



## ATEP news



|                      |  |       |
|----------------------|--|-------|
| <b>14:00</b> → 16:30 | <b>ENR ATEP Progress Meeting</b>   |       |
| <b>14:00</b>         | <b>ATEP news</b><br>Speaker: Philipp Lauber (IPP)  | 🕒 10m |
| <b>14:10</b>         | <b>Update on beat-driven and spontaneous excitation of ZF/ Update on calculation of low frequency spectrum including trapped particles</b><br>Speakers: Fulvio Zonca (ENEA), Matteo Valerio Falessi (ENEA) | 🕒 30m |
| <b>14:40</b>         | <b>Update on STRUPHY</b><br>Speaker: Stefan Possanner  | 🕒 20m |
| <b>15:00</b>         | <b>Update on ATEP-3D solver</b><br>Speaker: Guo Meng (IPP)   | 🕒 10m |
| <b>15:10</b>         | <b>Update on ORB5-ATEP PSZS comparison/ZF model in ATEP</b><br>Speaker: Philipp Lauber (IPP)   | 🕒 40m |
| <b>15:50</b>         | <b>short reports and discussion</b><br>Speaker: Philipp Lauber (IPP)   | 🕒 30m |



# announcement - review meeting



THURSDAY, 24 OCTOBER

**09:00** → 12:30 **Theory & Modelling Projects**

|              |  |       |
|--------------|--|-------|
| <b>09:00</b> | <b>Operation limiting plasma instabilities in high performance tokamaks: fundamental understanding and solutions for critical problems</b> ¶<br>ENR-MOD.01.EPFL<br>(25 min presentation + 15 min. discussions)<br><b>Speaker:</b> Jonathan Graves (EPFL) | 🕒 50m |
| <b>09:50</b> | <b>Development of machine learning methods and integration of surrogate model predictor schemes for plasma-exhaust and PWI in fusion</b><br>ENR-MOD.01.FZJ<br>(25 min presentation + 15 min. discussions)<br><b>Speaker:</b> Dr Sven Wiesen (DIFFER)     | 🕒 50m |
| <b>10:40</b> | <b>COFFEE BREAK</b>  | 🕒 10m |
| <b>10:50</b> | <b>Energetic particle optimization of stellarator devices using near-axis magnetic fields</b><br>ENR-MOD.01.IST<br>(25 min. presentation + 15 min. discussions)<br><b>Speaker:</b> Rogerio Jorge (IST)   | 🕒 50m |
| <b>11:40</b> | <b>Advanced energetic particle transport models (ATEP)</b><br>ENR-MOD.01.MPG<br>(25 min. presentation + 15 min. discussions)<br><b>Speaker:</b> Philipp Lauber (IPP)   | 🕒 50m |

**proposal: ATEP internal review meeting ~2-3 weeks before: beginning of October, 2024**



# **ORB5-LIGKA PSZS comparison**

## **status and open issues**

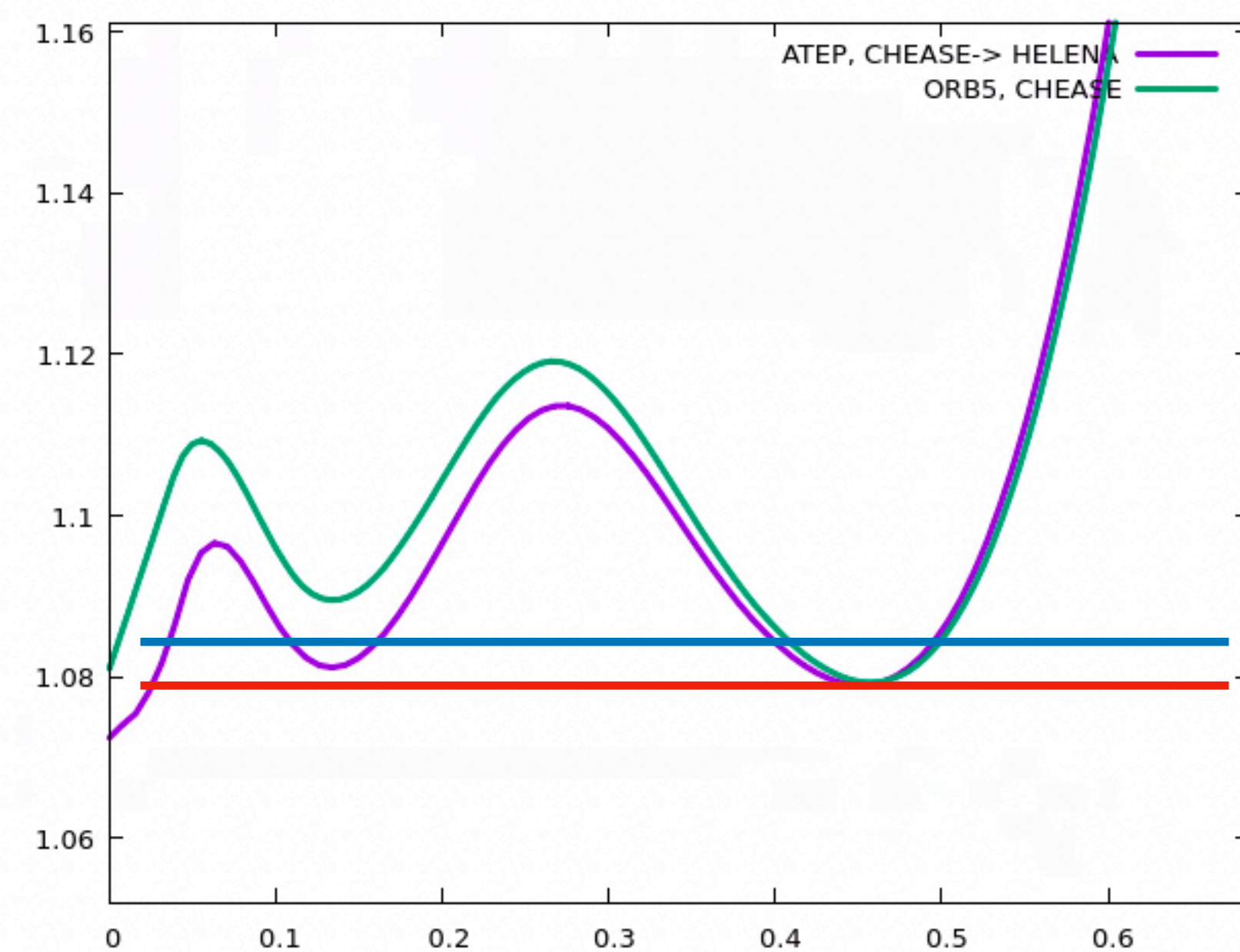
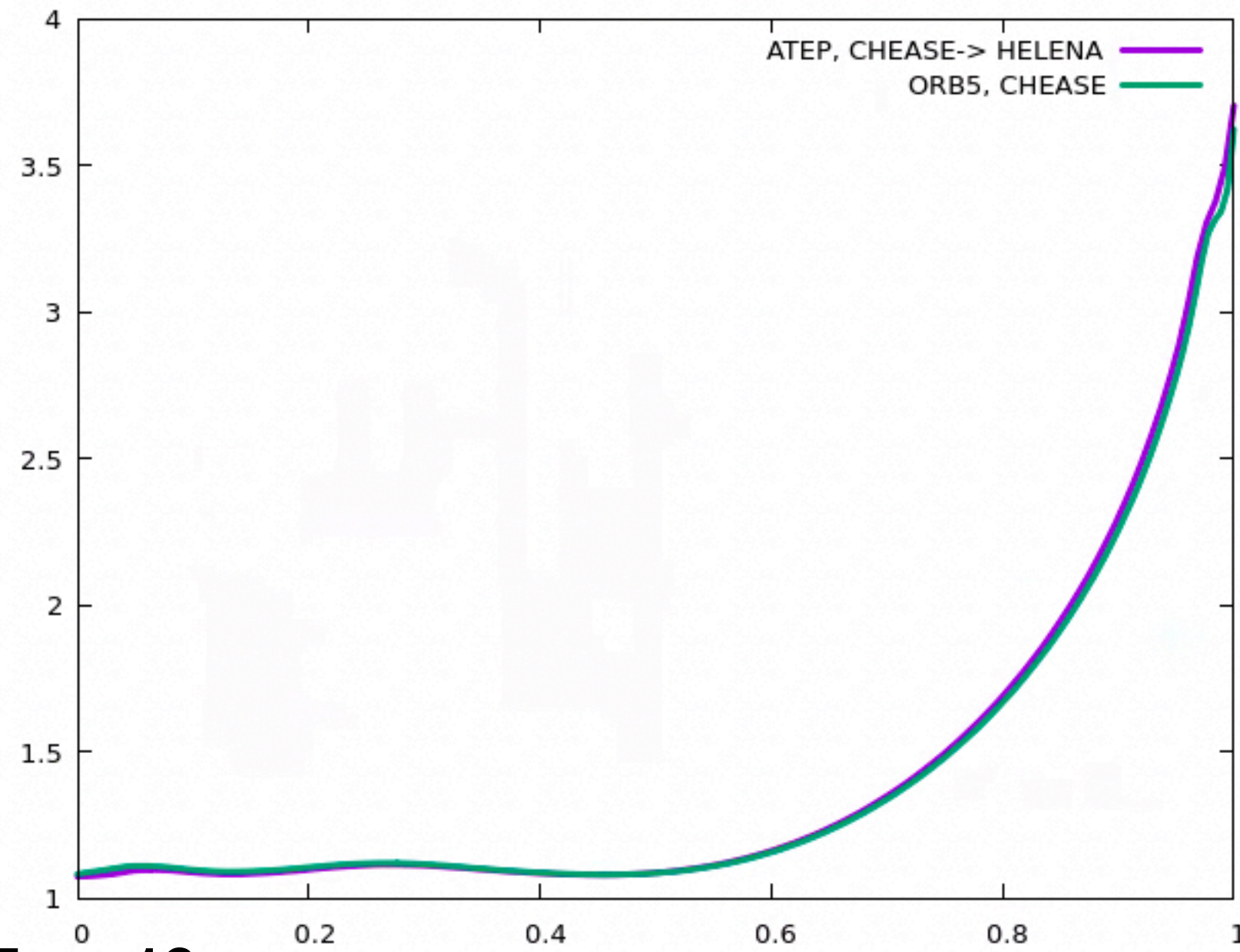


[T Hayward-Schneider,  
FEC 2023]

2 NBI beams: on-off

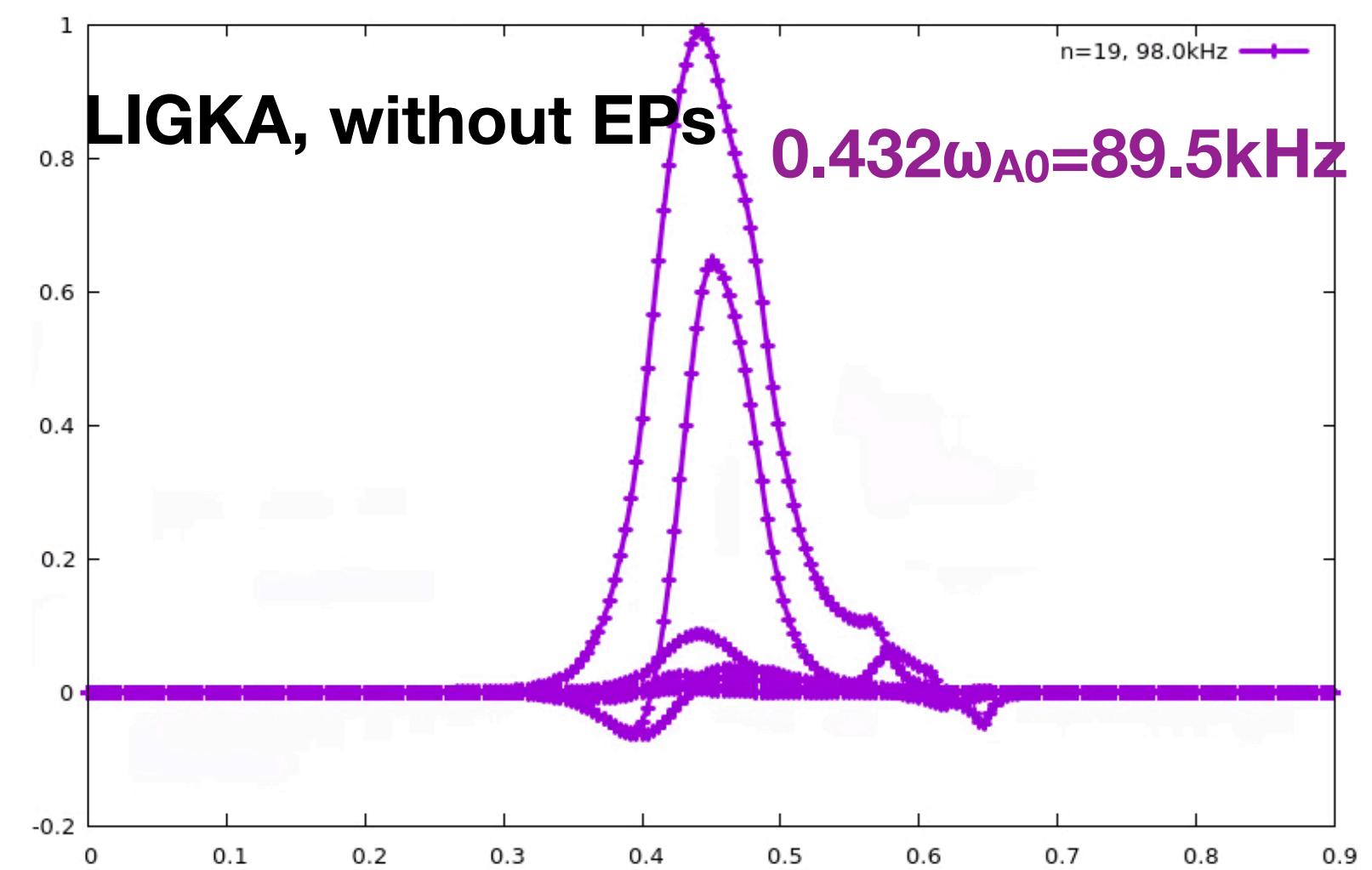
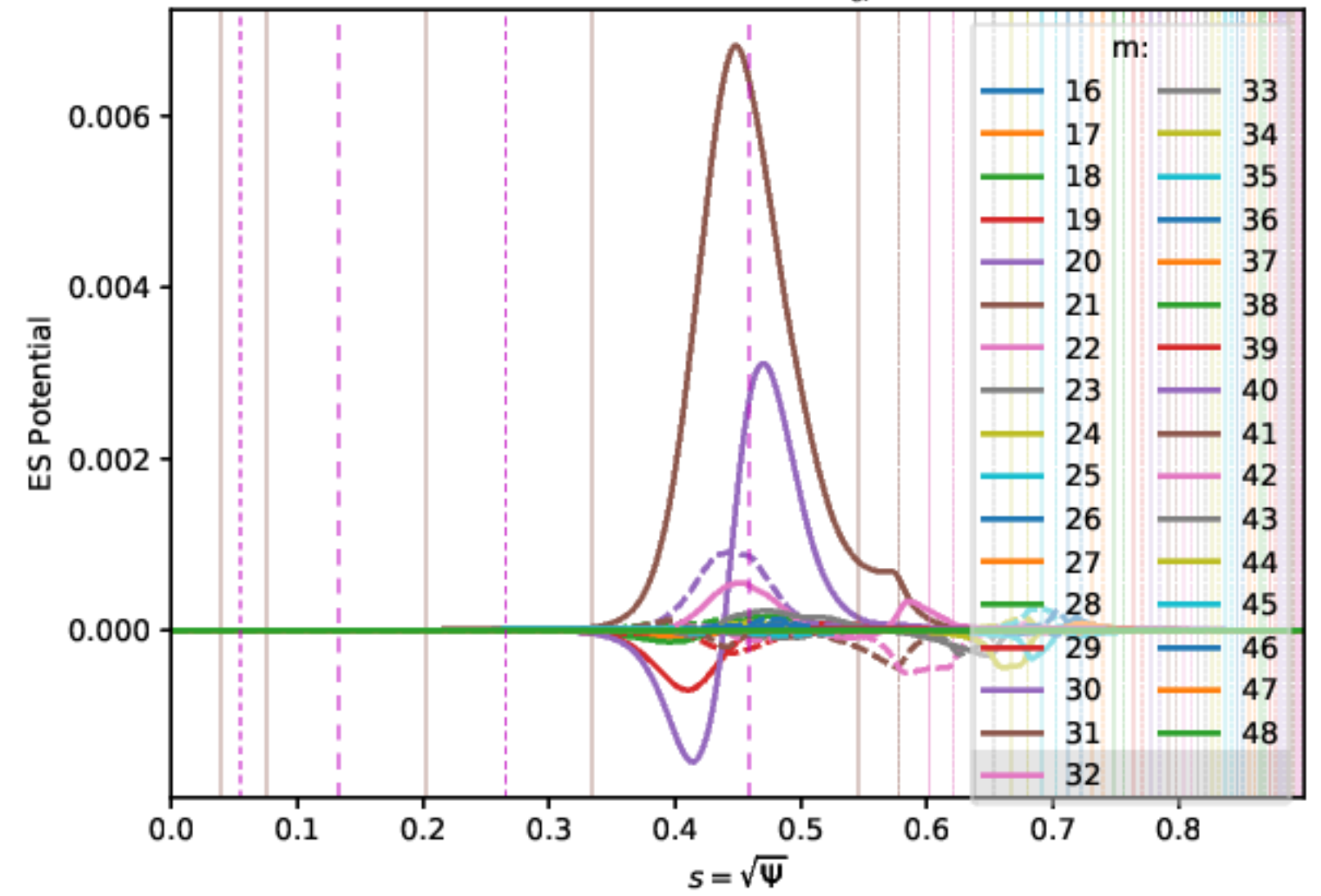
$q = q_{TAE}(n=18) = 19.5/18 = 1.0833$

$q = q_{TAE}(n=19) = 20.5/19 = 1.0789 = q_{min}$



ORB5: n=19

$t = 235300.0 \omega_{ci}^{-1}$



matching local  $q_{min}$ , differences in shear

mode structures very sensitive to  $q$



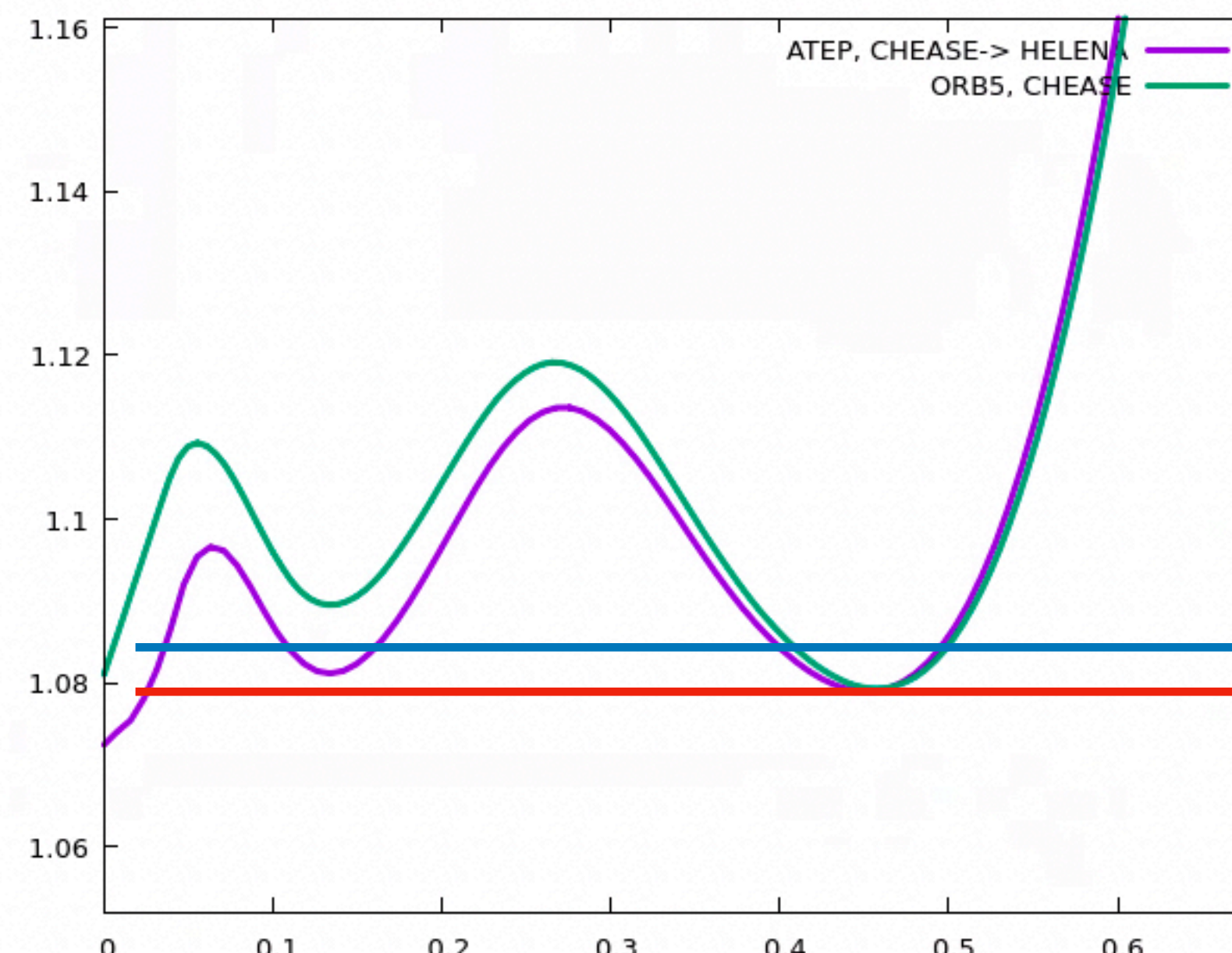
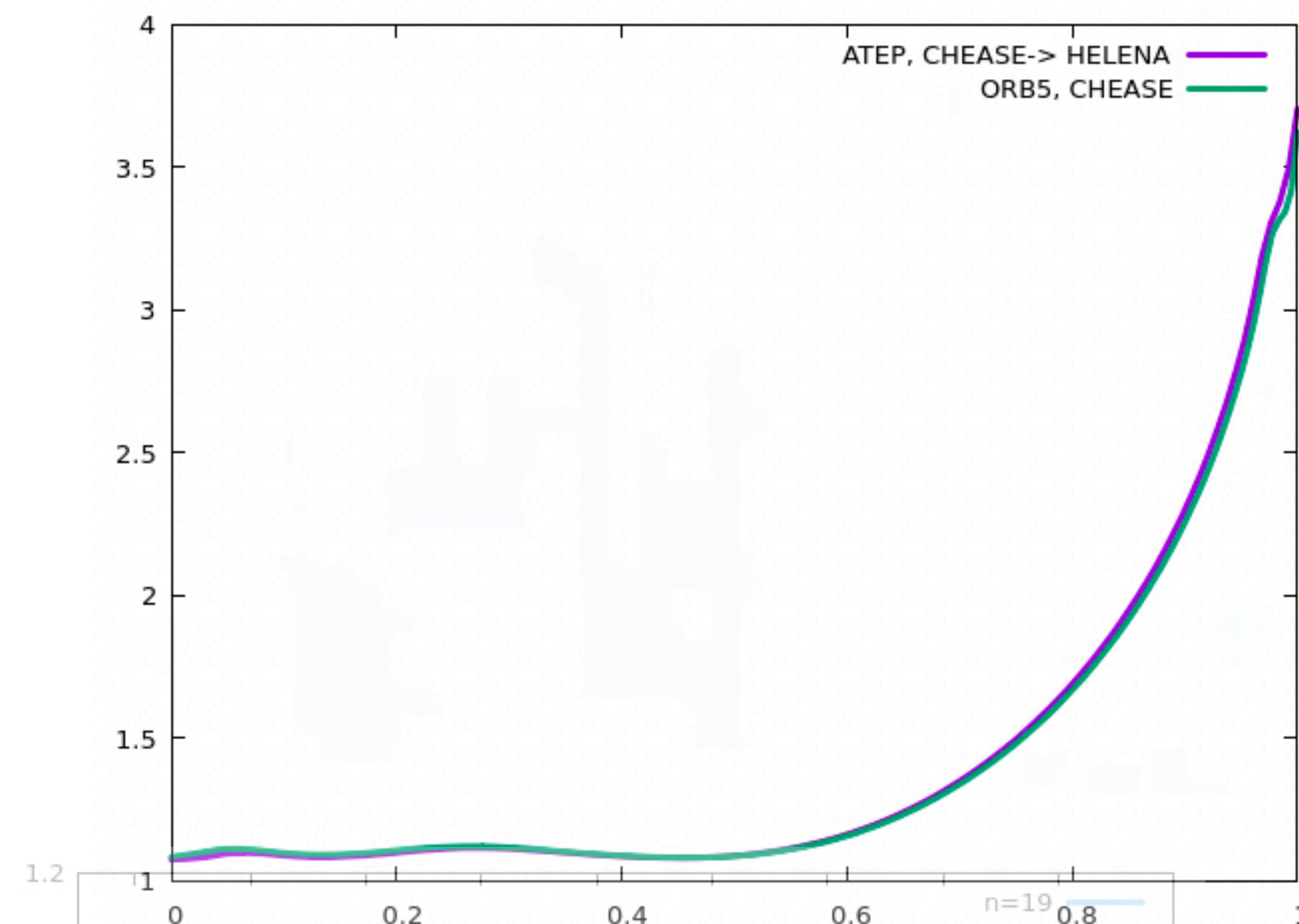


[T Hayward-Schneider,  
FEC 2023]

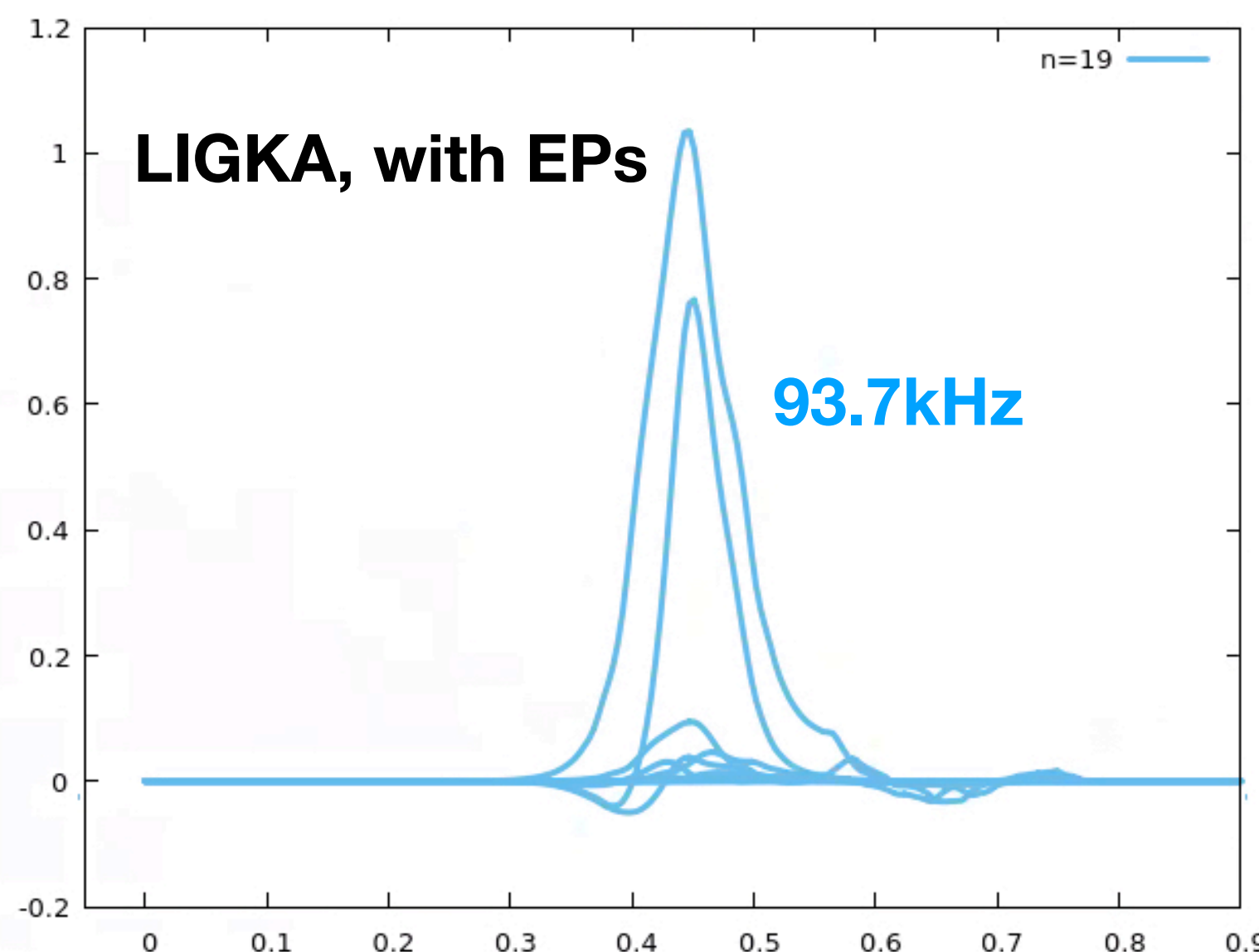
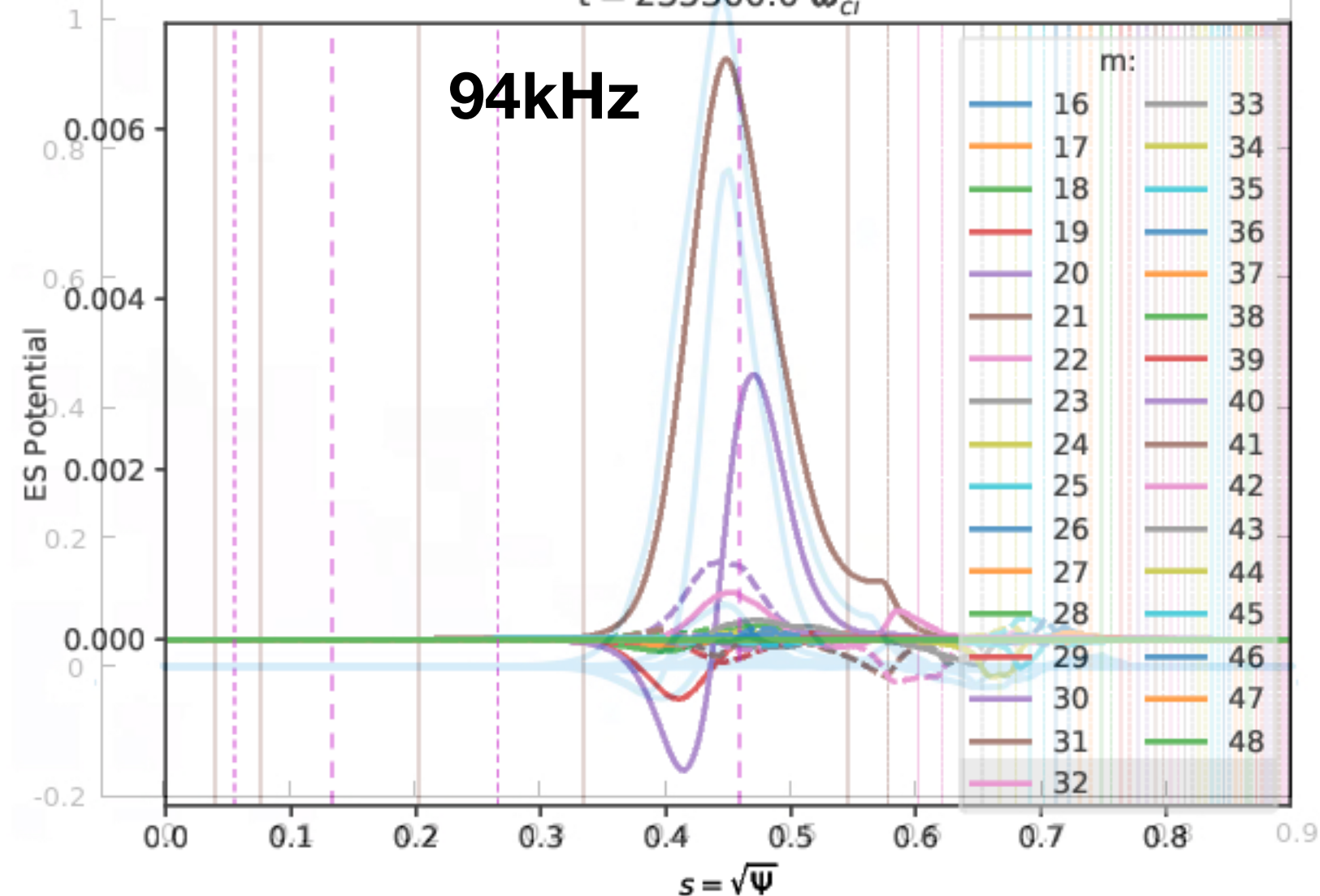
2 NBI beams: on-off

