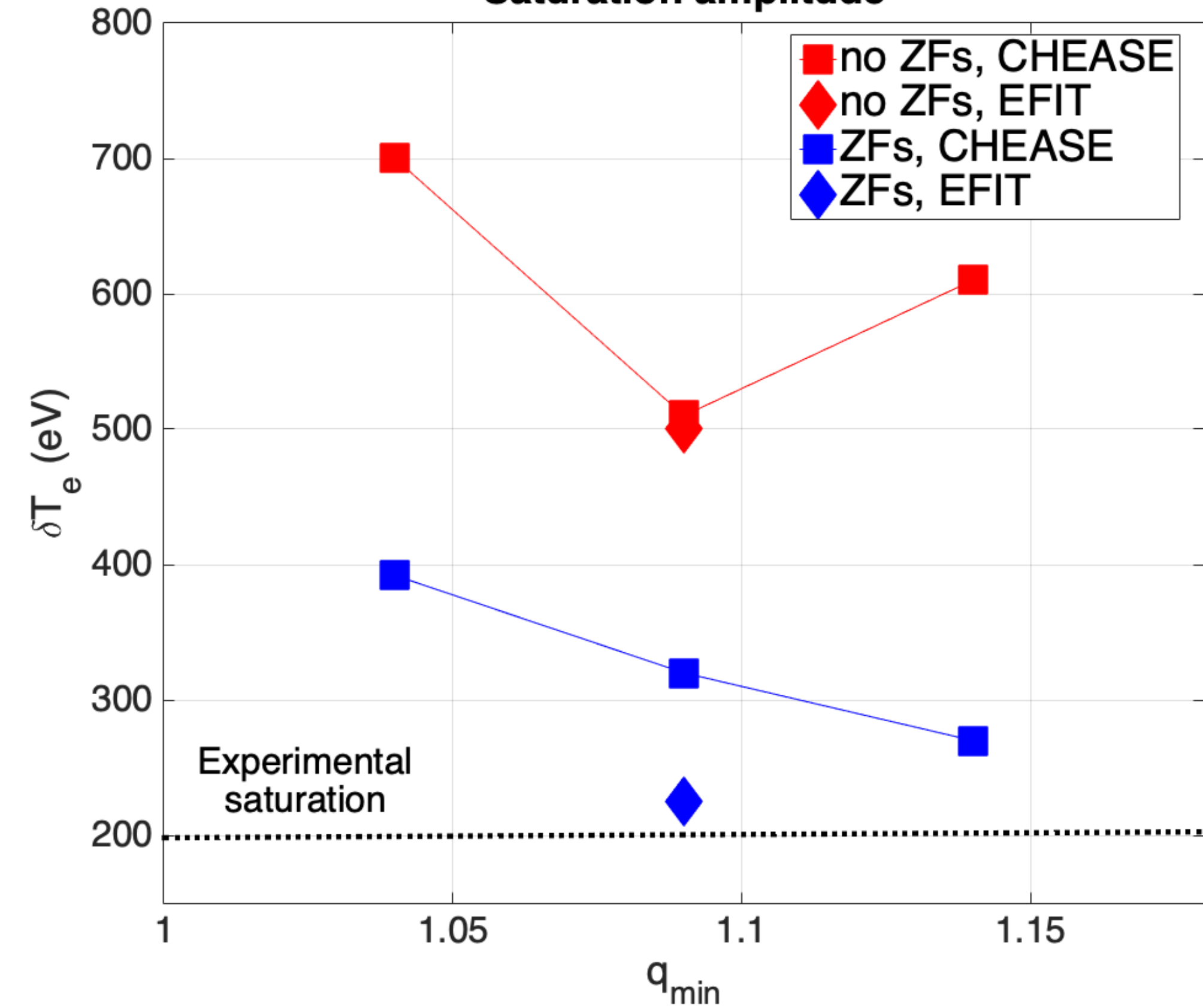


Sensitivity of fishbone amplitude on q_{min}

Safety factor profiles



Saturation amplitude



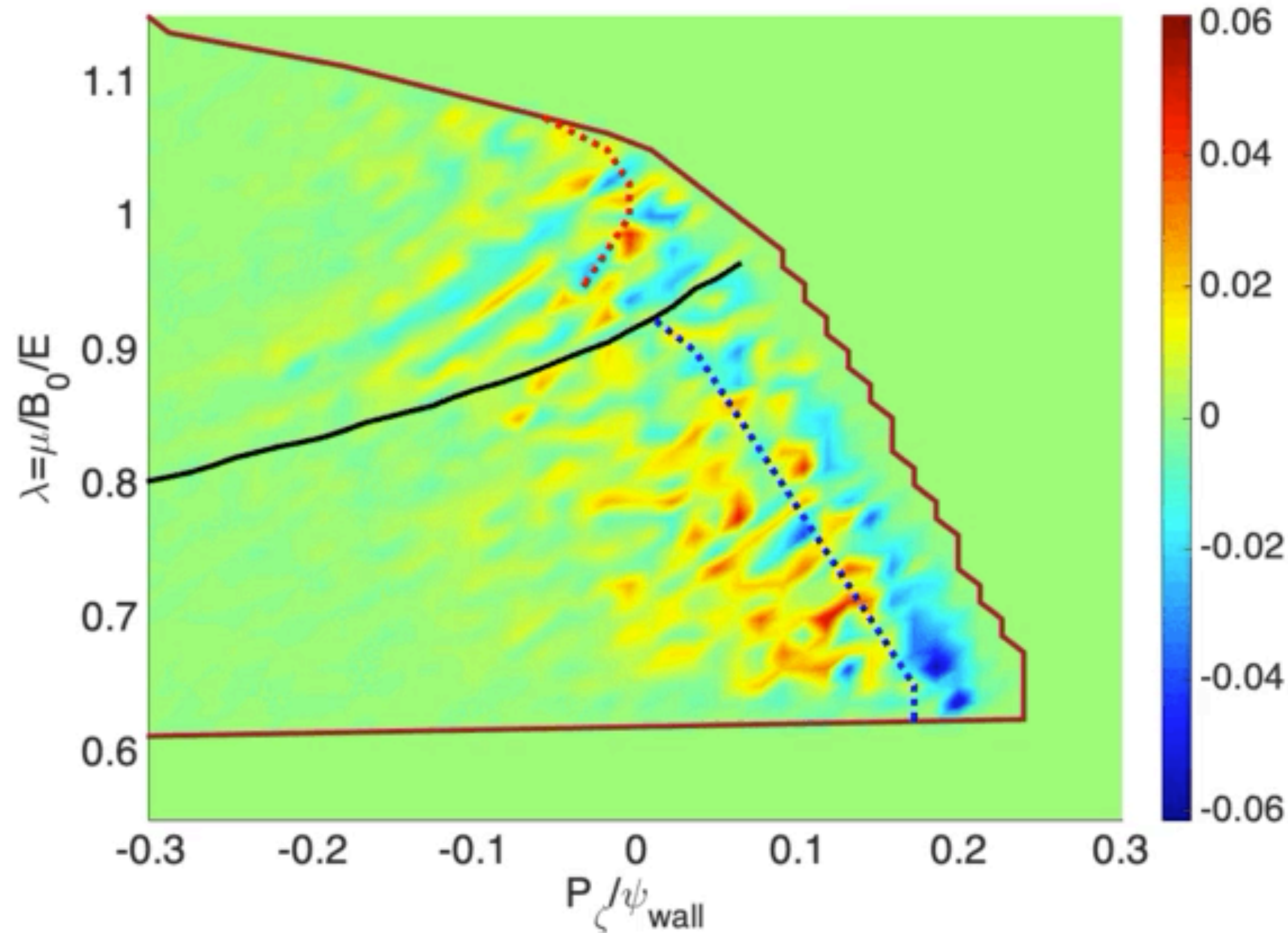
➤ CHEASE used to produce a set of q profiles with different q_{min} values

➤ Saturation amplitudes sensitive to q_{min} values and magnetic shear

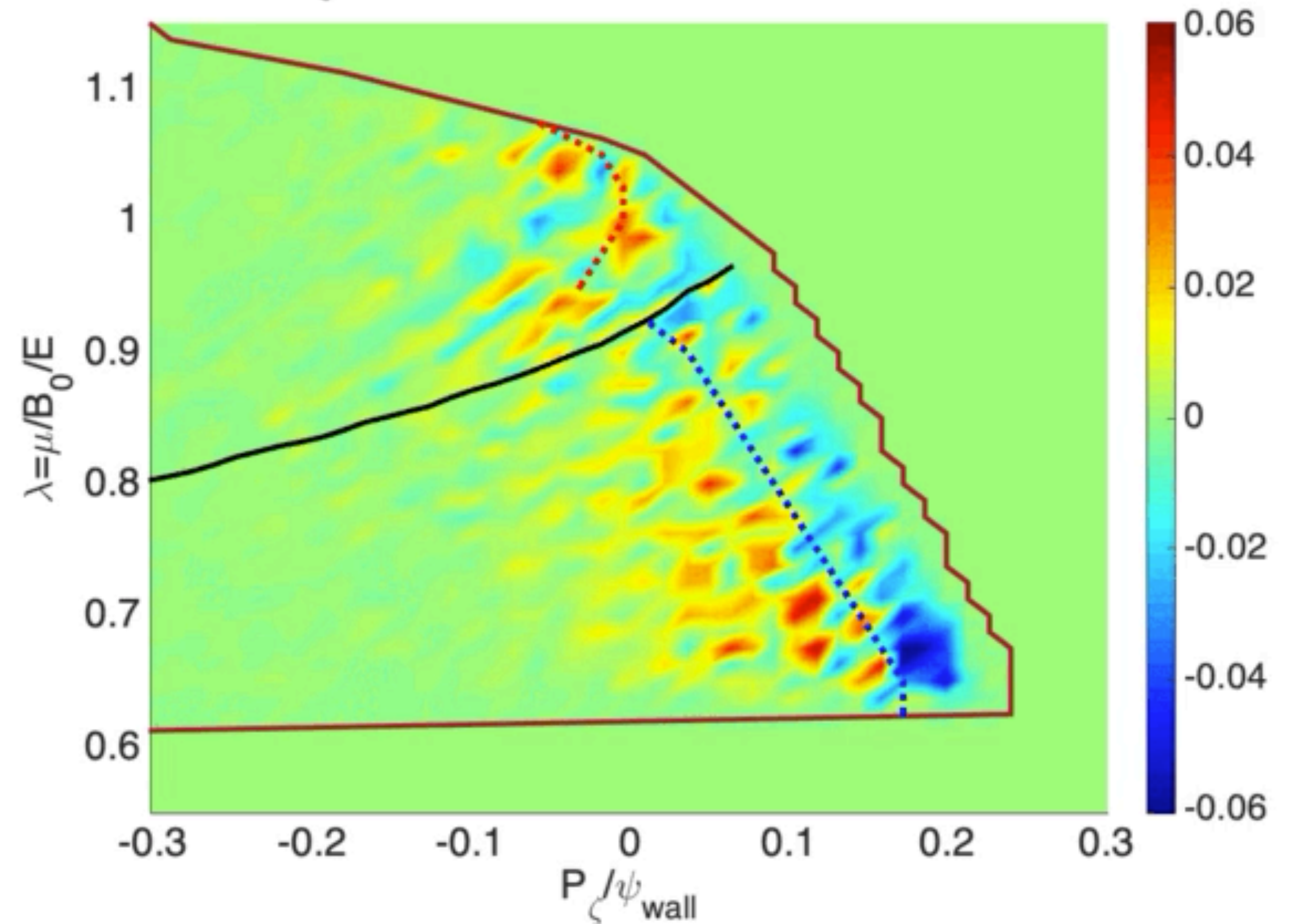
➤ Zonal flows inclusion decreases significantly saturation amplitude for all cases

Zonal flows prevent large EP radial excursion

$\partial_t \delta f$, **no ZFs**, $t=0.11655\text{ms}$

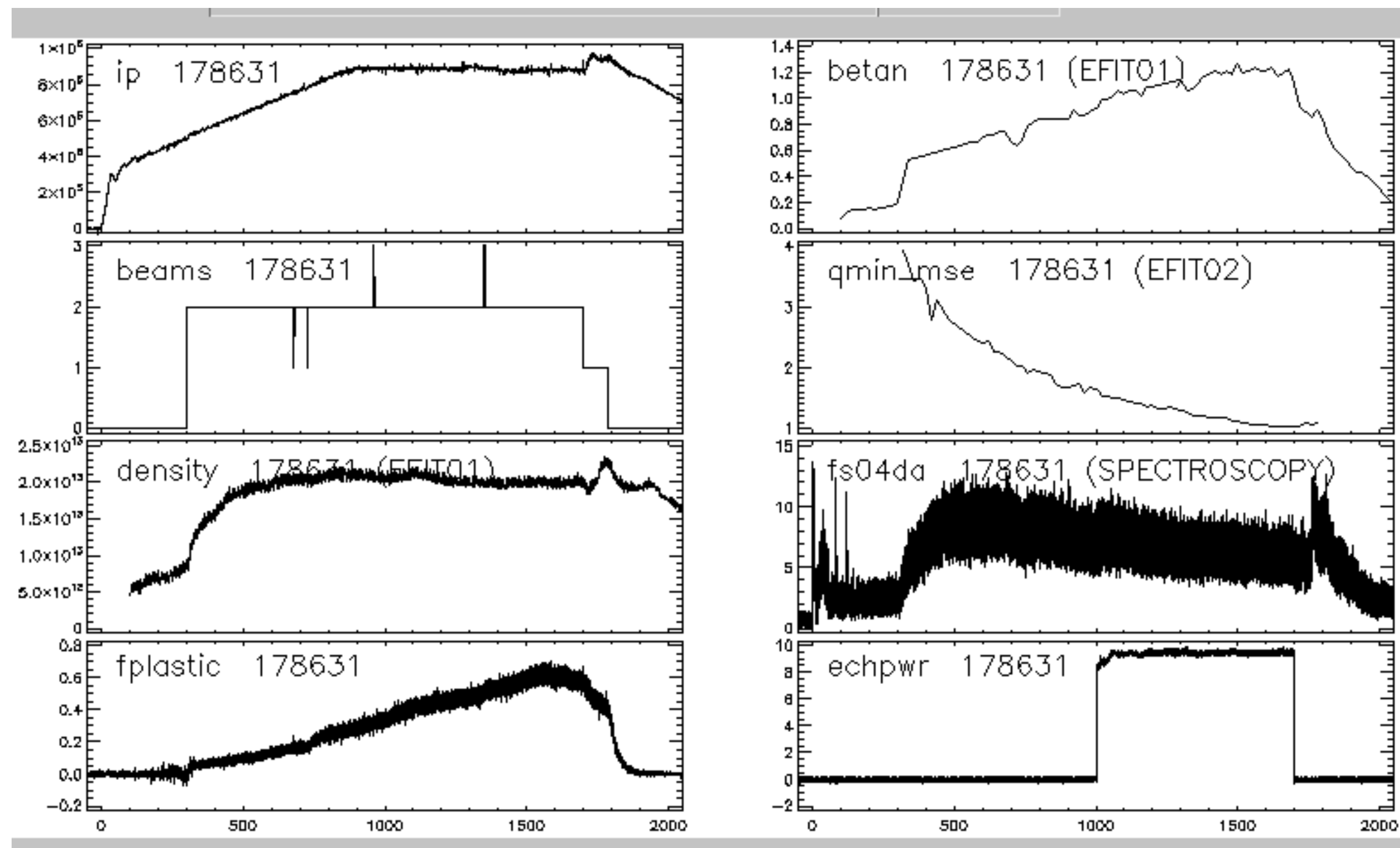
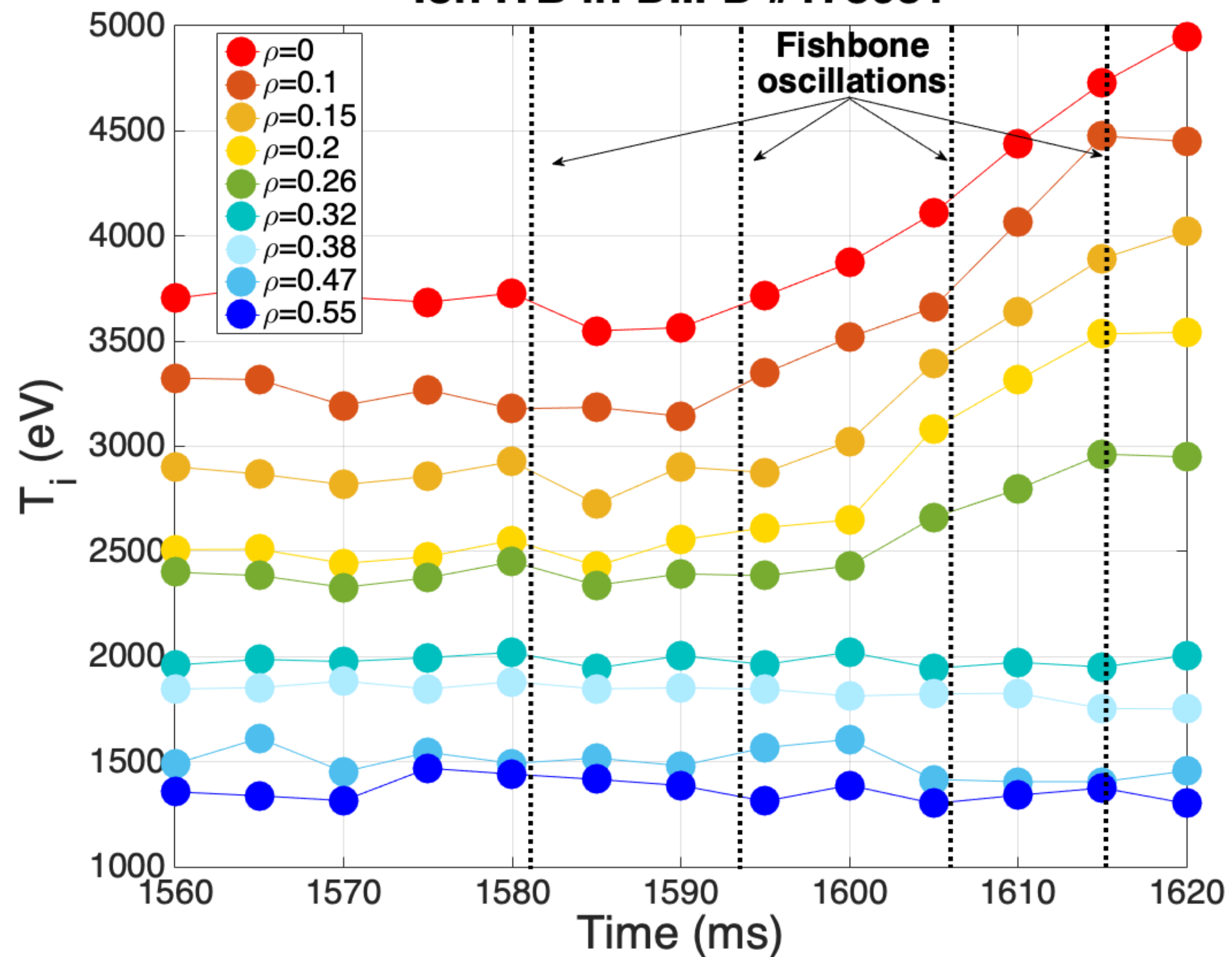


$\partial_t \delta f$, **with ZFs**, $t=0.11655\text{ms}$

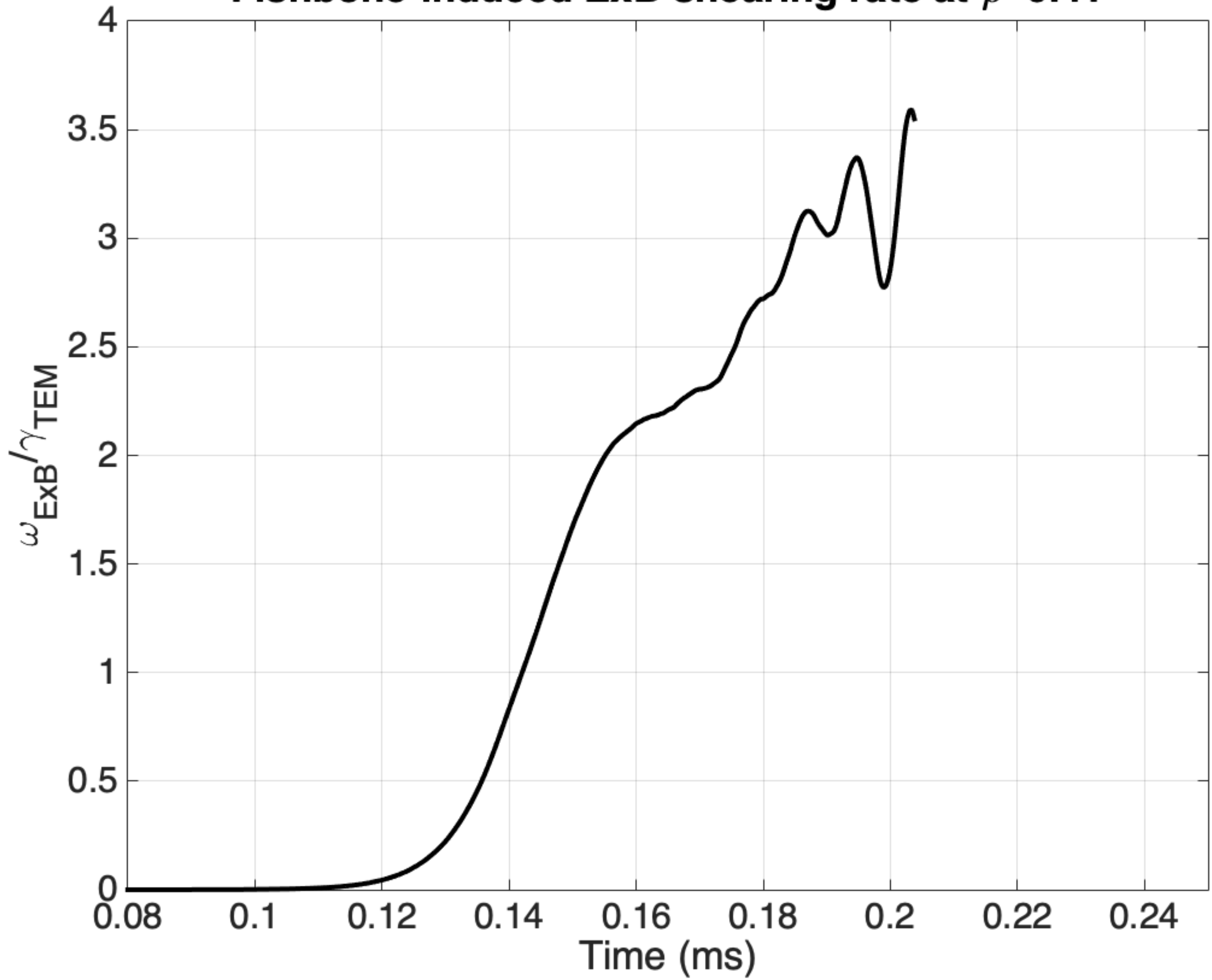


- **Hole and clump structures appear around both trapped and passing resonances**
- **EP transport from passing resonance stops earlier with zonal flows**
- **Zonal flows prevent hole and clump in trapped region to move as mode chirps down**