$q = q_{TAE}(n=18) = 19.5/18 = 1.0833$

$q = q_{TAE}(n=19) = 20.5/19 = 1.0789 = q_{min}$



ORB5: n=19

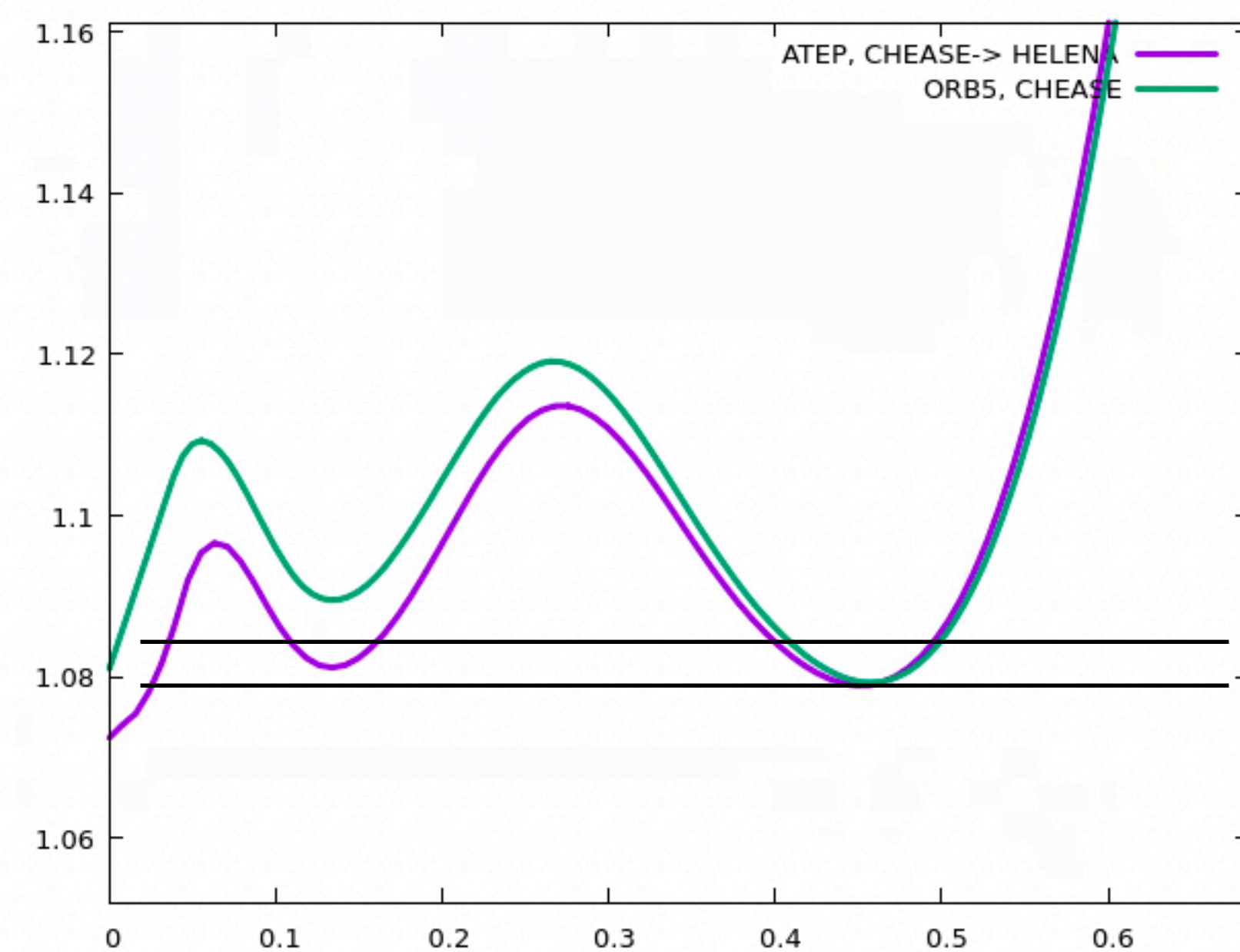
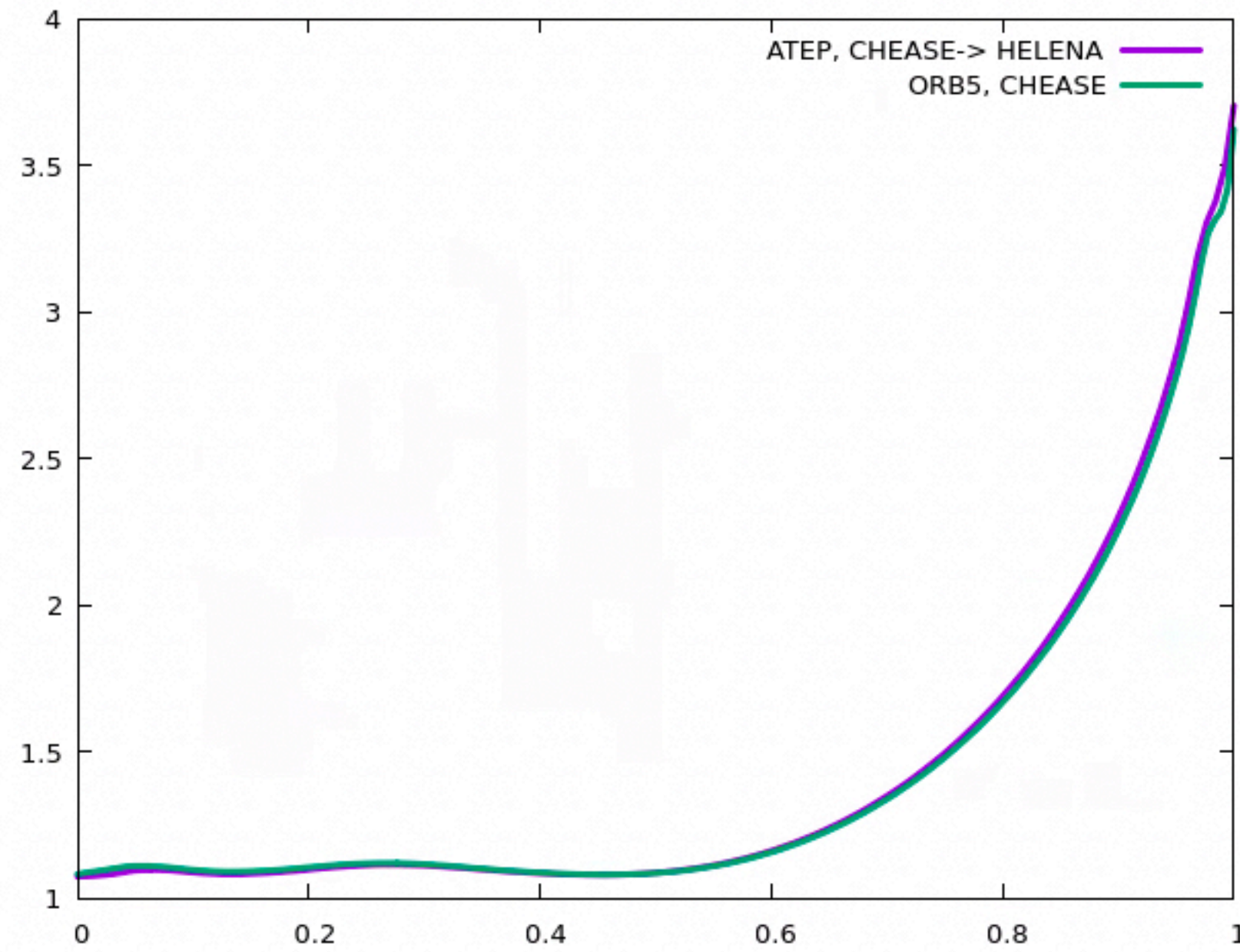


matching local  $q_{min}$ , differences in shear

mode structures very sensitive to  $q$

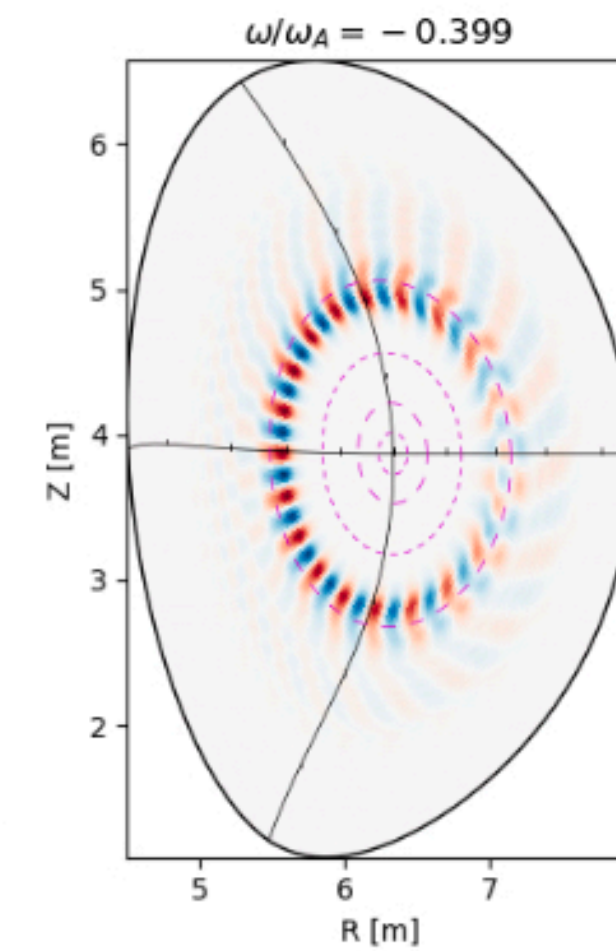
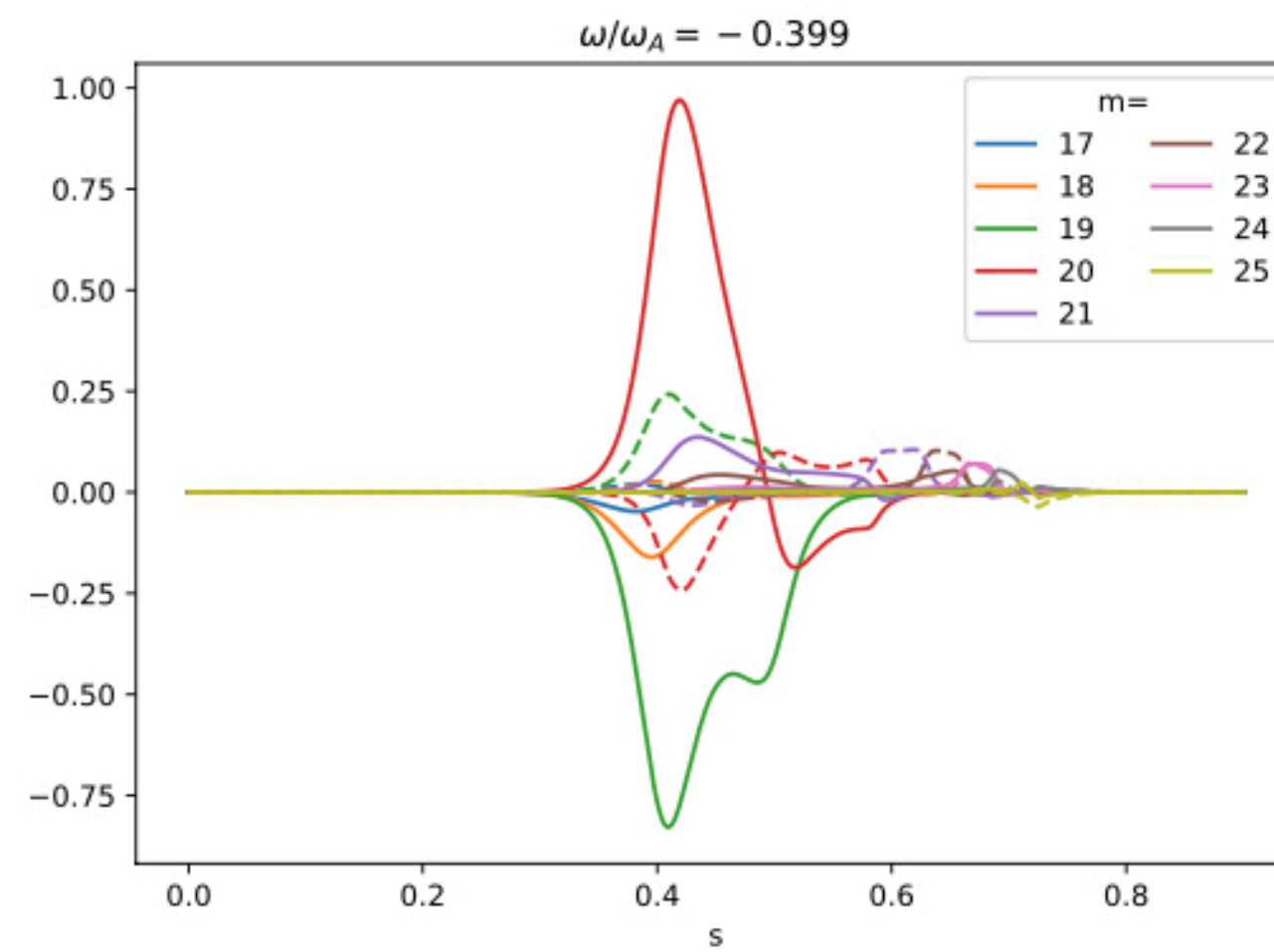
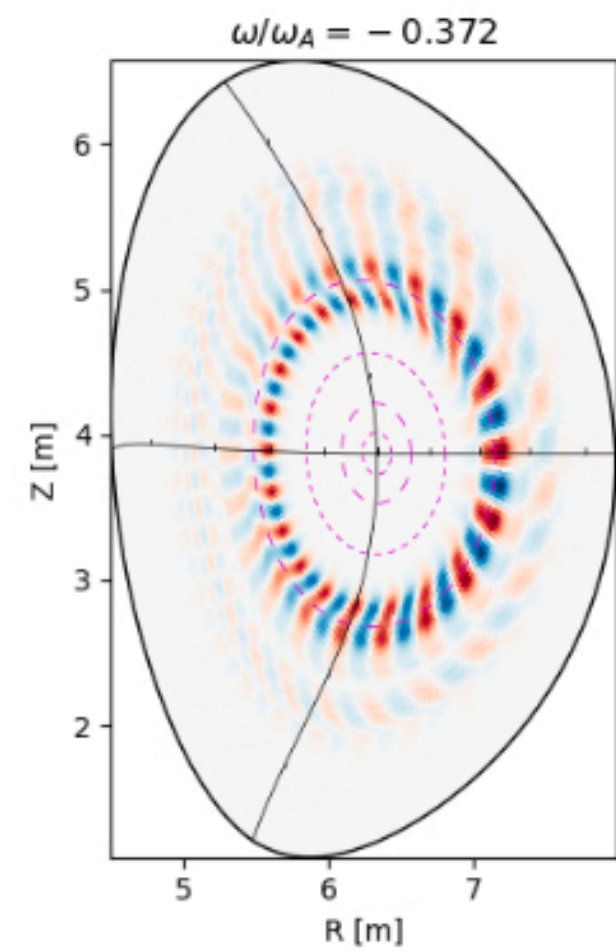
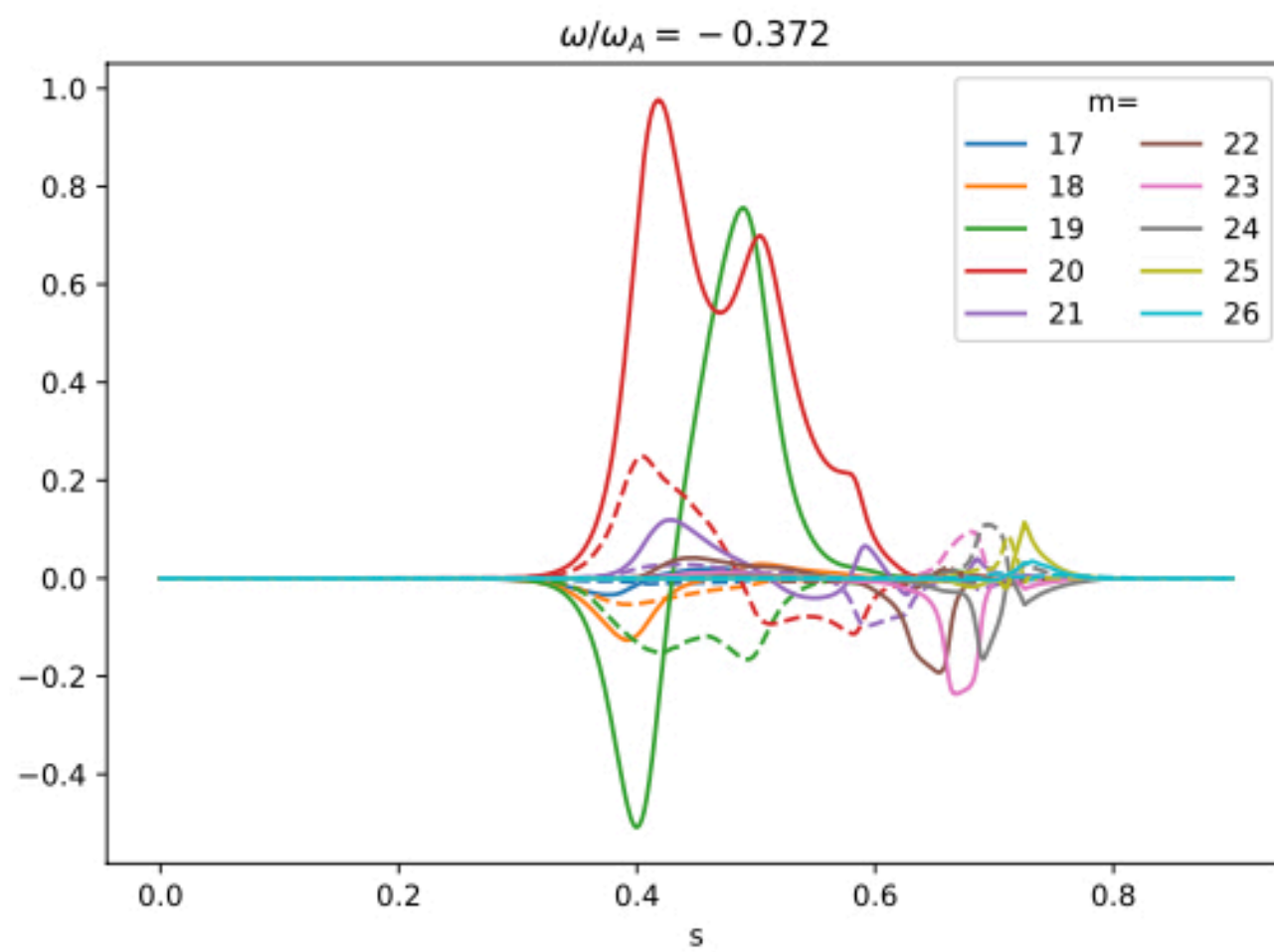


# ORB5-LIGKA PSZS comparison improving, ITER #101006



$q=q_{TAE}(n=18)=19.5/18=1.0833$   
 $q=q_{TAE}(n=19)=20.5/19=1.0789$

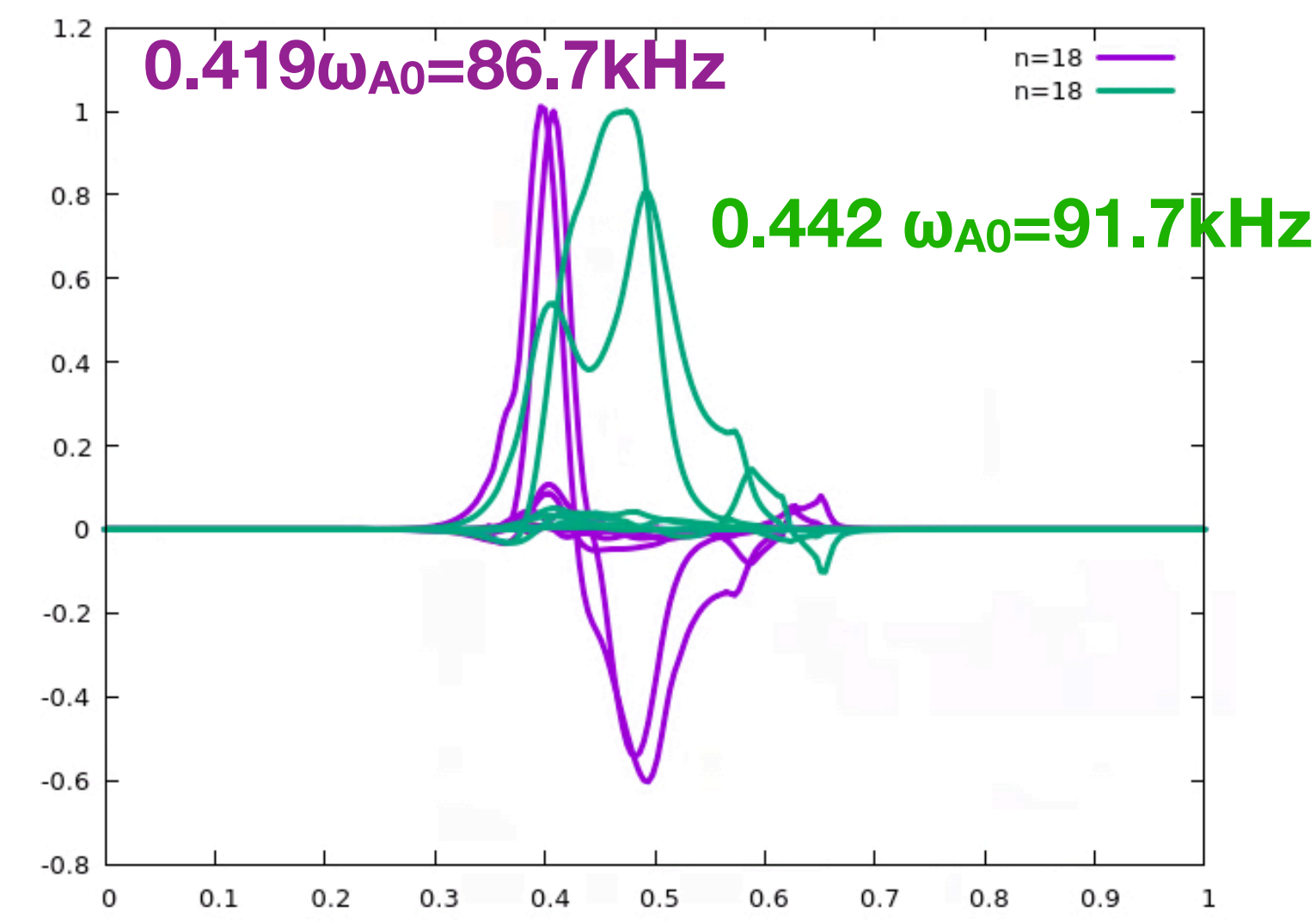
**ORB5: n=18**



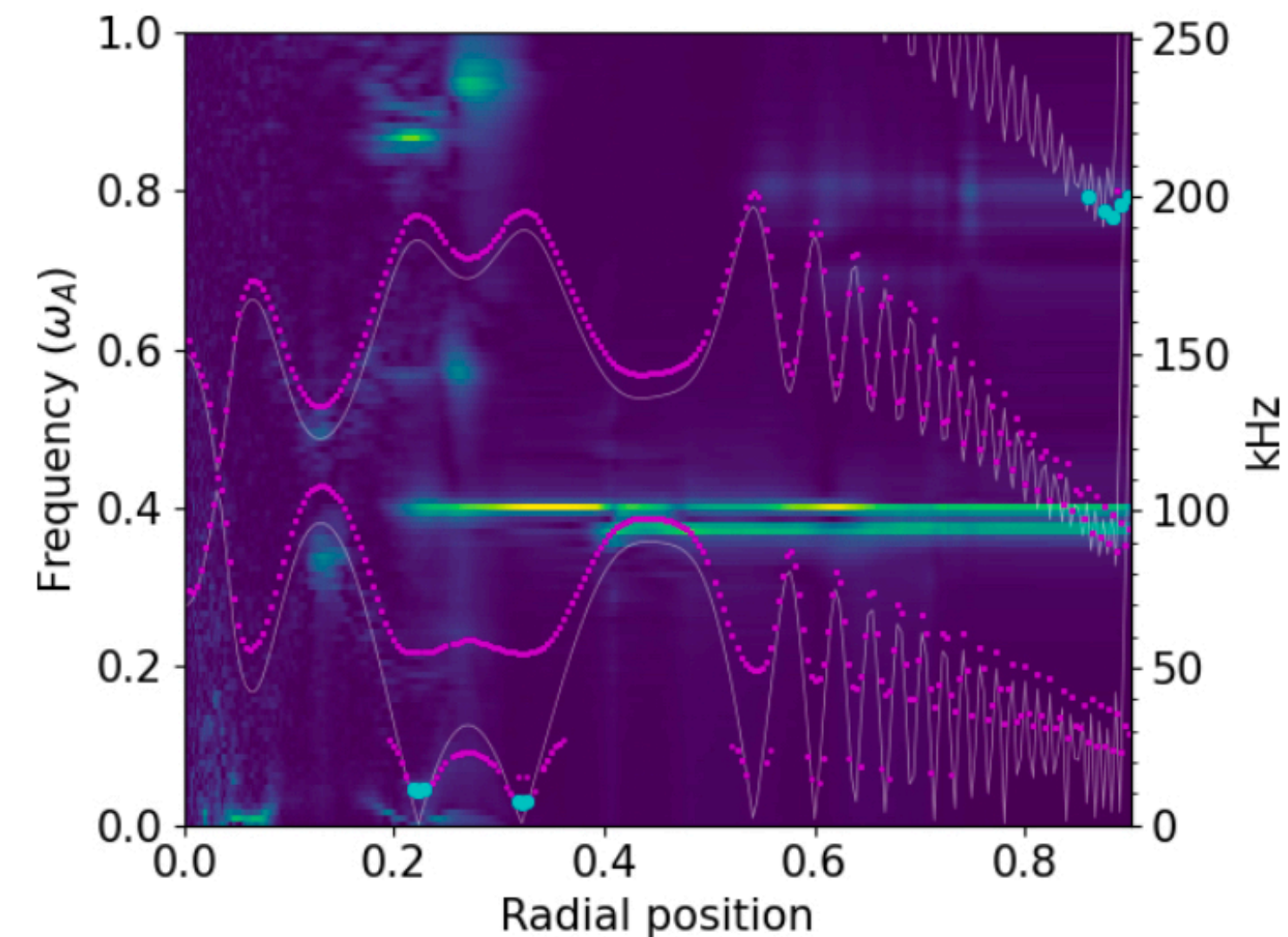
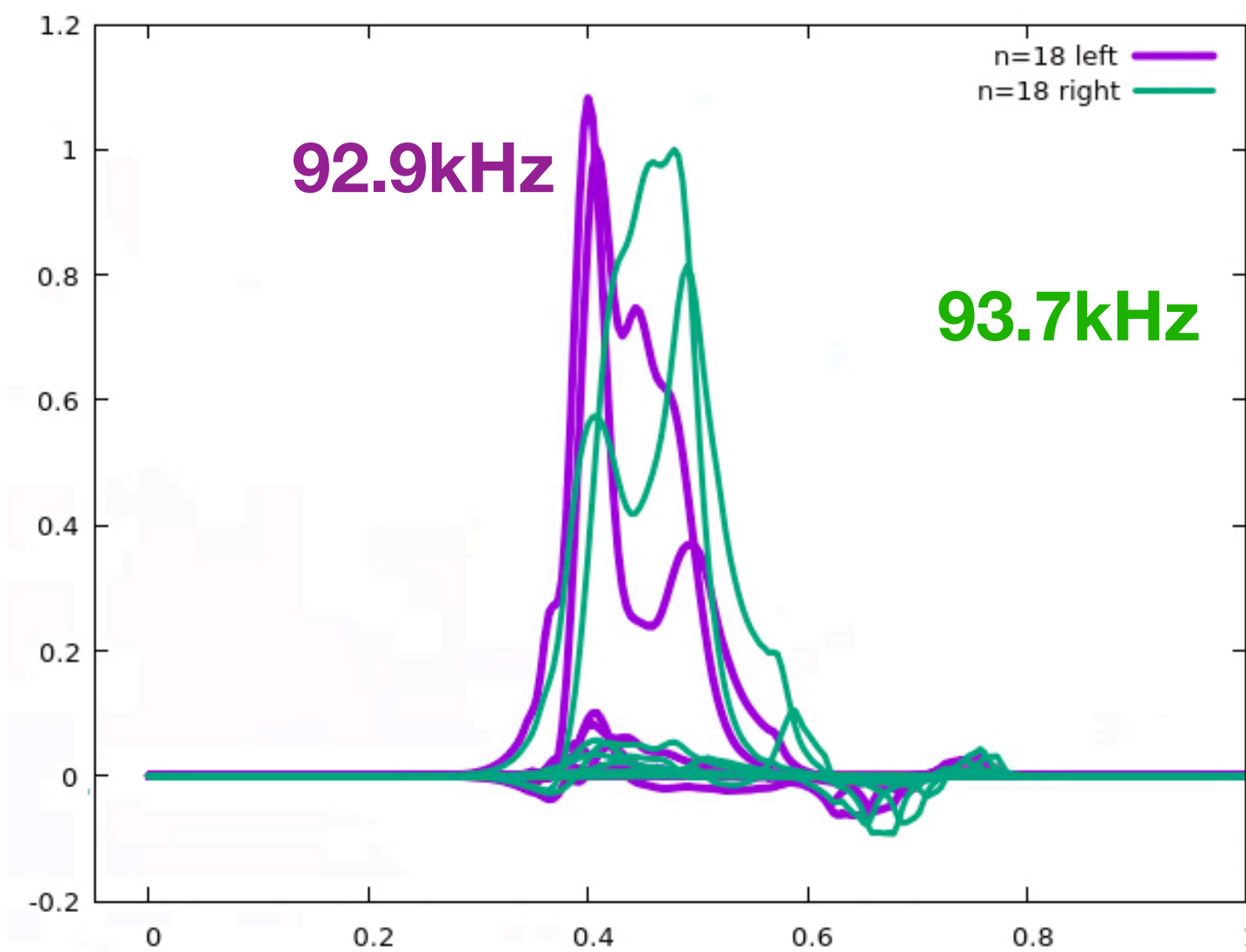
**[T Hayward-Schneider  
FEC 2023]**