Ion ITB in DIII-D #178631

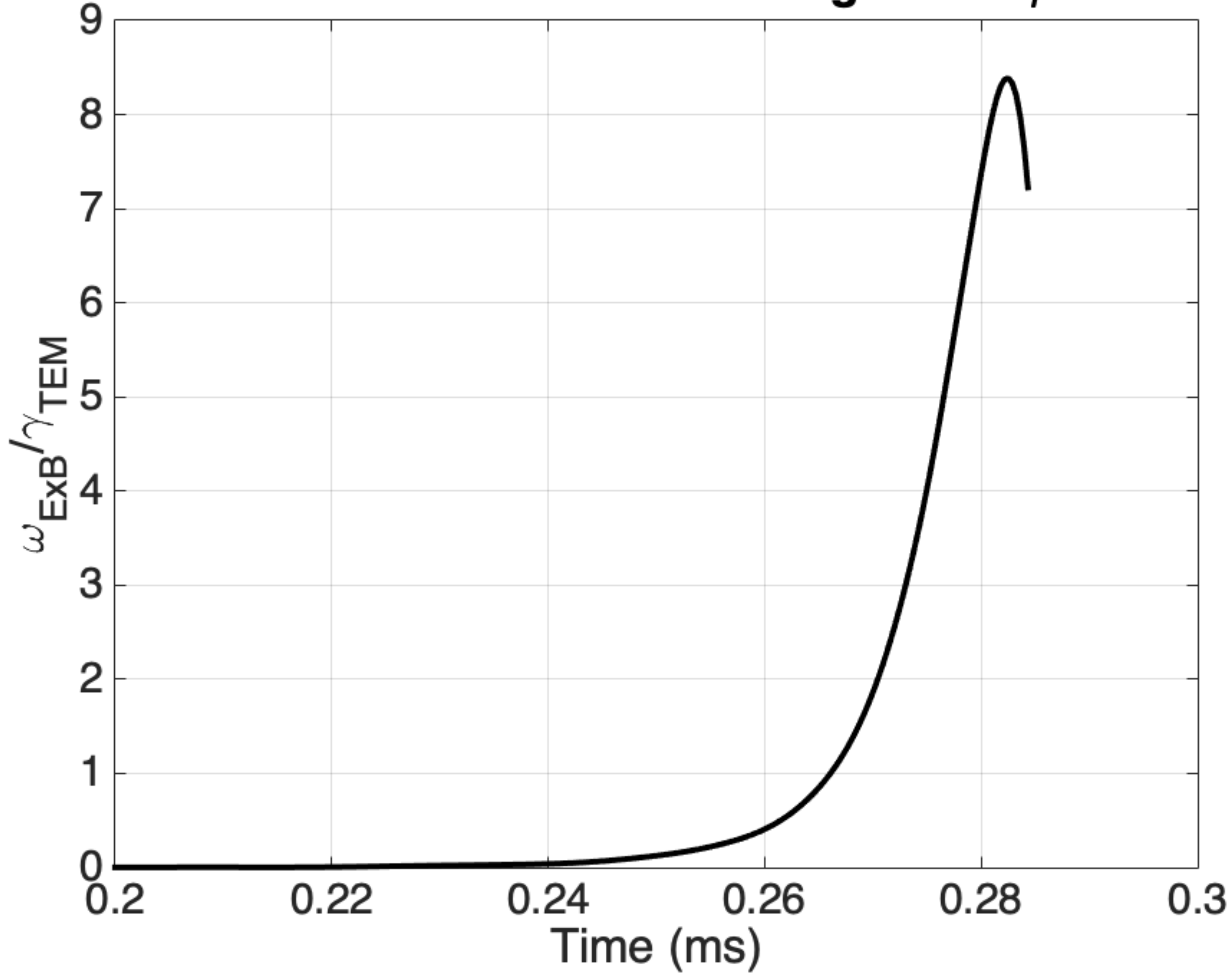


Fishbone-induced ExB shearing rate at $\rho=0.41$



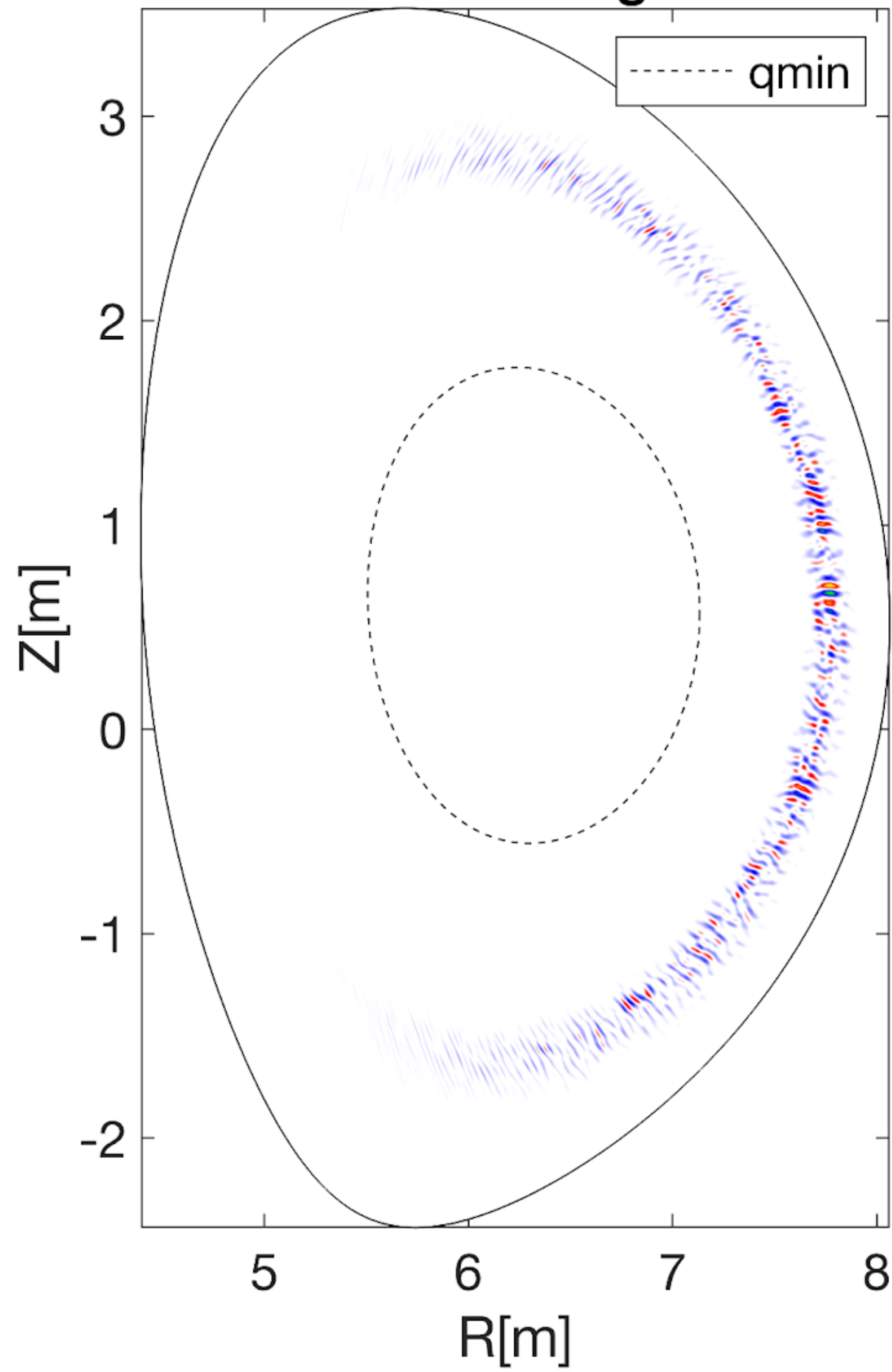
DIII-D

Fishbone-induced ExB shearing rate at $\rho=0.77$

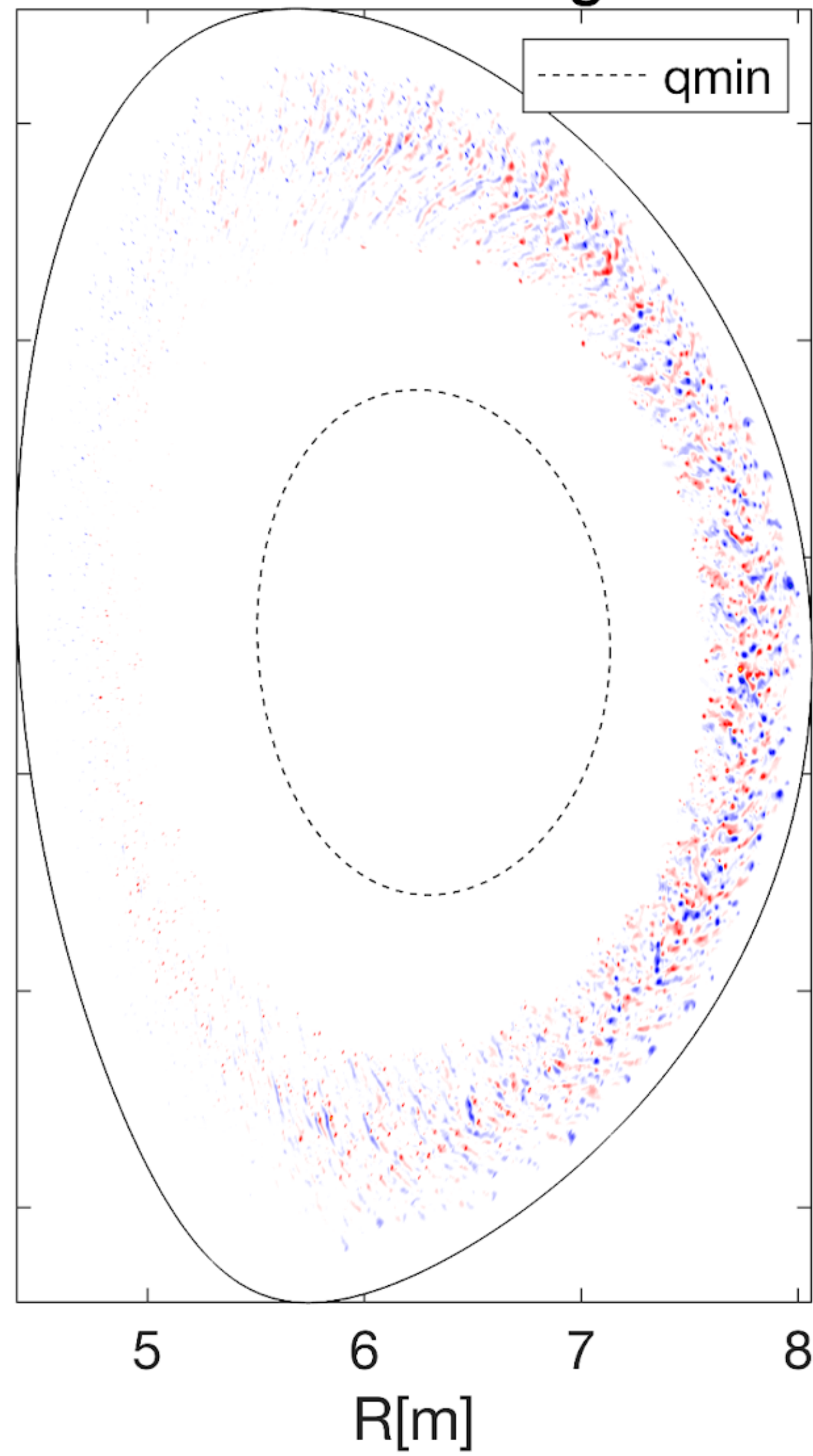


ITER

Linear stage



Nonlinear stage



GTC gyrokinetic model

Nonlinear gyrokinetic equation

$$(\partial_t + \dot{\mathbf{X}} \cdot \nabla + \dot{v}_{\parallel} \cdot \nabla_{v_{\parallel}}) F = 0$$

Poisson equation

$$\frac{Z_i^2 n_i}{T_i} (\phi - \tilde{\phi}) = \sum_s q_s n_s \delta n_s$$

Ampère equations

$$en_e \delta u_{\parallel,e} = \nabla_{\perp}^2 \delta A_{\parallel} + e \sum_{s \neq e} Z_s n_s \delta u_{\parallel,s}$$

$$\delta B_{\parallel} B_0 (1 + \sum_s \beta_s) = -4\pi \sum_s \delta P_{\perp,s}$$

Electron continuity equation

$$\frac{\partial \delta n_e}{\partial t} = -\nabla \cdot \left[n_{e,0} u_{e,\parallel} \frac{\mathbf{B}_0 + \delta \mathbf{B}_{\perp}}{B_0} + n_e \mathbf{v}_E - \frac{P_{e,\parallel} \mathbf{b}_0 \times \boldsymbol{\kappa}}{e B_0} - \frac{P_{e,\perp} \mathbf{b}_0 \times \nabla B_0}{e B_0^2} - \frac{P_{e,\perp} \mathbf{b}_0 \times \nabla \delta B_{\parallel}}{e B_0^2} \right]$$

Adiabatic perturbed electron pressure

$$\delta P_{e,\perp} = en_{e,0} \phi_{eff} + \frac{\partial(n_{e,0} T_{e,0})}{\partial \psi_0} \delta \psi - 2 \frac{\delta B_{\parallel}}{B_0} n_{e,0} T_{e,0} \quad \delta P_{e,\parallel} = en_{e,0} \phi_{eff} + \frac{\partial(n_{e,0} T_{e,0})}{\partial \psi_0} \delta \psi - \frac{\delta B_{\parallel}}{B_0}$$

[1] W.Deng et al., *Nucl. Fusion*, **52**, 023005 (2012)

[2] G.Dong et al., *Phys. Plasmas*, **24**, 081205 (2017)

Reduction to linear ideal MHD

Poisson equation

$$\delta n = -\frac{Z_i^2 n_i}{e T_i} (\phi - \tilde{\phi})$$

Perpendicular Ampère law

$$\delta B_{\parallel} = -4\pi \frac{\delta P_{\perp}}{B_0}$$

Parallel Ampère law

$$en_e \delta u_{\parallel} = \nabla_{\perp}^2 A_{\parallel}$$

Continuity equation

$$\begin{aligned} \frac{\partial \delta n}{\partial t} + \mathbf{B}_0 \cdot \nabla \left(\frac{n_0 \delta u_{\parallel}}{B_0} \right) + \delta \mathbf{B}_{\perp} \cdot \nabla \left(\frac{n_0 u_{\parallel,0}}{B_0} \right) + \frac{\boldsymbol{\kappa} \times \mathbf{B}_0}{e B_0^2} \cdot \nabla \left(2P_0 \frac{\delta B_{\parallel}}{B_0} - \delta P_{\parallel} - \delta P_{\perp} \right) \\ - \frac{P_0}{e B_0^2} \mathbf{b}_0 \times \nabla B_0 \cdot \frac{\nabla \delta B_{\parallel}}{B_0} - \frac{\mathbf{b}_0 \times \nabla \delta B_{\parallel}}{e B_0} \cdot \nabla P_0 = 0 \end{aligned}$$

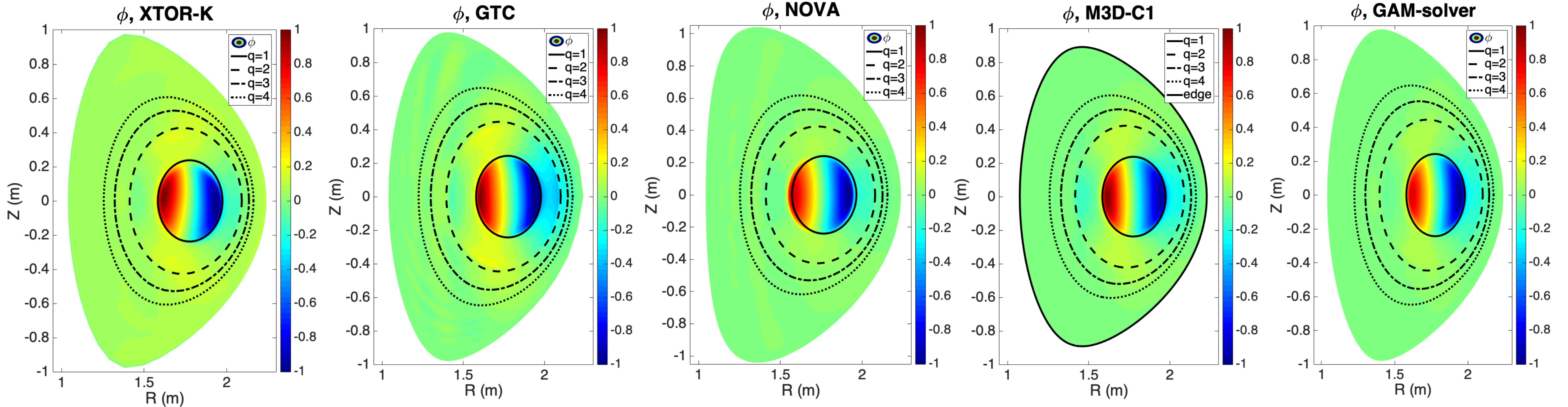
➤ This physical model leads to the following dispersion relation

$$\begin{aligned} \frac{\omega^2}{v_A^2} \nabla_{\perp}^2 \phi + \mathbf{B}_0 \cdot \nabla \left[\frac{\nabla_{\perp}^2 (k_{\parallel} \phi)}{B_0} \right] - (\nabla (k_{\parallel} \phi) \times \mathbf{b}_0) \cdot \nabla \left(\frac{J_{\parallel,0}}{\mu_0 e B_0} \right) + \frac{\boldsymbol{\kappa} \times \mathbf{B}_0}{e B_0^2} \cdot \nabla \left(2P_0 \frac{\delta B_{\parallel}}{B_0} - \delta P_{\parallel} - \delta P_{\perp} \right) \\ - \frac{P_0}{e B_0^2} \mathbf{b}_0 \times \nabla B_0 \cdot \frac{\nabla \delta B_{\parallel}}{B_0} - \frac{\mathbf{b}_0 \times \nabla \delta B_{\parallel}}{e B_0} \cdot \nabla P_0 = 0 \end{aligned}$$

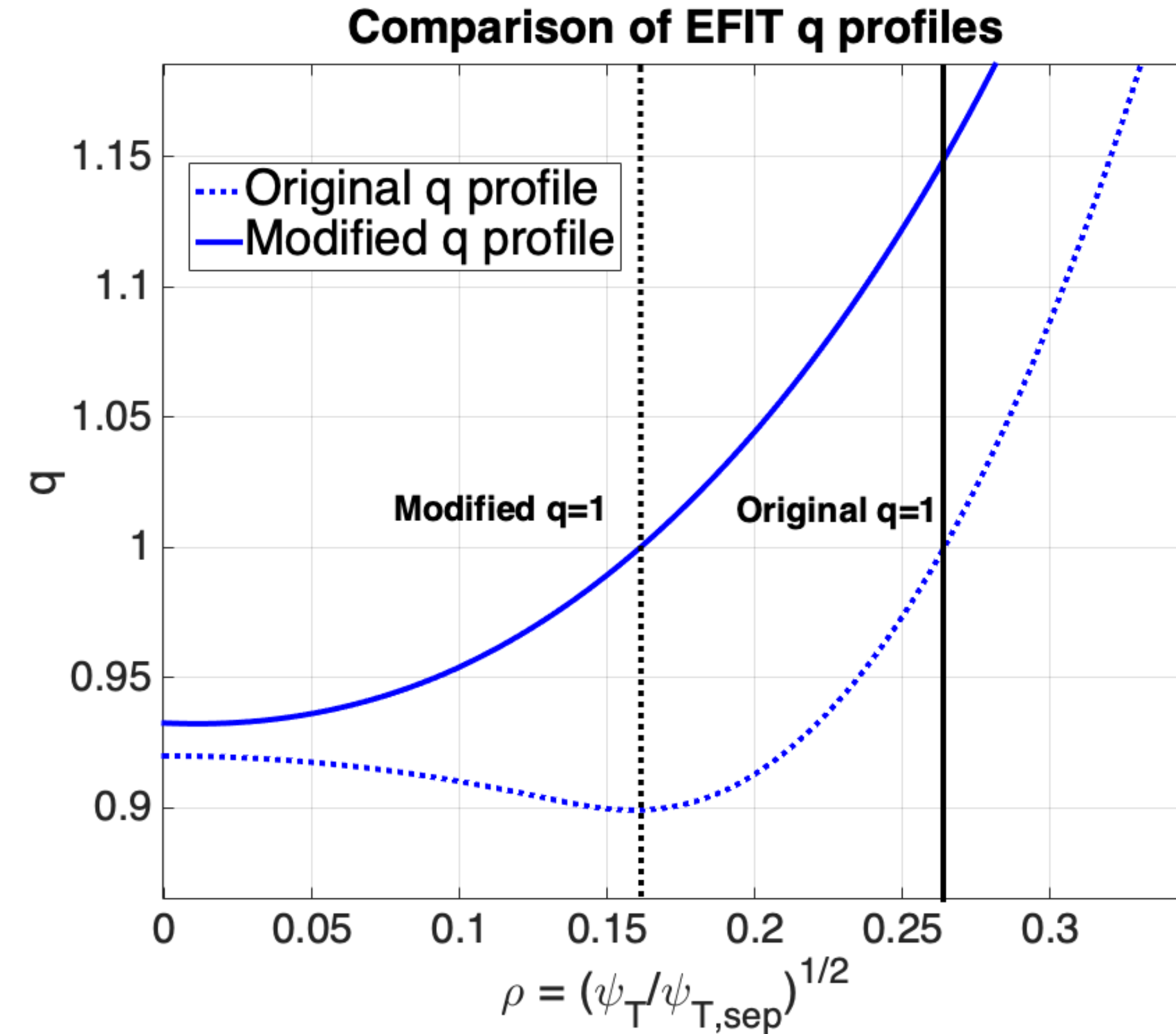
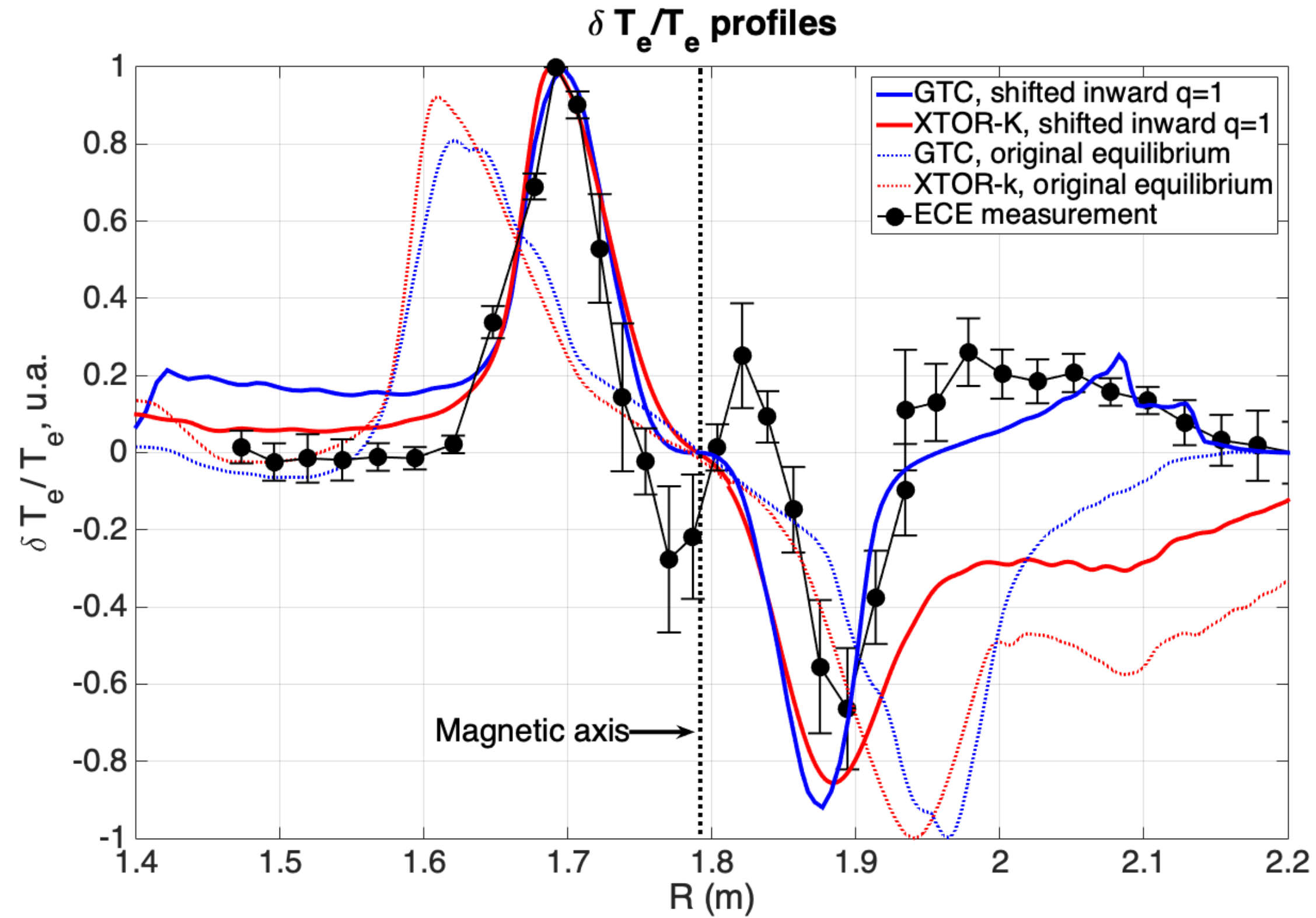
[1] W.Deng et al., *Nucl. Fusion*, **52**, 023005 (2012)

[2] G.Dong et al., *Phys. Plasmas*, **24**, 081205 (2017)

Identical mode structure for electrostatic potential



Experimental linear validation requires inward q=1 surface



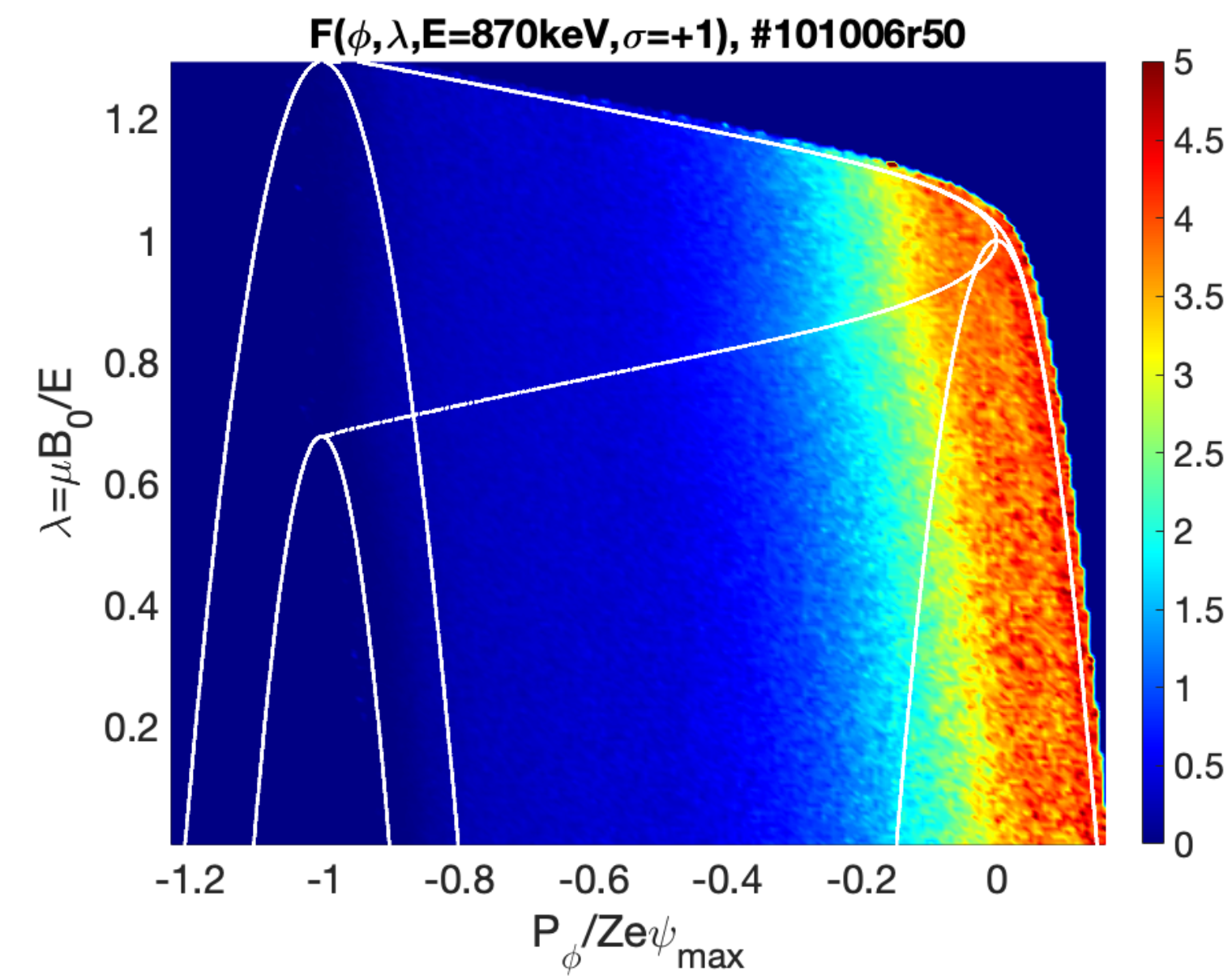
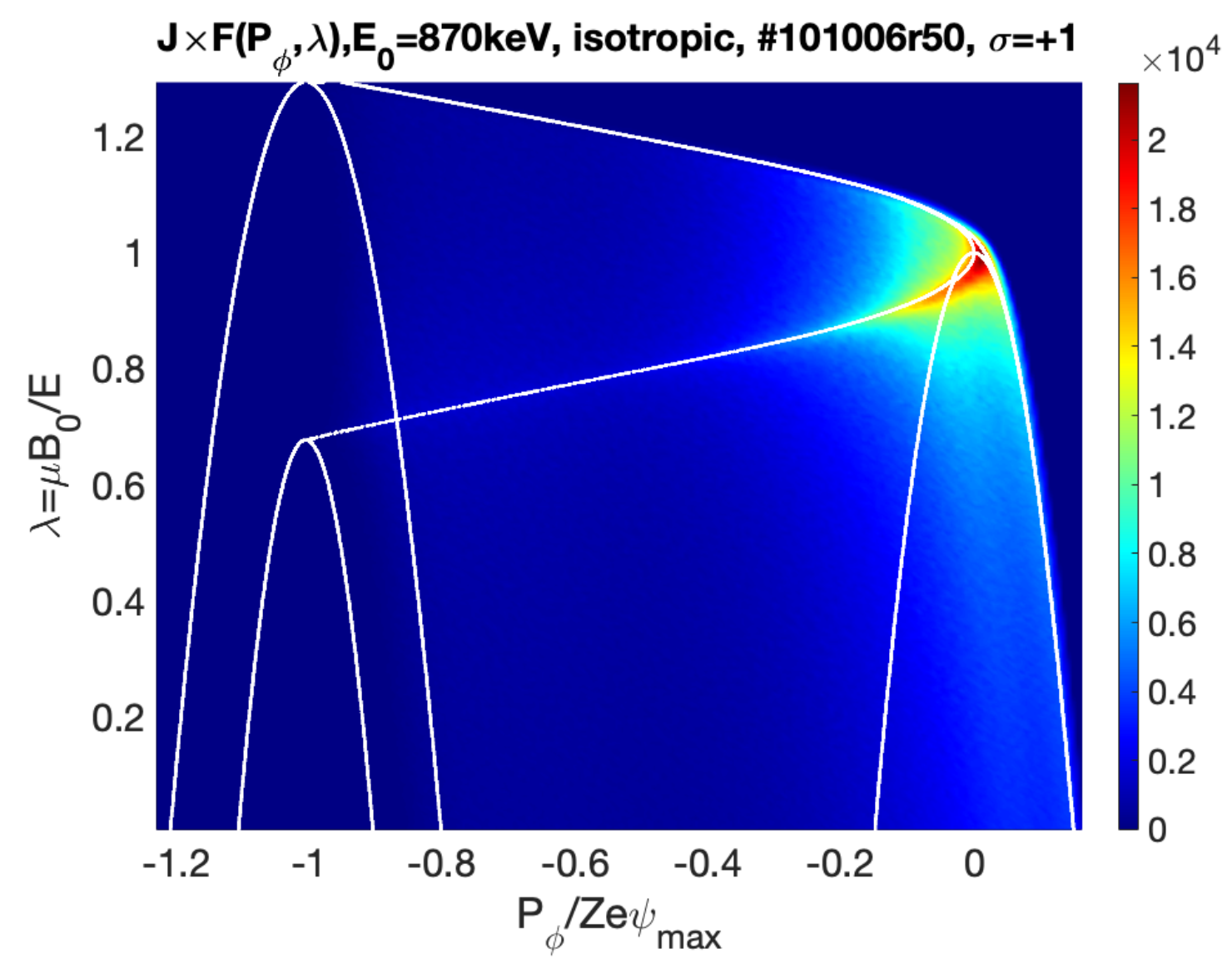
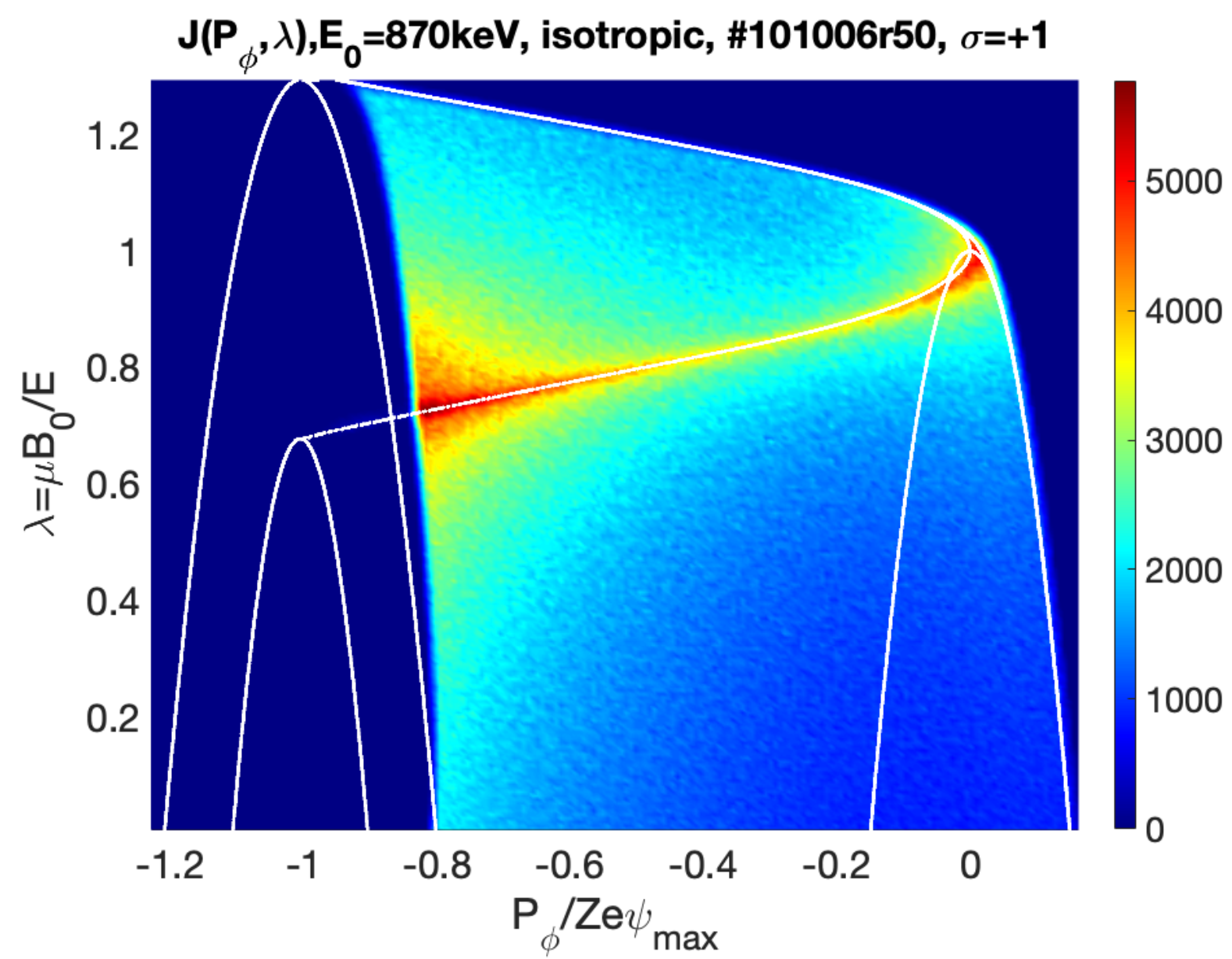
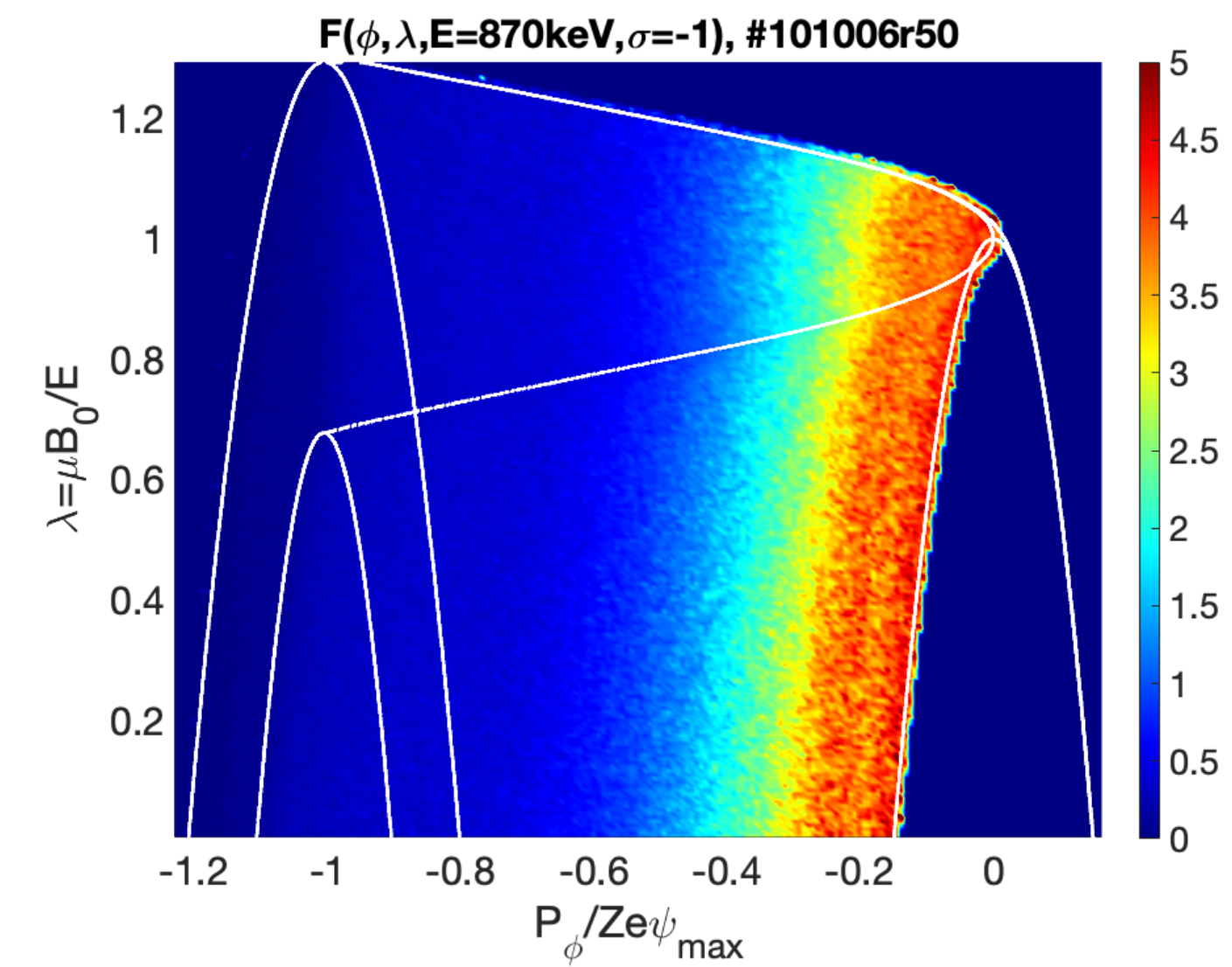
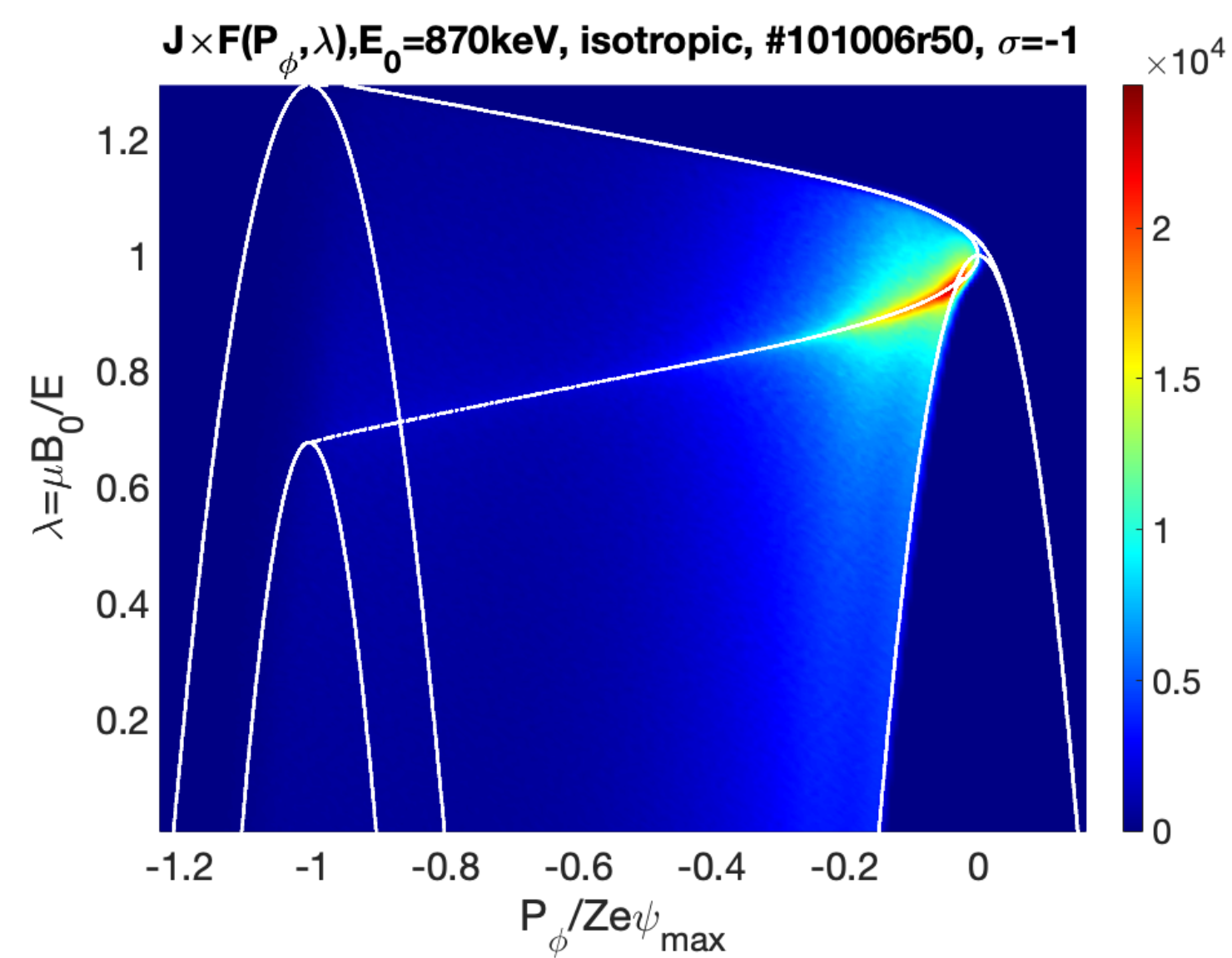
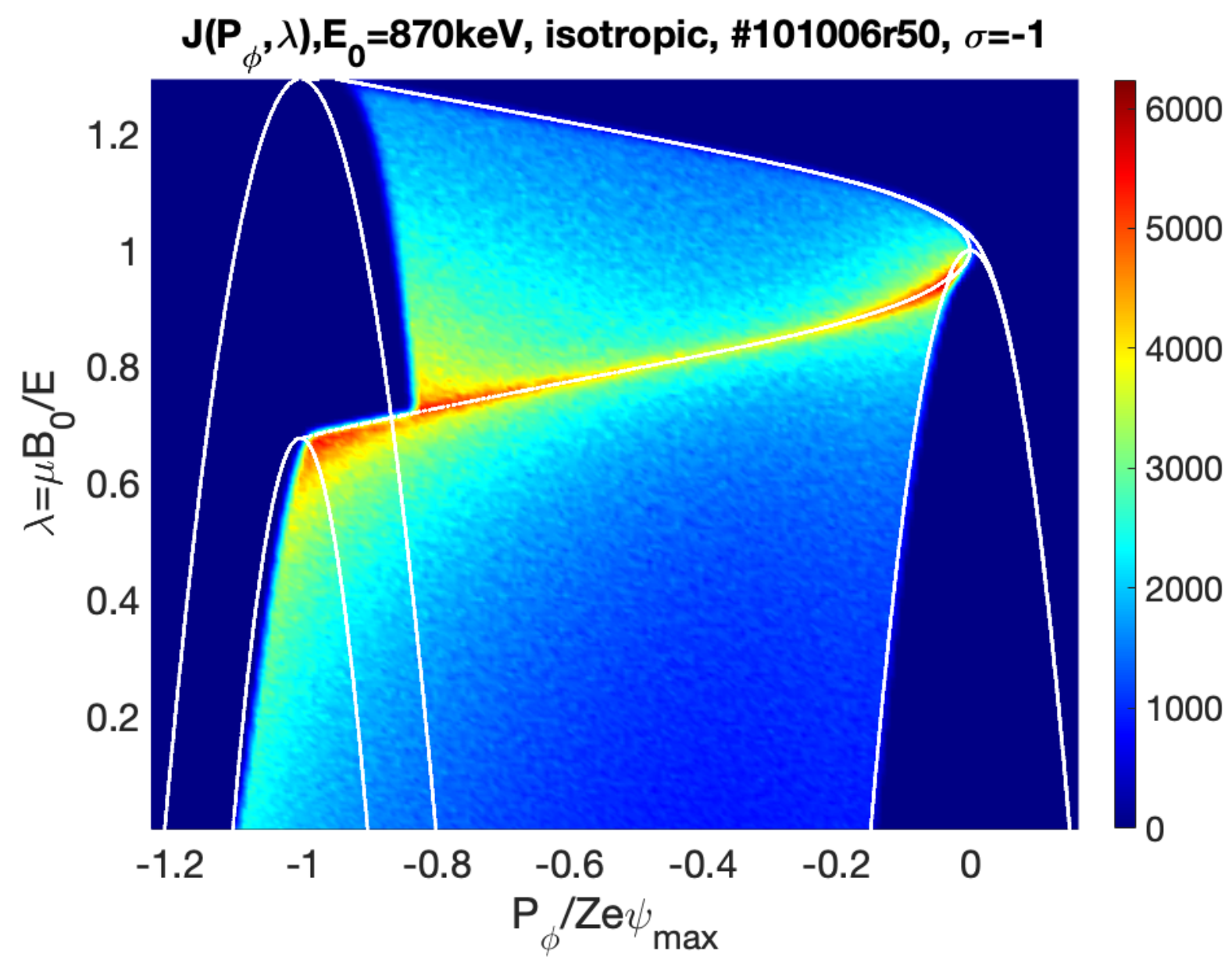
- The **EFIT reconstruction** needs to be adjusted to recover a **correct position** for **q=1**
- Both MHD equilibria are **equally plausible** due to the **experimental uncertainties**
- A **fair agreement** is obtained for the internal kink **linear mode structure** between the **ECE measurement** for **fluid** simulations with **GTC** and **XTOR-K**