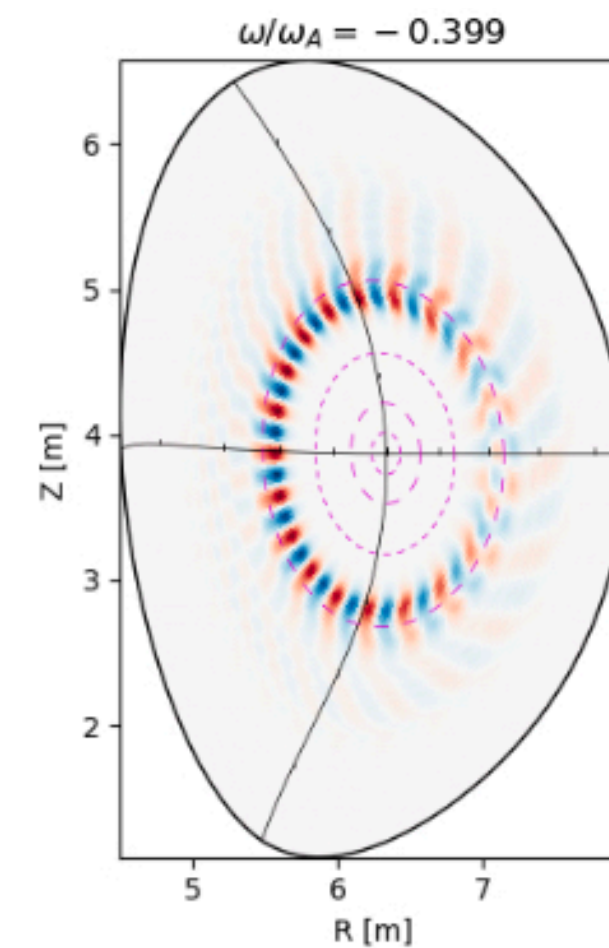
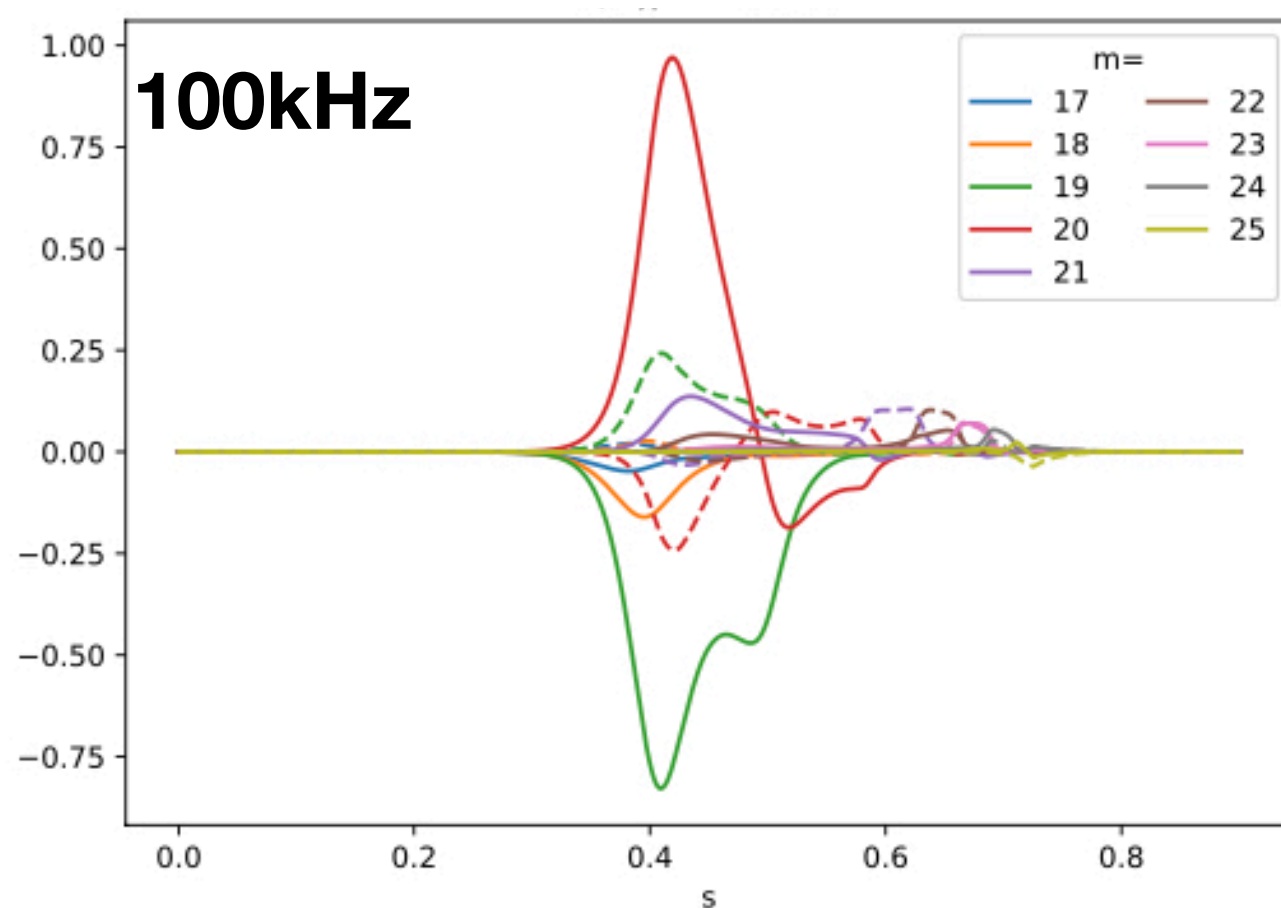
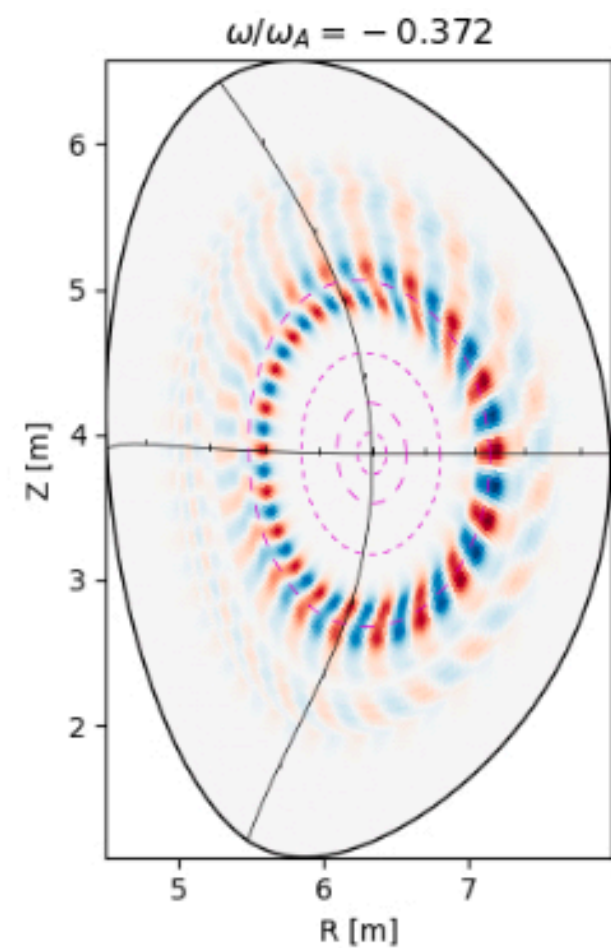
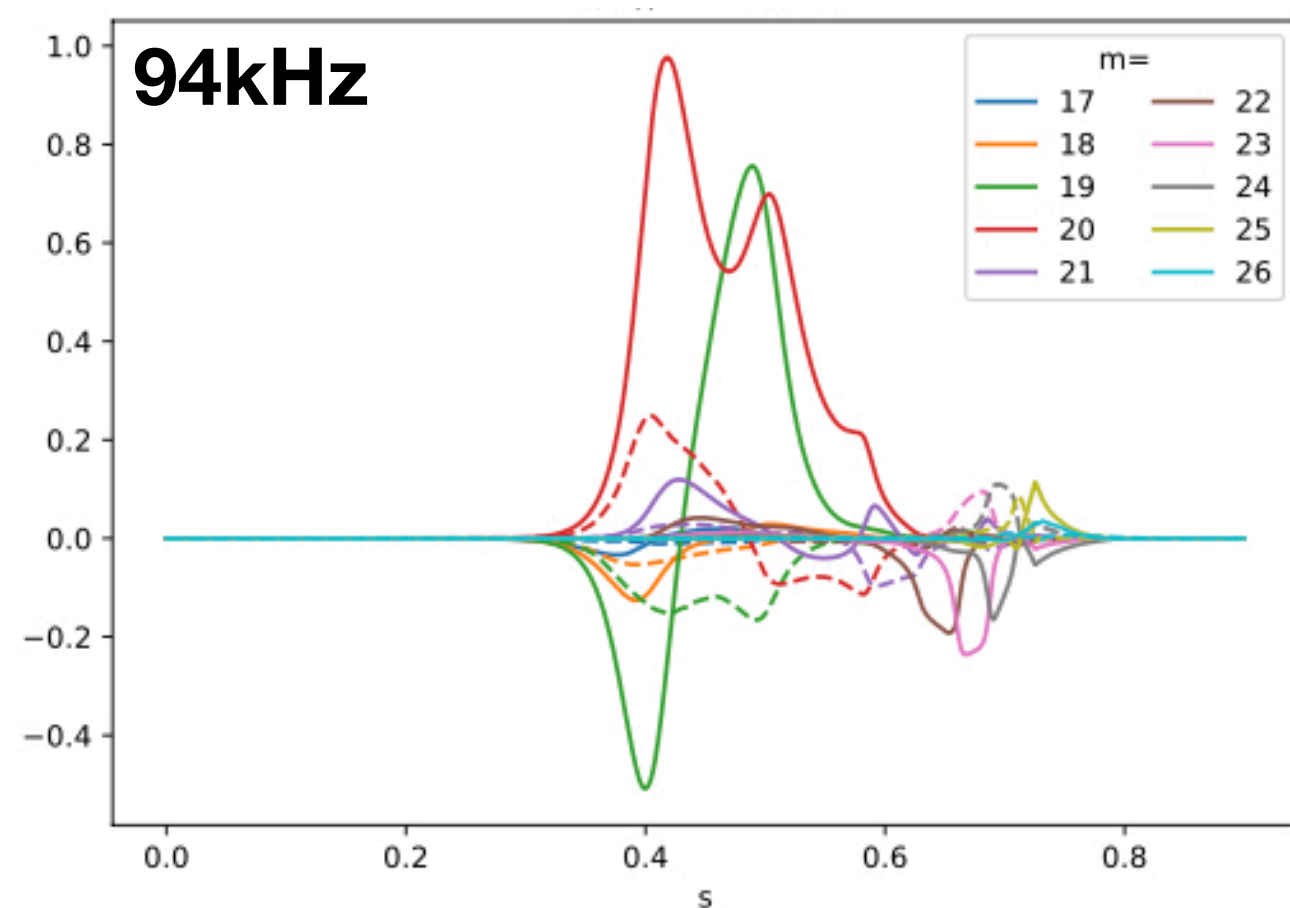
### LIGKA: n=18, no EPs



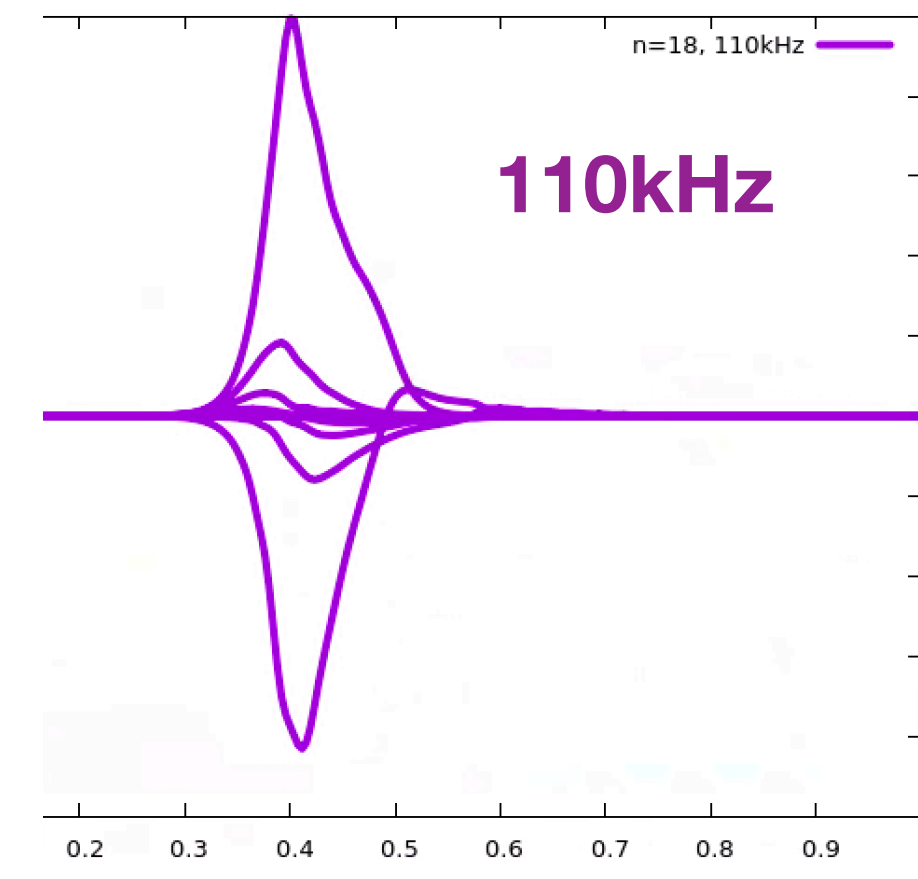
### LIGKA, n=18 with EPs



### ORB5 (with EPs): n=18

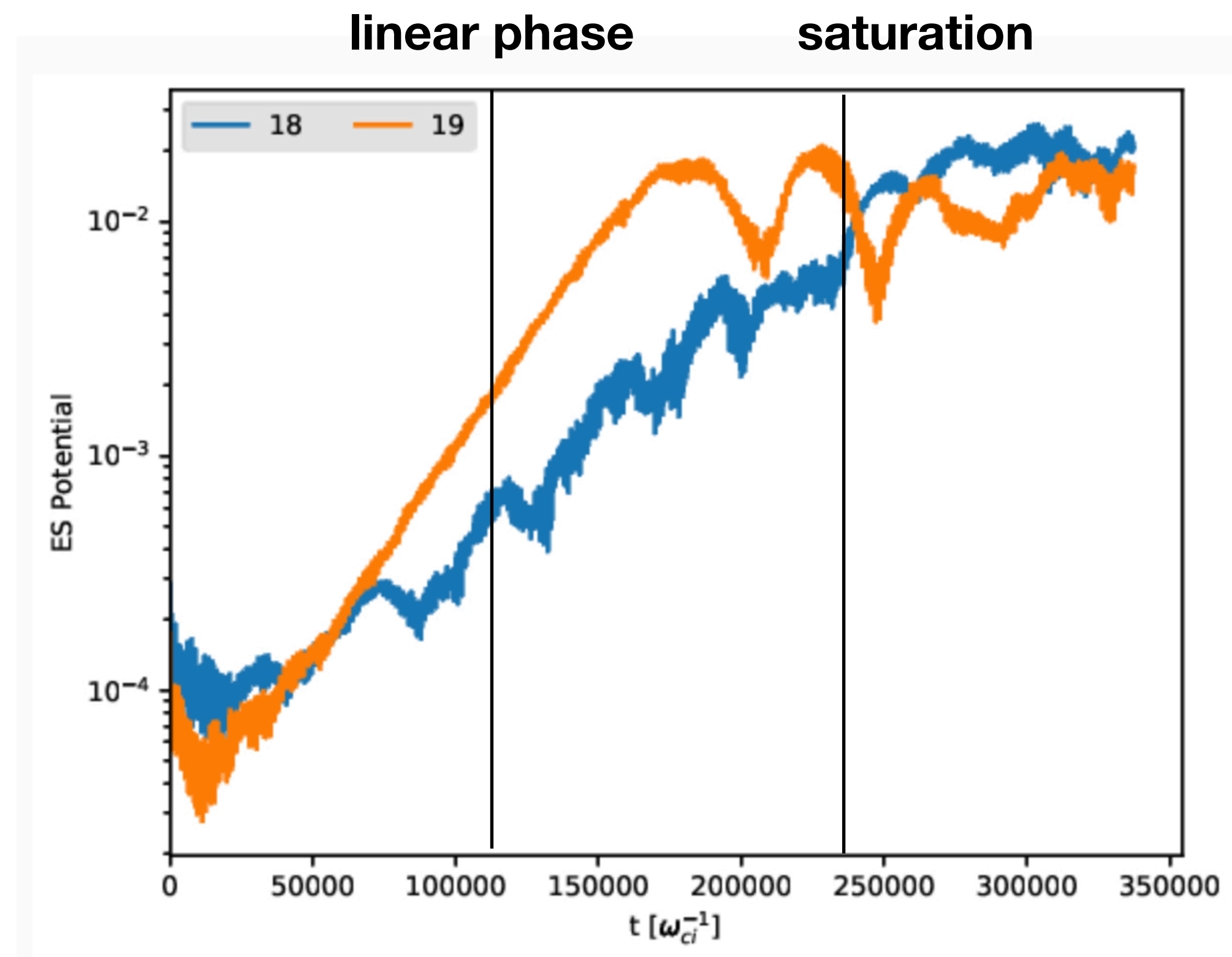


### odd, n=18 with EPs



### odd, n=18 without EPs

118kHz



growth rates:  
ORB5: n=19: 2%  
LIGKA: n=19: 2.3%

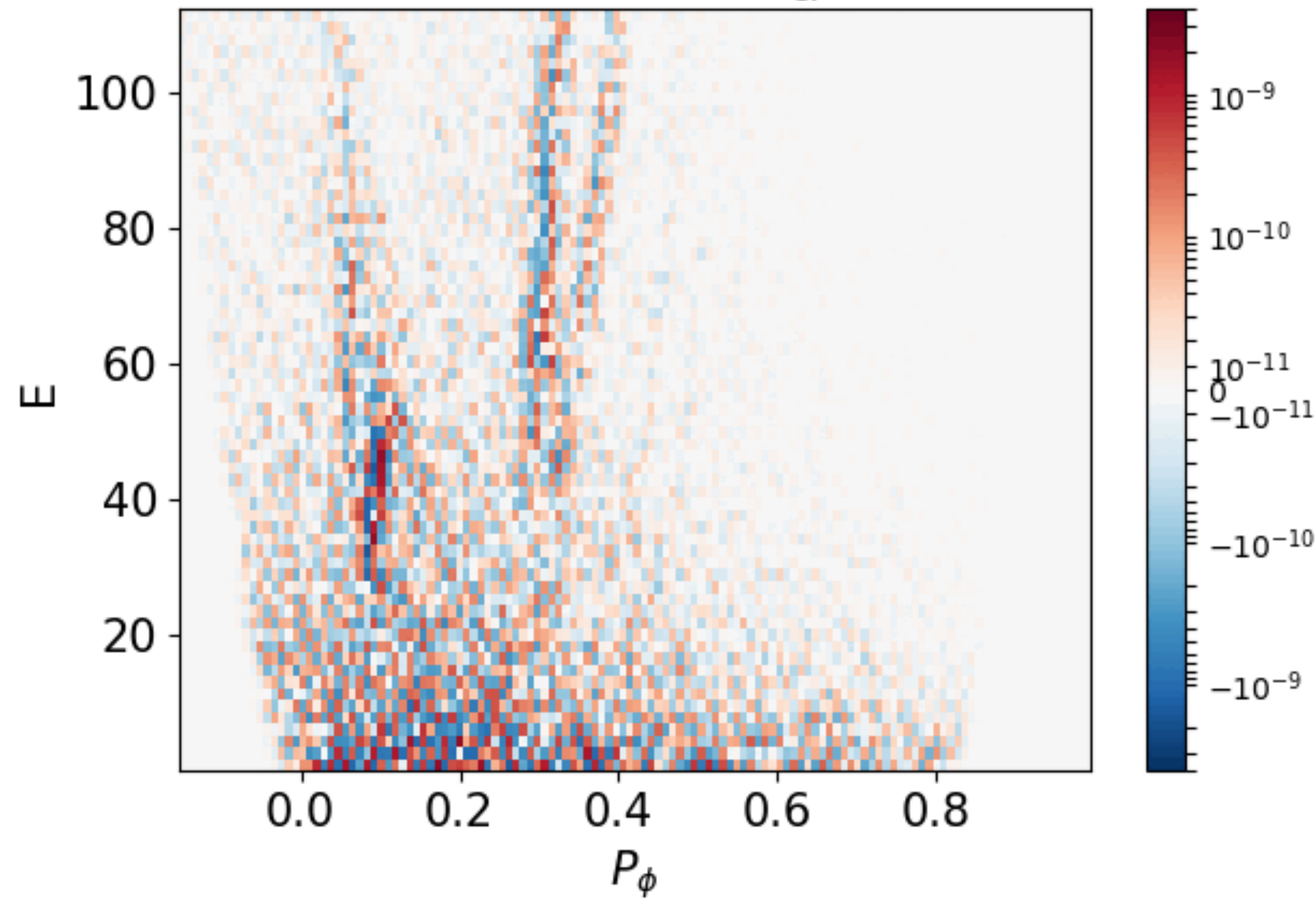
ORB5: n=18: ~2%  
LIGKA: n=18 even: 0.5%  
LIGKA: n=18 odd: 1.0%

**ORB5: isotropic slowing down**

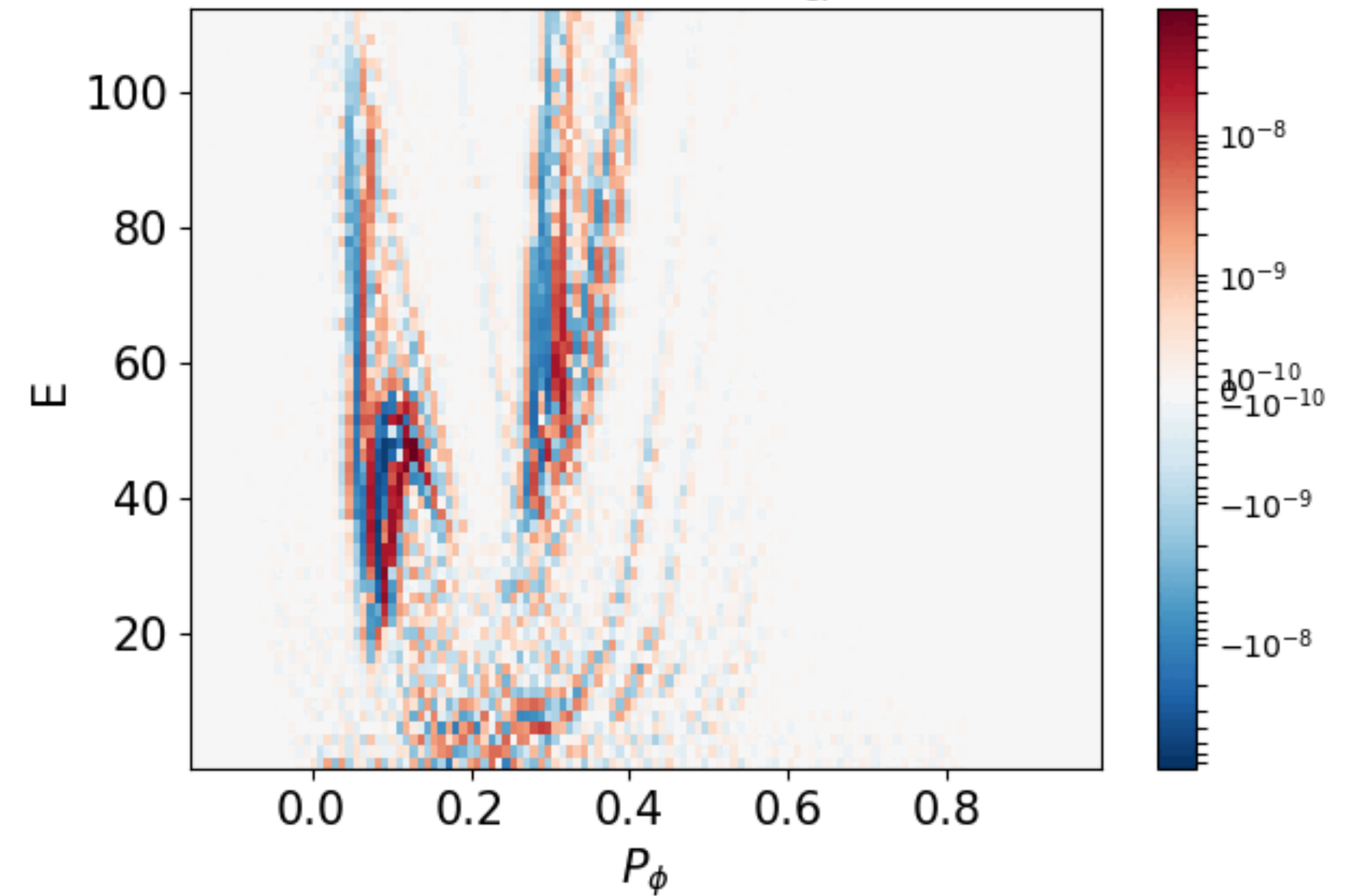
**ATEP/LIGKA: equivalent pressure Maxwellian**



sp=fast;  $t = 120000 \omega_{ci}^{-1}$ ;  $\Lambda = 0.0$



sp=fast;  $t = 237000 \omega_{ci}^{-1}$ ;  $\Lambda = 0.0$



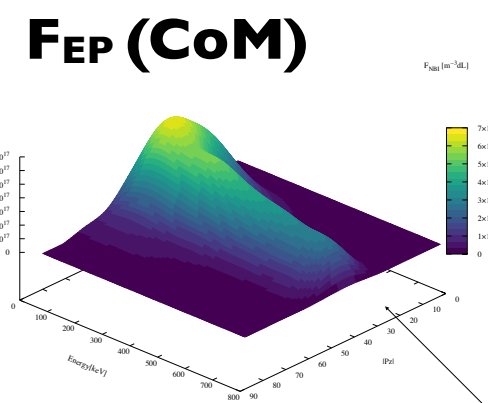
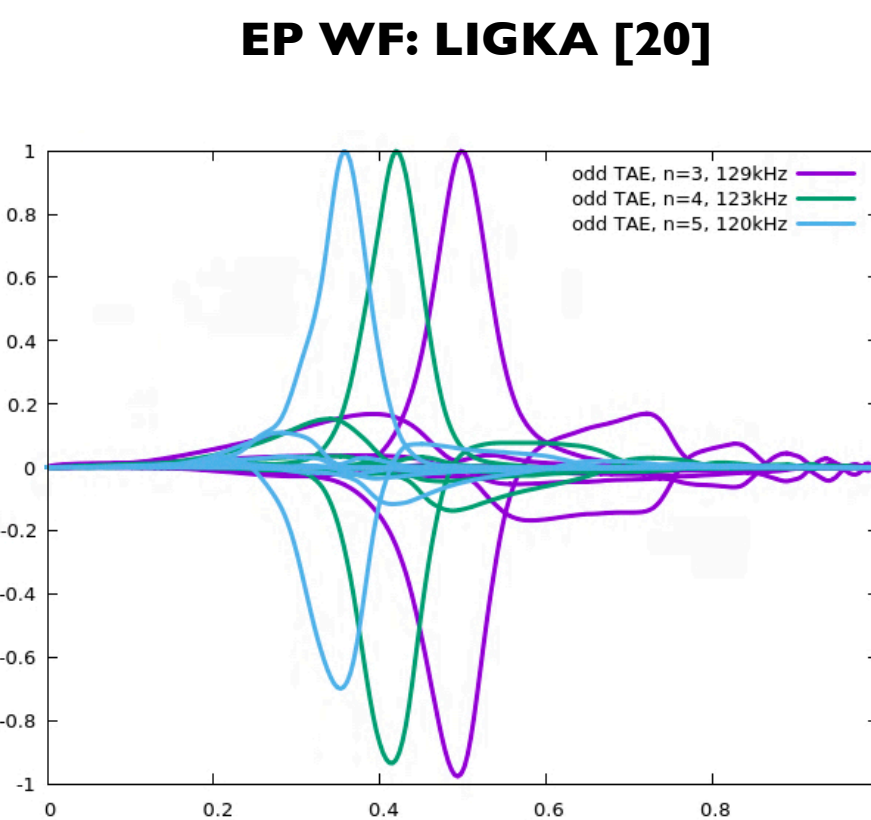
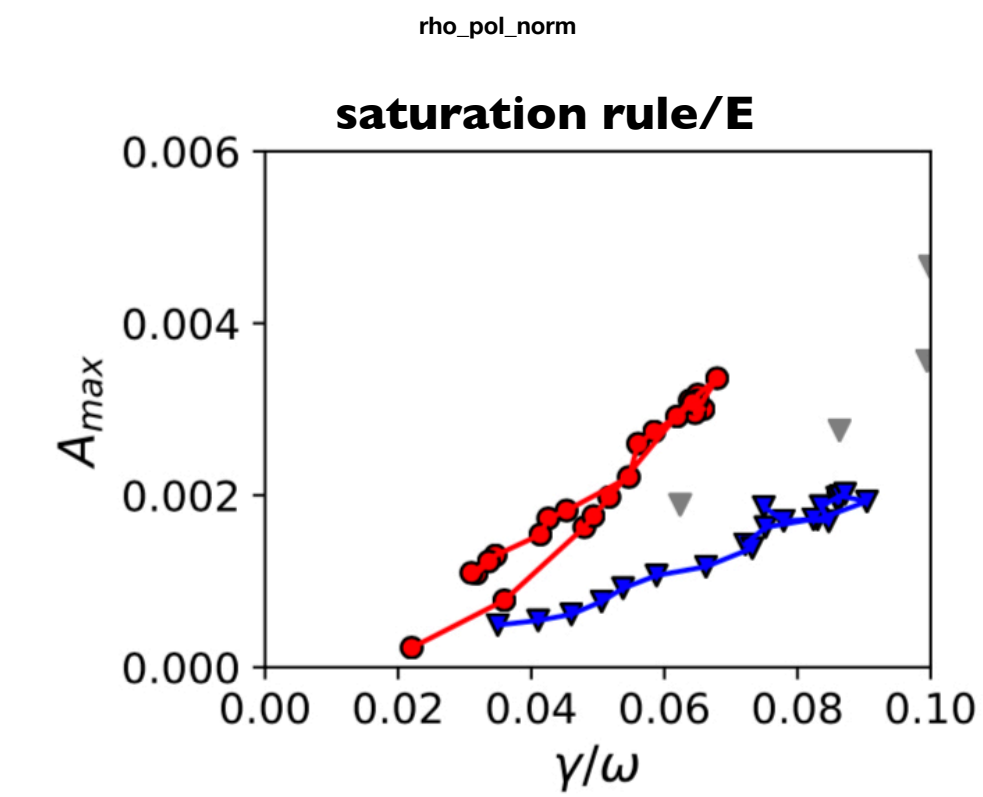
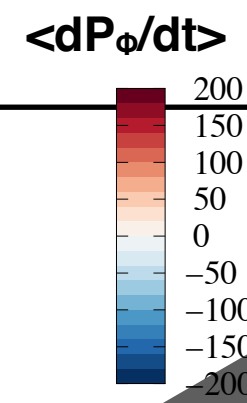
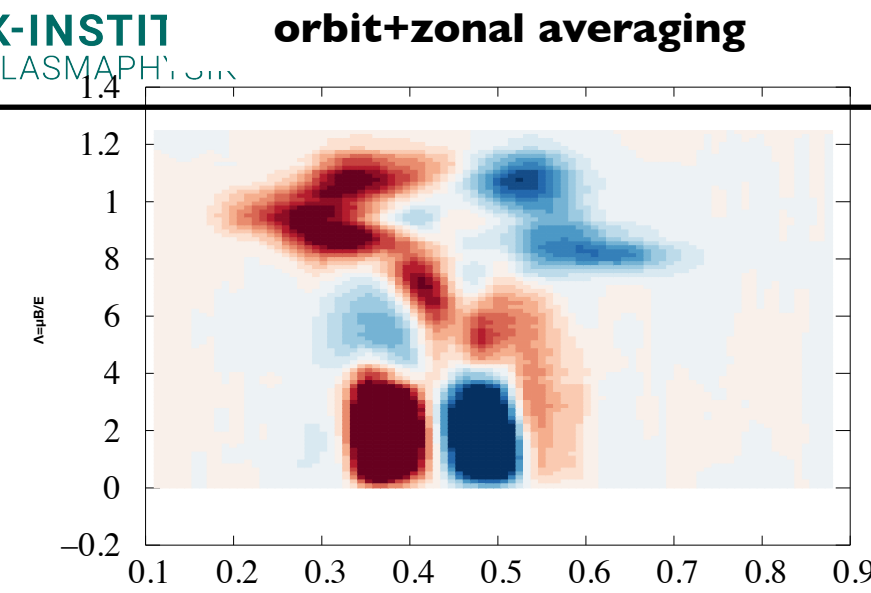
[keV/10]

$E$

radially outwards

isotropic slowing down

# ATEP code: physics and structure



transport code

calculate PSZS

use NL code/model for intensity closure

or kick model

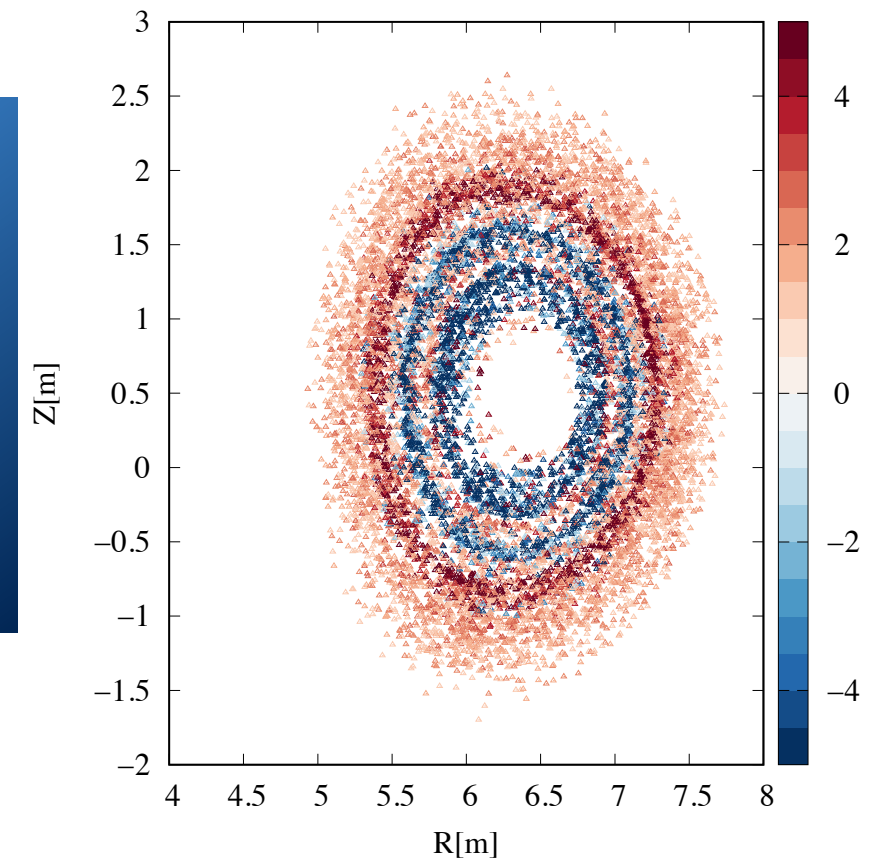
calculate linear mode spectrum

PSZS transport theory [M. Falessi et al, 2017-23]