Necessary inputs for eigenvalue codes/ reduced models

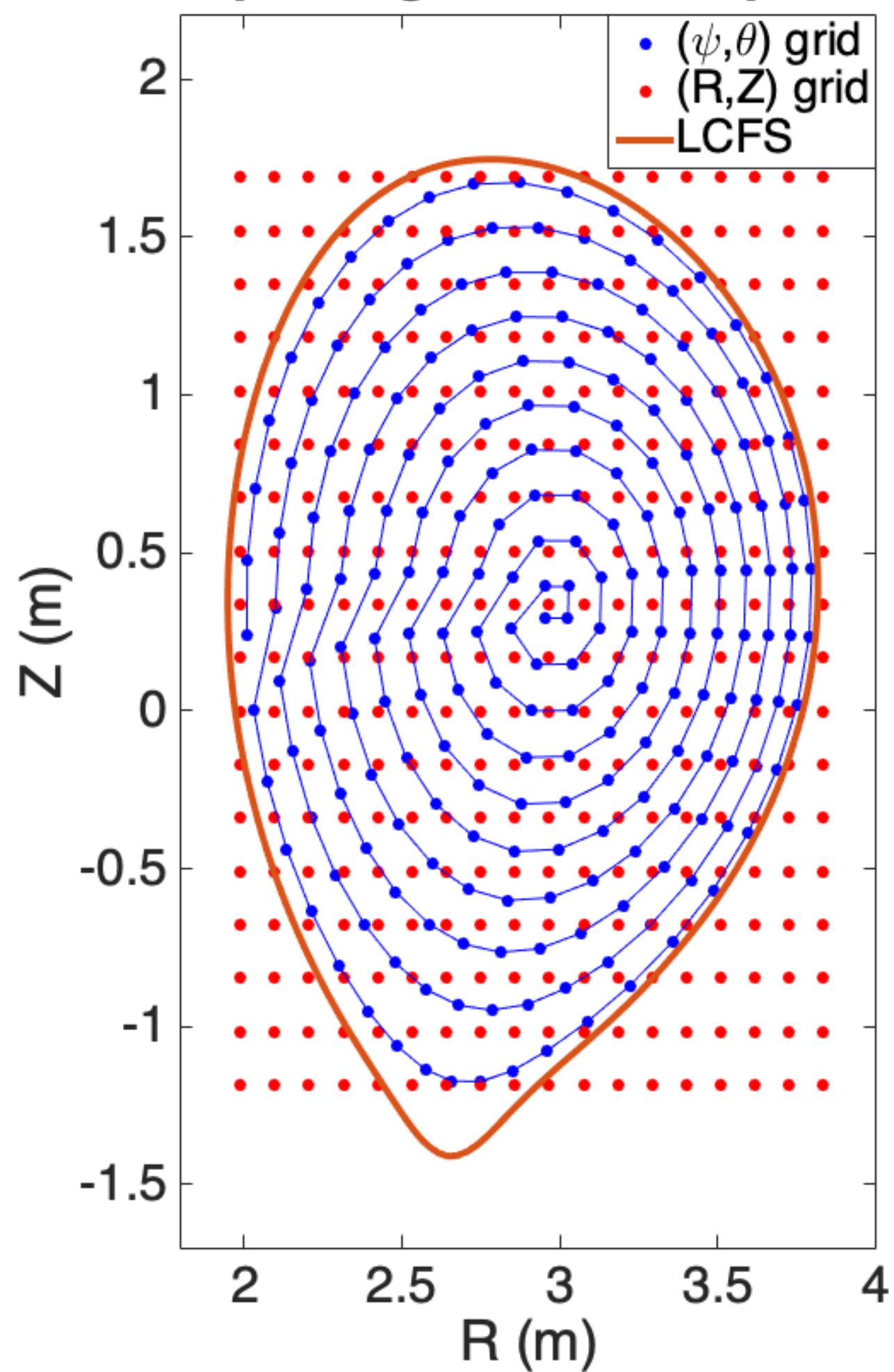
HALO	1st order CoM derivatives on a	$(E, \mu, P_\varphi, \sigma)$ grid
NOVA	1st order CoM derivatives on a	$(E, \lambda, P_\varphi, \sigma)$ grid
LIGKA	1st order CoM derivatives on a	$(E, \lambda, P_\varphi, \sigma)$ grid
RBQ	Same as NOVA	

Necessary inputs for initial value codes

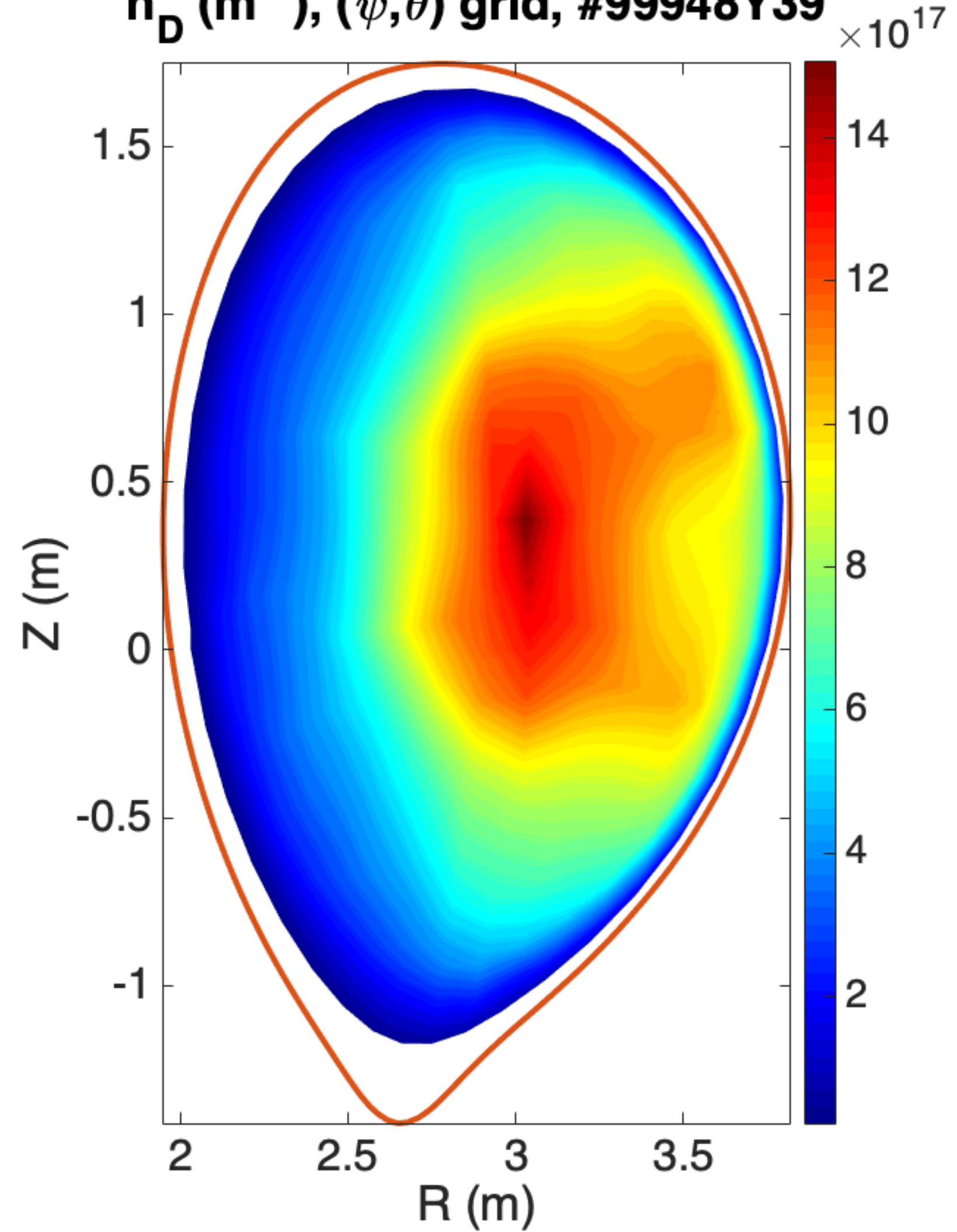
XTOR-K / JOREK	<ul style="list-style-type: none"> • Full orbit 6D markers in phase space cylindrical coordinates for full-F PIC simulations 	
GTC	<ul style="list-style-type: none"> • Gyrokinetic 5D markers in Boozer coordinates for full-F PIC simulations • $\nabla F _{\mu, v_{\parallel}}$ and $\partial_{v_{\parallel}} F _{\mu, X}$ derivatives evaluated at Boozer + (v_{\parallel}, μ) coordinates for F PIC simulations (distributions at gyrocenters) 	δ
MEGA	<ul style="list-style-type: none"> • Gyrokinetic 5D markers in cylindrical + (v_{\parallel}, μ) coordinates for full-F PIC simulations • First order CoM derivatives on a $(E, \lambda, P_{\varphi}, \sigma)$ grid for F PIC simulations (distributions at guiding centers) 	δ
M3D-C1	<ul style="list-style-type: none"> • $\nabla F _{\mu, v_{\parallel}}$ and $\partial_{v_{\parallel}} F _{\mu, X}$ derivatives evaluated at cylindrical + (v_{\parallel}, μ) coordinates for F PIC simulations (distributions at guiding centers) (similar to GTC) 	δ
GYSELA	<ul style="list-style-type: none"> • Distributions of gyrocenters on a $(R, \text{phi}, Z, v_{\parallel}, \mu)$ grid for full-F semi-lagrangian simulations 	
ORB-5	<ul style="list-style-type: none"> • $\nabla F _{\mu, v_{\parallel}}$ and $\partial_{v_{\parallel}} F _{\mu, X}$ derivatives evaluated at field aligned + (v_{\parallel}, μ) coordinates for F PIC simulations (distributions at gyrocenters) (to confirm) 	δ
FAR-3D	<ul style="list-style-type: none"> • Specific fluid closure to obtain kinetic effects in gyro-fluid simulations, kinetic module currently being implemented 	



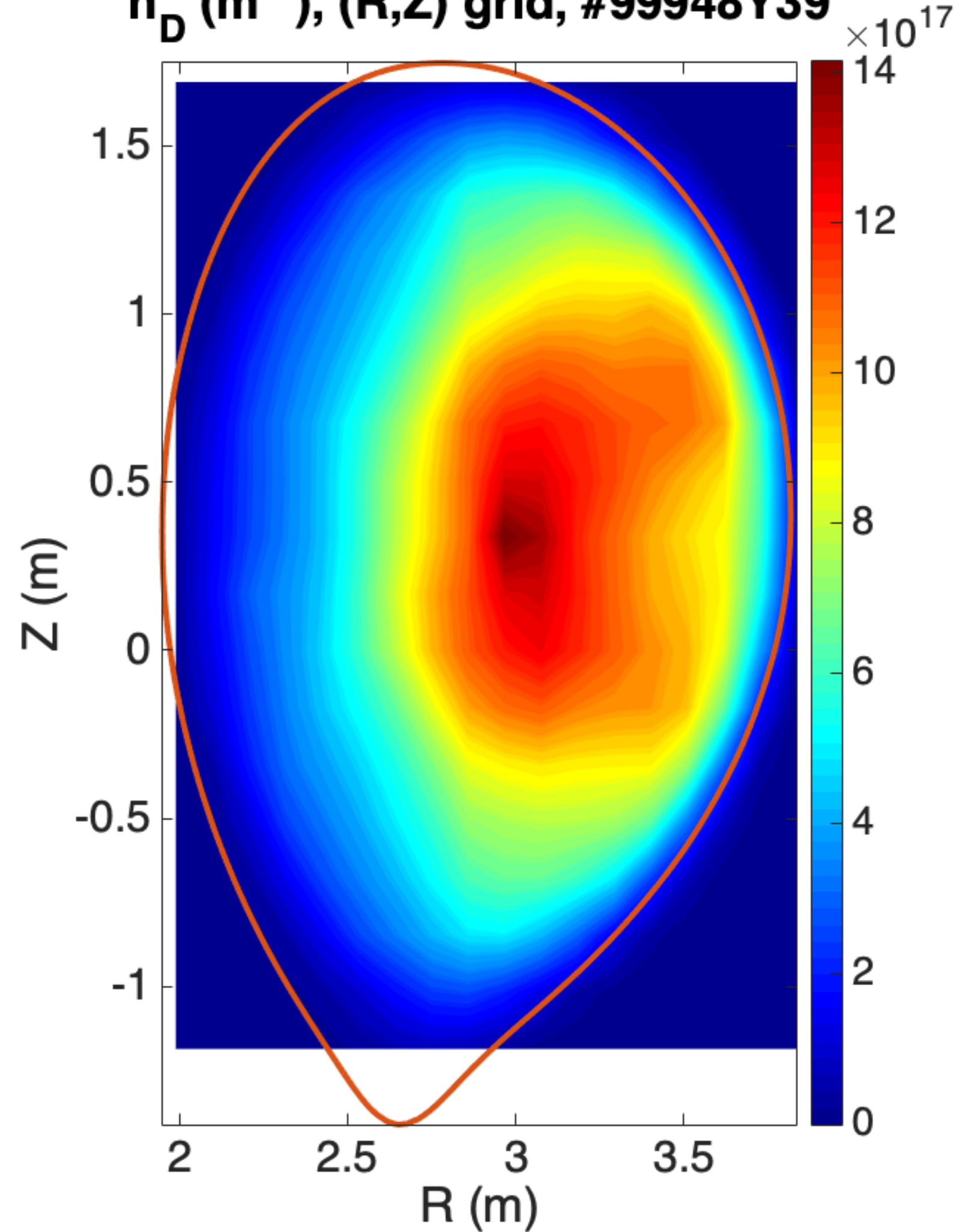
Spatial grid for CoM pdfs



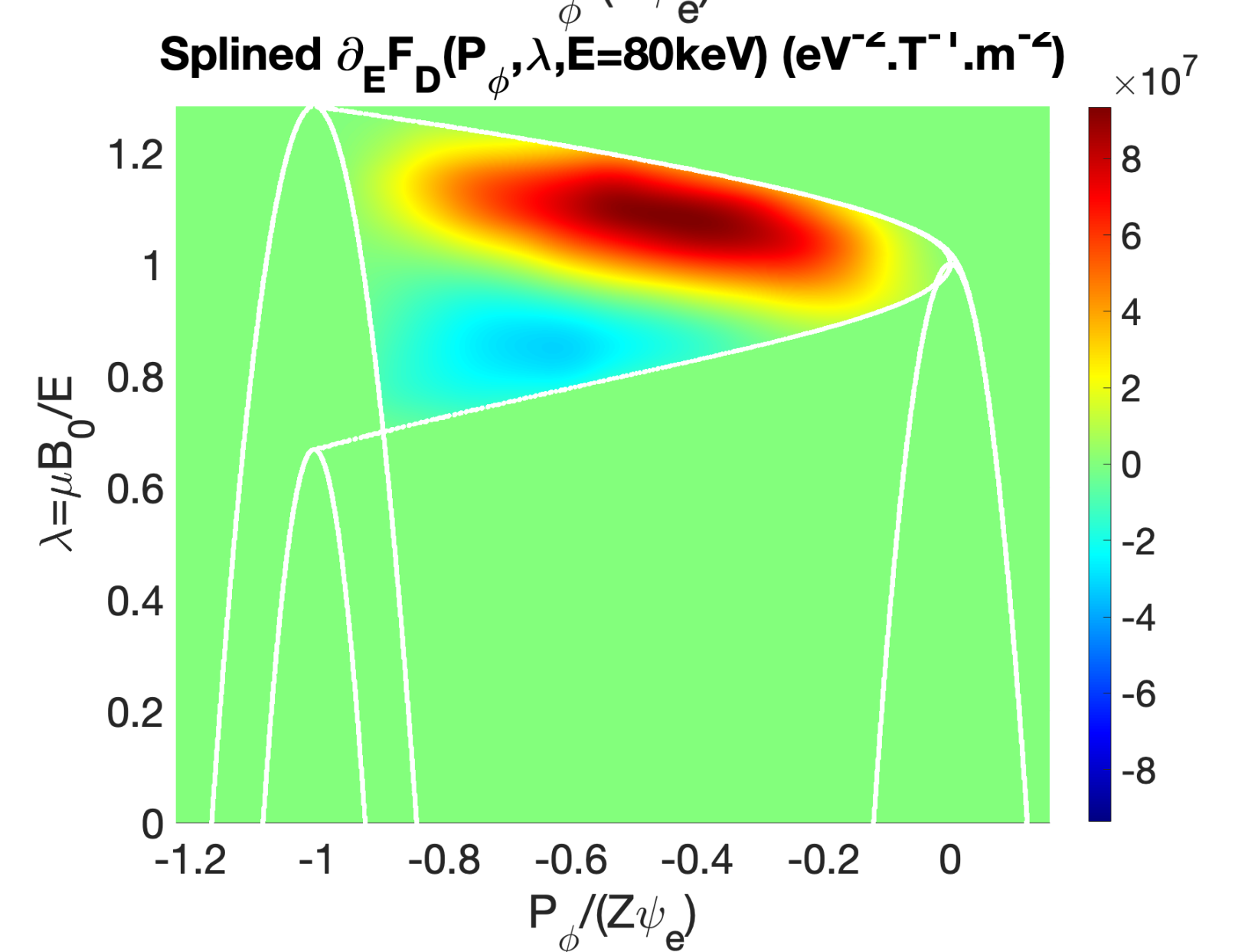
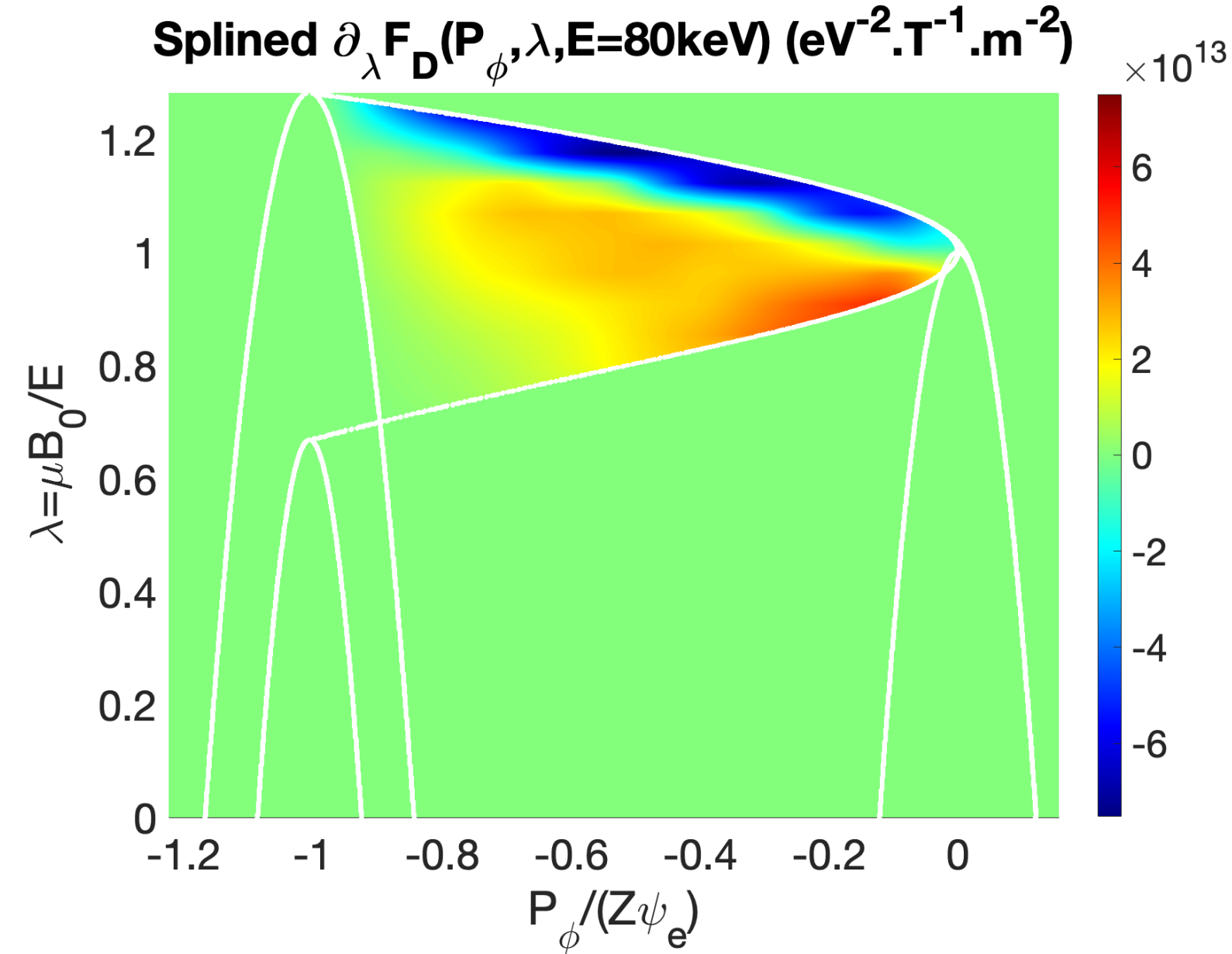
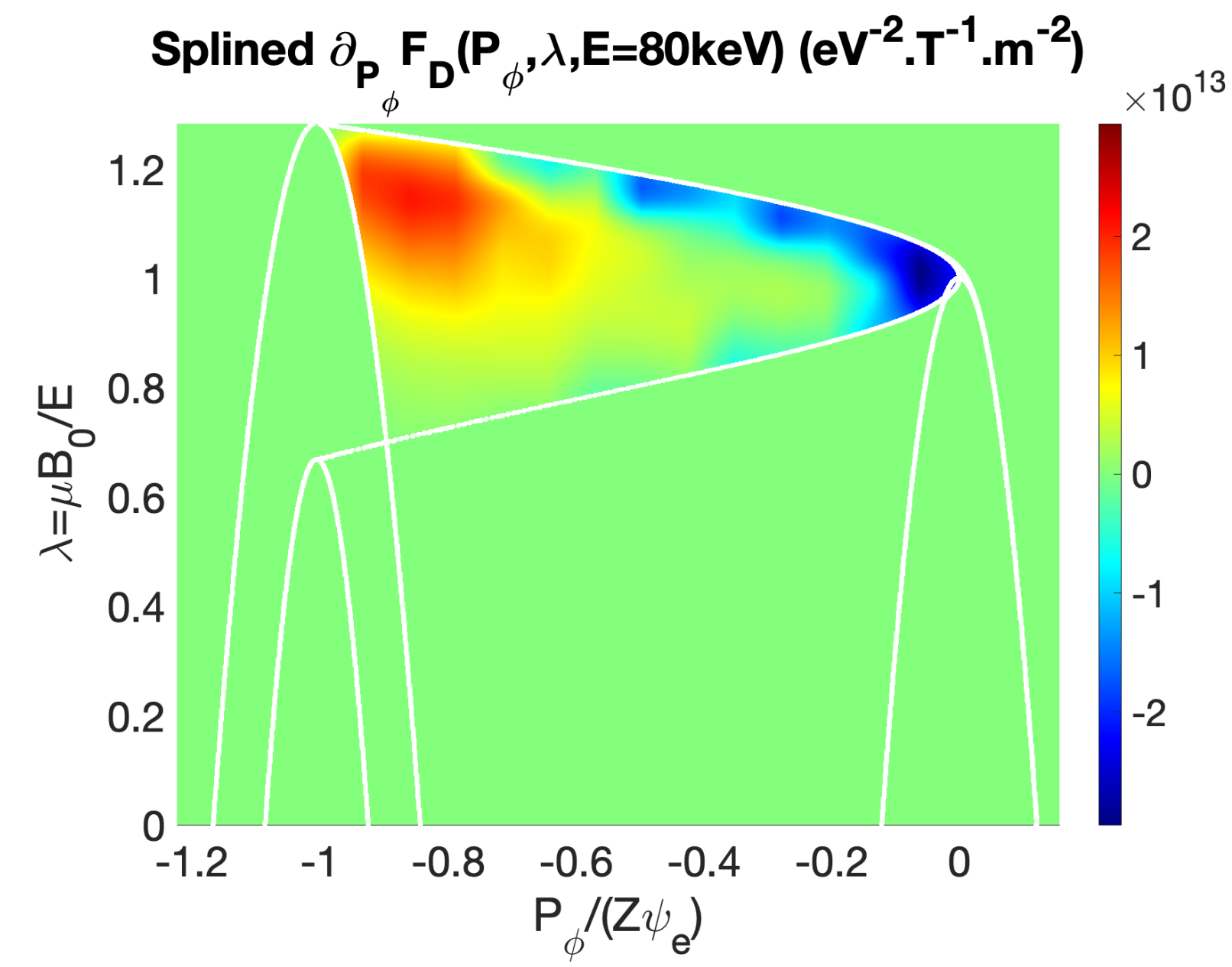
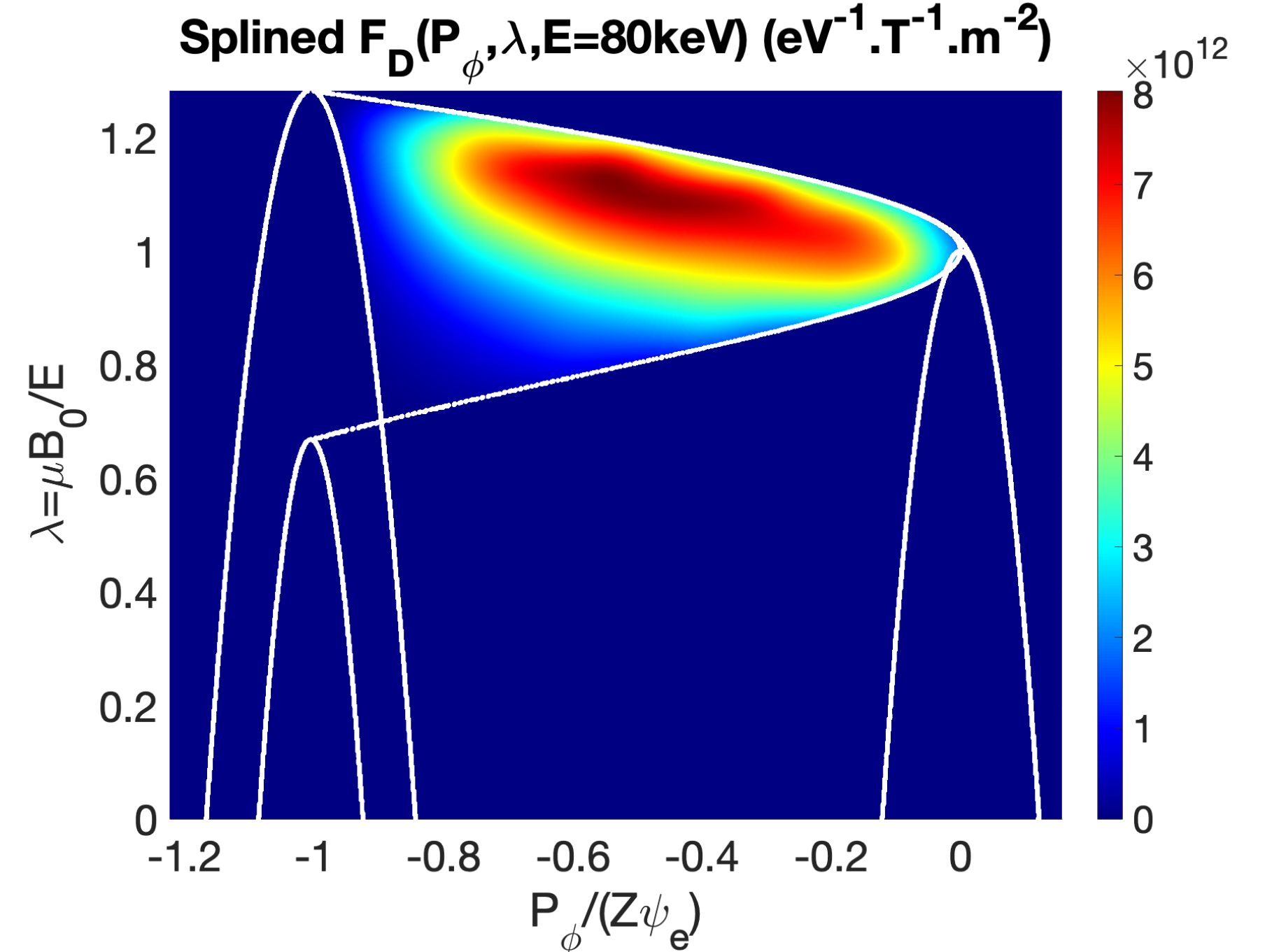
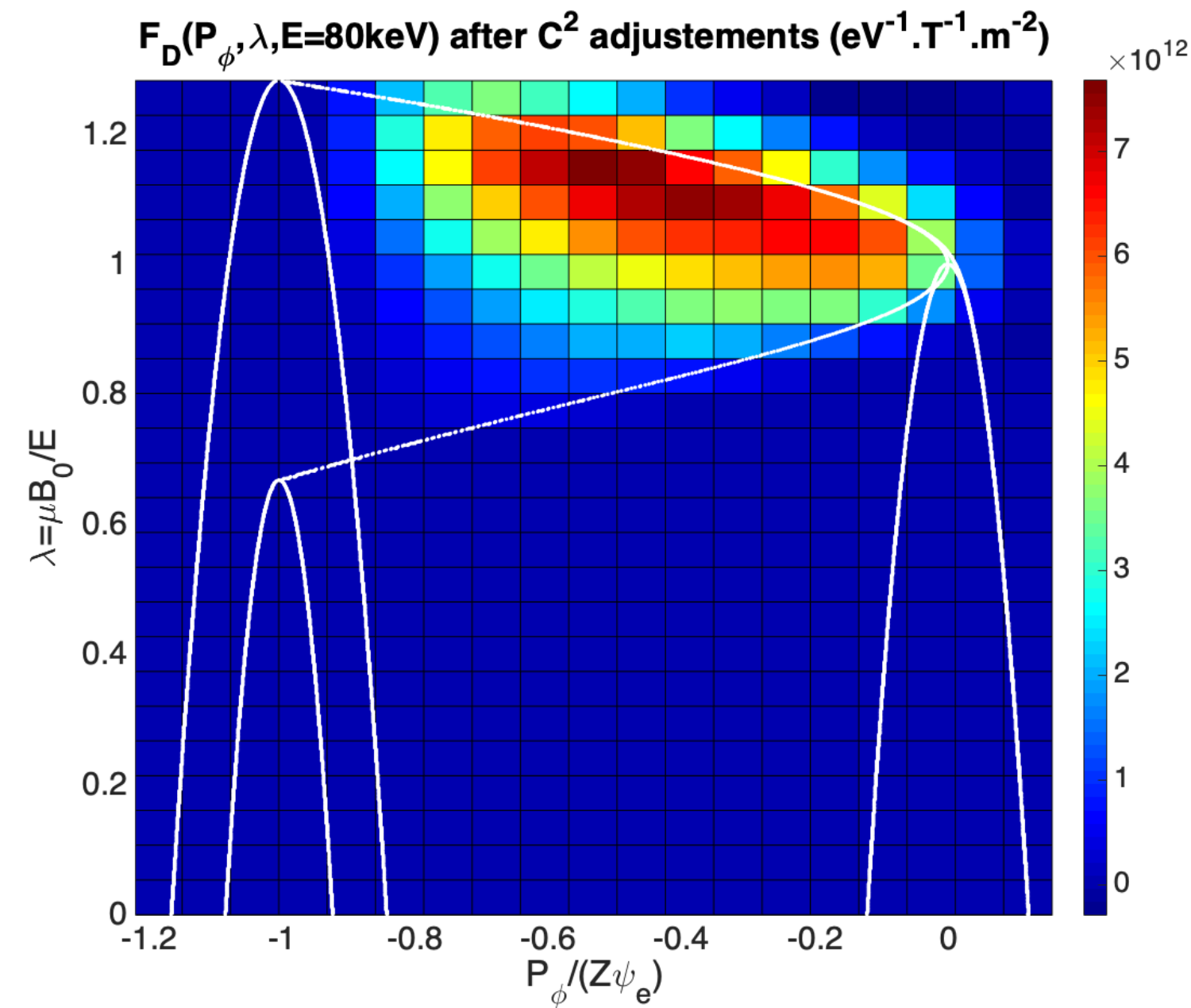
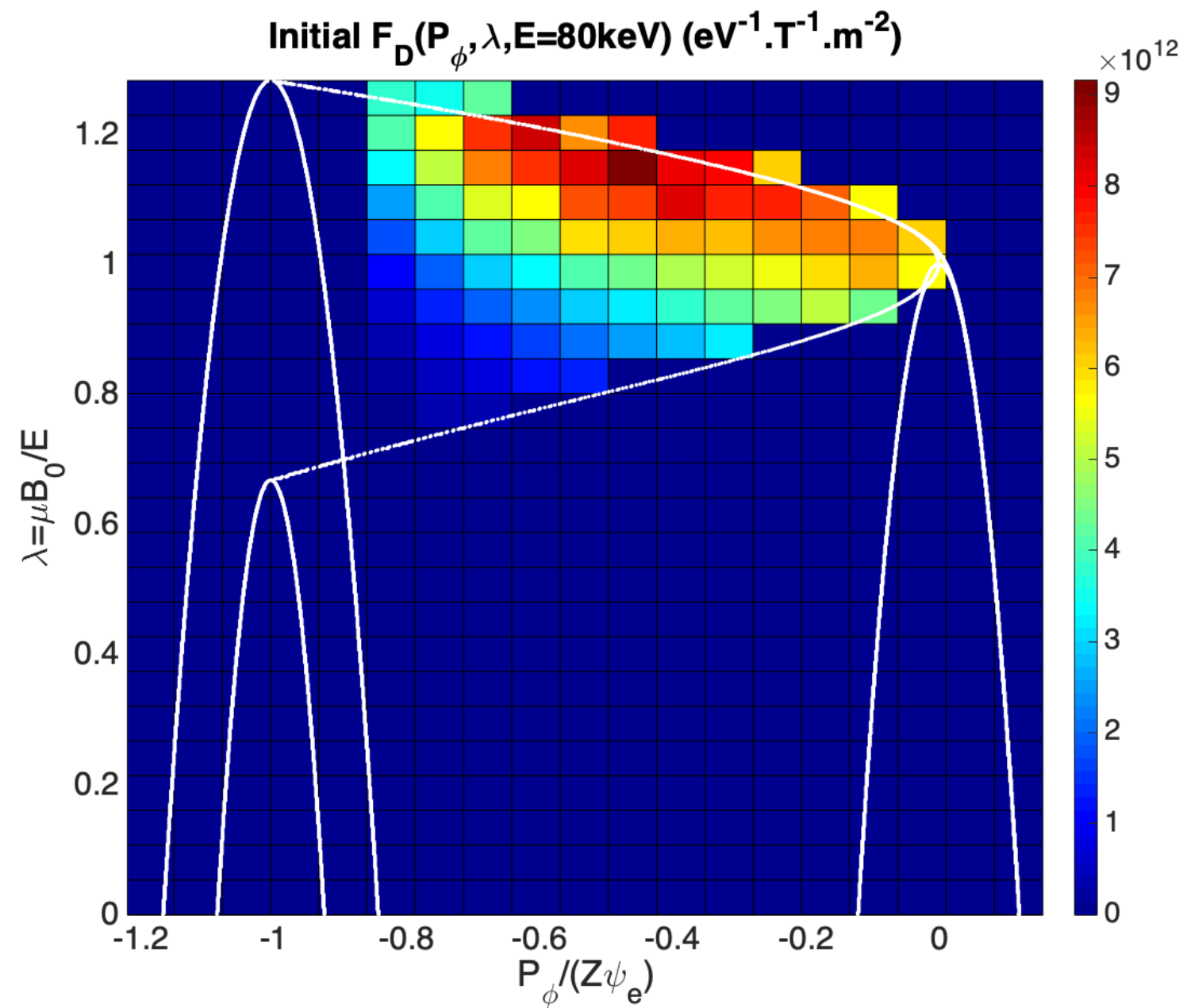
n_D (m^{-3}), (ψ, θ) grid, #99948Y39