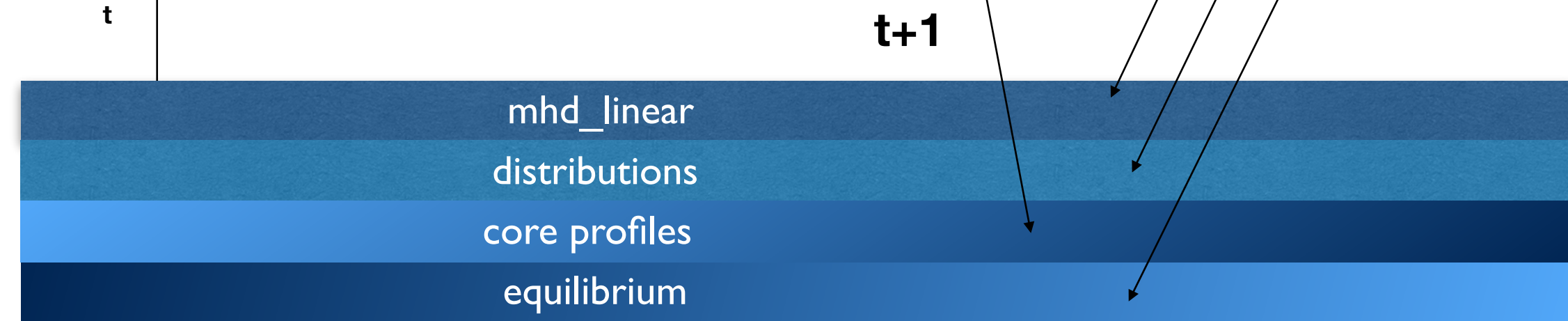
$$\frac{\partial \overline{F_{z0}}}{\partial t} + \frac{1}{\tau_b} \left[ \frac{\partial}{\partial P_\phi} \overline{(\tau_b \delta \dot{P}_\phi \delta F)}_z + \frac{\partial}{\partial \mathcal{E}} \overline{(\tau_b \delta \dot{\mathcal{E}} \delta F)}_z \right]_S = \left( \sum_b C_b^g [F, F_b] + \mathcal{S} \right)_{zS}$$

calculate  $D(r,E)$

advance  $F_{EP}$  and return updated distribution IDS, or its moments

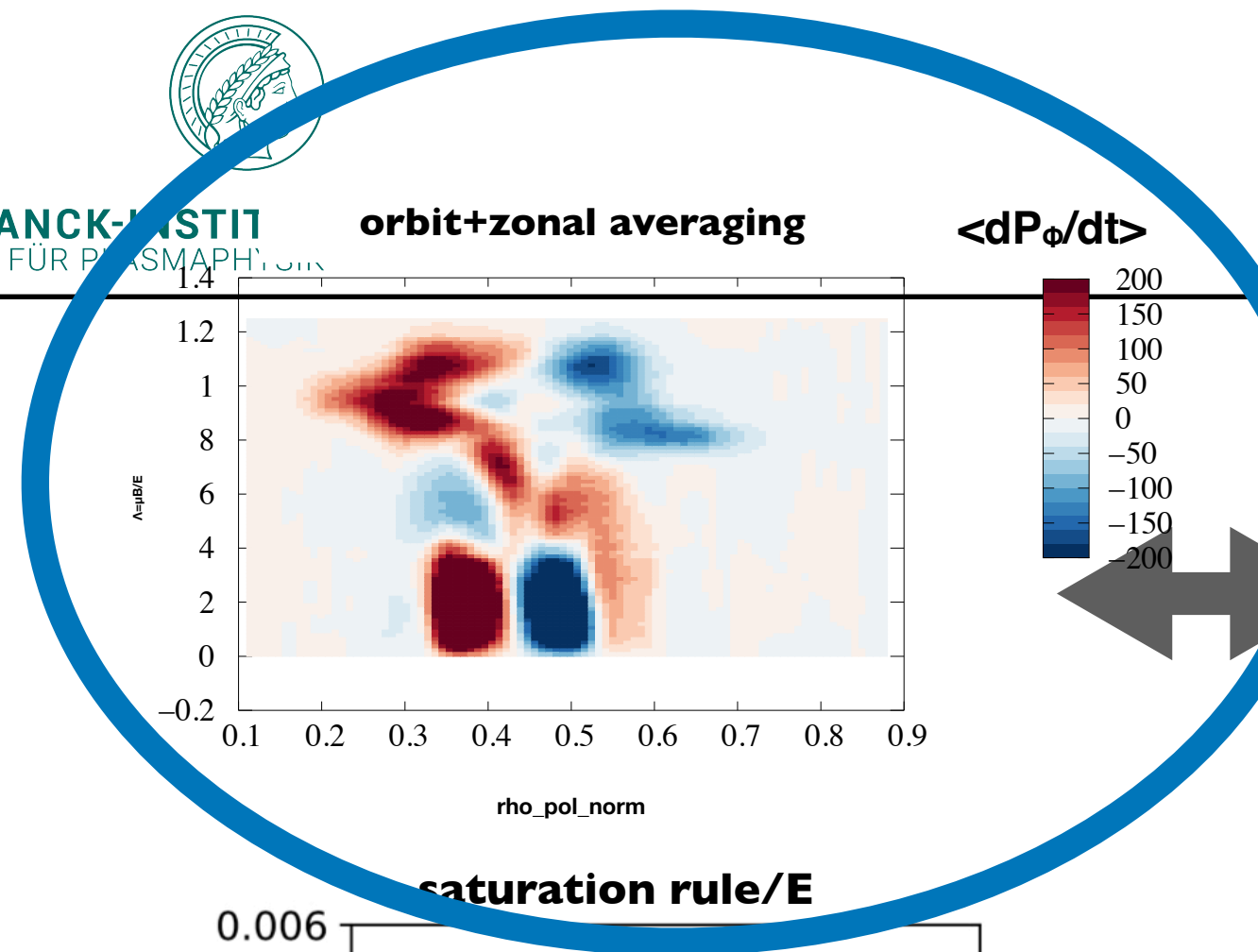


ATEP code [Ph. Lauber, G. Meng, 2022]



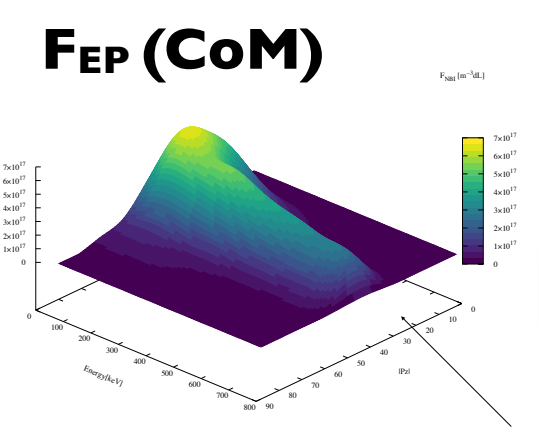
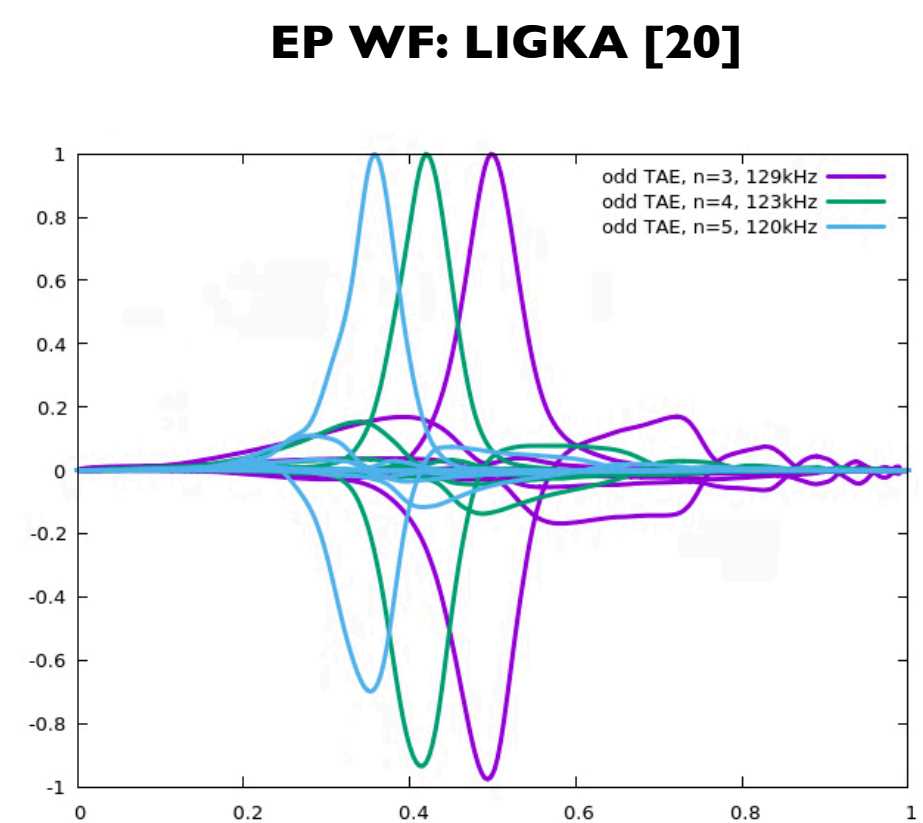
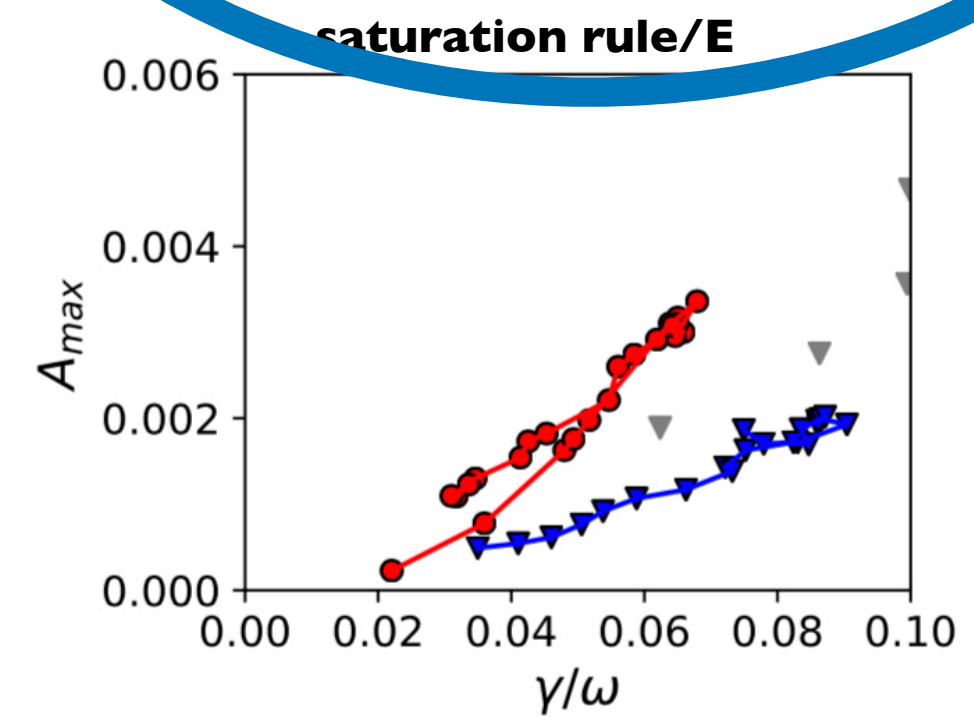
time





in the following:

- use EP-Stability WF to create HAGIS perturbations,
- follow test particles in prescribed perturbations
- 256 radial/ $P_\phi$ , 96 energy, 96 Lambda,
- 5 complete orbits of all test particles will be followed
- zonal average: 8 particles per wave period
- construct  $\langle dP_\phi/dt \rangle_z$  and  $\langle dE/dt \rangle_z$
- calculate PSZS from single TAEs, and combinations of  $n=18,19$  TAEs (3 different modes, with and without EPs)



transport code

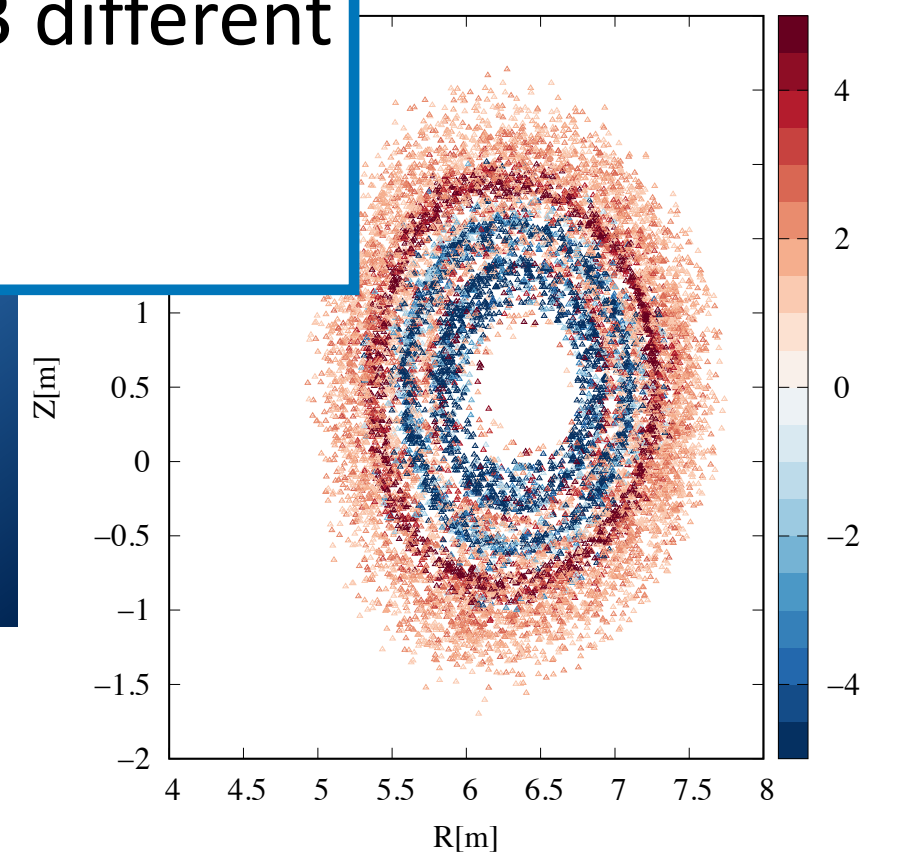
calculate linear mode spectrum

or kick model

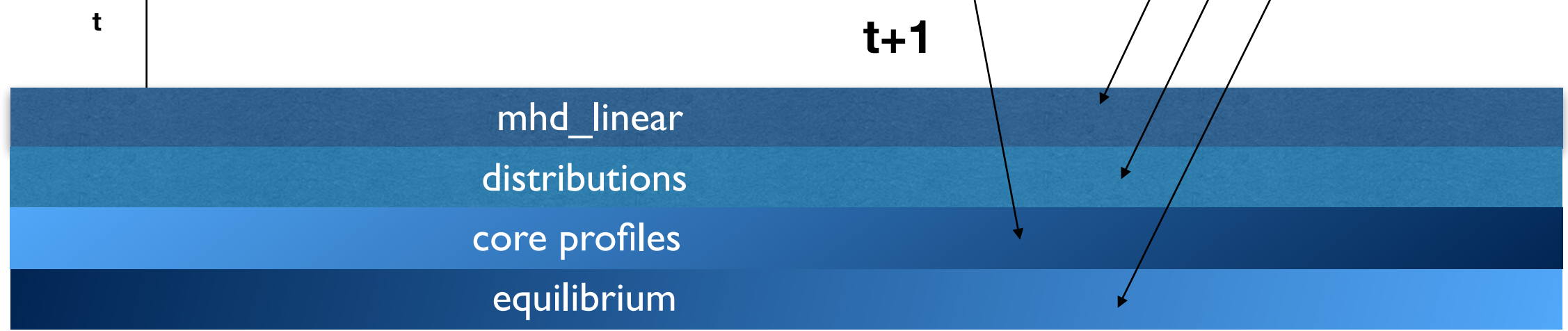
calculate  $D(r,E)$

or

and return updated distribution IDS, or its moments



ATEP code [Ph. Lauber, G. Meng, 2022]





$\Lambda = \mu B/E = 0.0$

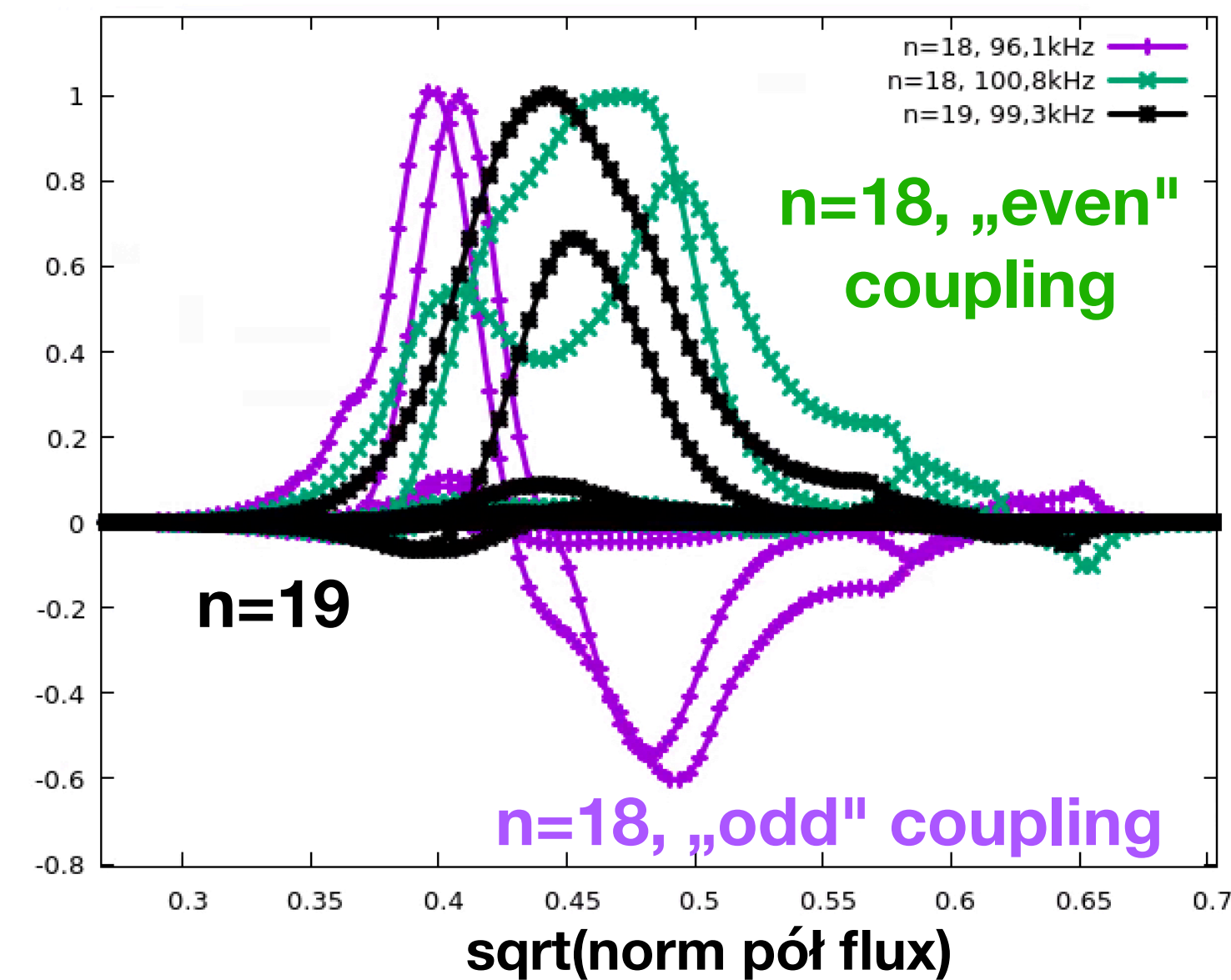
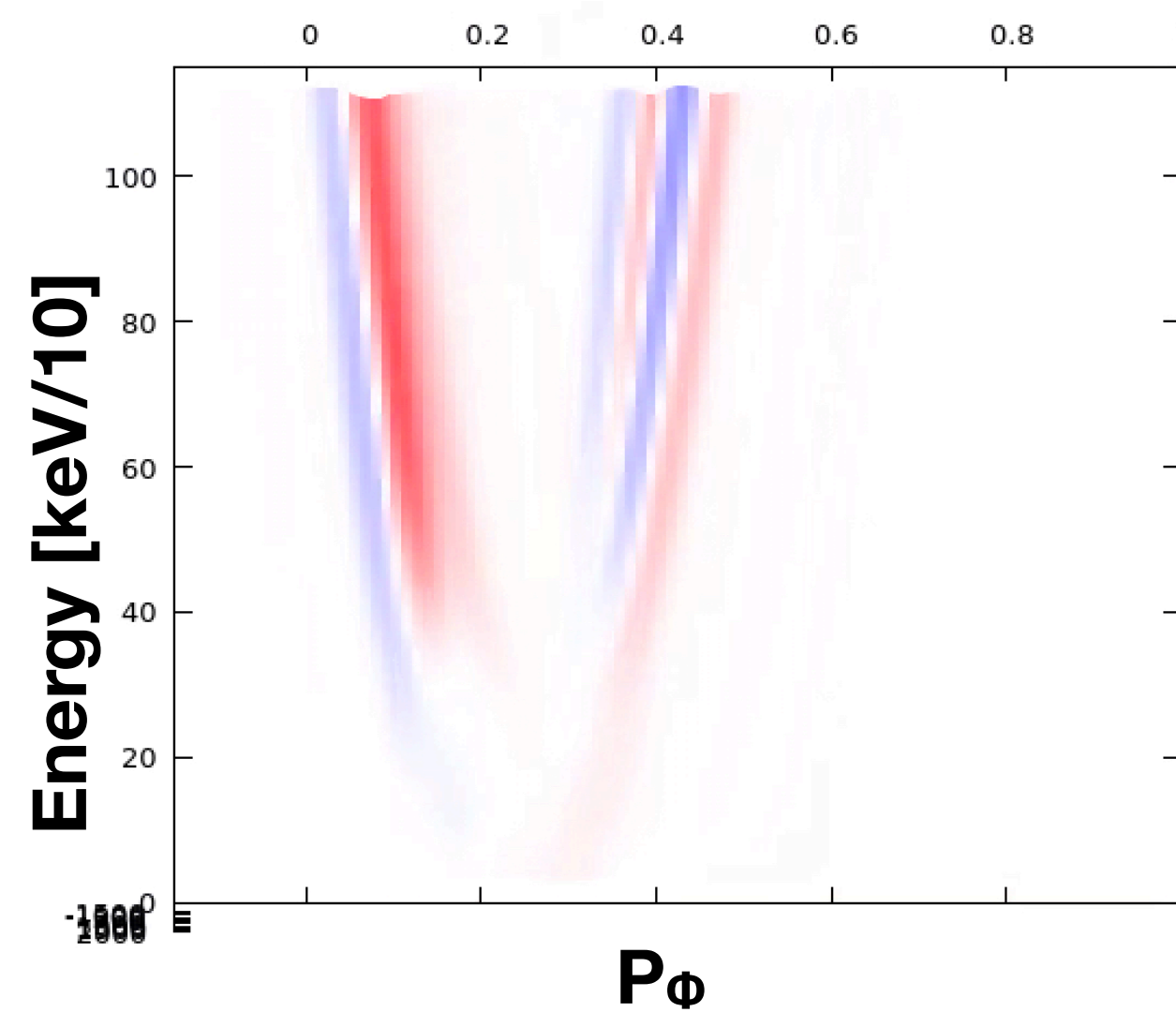
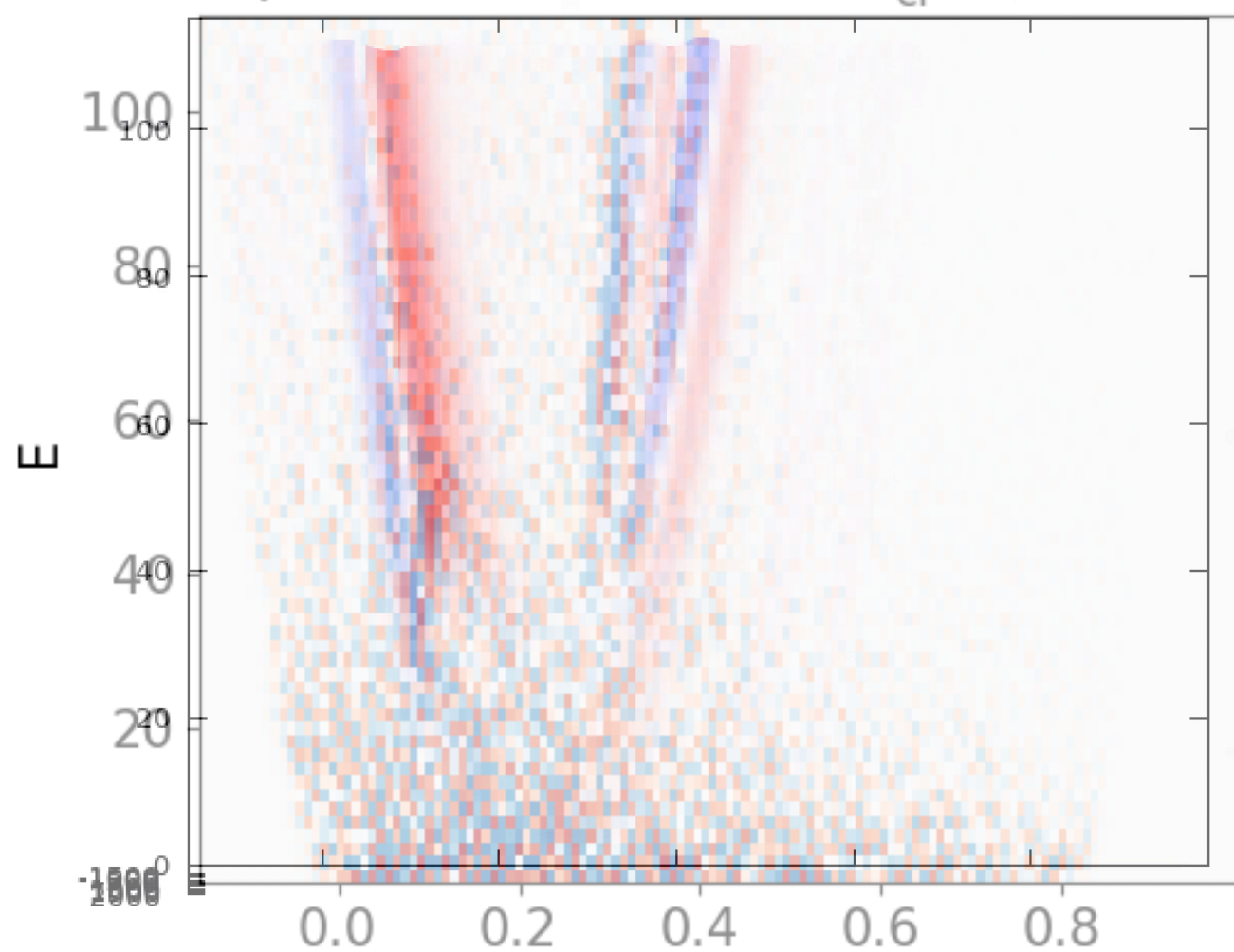
only n=19

no EPs - mode structures



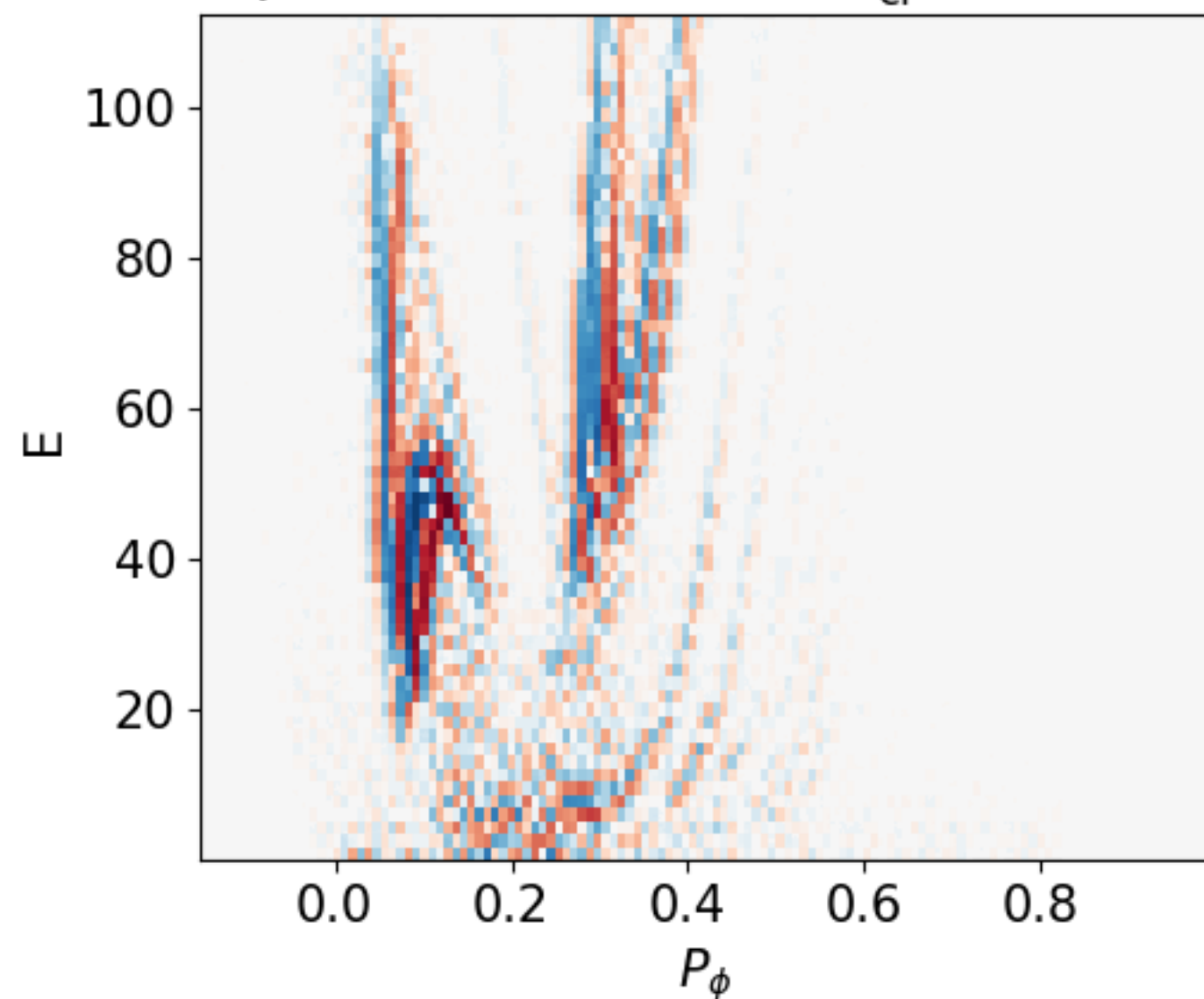
### ORB5 linear - n=19 dominant

sp=fast;  $t = 120000 \omega_{ci}^{-1}$ ;  $\Lambda = 0.0$

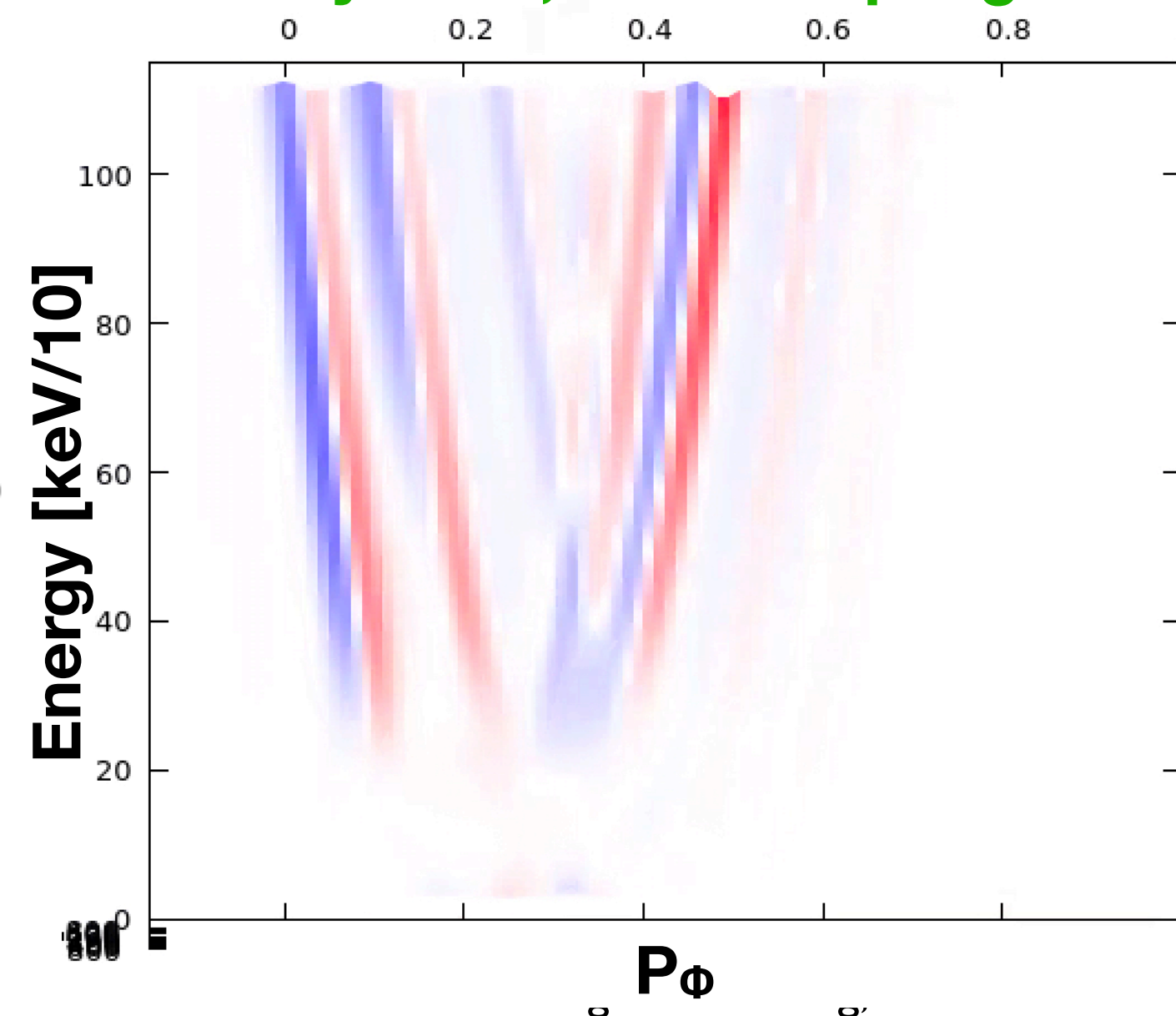


### ORB5 non-linear: n=19 + 18

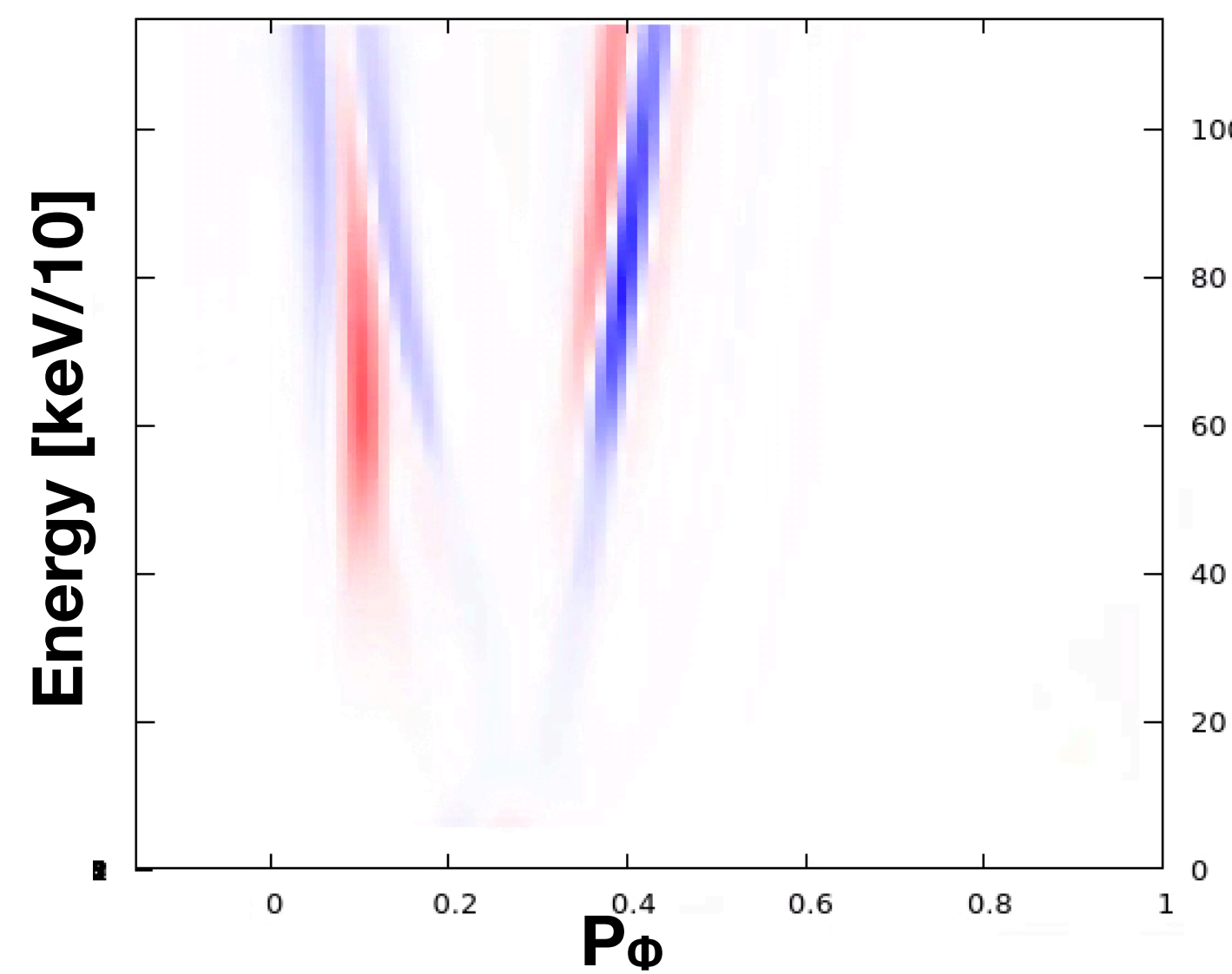
sp=fast;  $t = 237000 \omega_{ci}^{-1}$ ;  $\Lambda = 0.0$



only n=18, even coupling



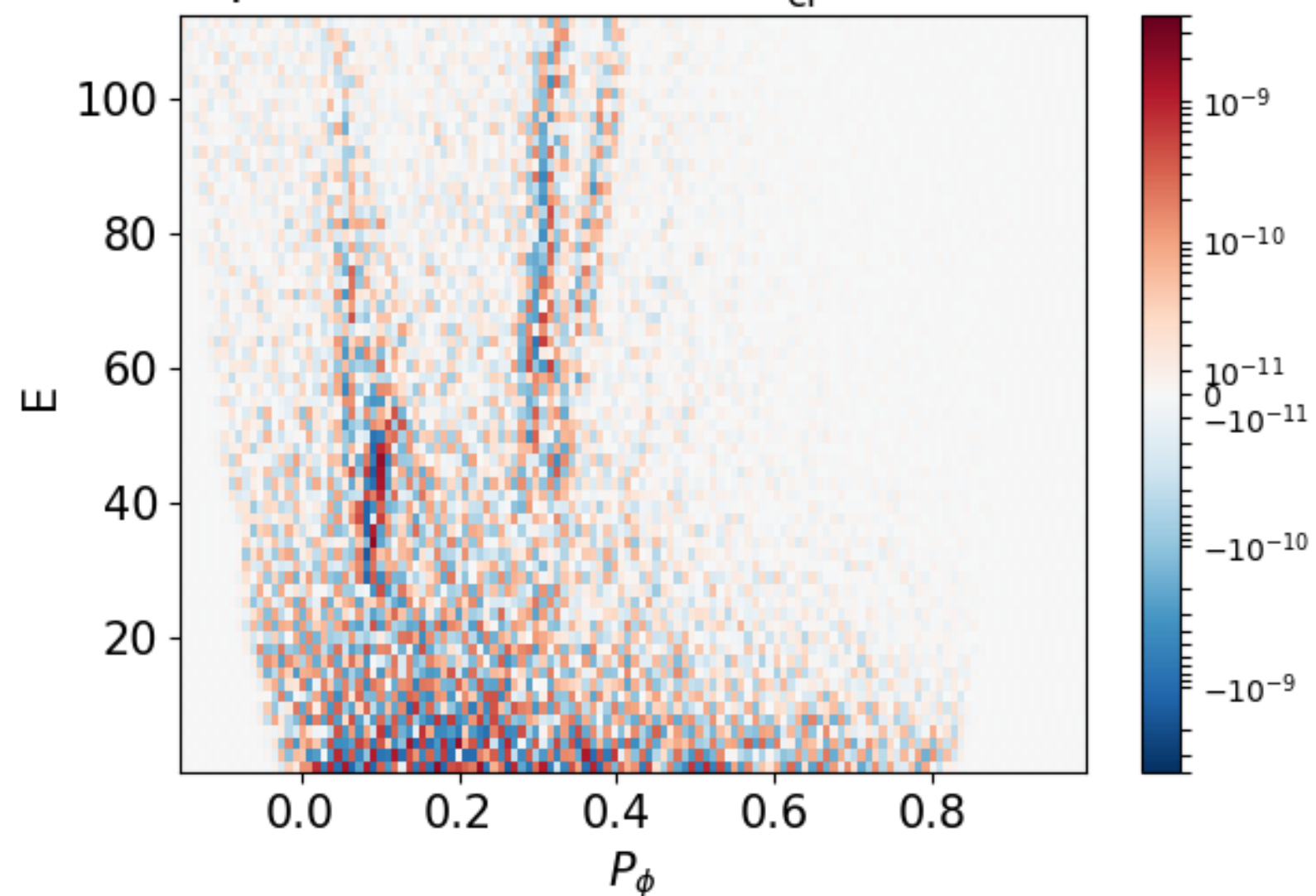
only n=18, odd coupling





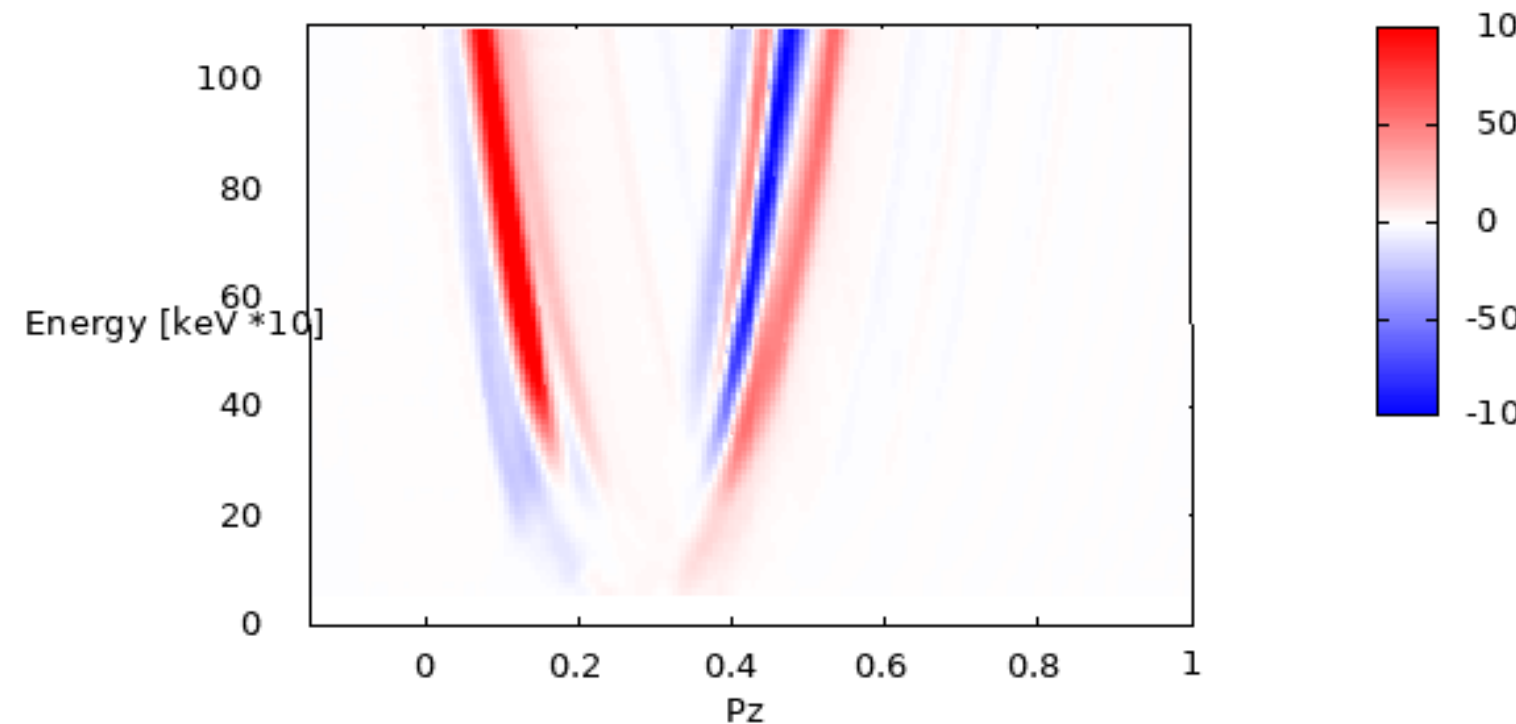
# with EPs $\Lambda = \mu B / E = 0.0$

sp=fast;  $t = 120000 \omega_{ci}^{-1}$ ;  $\Lambda = 0.0$



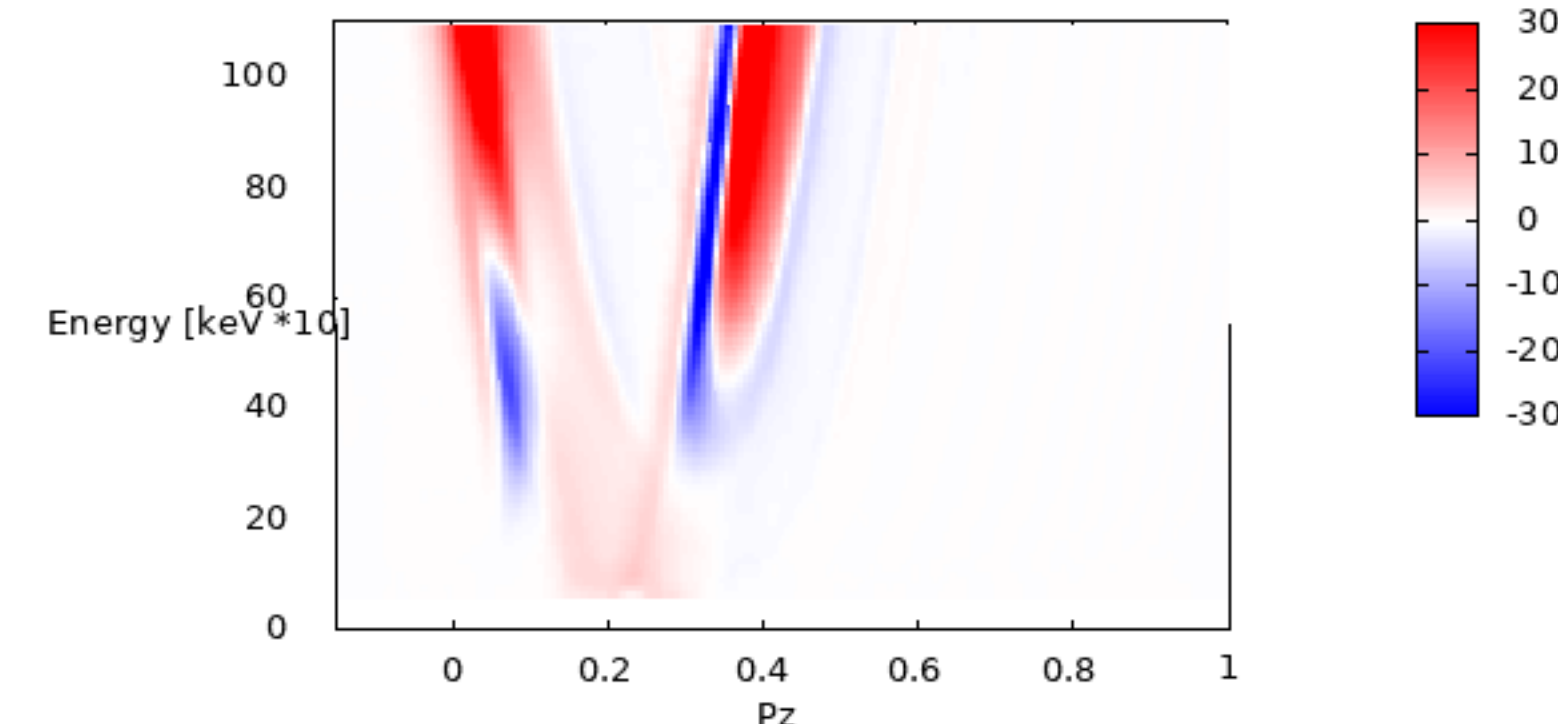
dPz (Pz,E), Lamda=0

only n=19

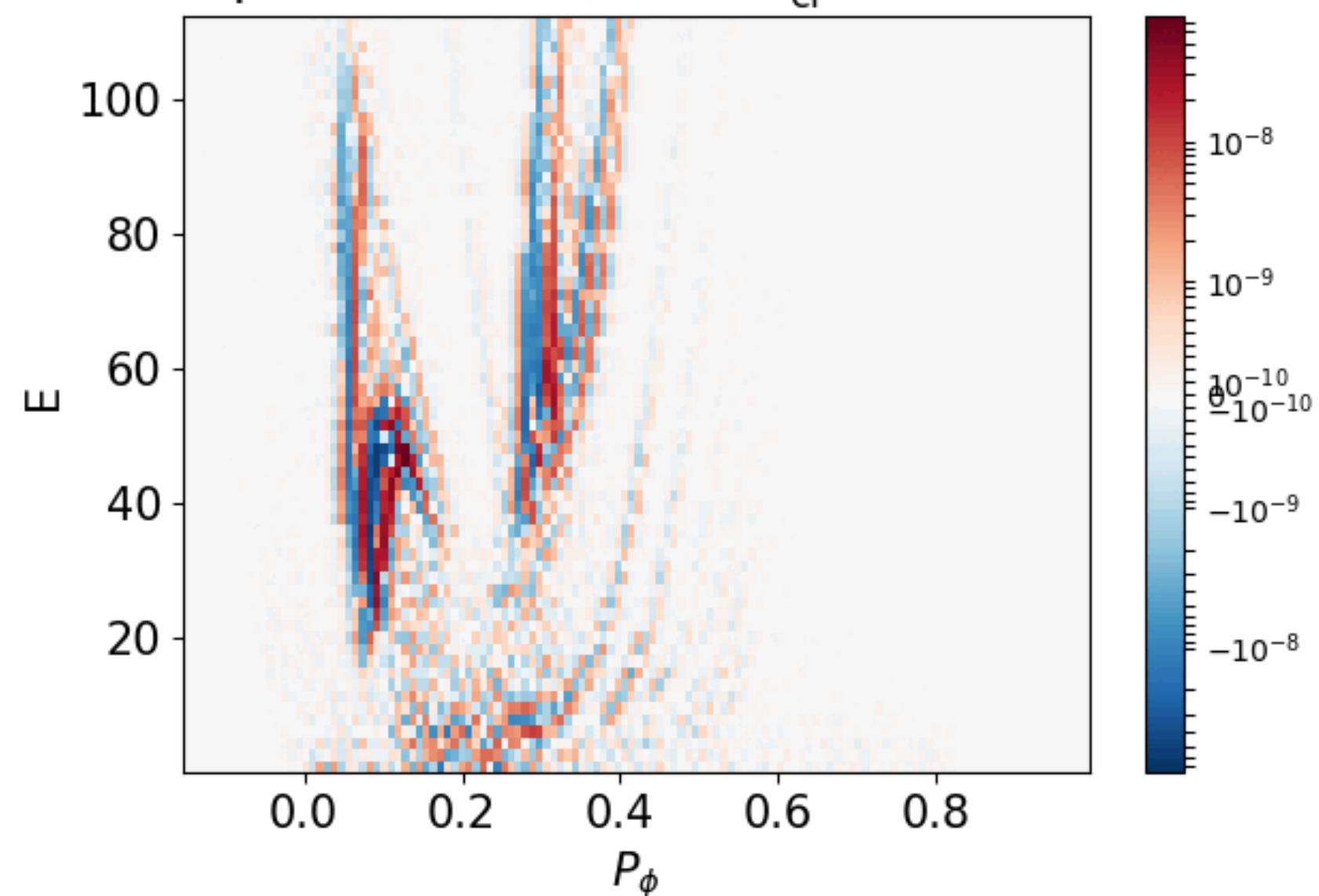


dPz (Pz,E), Lamda=0

only n=18, odd TAE

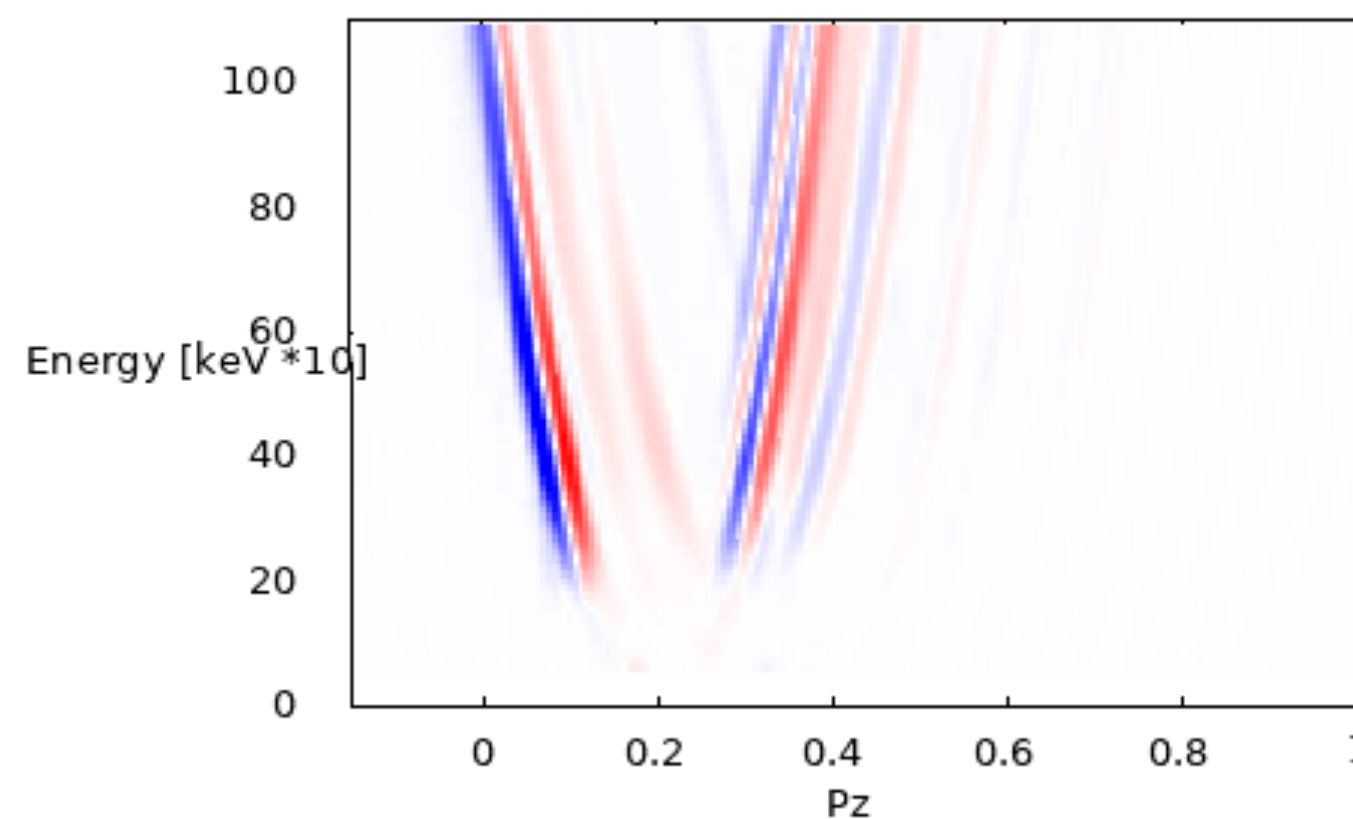


sp=fast;  $t = 237000 \omega_{ci}^{-1}$ ;  $\Lambda = 0.0$



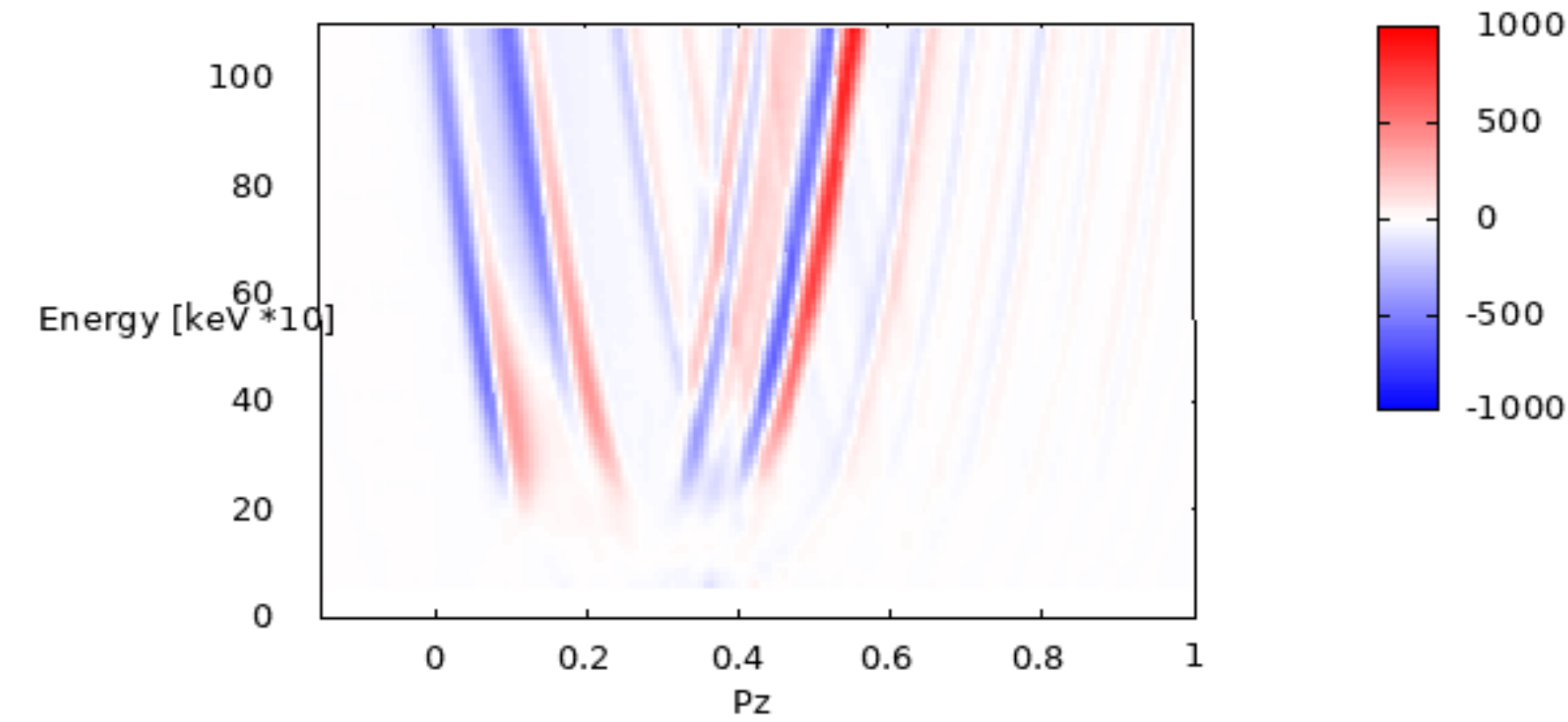
dPz (Pz,E),

only n=18, even, inner



dPz (Pz,E), Lamda=0

only n=18, even, outer

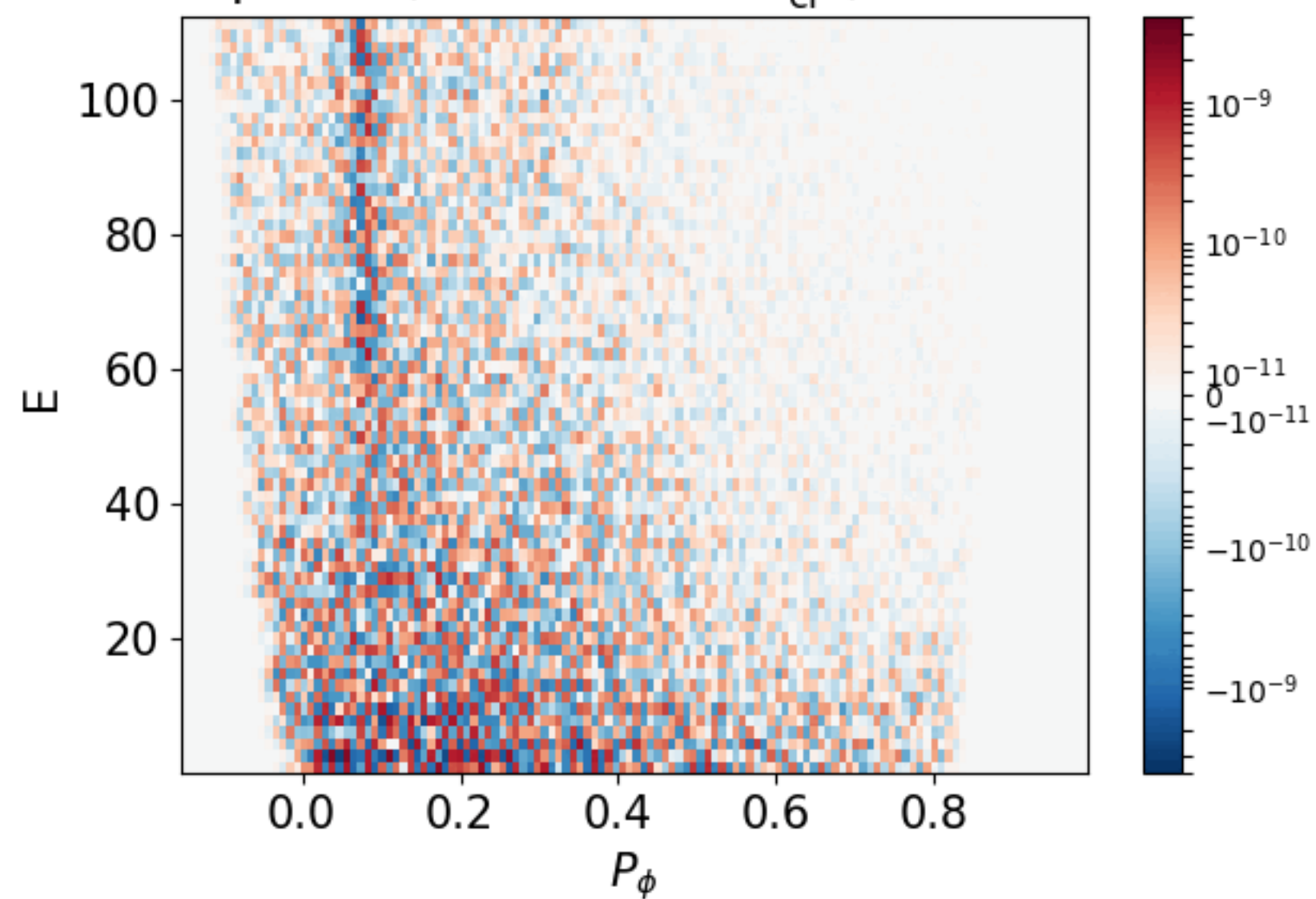






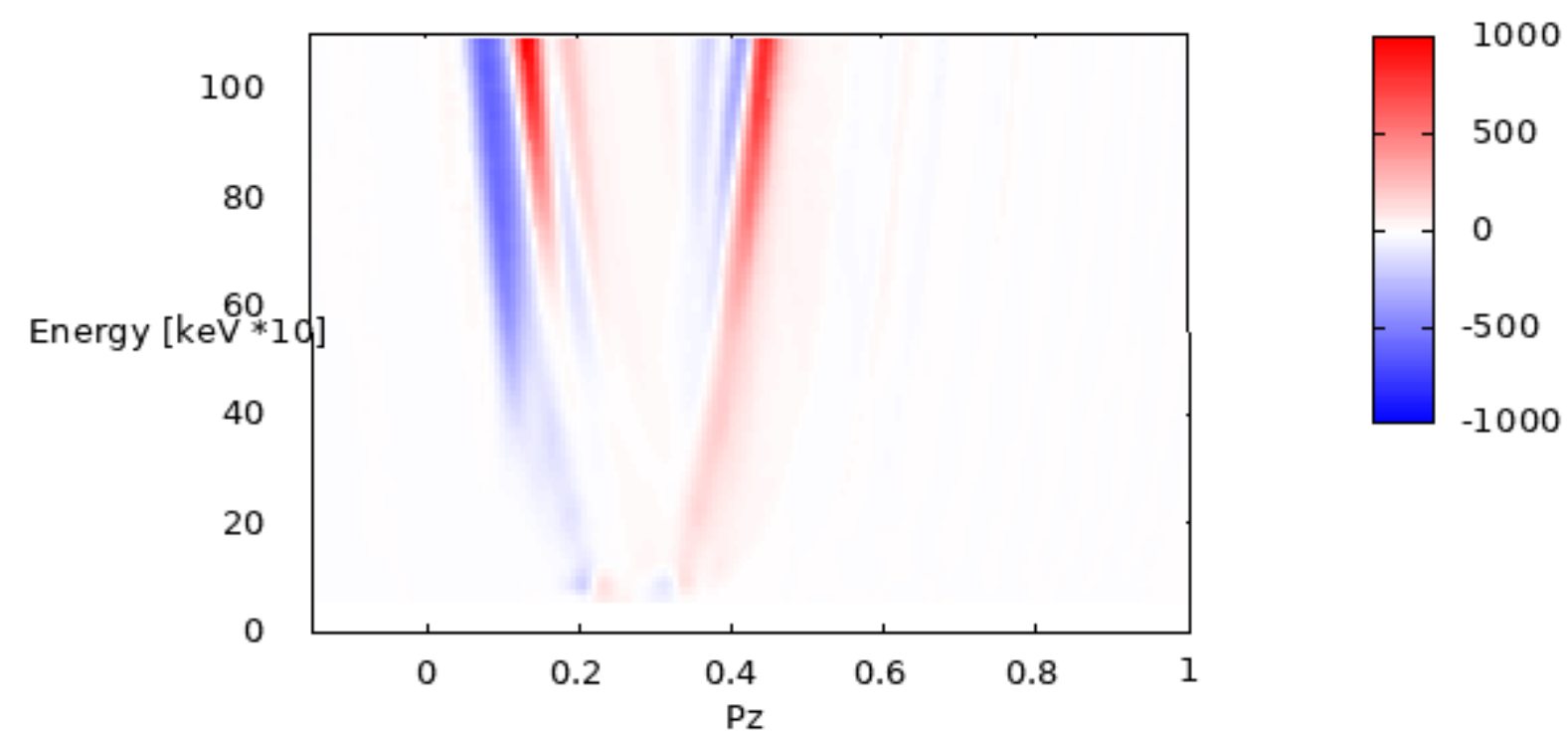