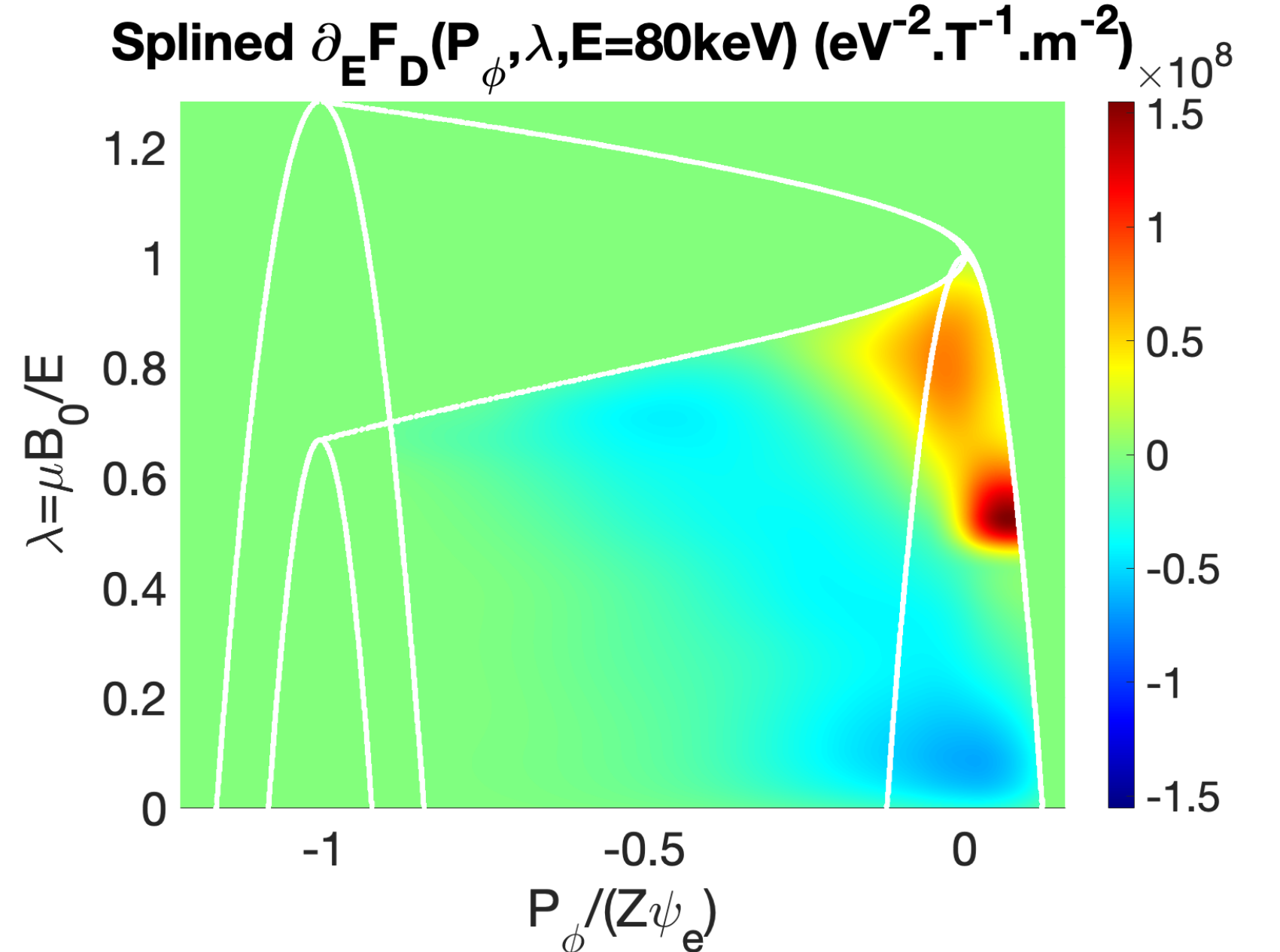
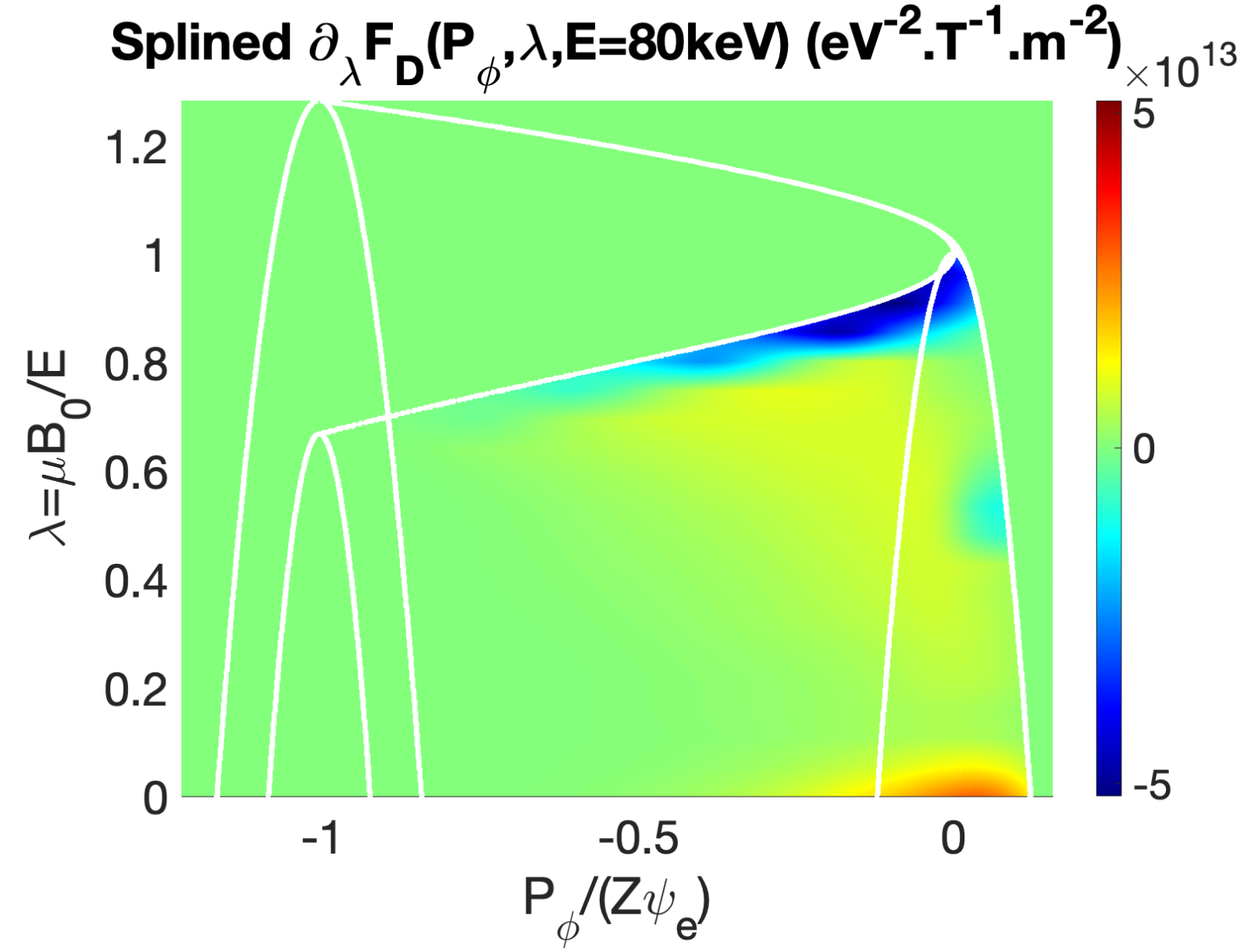
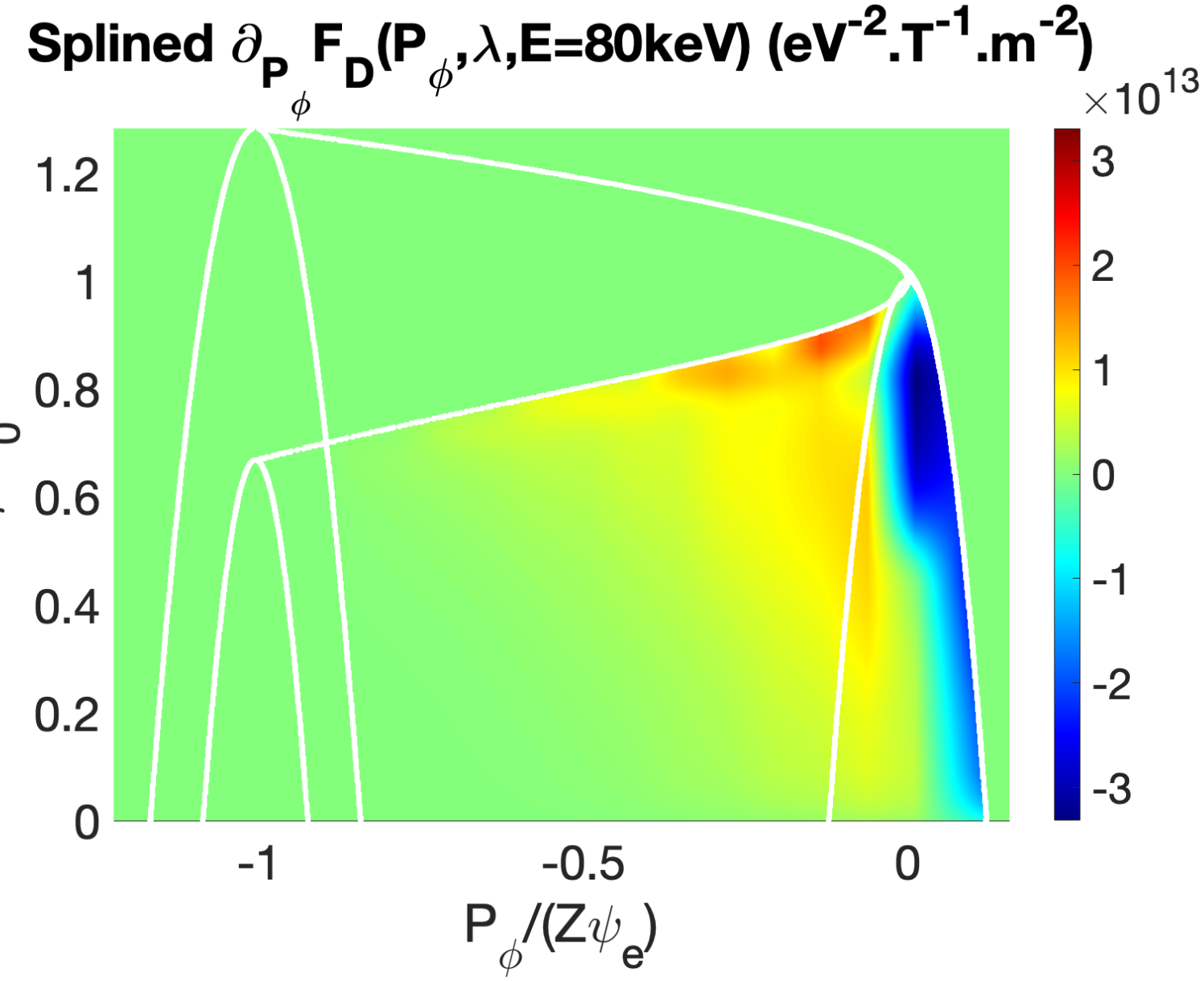
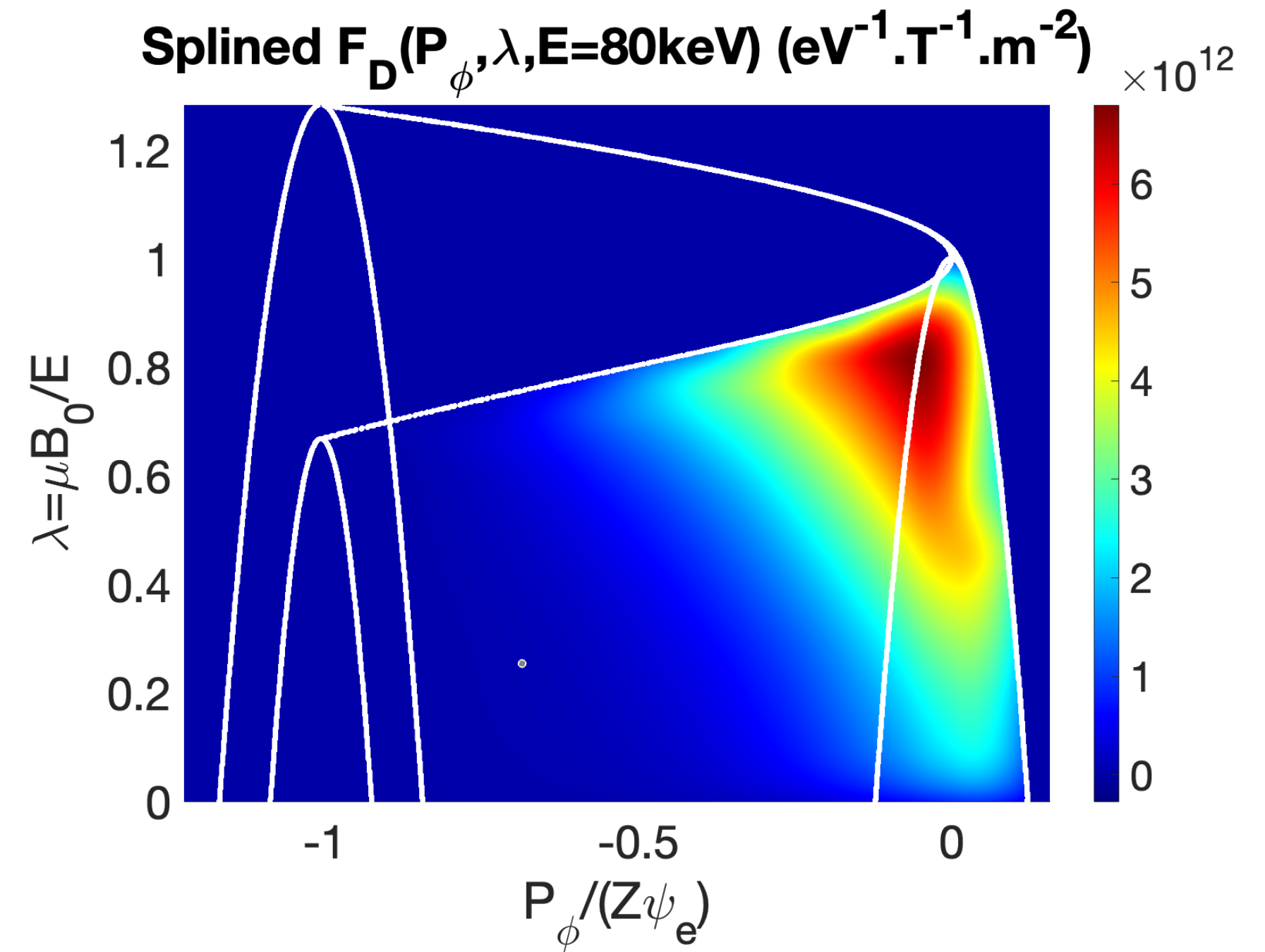
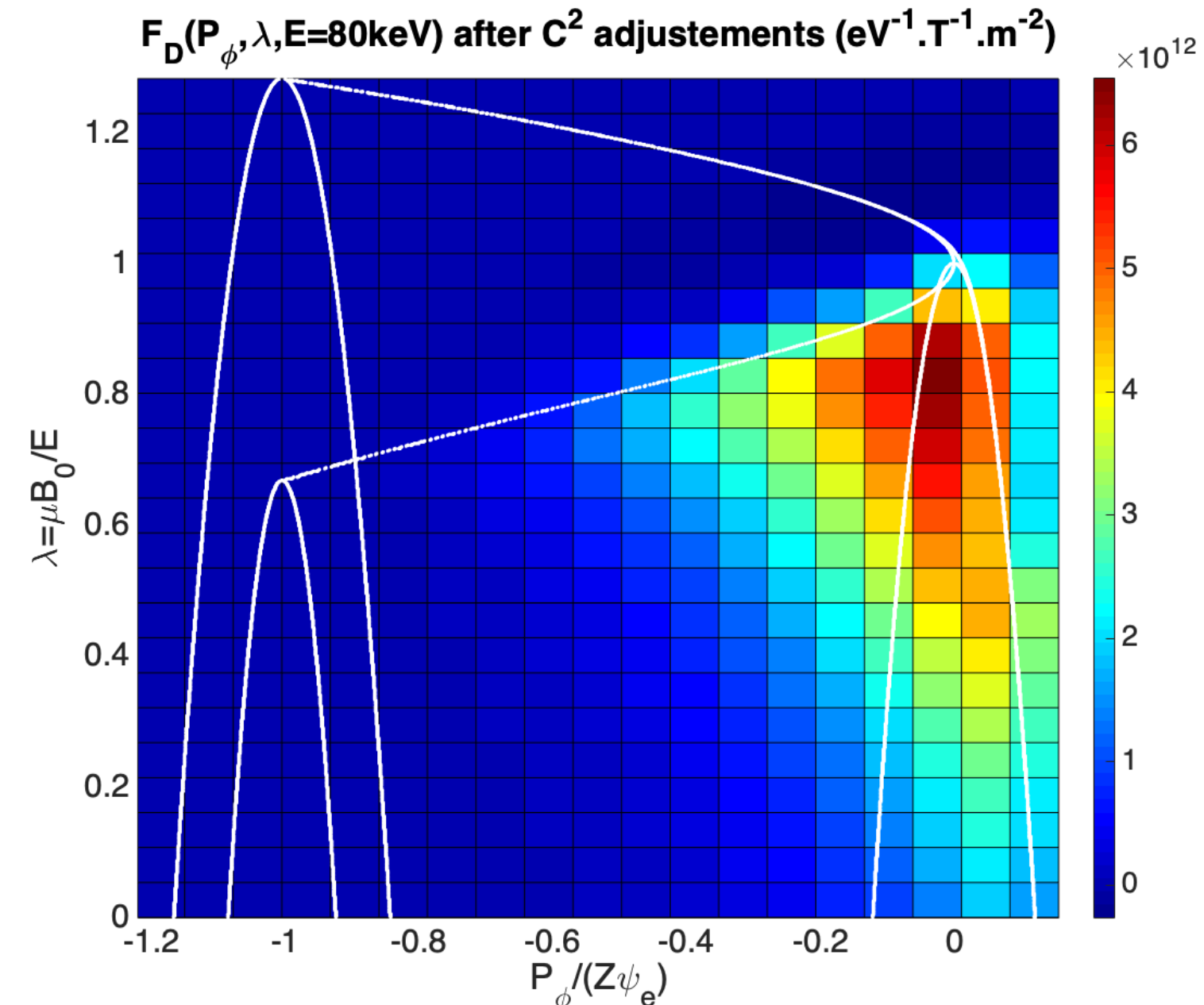
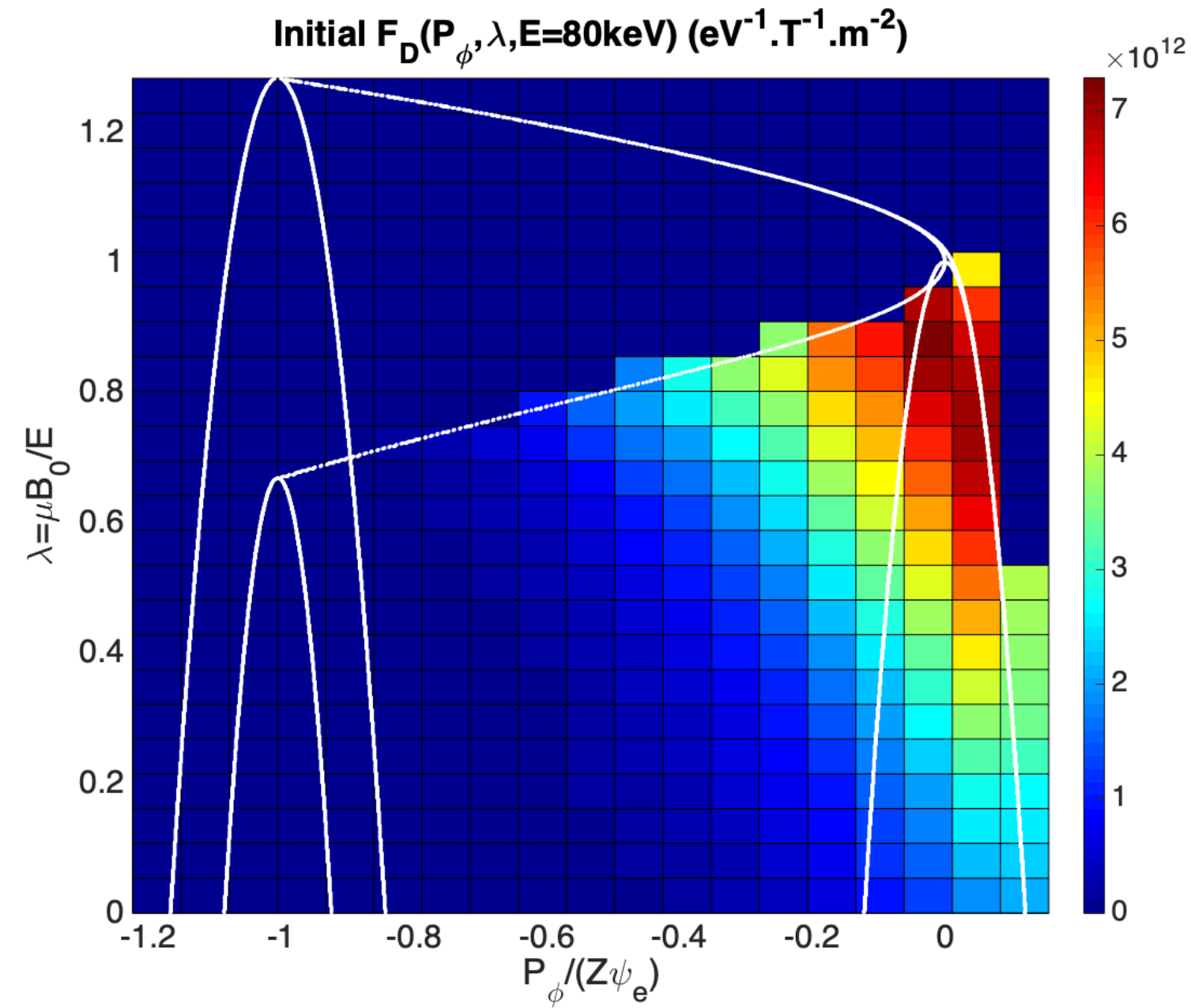
n_D (m^{-3}), (R, Z) grid, #99948Y39