# with EPs $\Lambda = \mu B / E = 0.5$

sp=fast;  $t = 120000 \omega_{ci}^{-1}$ ;  $\Lambda = 0.5$



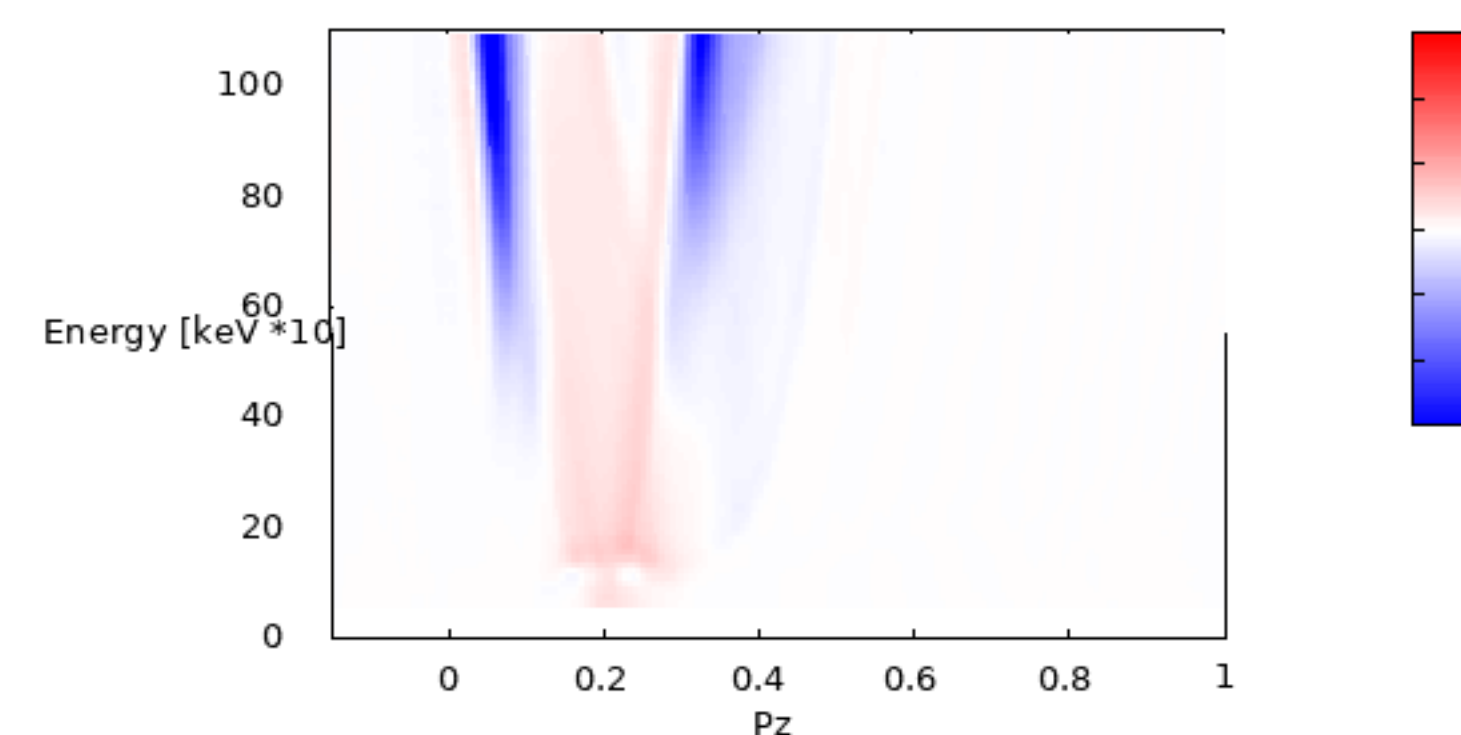
only n=19

dPz (Pz,E), Lamda=504

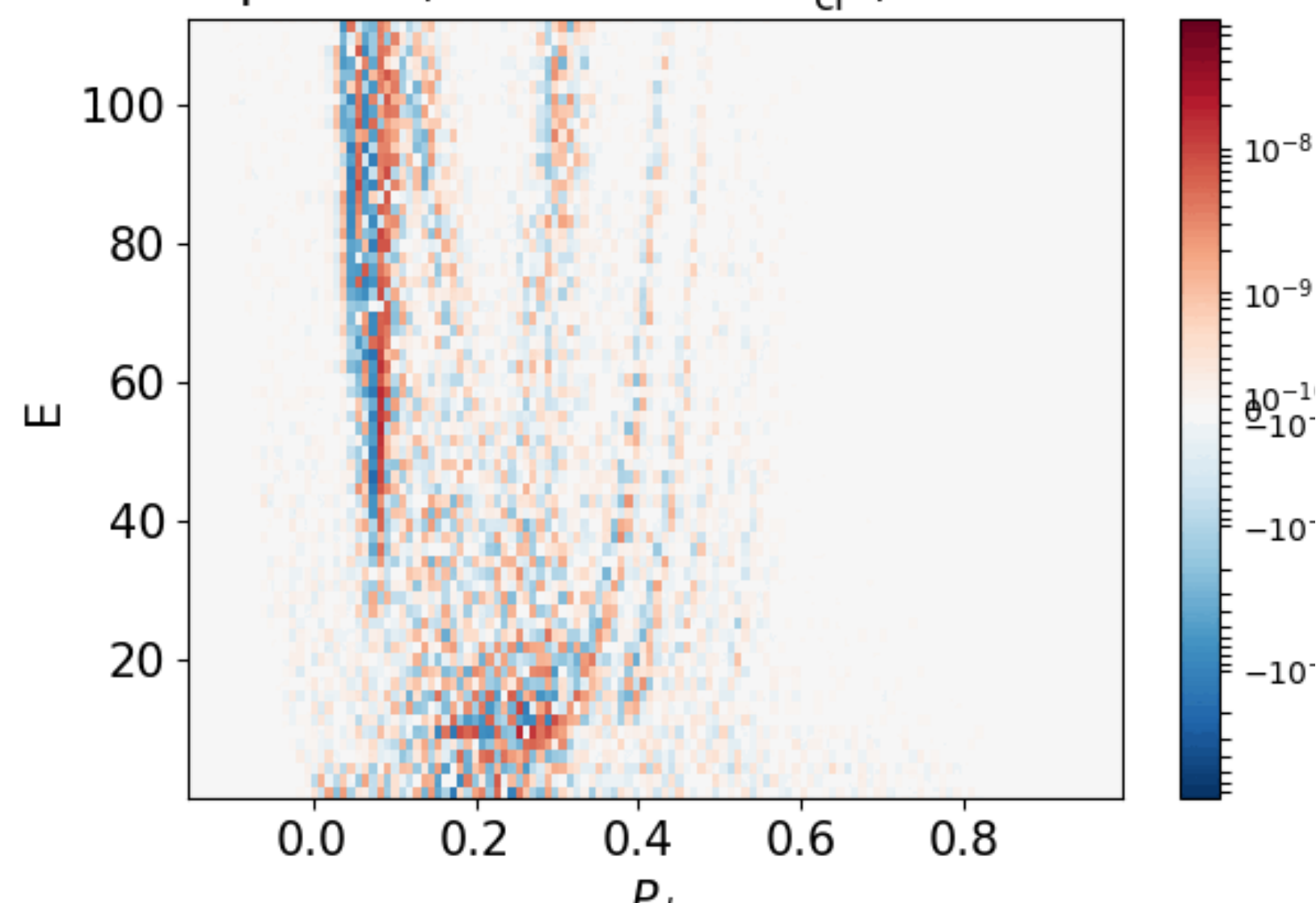


only n=18, odd TAE

dPz (Pz,E), Lamda=504

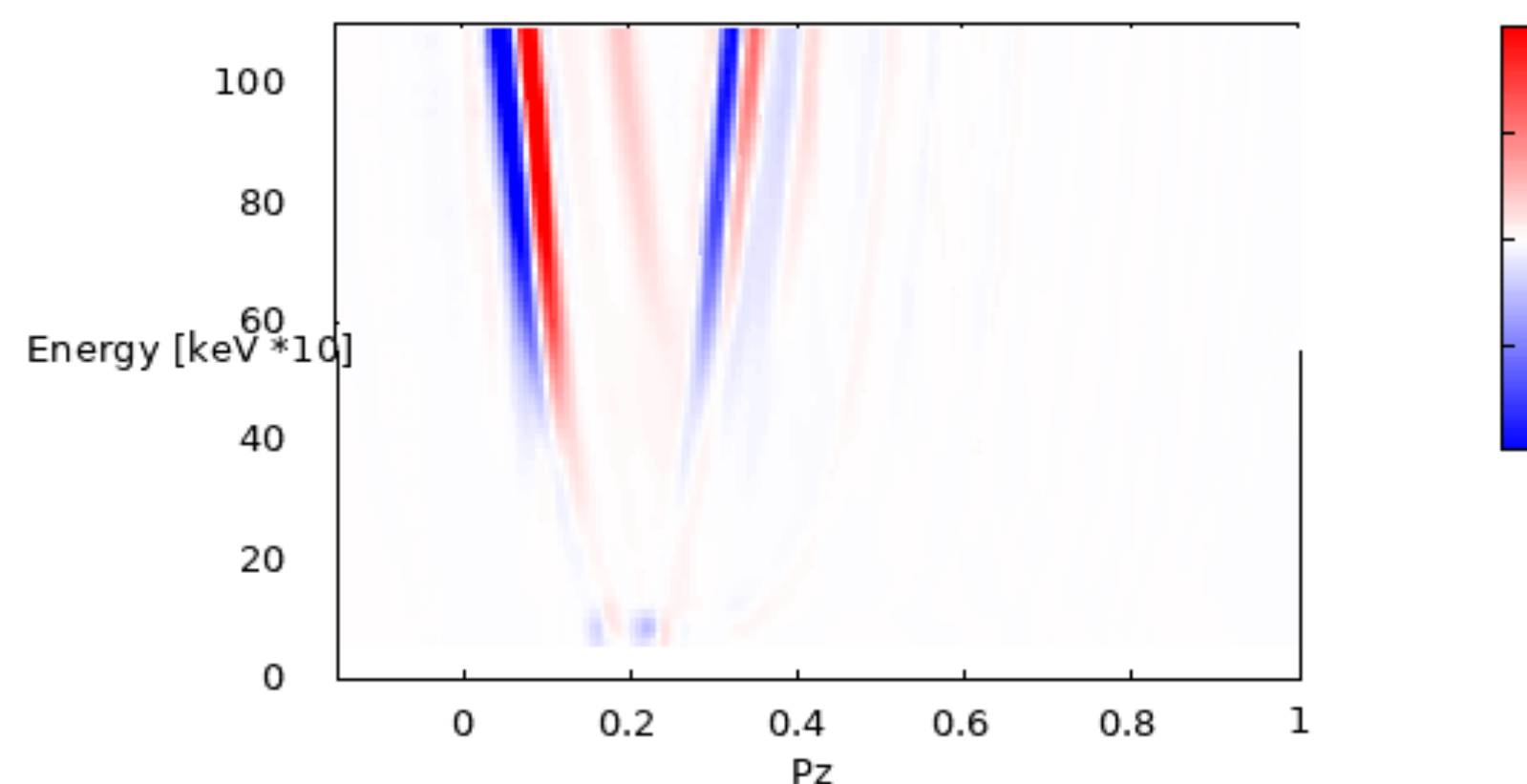


sp=fast;  $t = 237000 \omega_{ci}^{-1}$ ;  $\Lambda = 0.5$

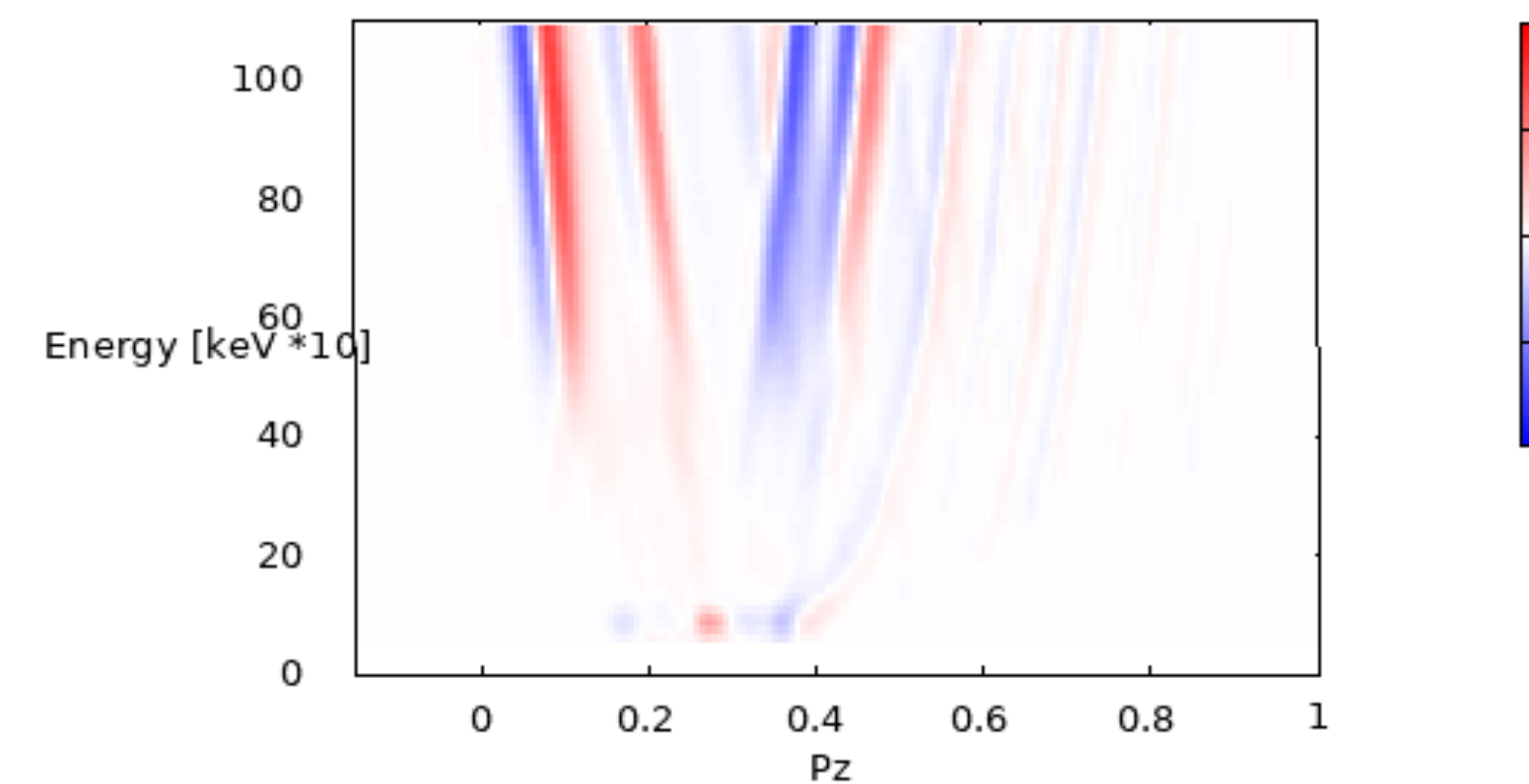


only n=18, even, inner

dPz (Pz,E), Lamda=504

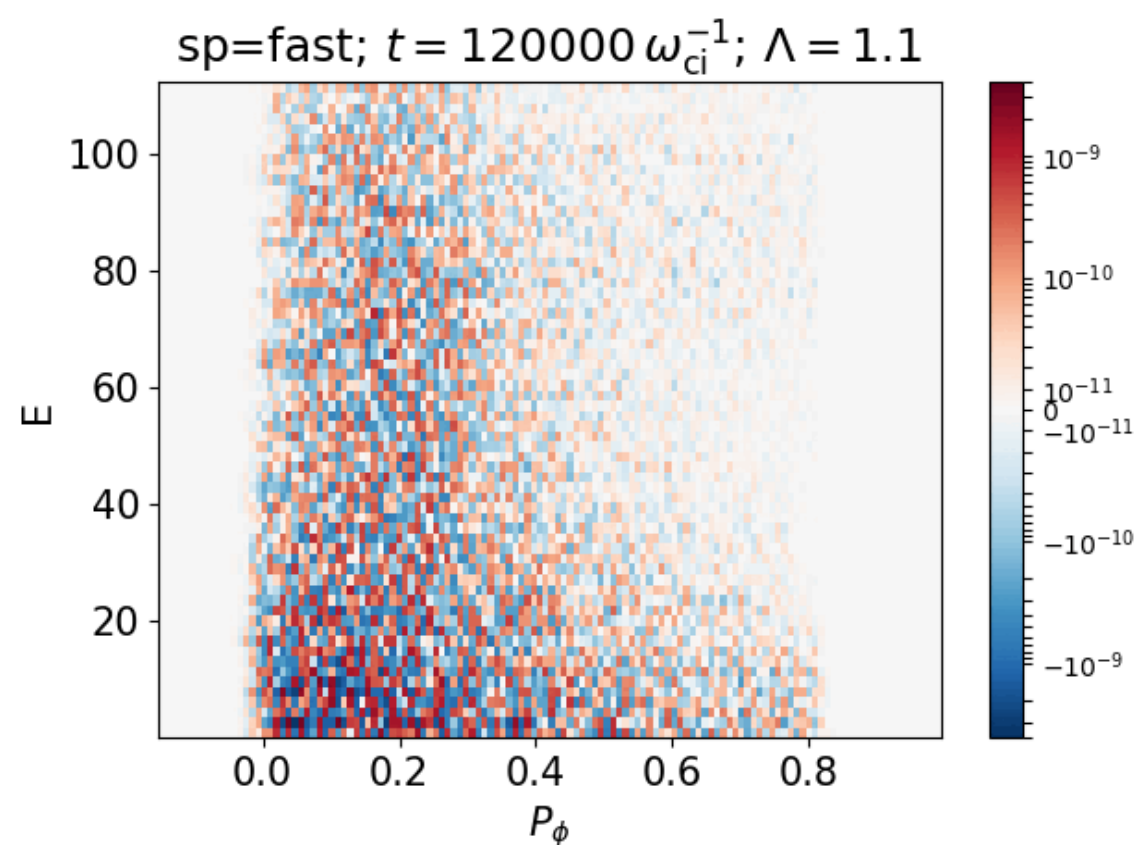


only n=18, even, outer

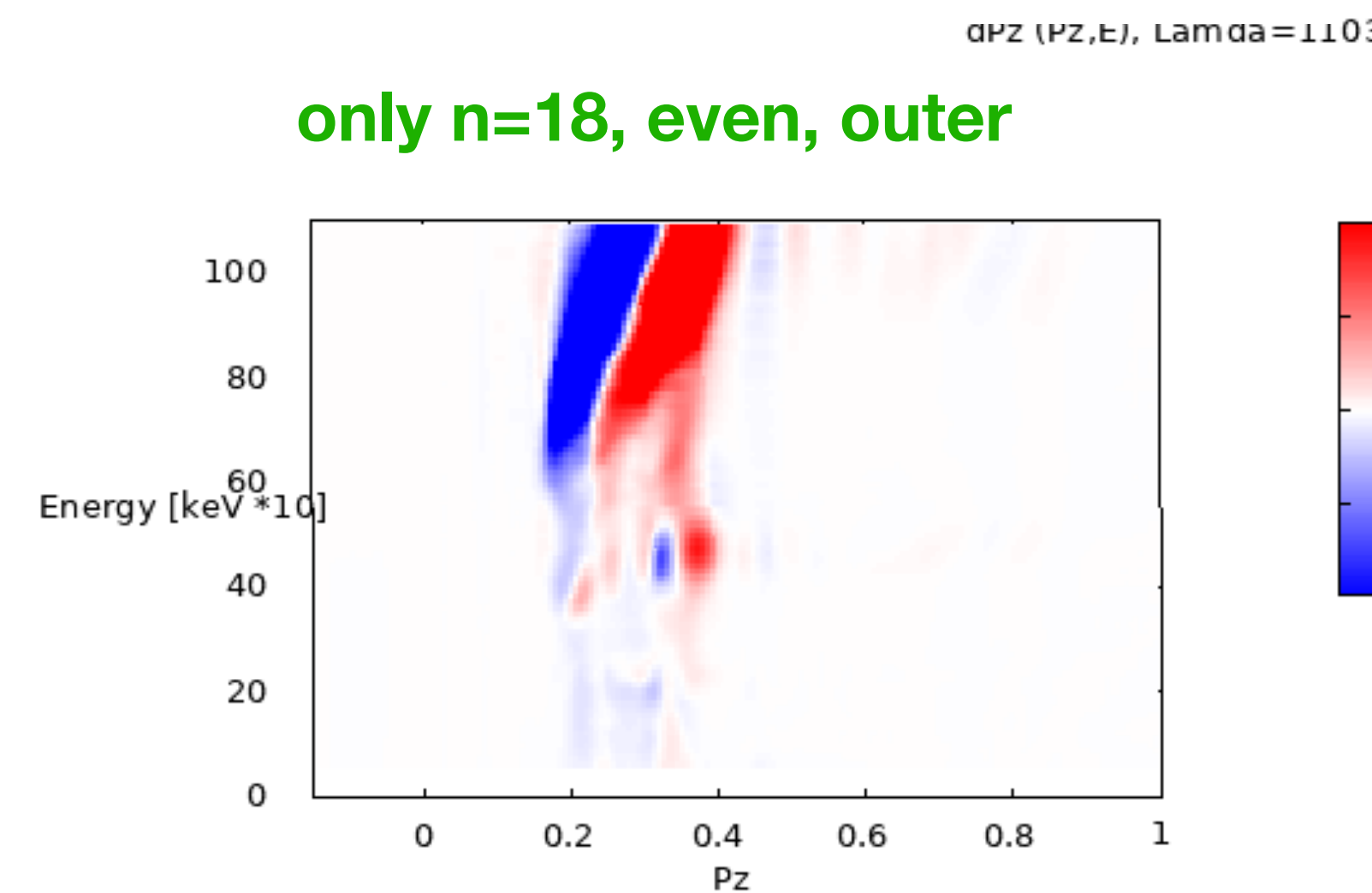
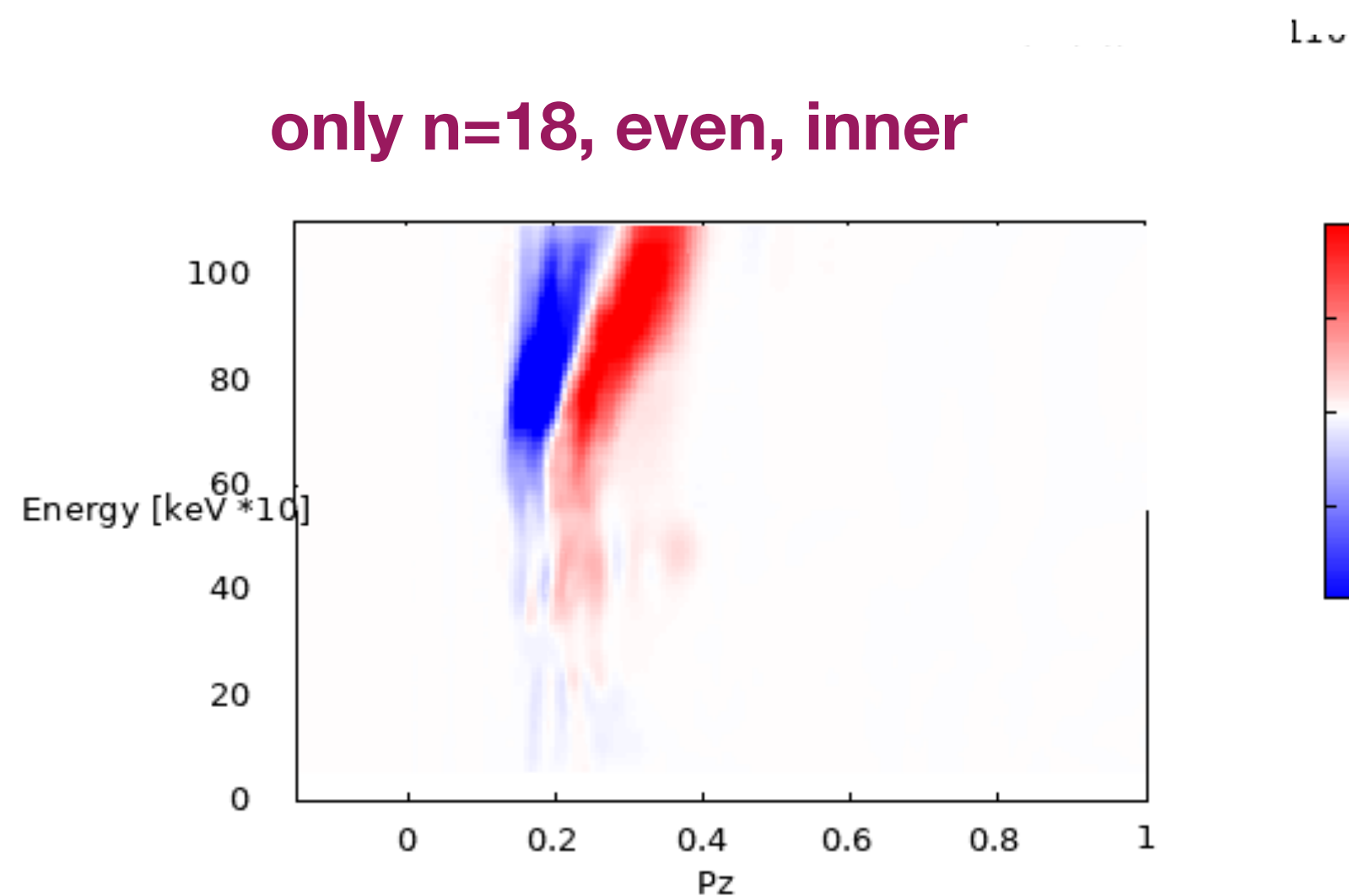
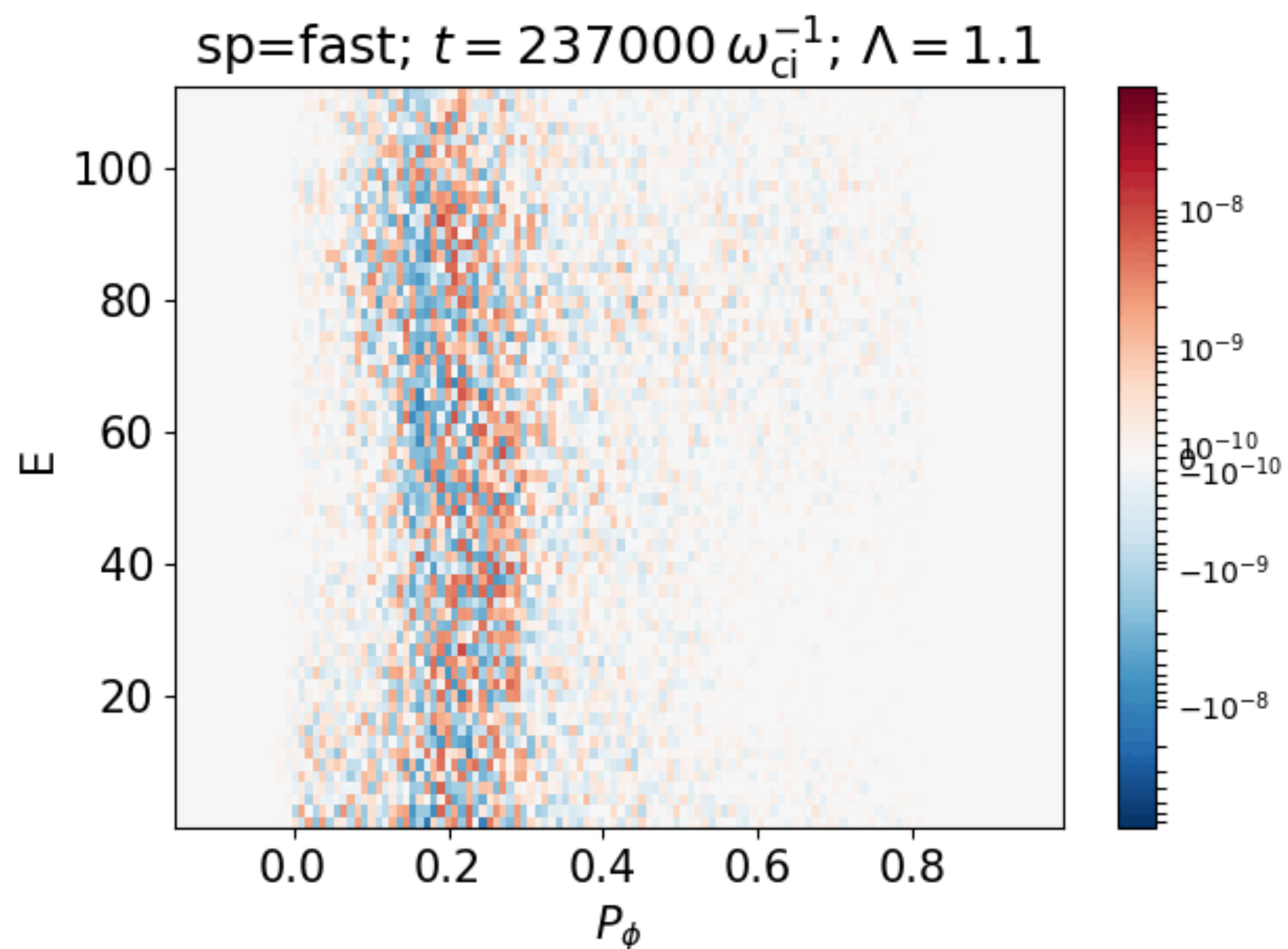
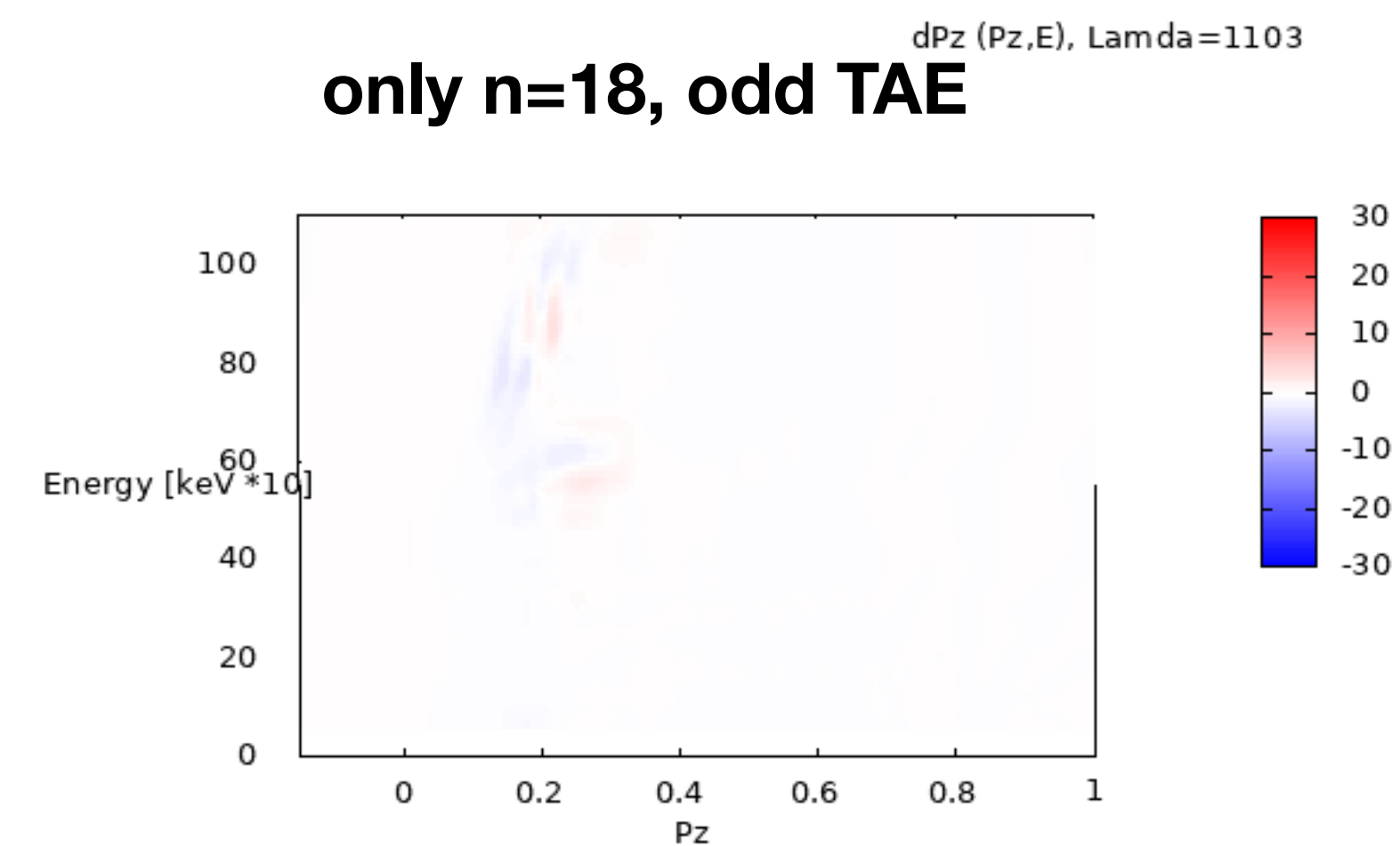
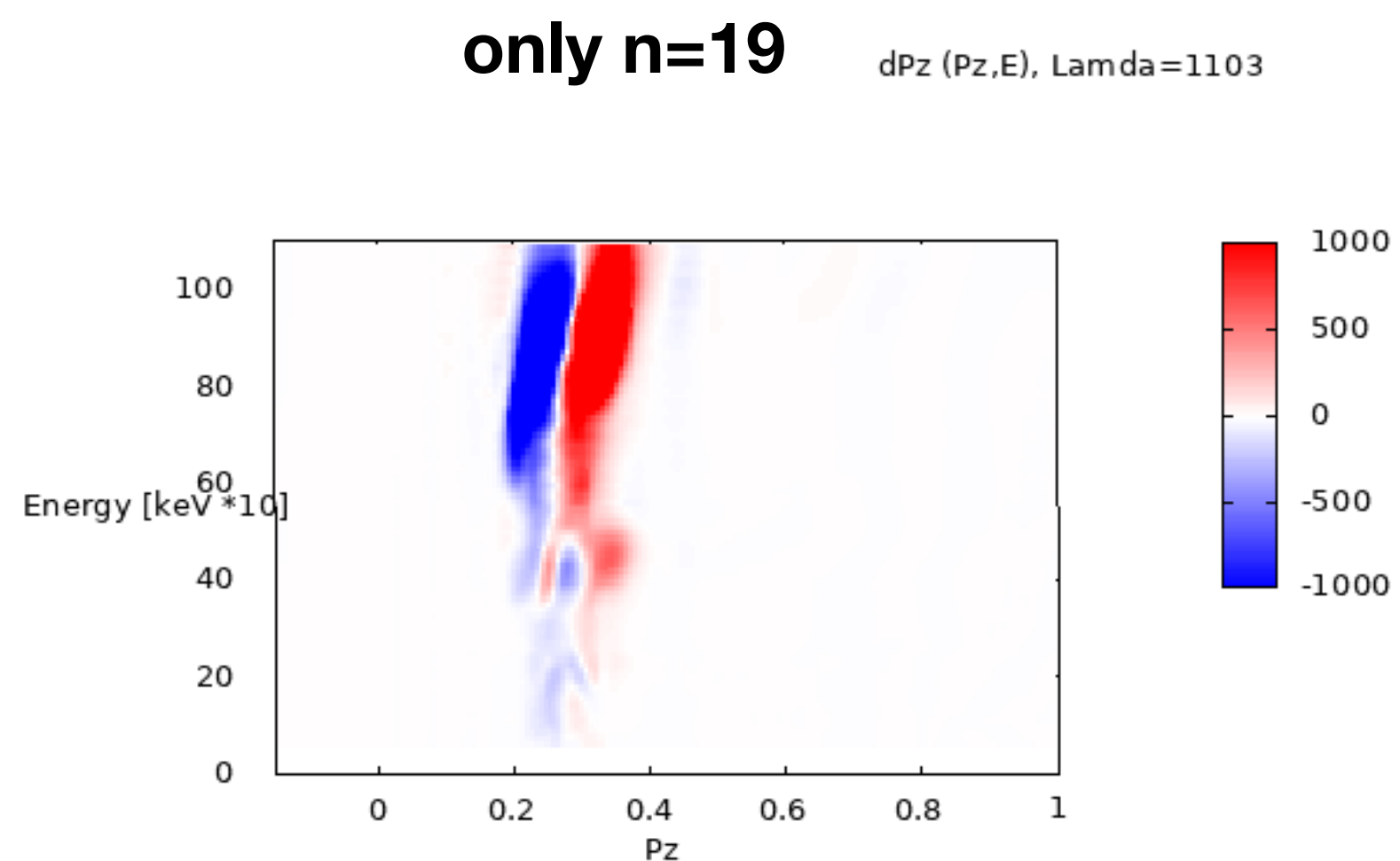