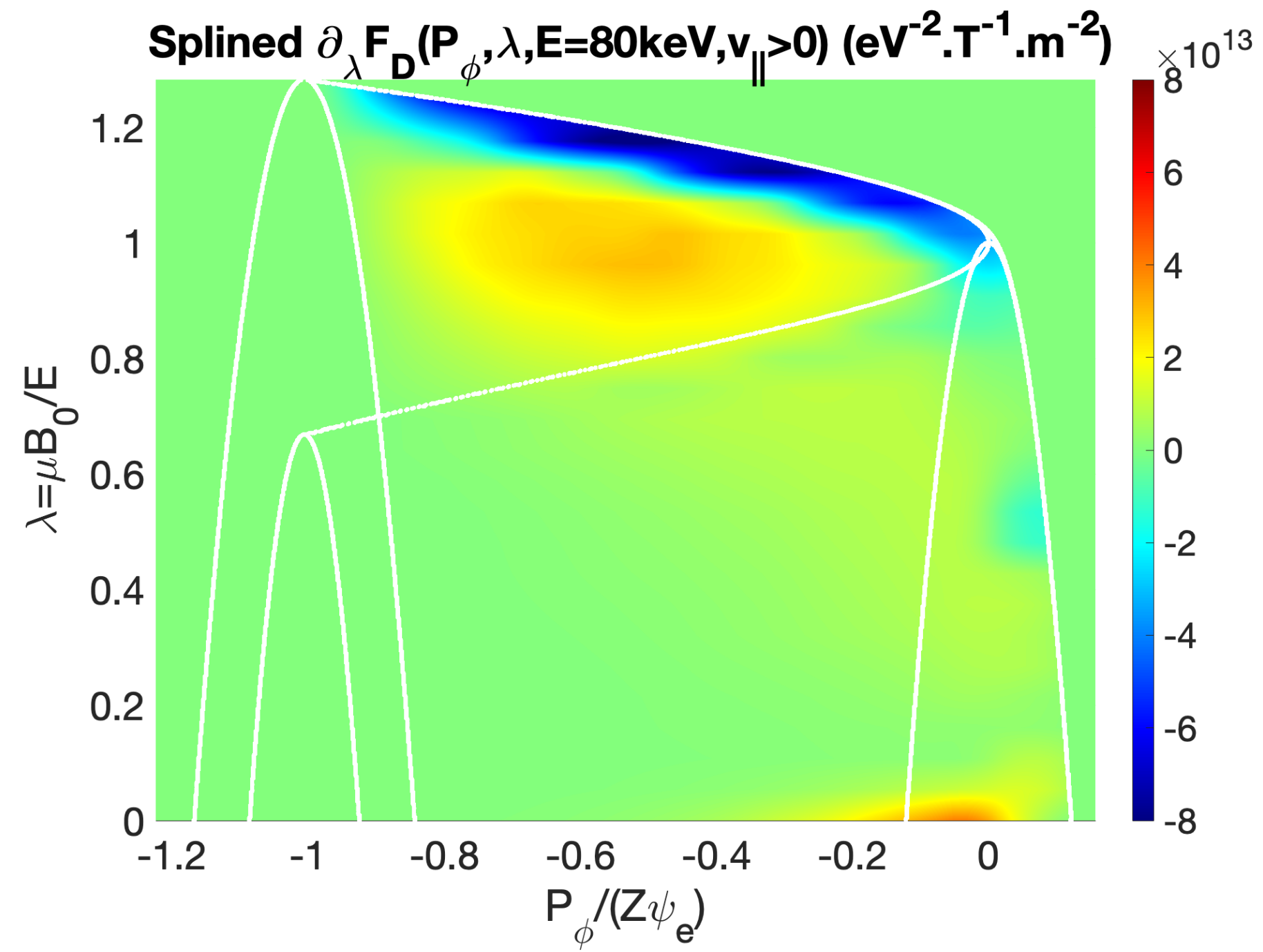
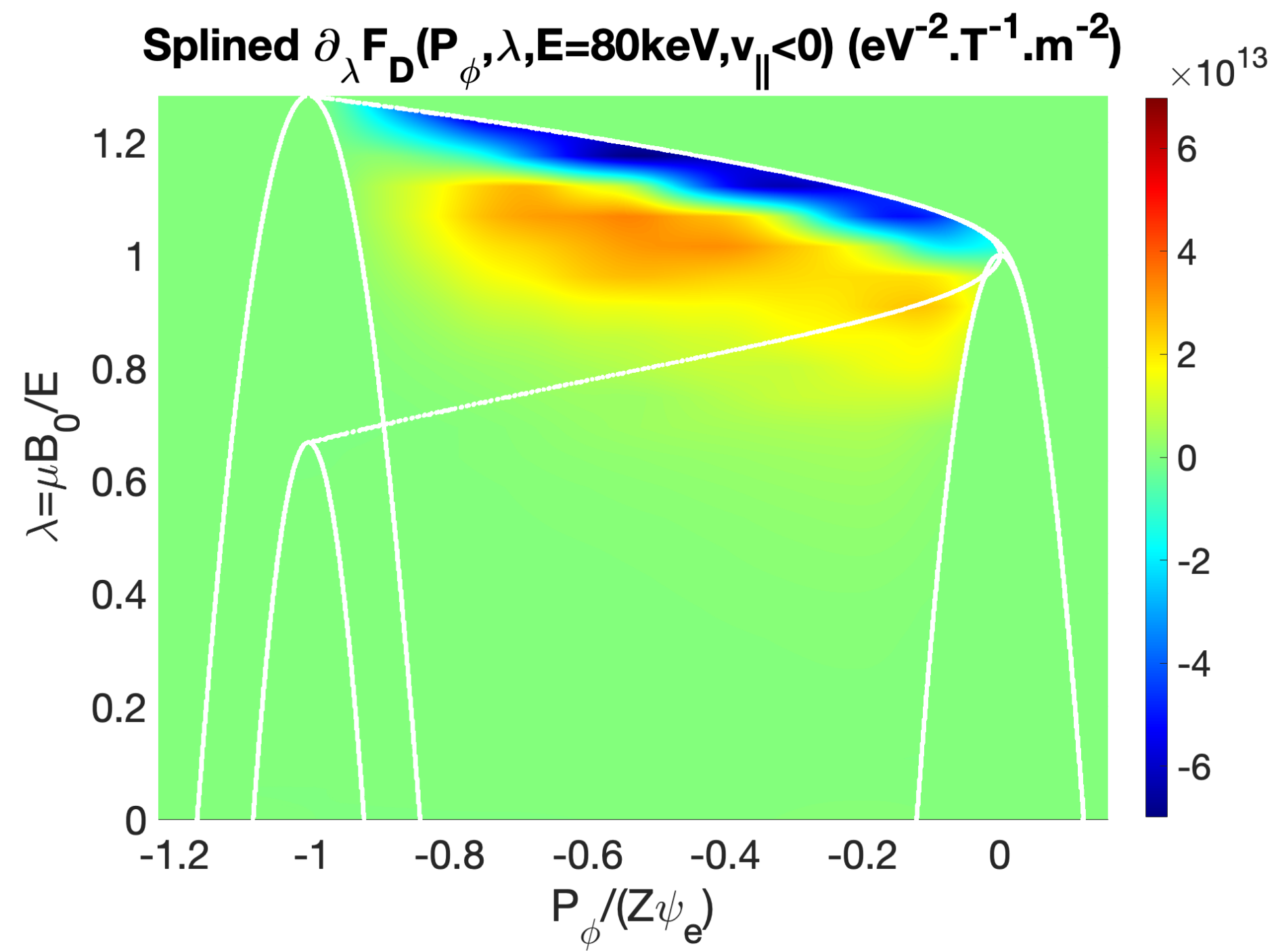
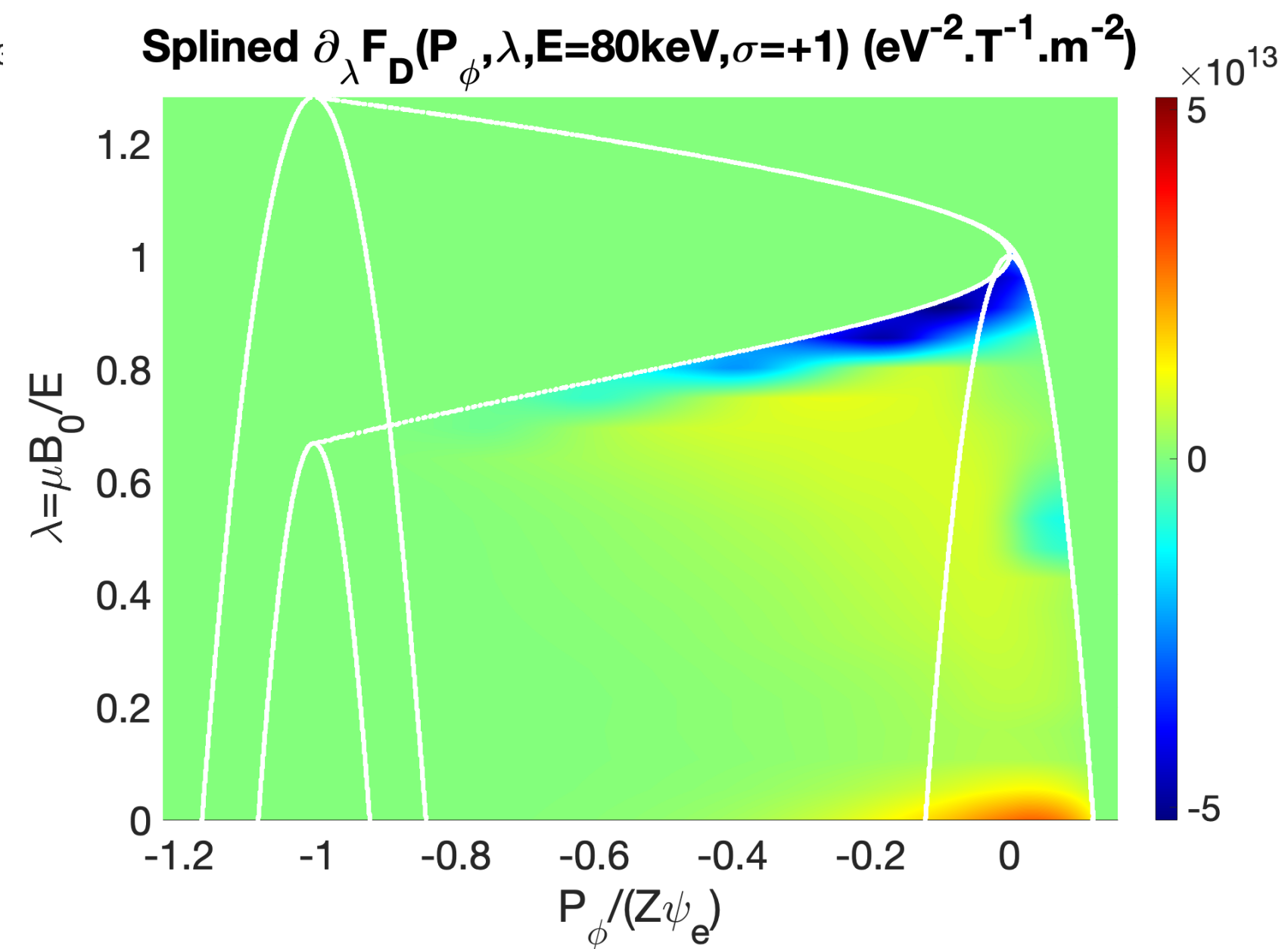
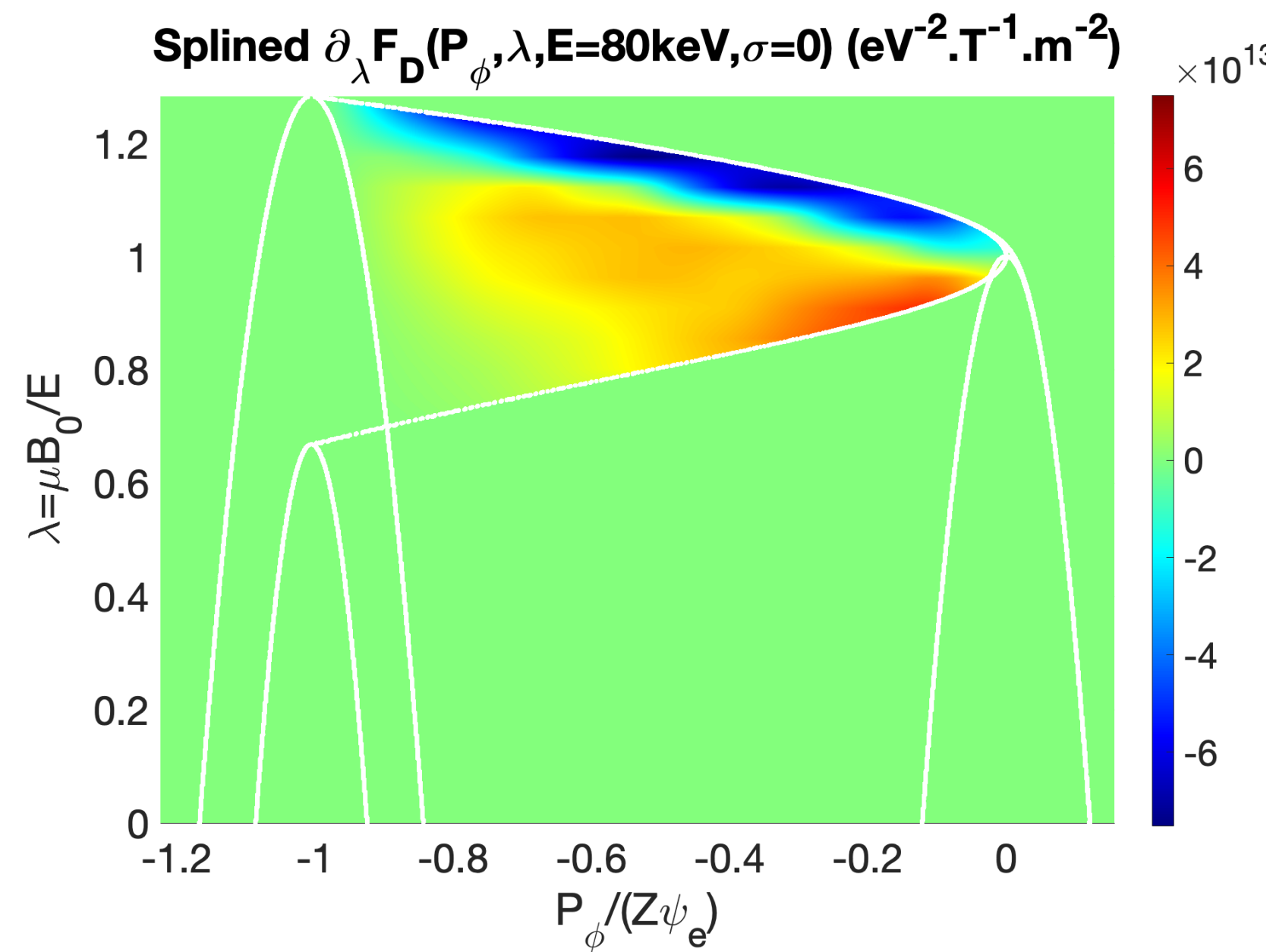
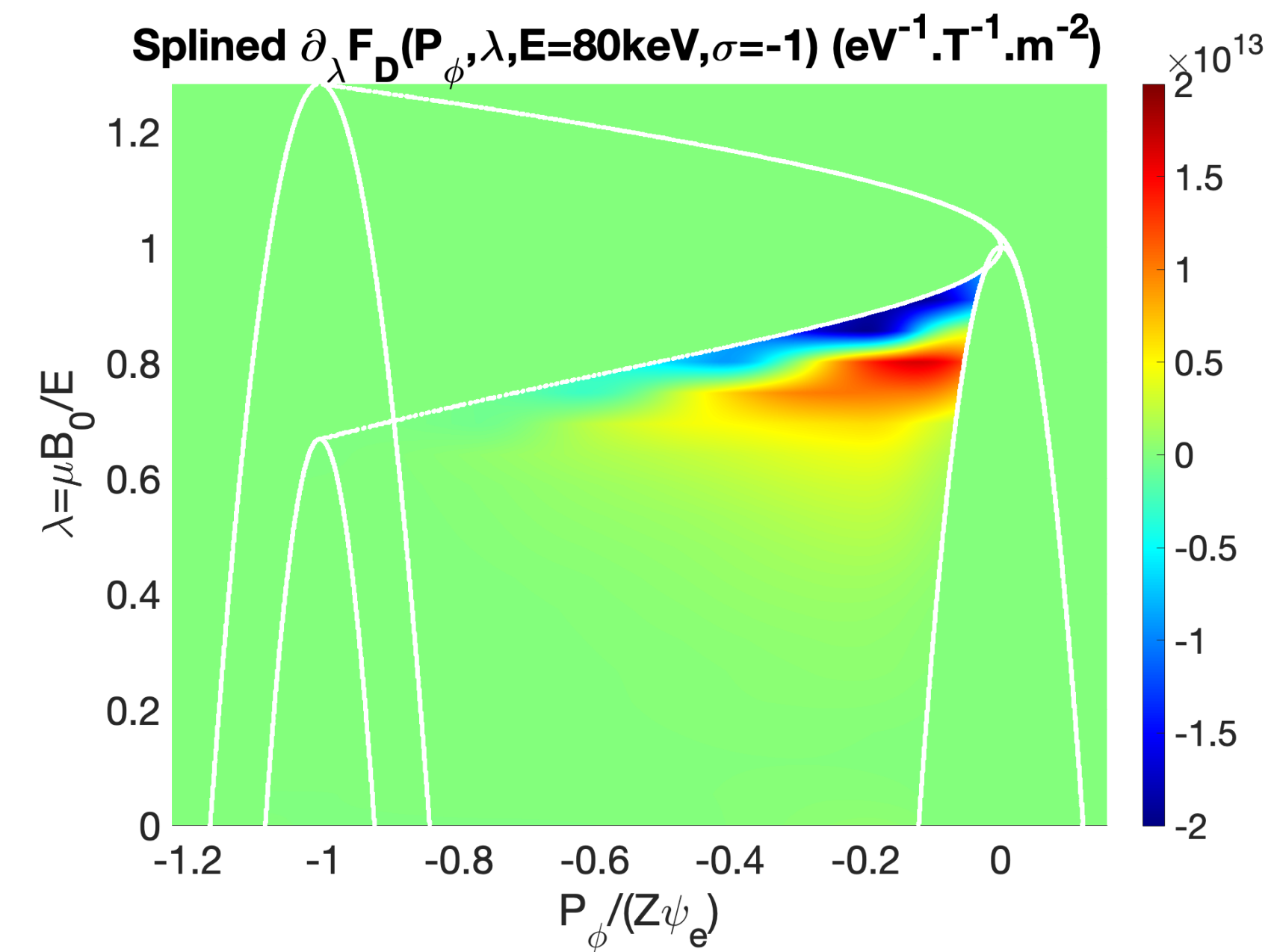


Spline pdf and derivatives (trapped orbits)