# with EPs $\Lambda = \mu B / E = 1.1$



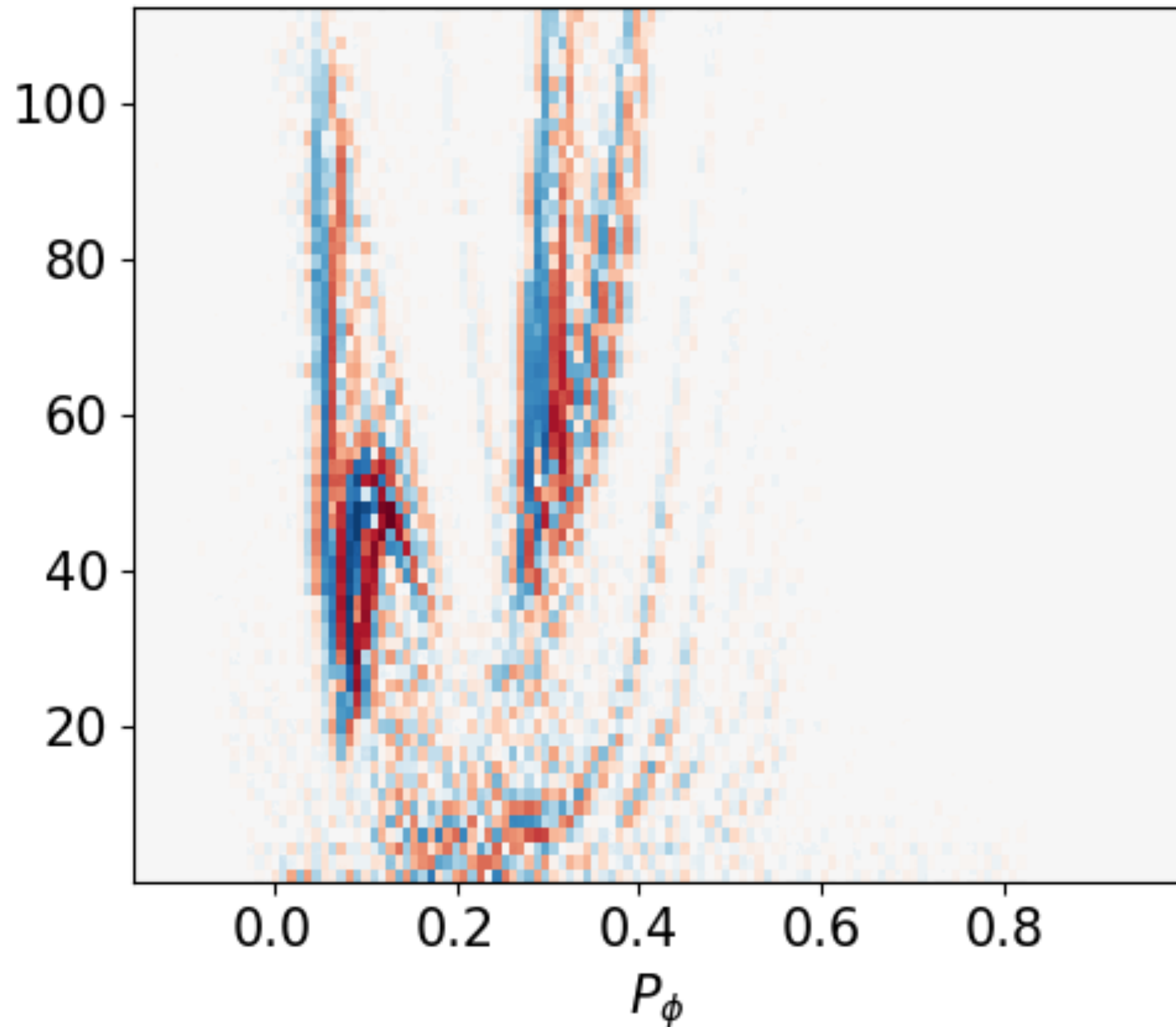
**note that local aspect ratio is  $\sim 10$ ,  
very few trapped particles**



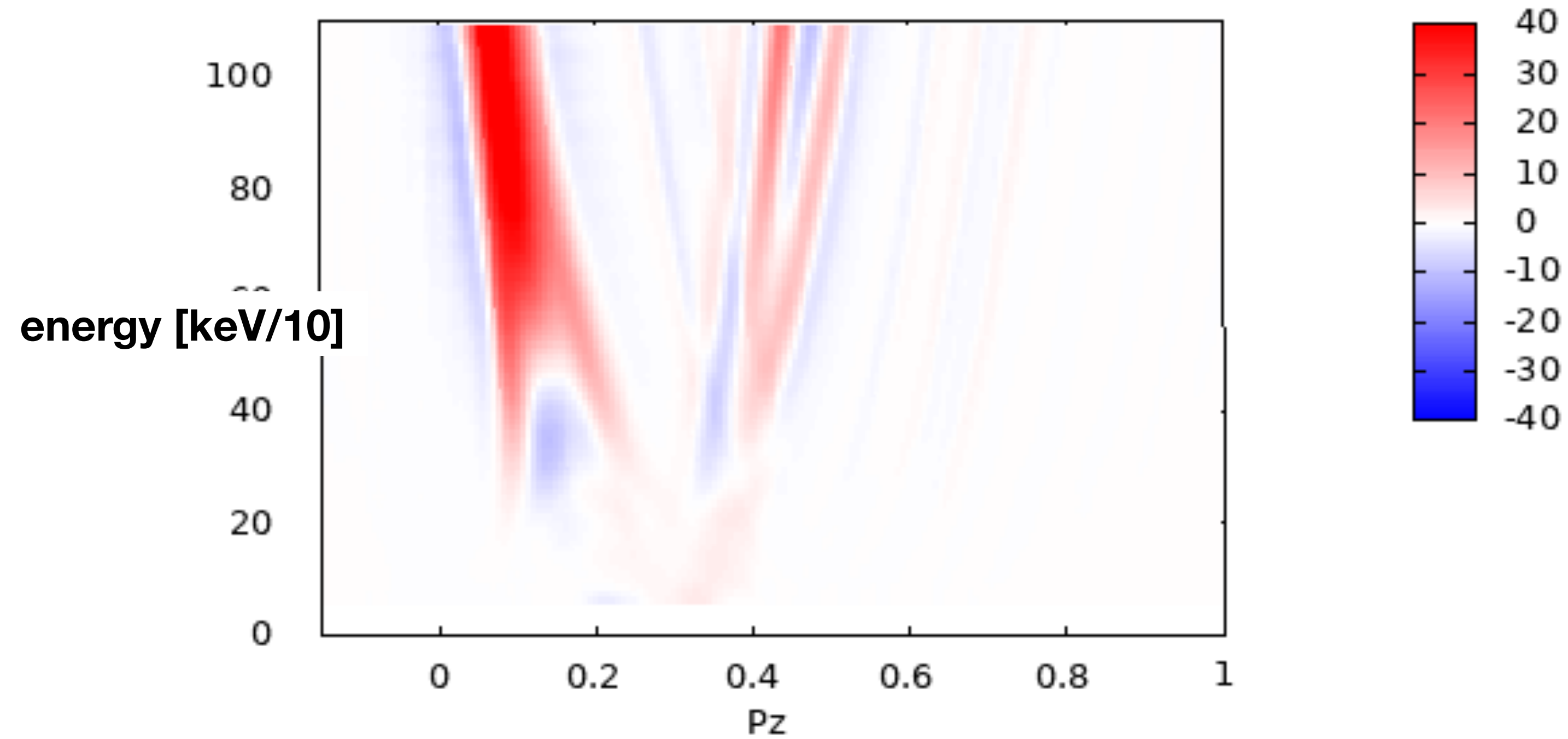
n=18(even 1)  $\delta B/B=1.0e-5$   
n=18 (even 2)  $\delta B/B=4.0e-5$   
n=19  $\delta B/B=5.0e-5$

scale A  $\sim (\gamma_L - \gamma_{damp})^2$

sp=fast;  $t = 237000 \omega_{ci}^{-1}$ ;  $\Lambda = 0.0$



$dP_z (P_z, E)$ , Lamda=109



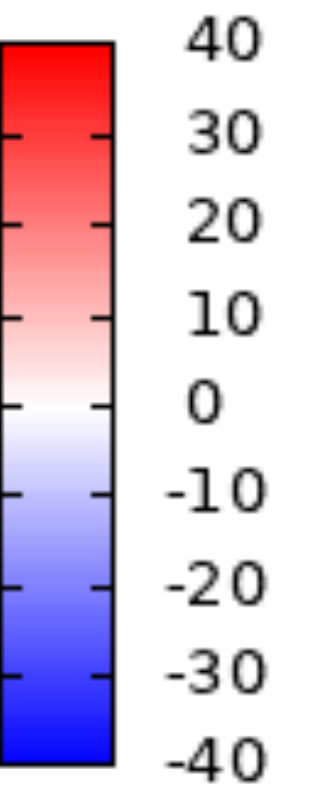
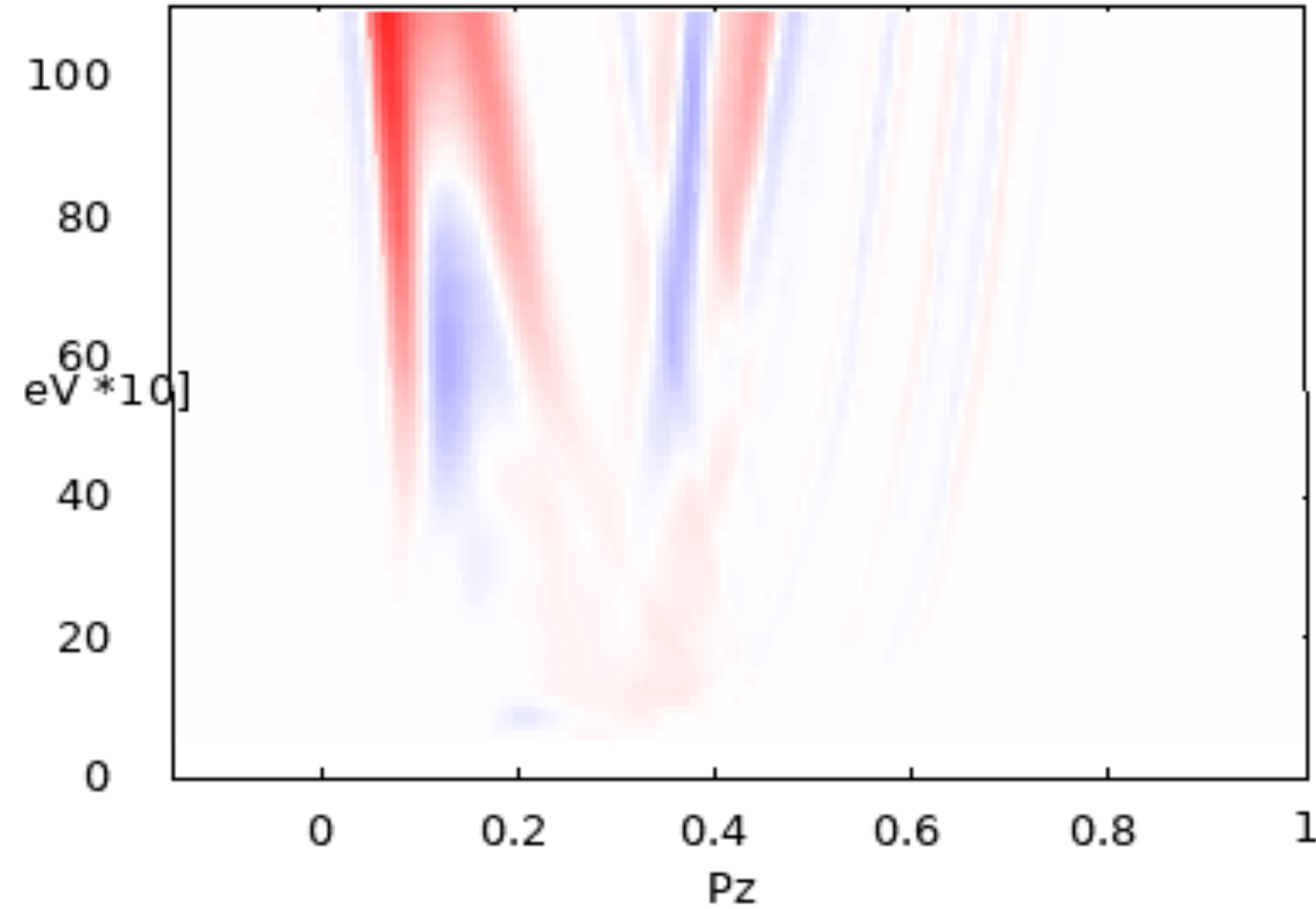
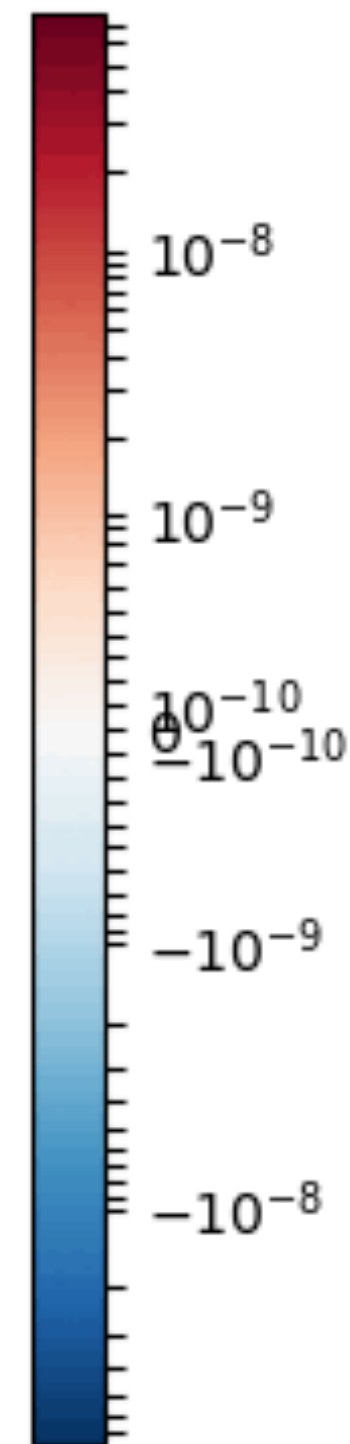
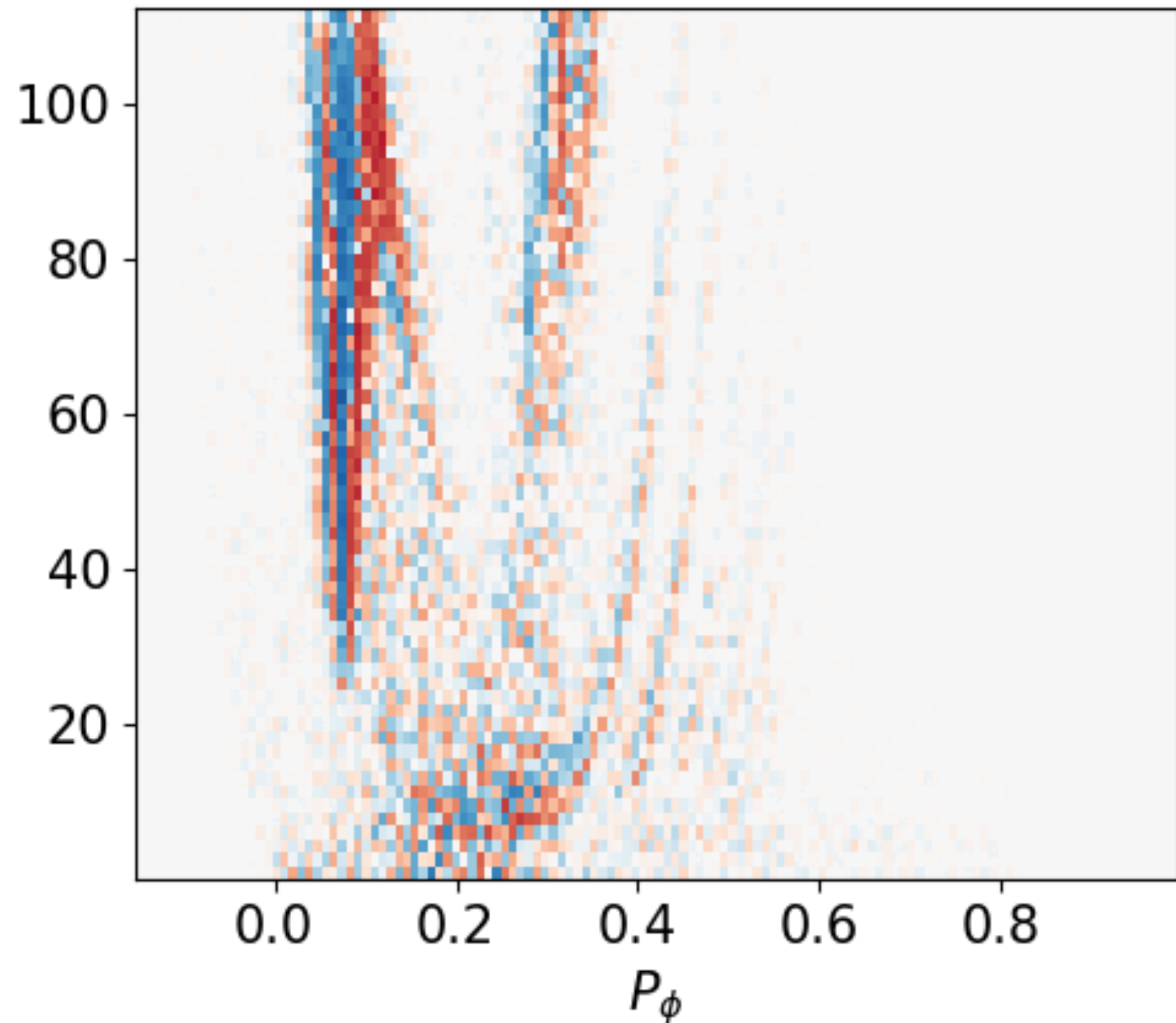


n=18(even 1)  $\delta B/B=1.0e-5$   
n=18 (even 2)  $\delta B/B=4.0e-5$   
n=19  $\delta B/B=5.0e-5$

scale A  $\sim (\gamma_L - \gamma_{damp})^2$

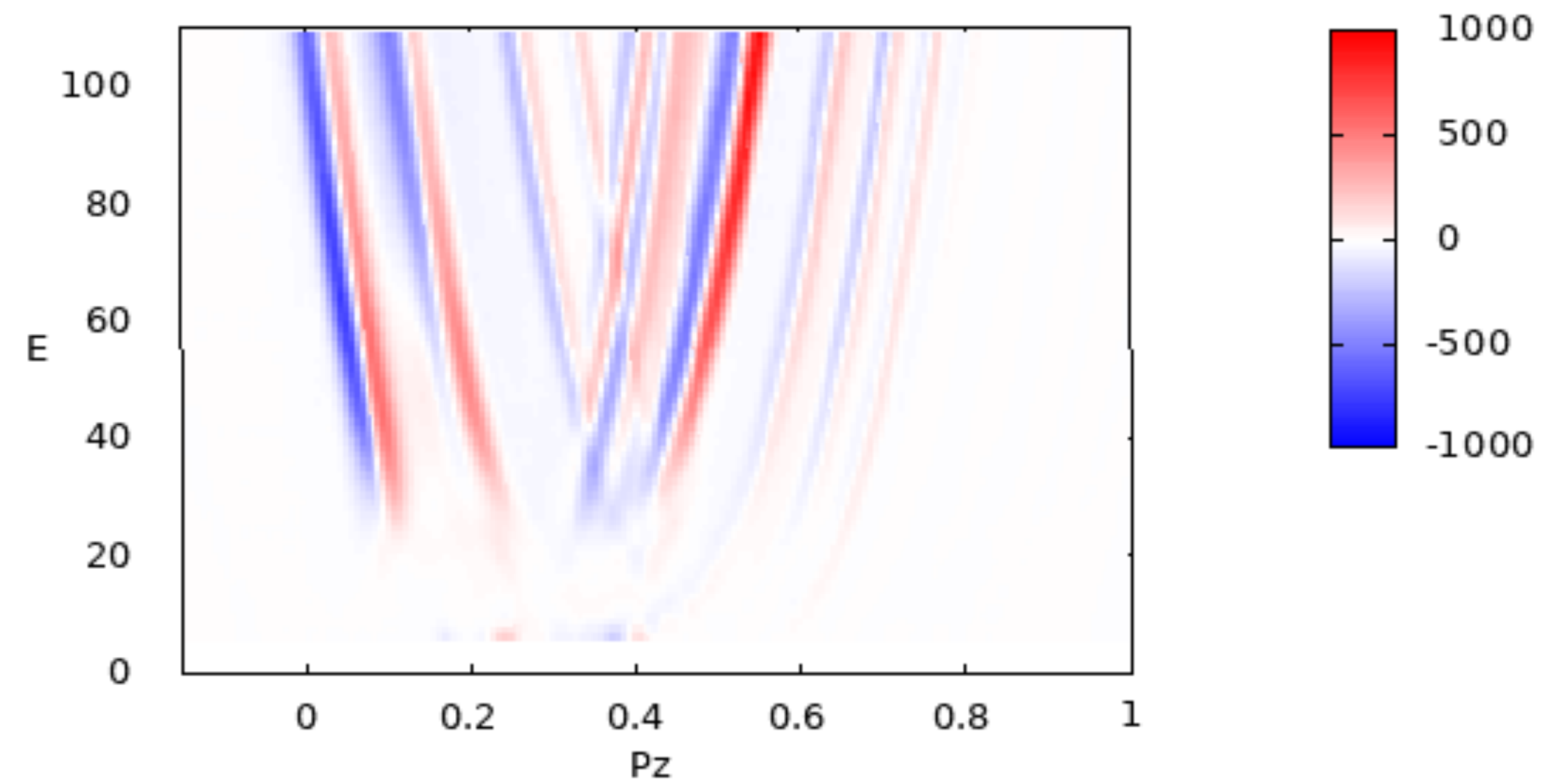
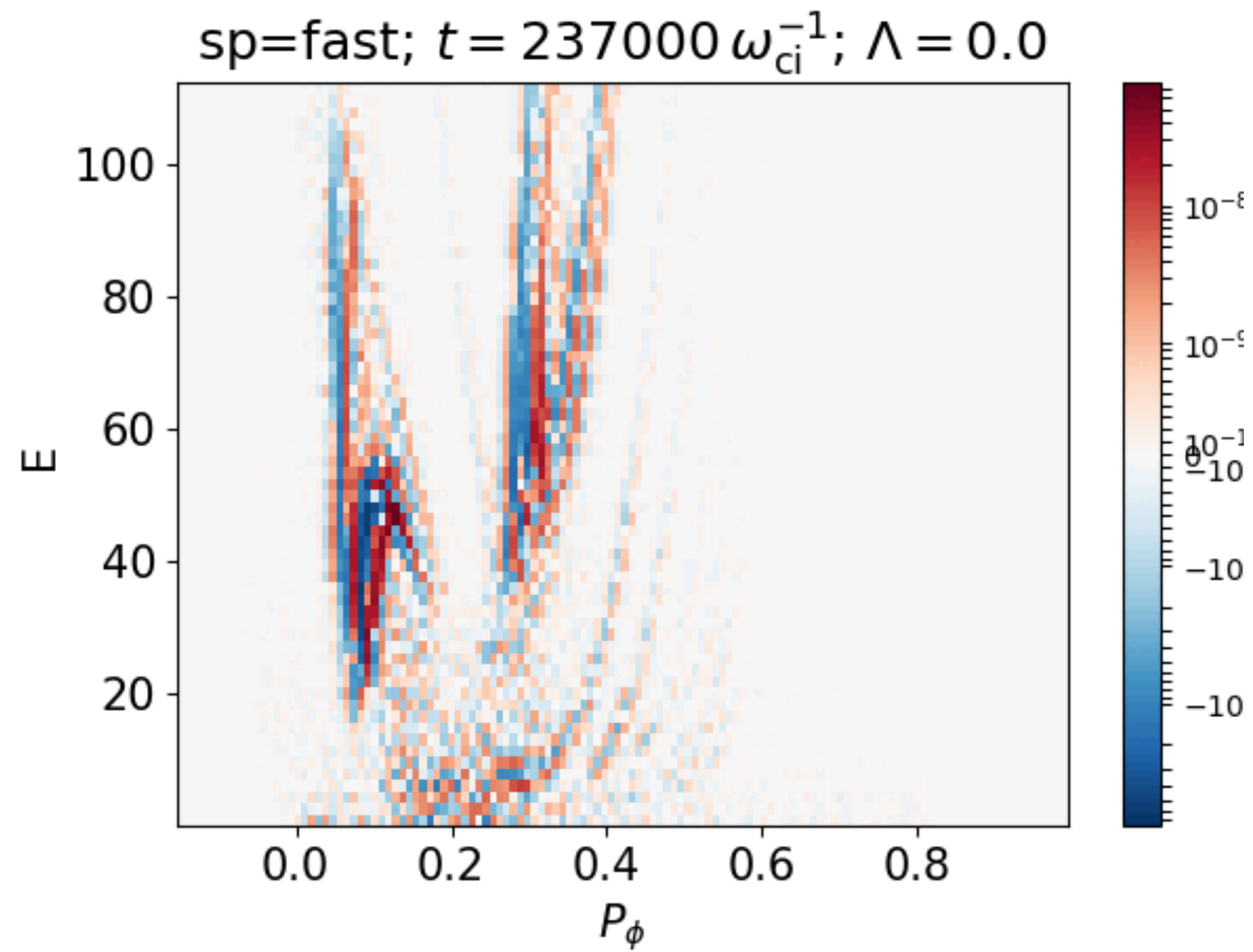
dPz (Pz,E), Lamda=409

sp=fast;  $t = 237000 \omega_{ci}^{-1}$ ;  $\Lambda = 0.4$



n=18(even inner)  $\delta B/B=1.0e-4$   
n=18 (even outer)  $\delta B/B=1.0e-3$   
n=19  $\delta B/B=1.0e-4$