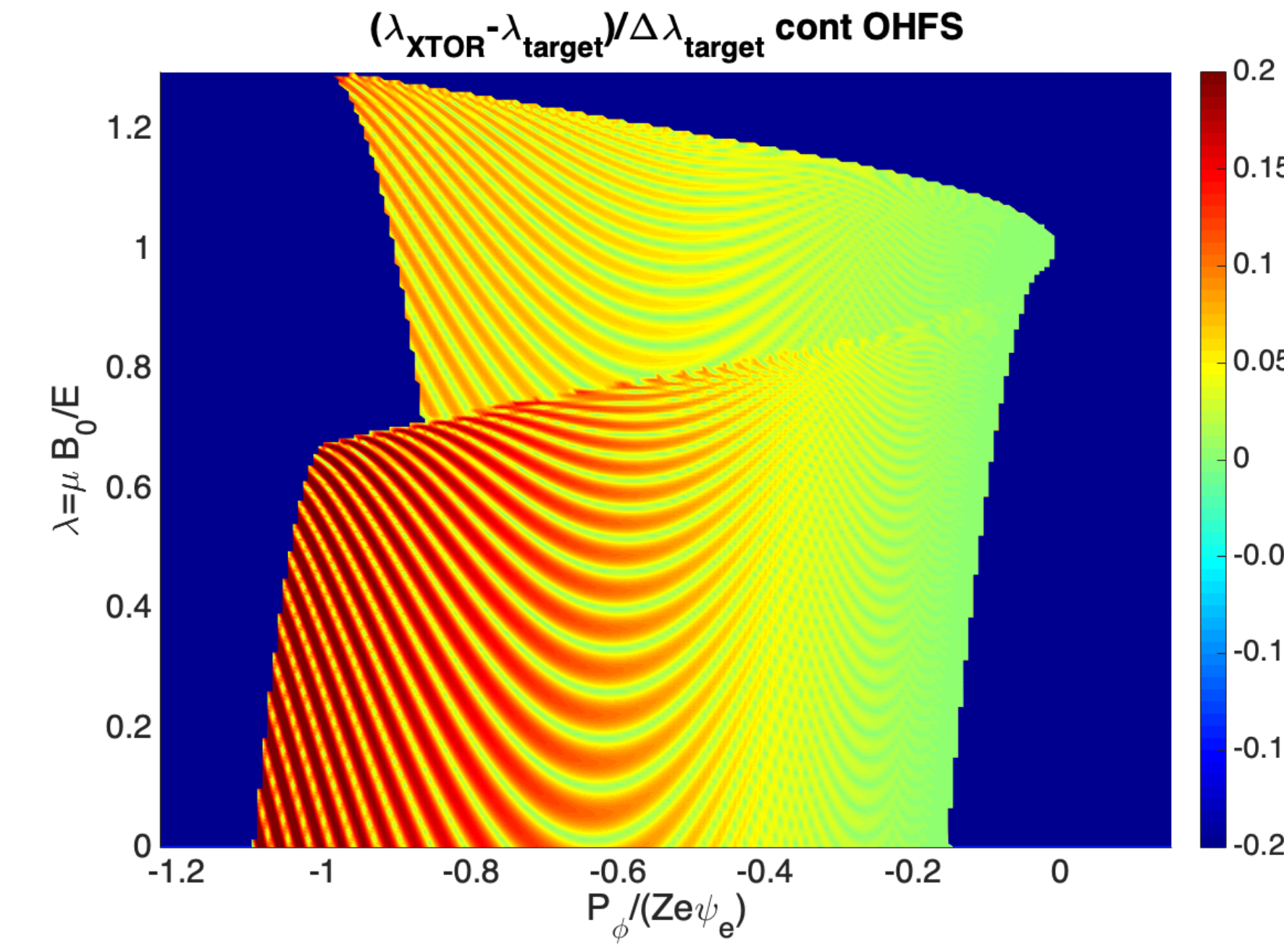
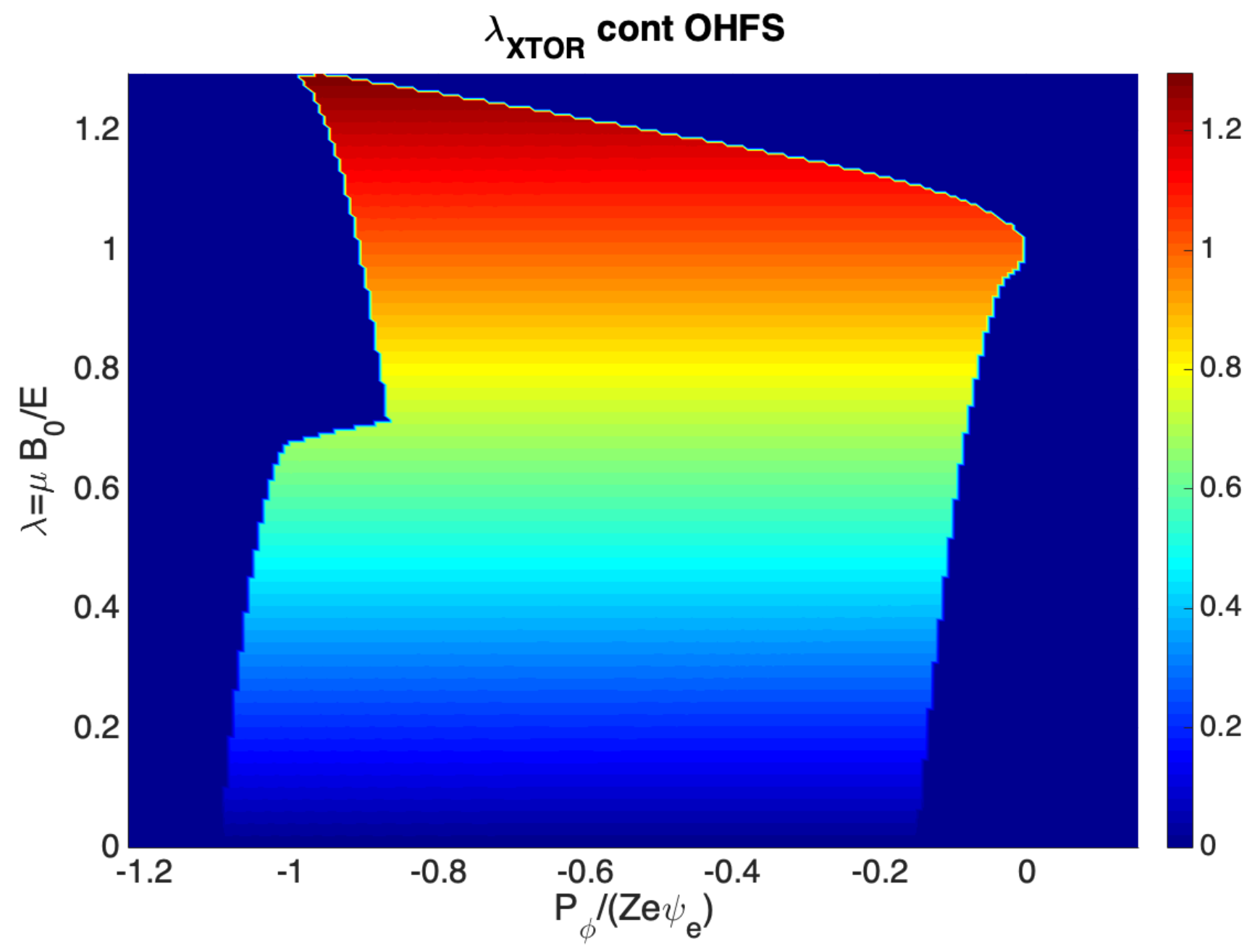
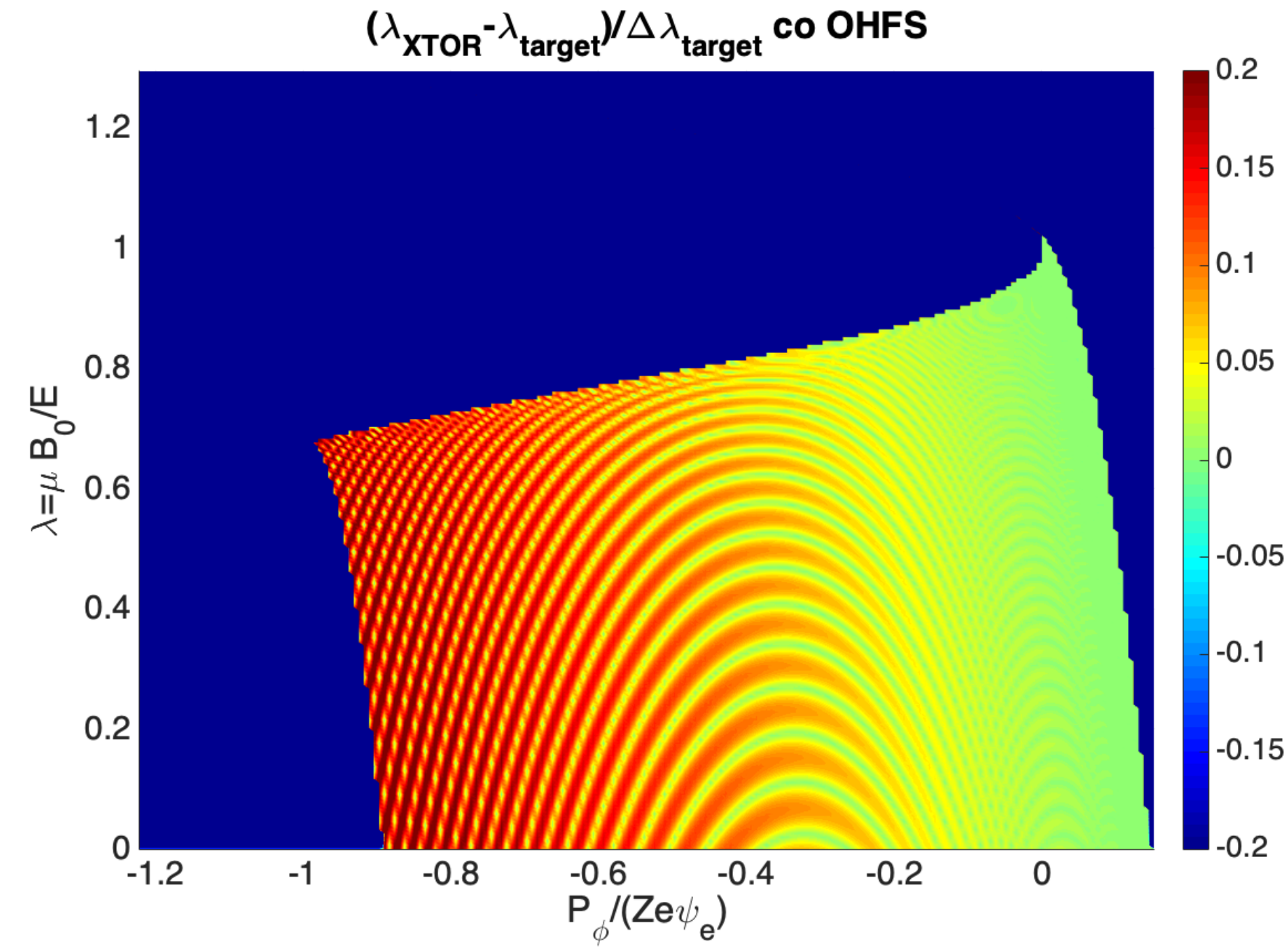
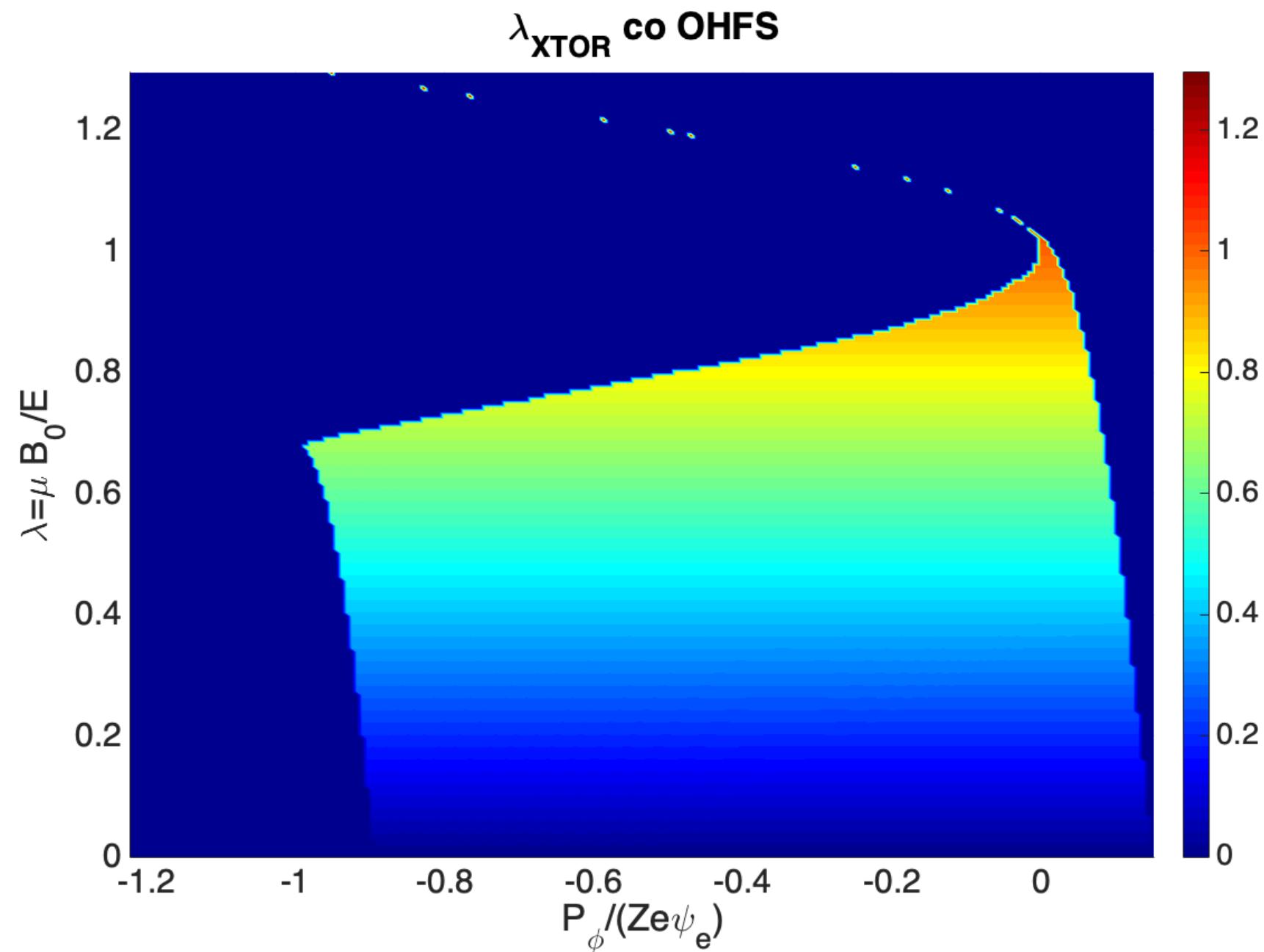


Spline pdf and derivatives (co-passing orbits)





Precision of λ initialisation in XTOR-K



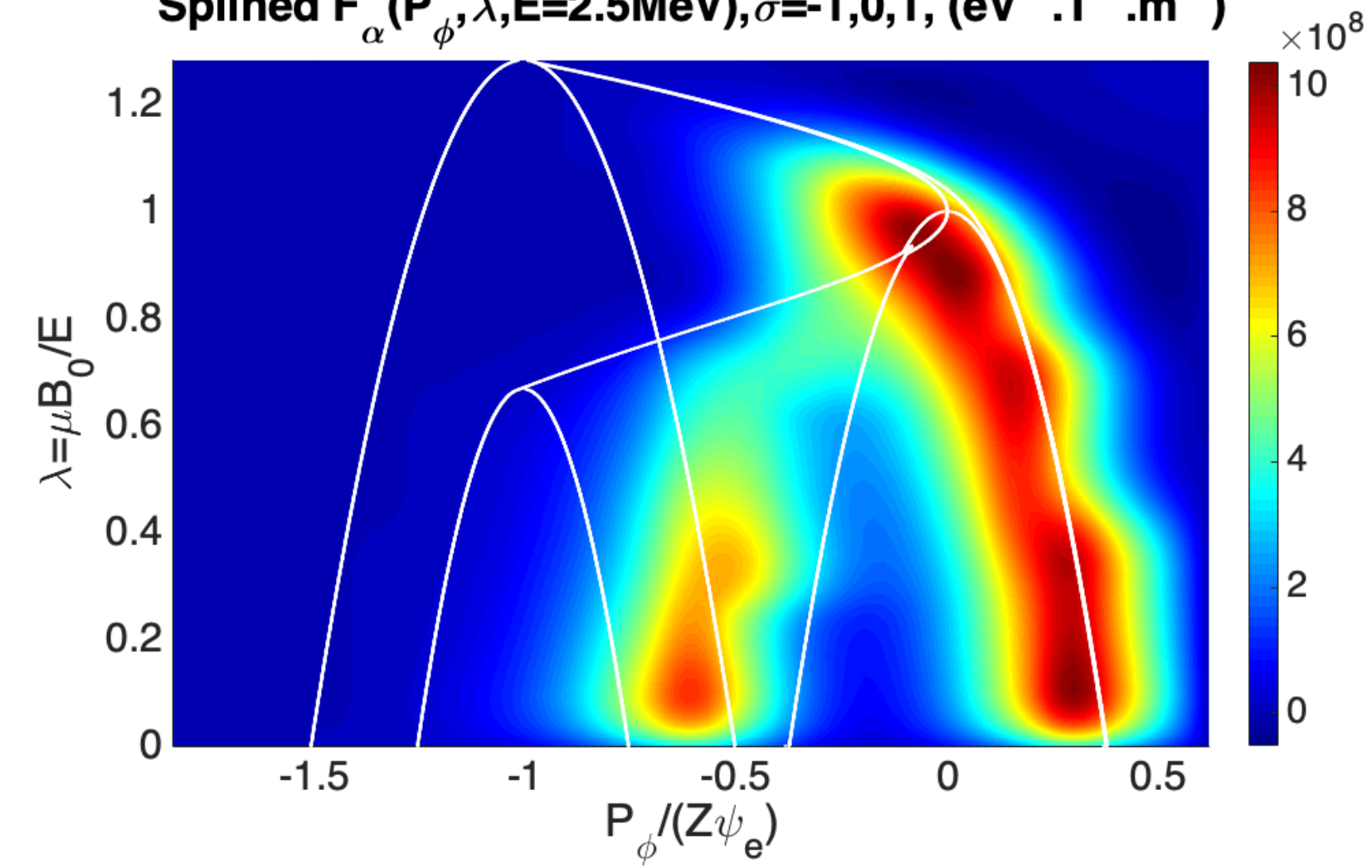
➤ Particles initialized on a 200×200 (P_ϕ, λ) grid

➤ Initialisation precision satisfying

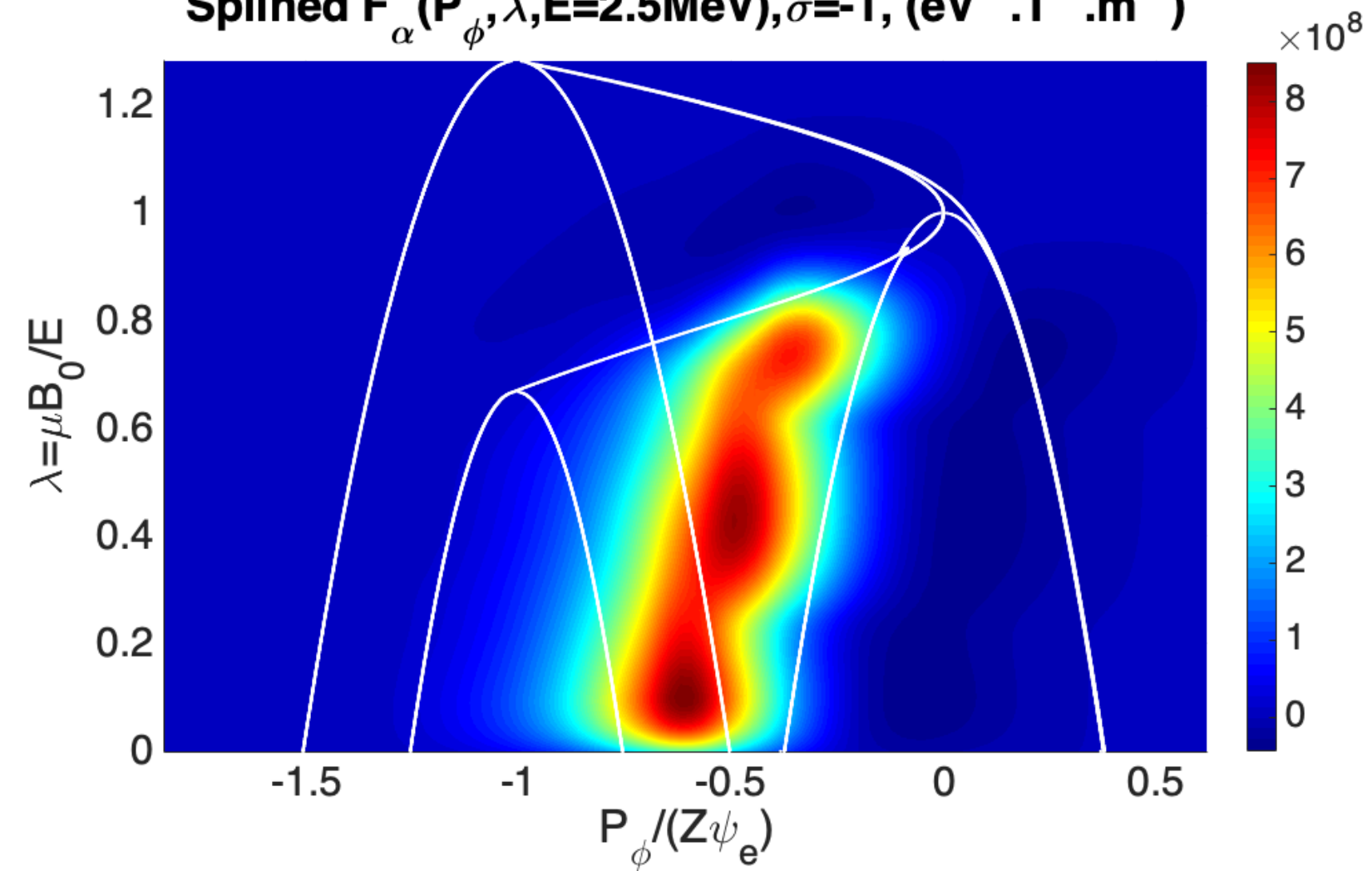
➤ Finite errors due to interpolation over the poloidal plane

Alpha CoM distributions

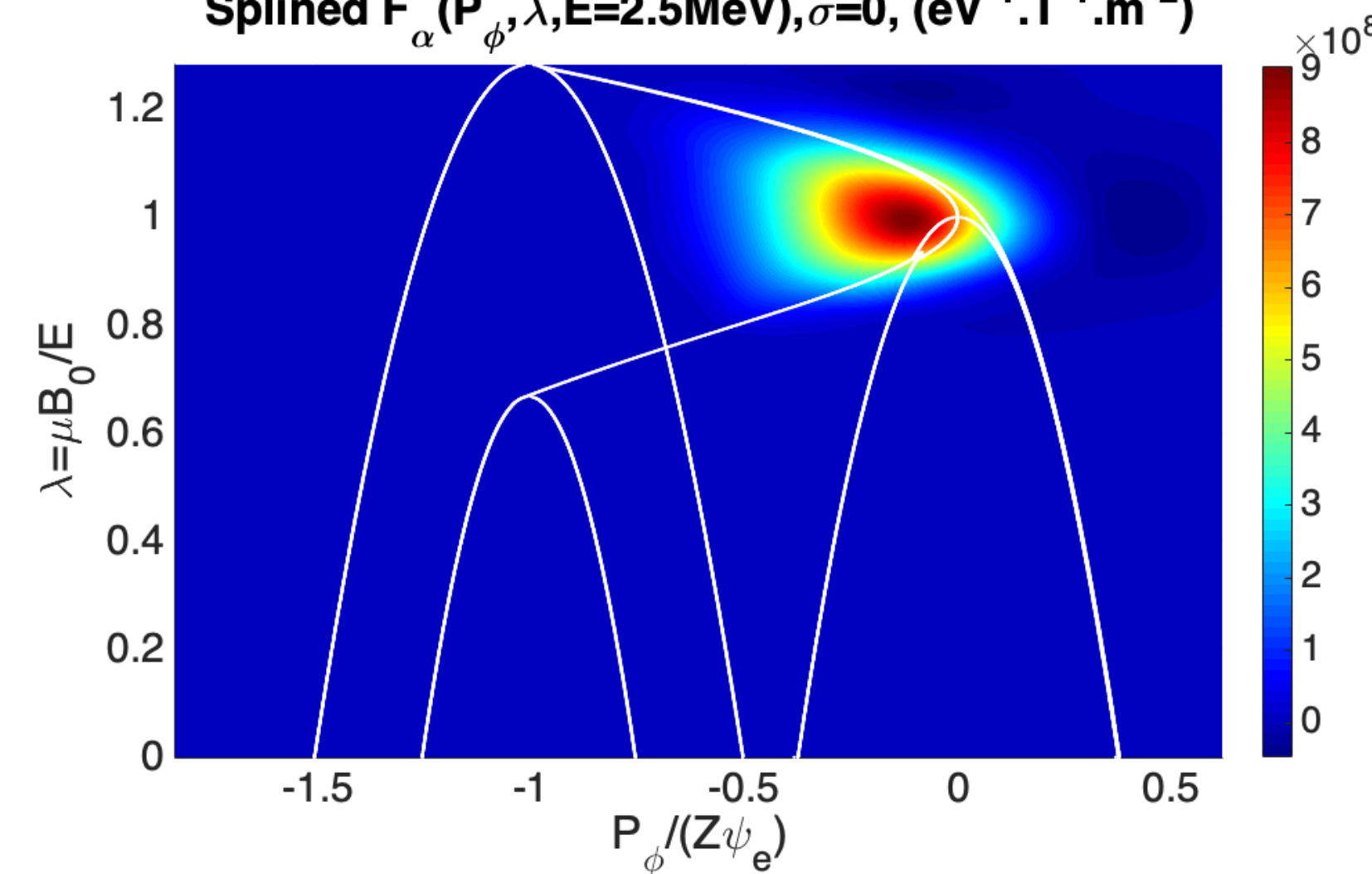
Splined $F_\alpha(P_\phi, \lambda, E=2.5\text{MeV}, \sigma=-1, 0, 1)$, ($\text{eV}^{-1} \cdot \text{T}^{-1} \cdot \text{m}^{-2}$)



Splined $F_\alpha(P_\phi, \lambda, E=2.5\text{MeV}, \sigma=-1)$, ($\text{eV}^{-1} \cdot \text{T}^{-1} \cdot \text{m}^{-2}$)



Splined $F_\alpha(P_\phi, \lambda, E=2.5\text{MeV}, \sigma=0)$, ($\text{eV}^{-1} \cdot \text{T}^{-1} \cdot \text{m}^{-2}$)



Splined $F_\alpha(P_\phi, \lambda, E=2.5\text{MeV}, \sigma=1)$, ($\text{eV}^{-1} \cdot \text{T}^{-1} \cdot \text{m}^{-2}$)