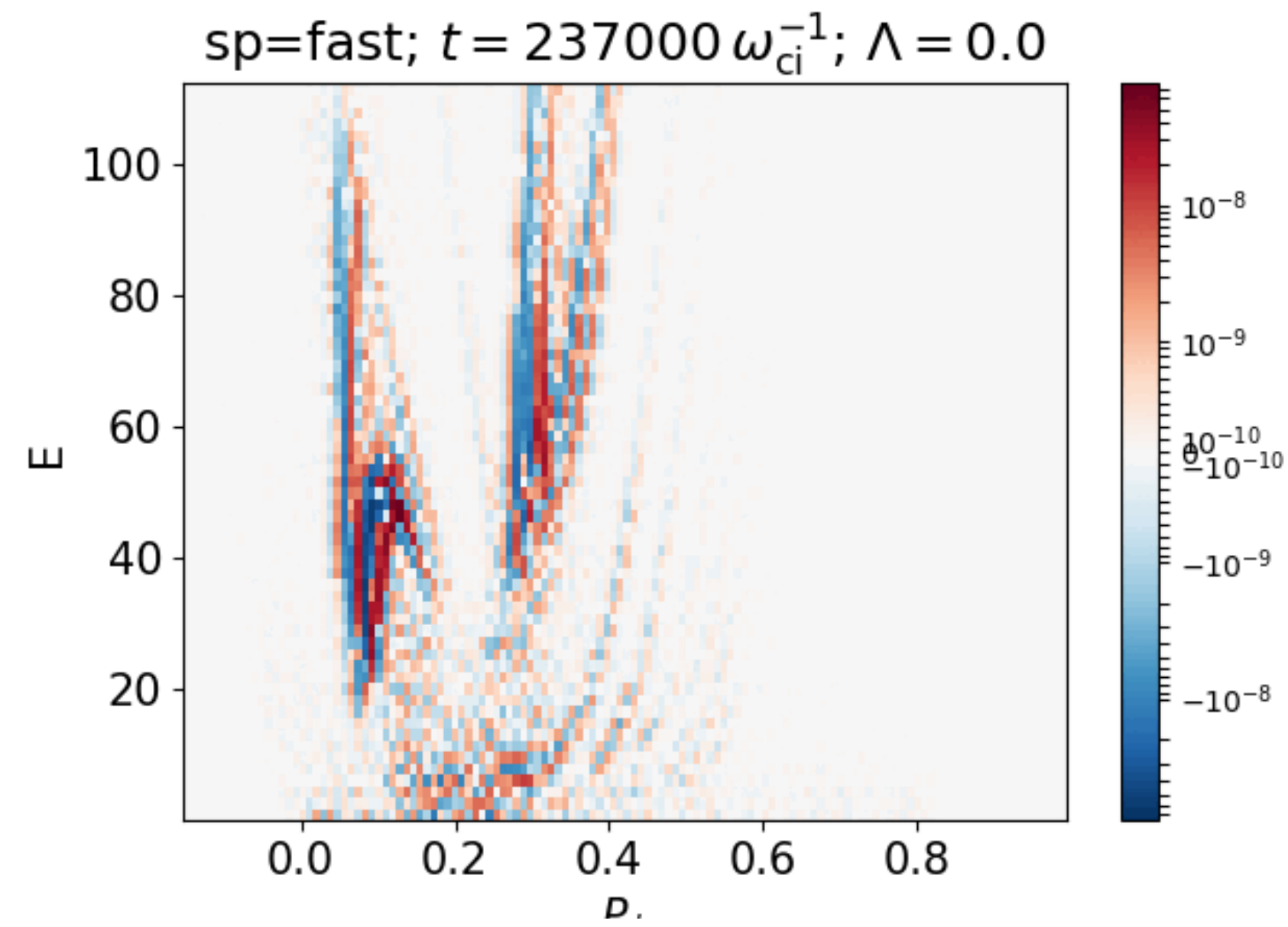
dPz (Pz,E), Lamda=0



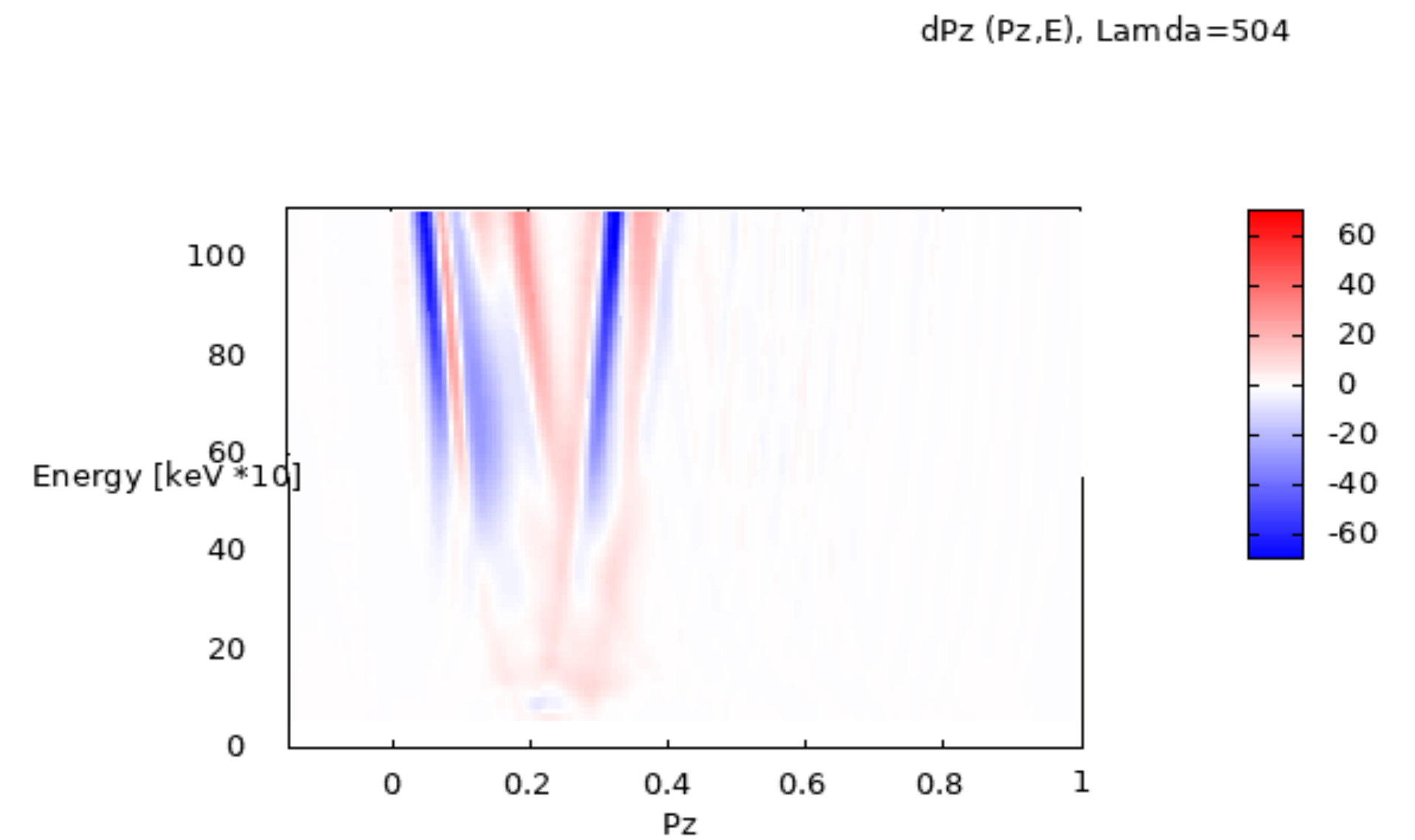
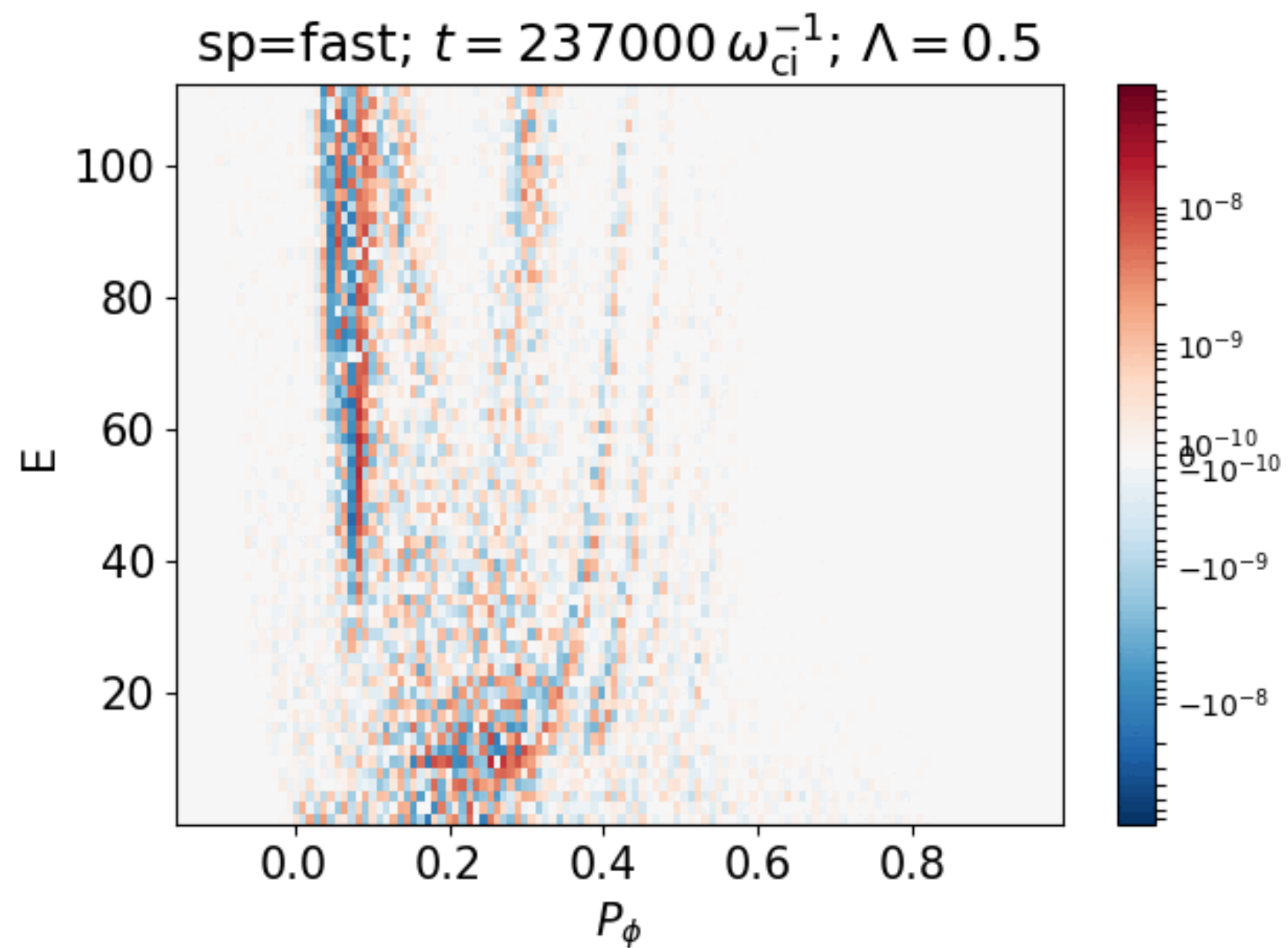
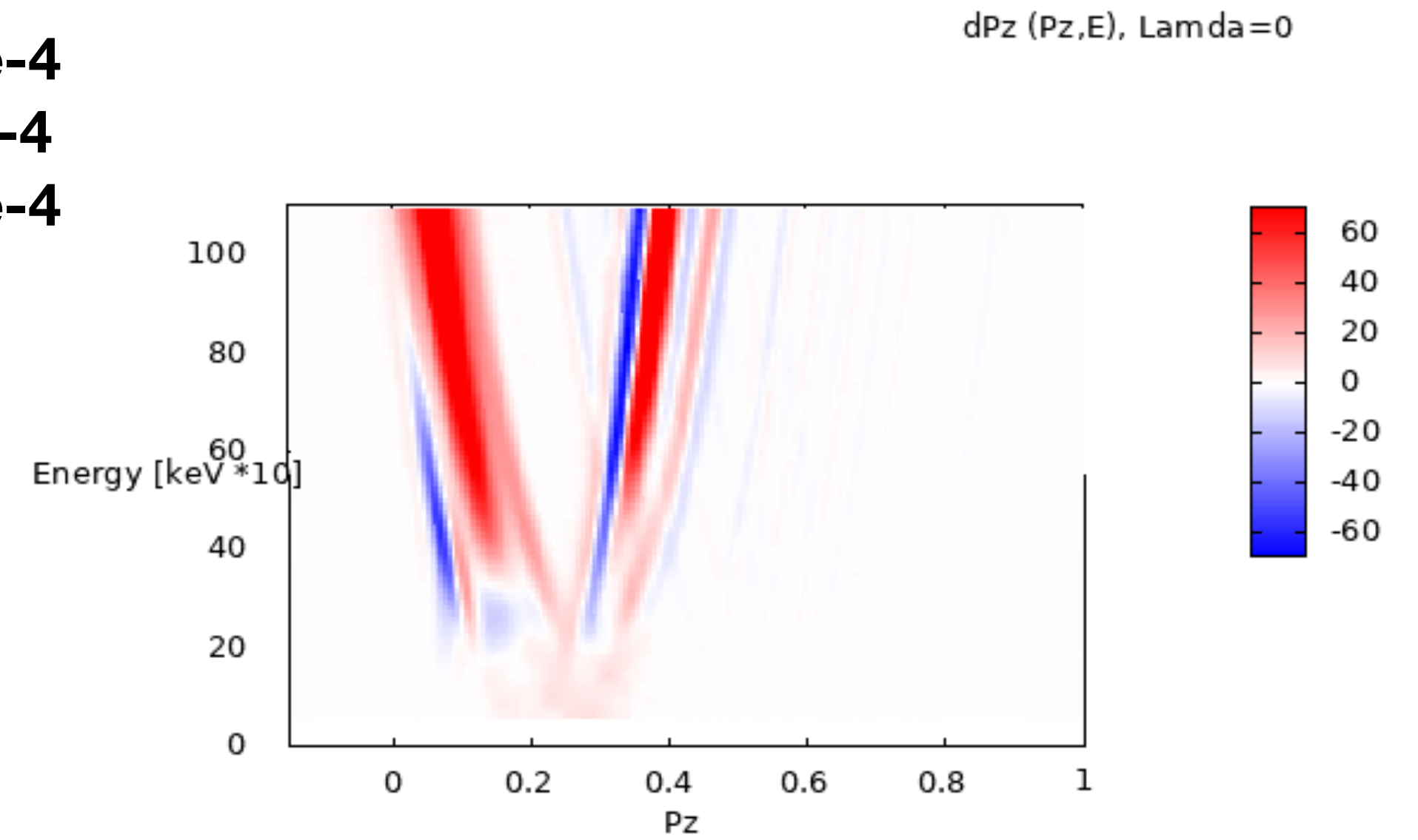
**dominating n=18 ,even outer' does not compare as well as other combinations- in agreement with linear growth rates!**

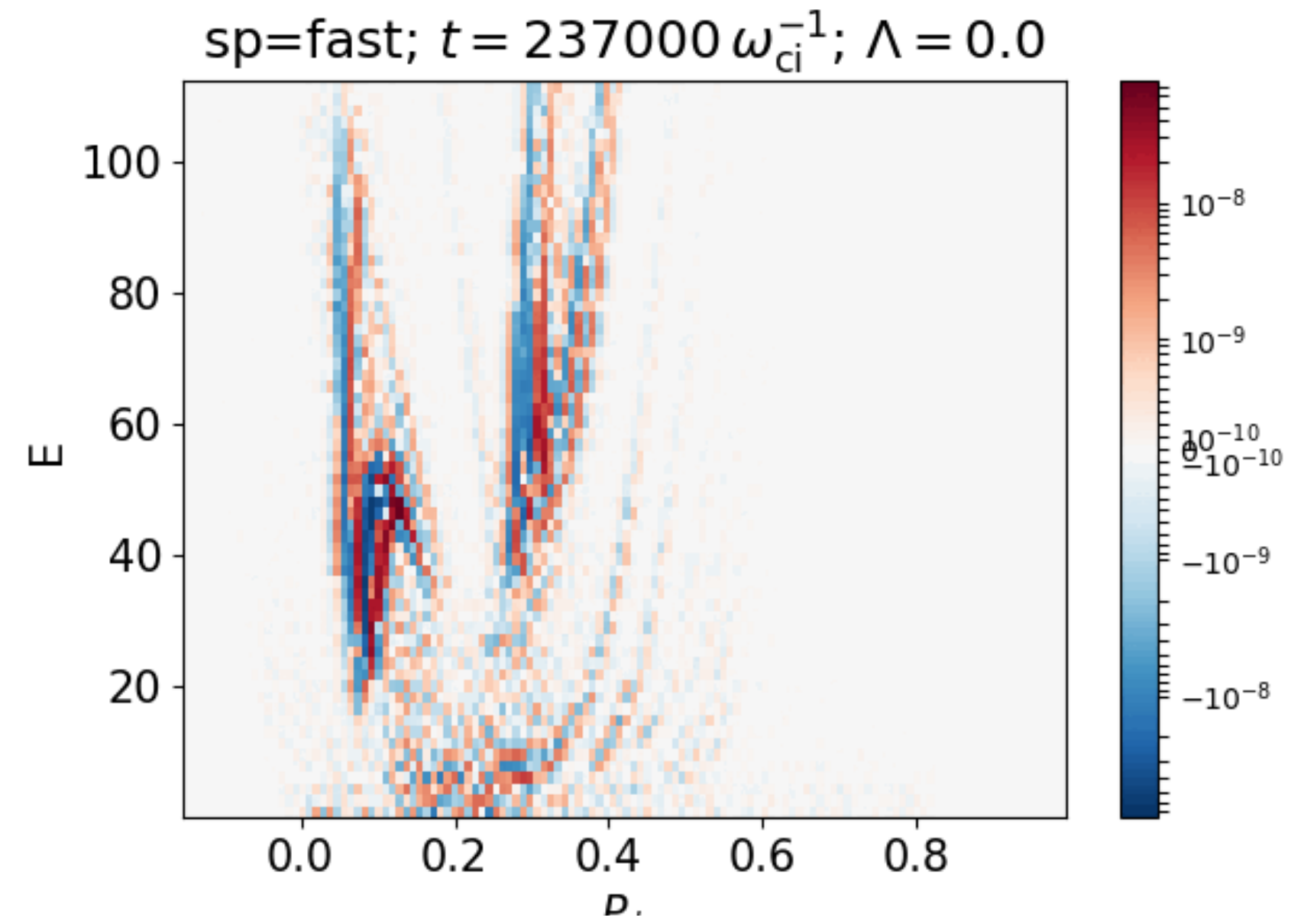


# ORB5- ATEP PSZS comparison: ,EP' eigenfunctions, combination of n=18 even and odd ,n=19 modes

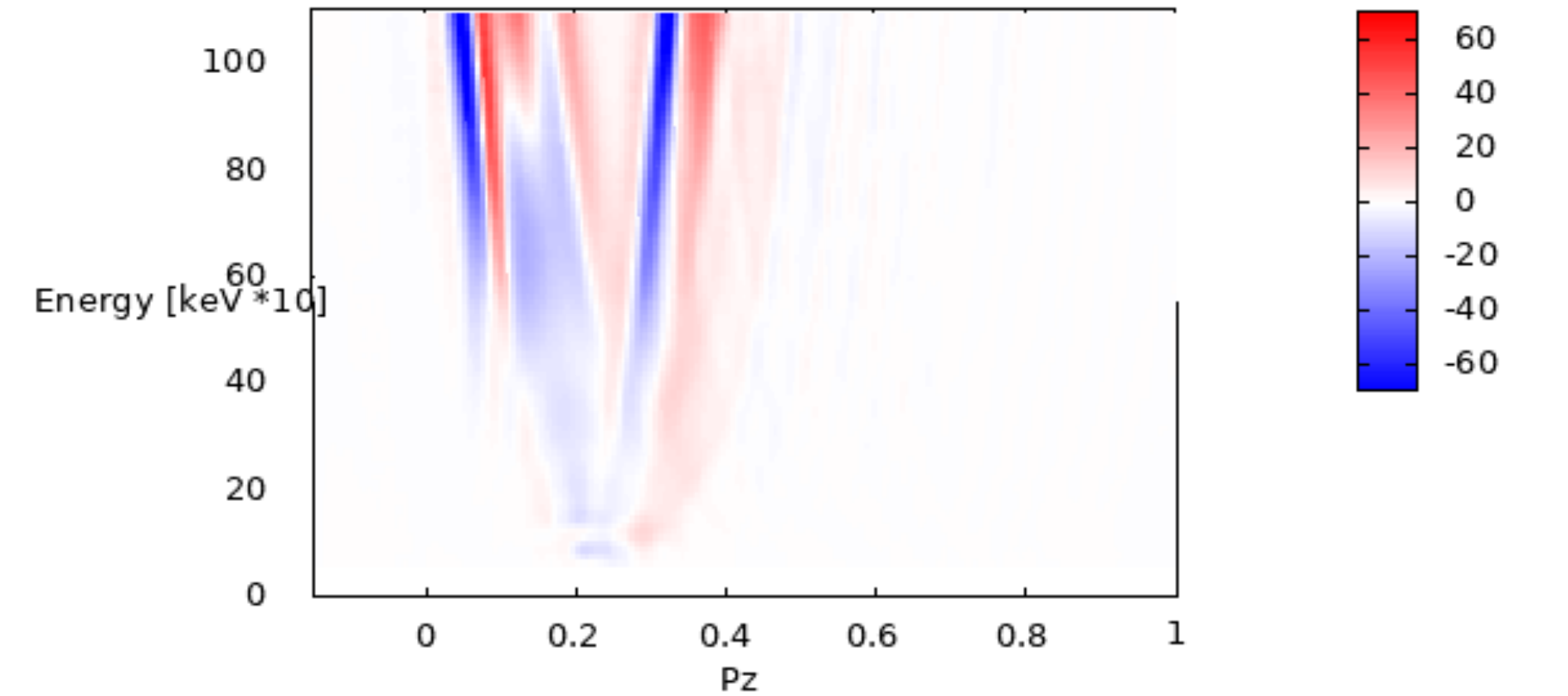
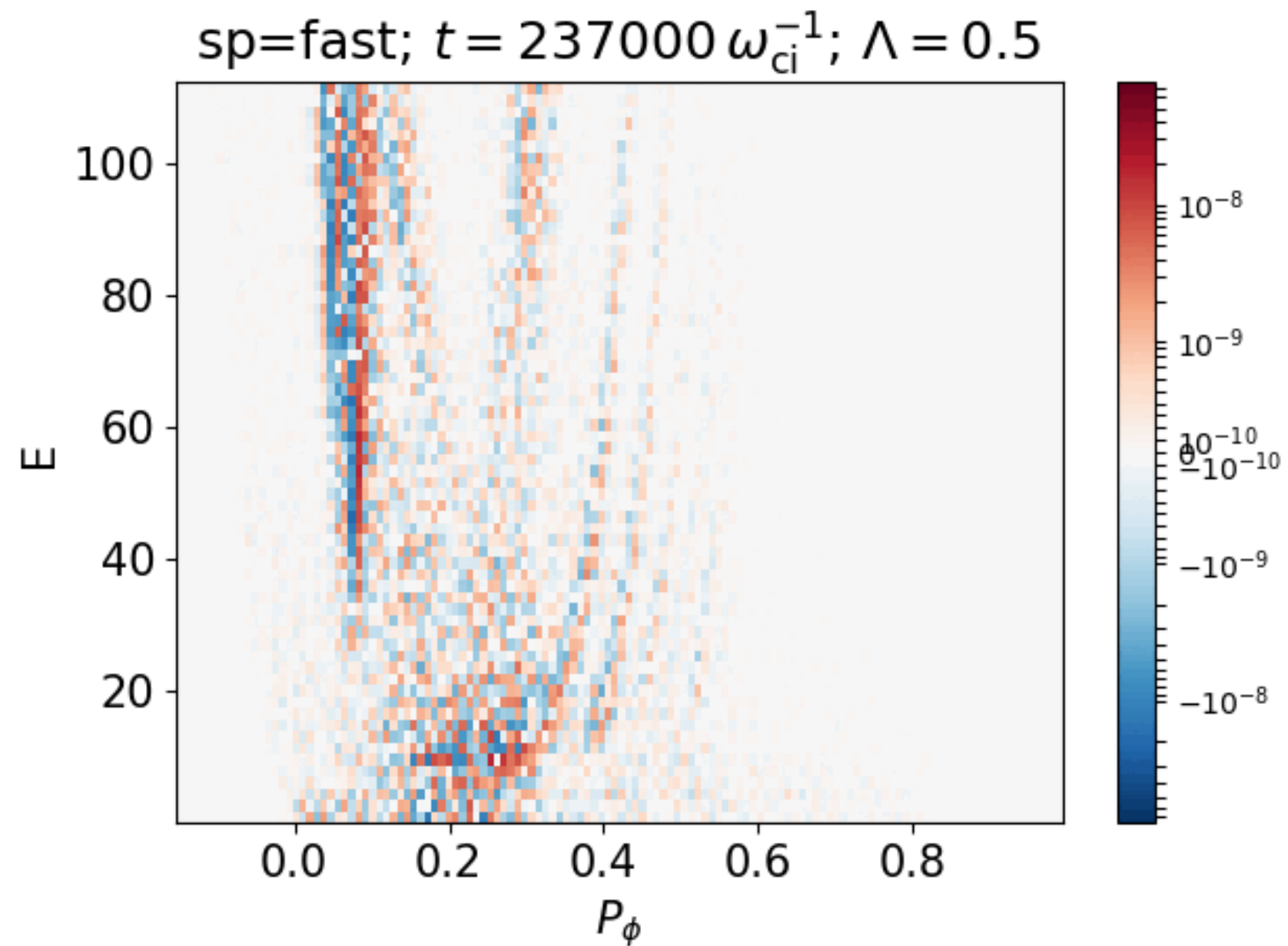
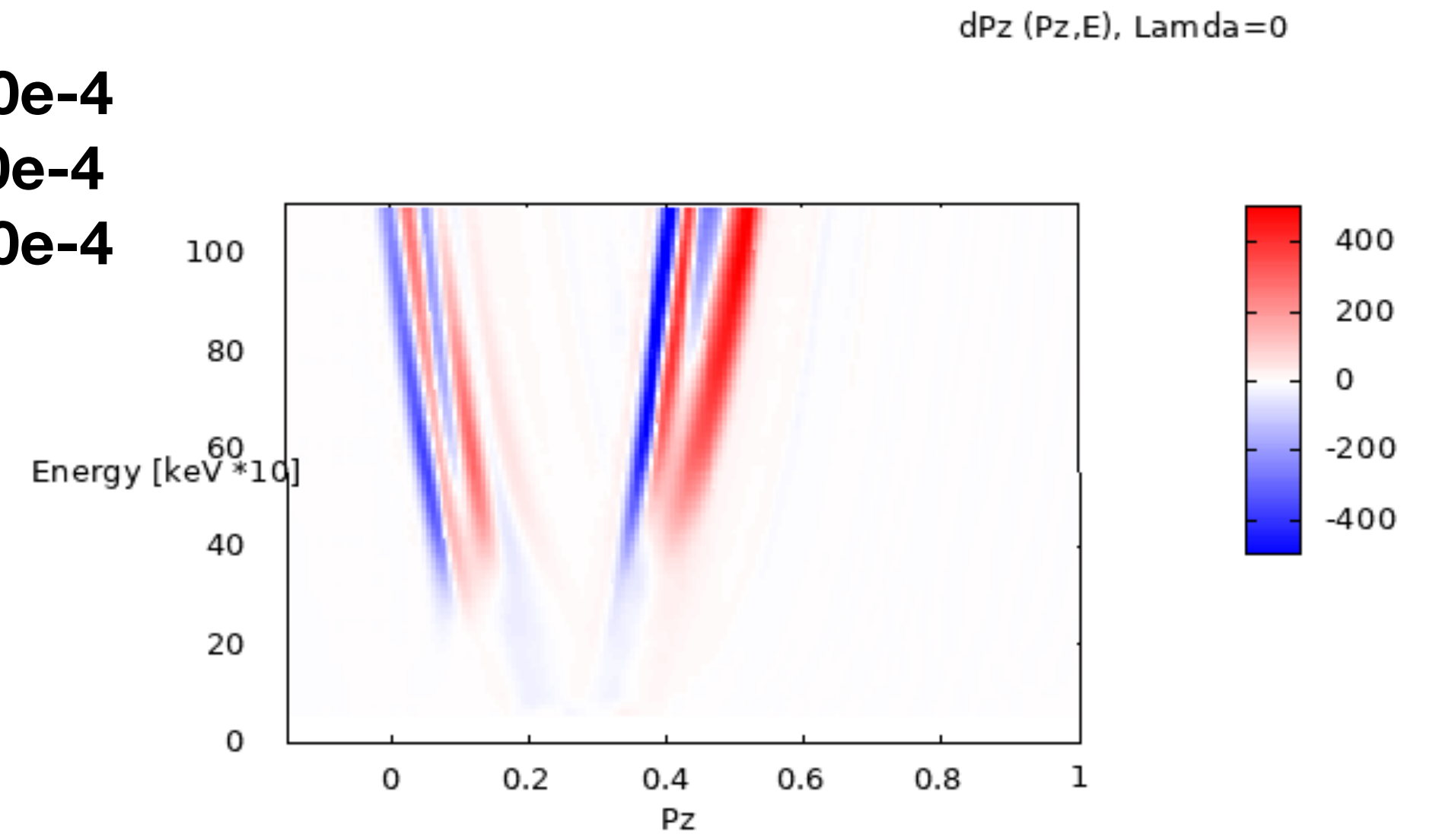


n=18(even)  $\delta B/B=1.0e-4$   
n=18 (odd)  $\delta B/B=1.0e-4$   
n=19 (even)  $\delta B/B=1.0e-4$



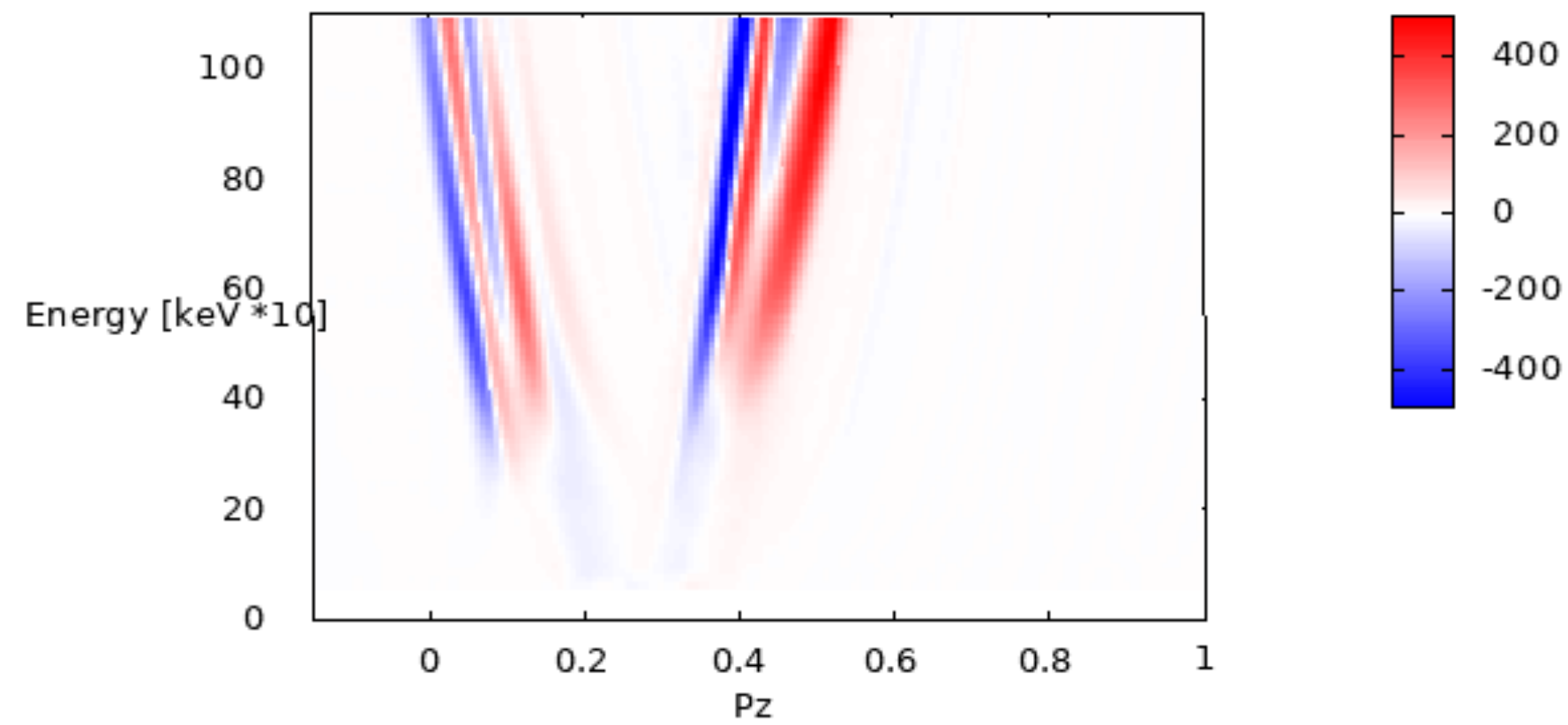


n=18(even)  $\delta B/B=1.0e-4$   
n=18 (odd)  $\delta B/B=5.0e-4$   
n=19 (even)  $\delta B/B=1.0e-4$



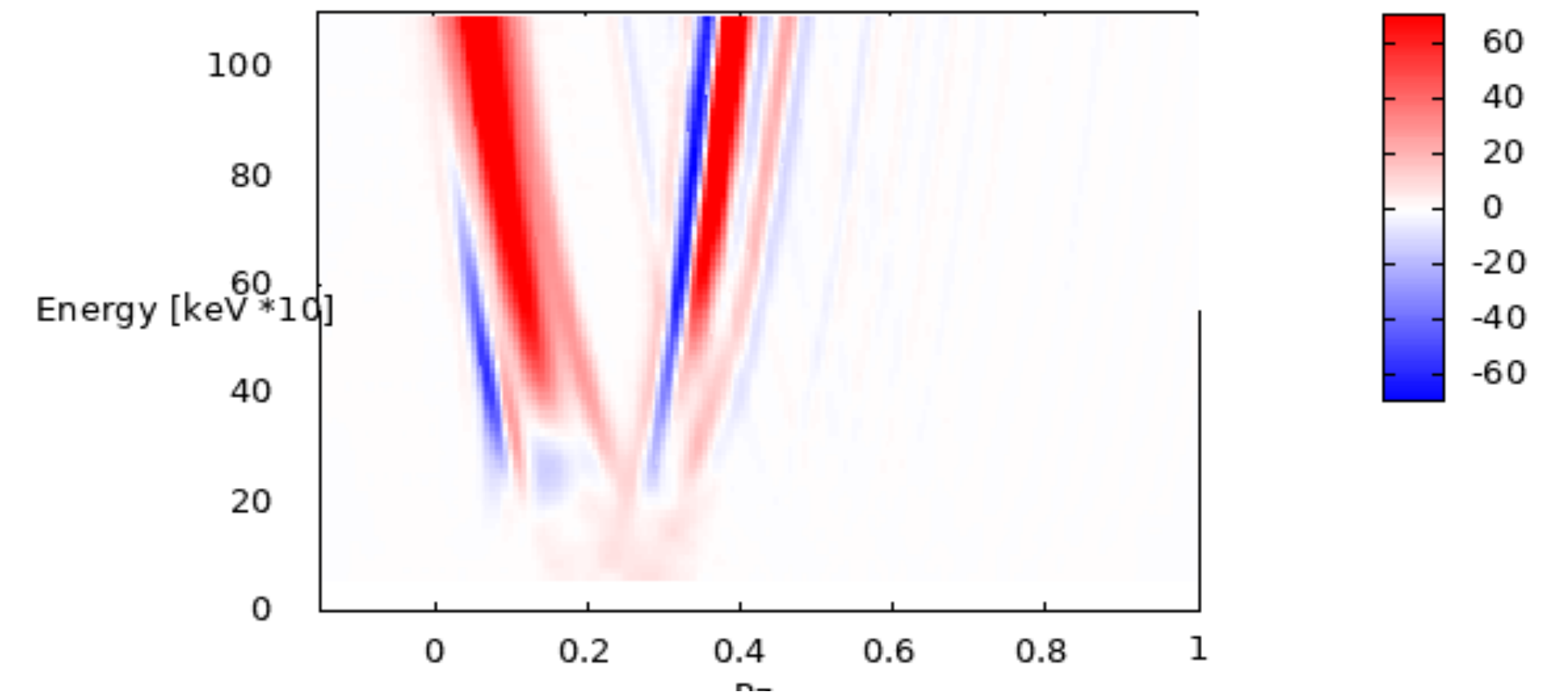
n=18(even)  $\delta B/B=1.0e-4$   
n=18 (odd)  $\delta B/B=5.0e-4$   
n=19 (even)  $\delta B/B=1.0e-4$

dPz (Pz,E), Lamda=0

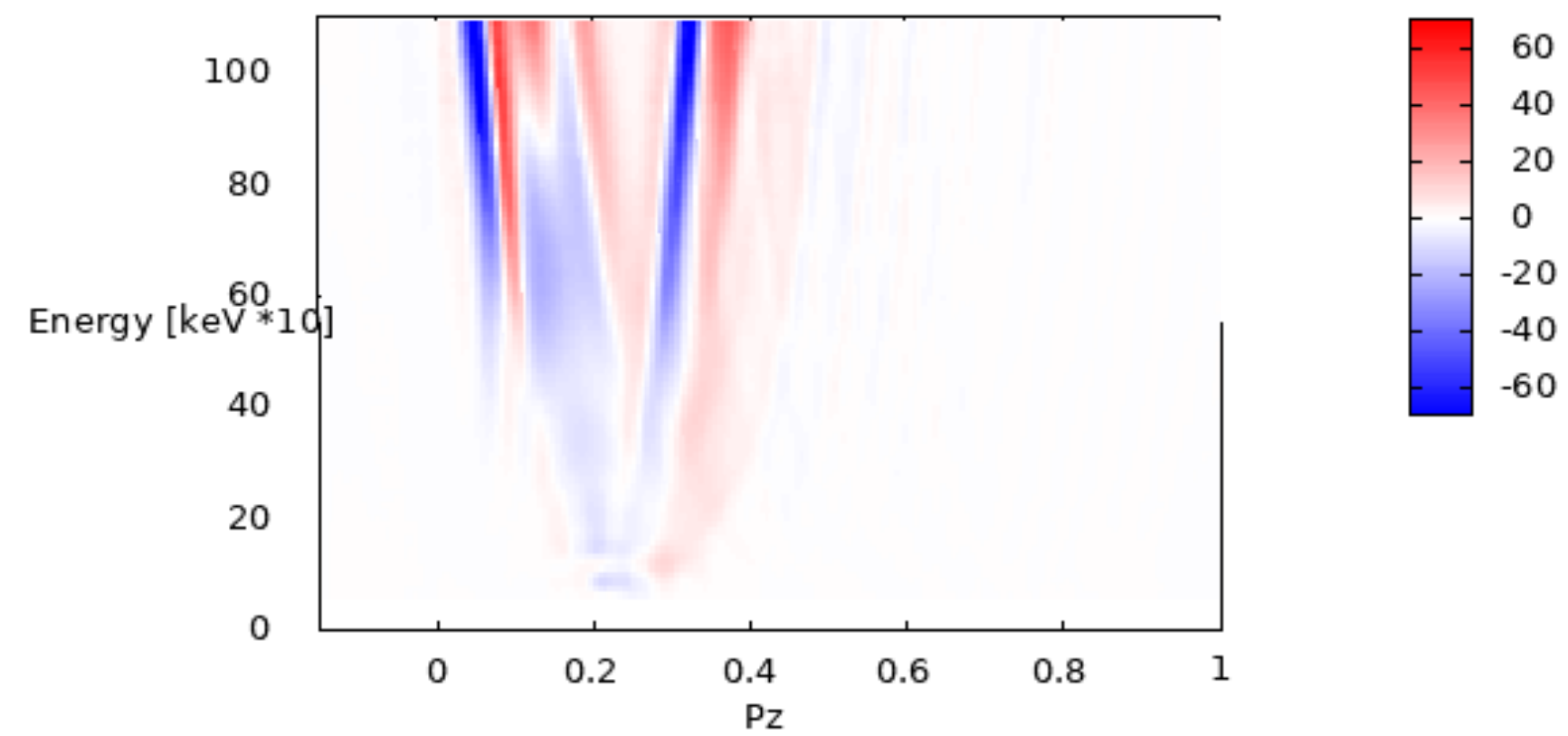


n=18(even)  $\delta B/B=1.0e-4$   
n=18 (odd)  $\delta B/B=1.0e-4$   
n=19 (even)  $\delta B/B=1.0e-4$

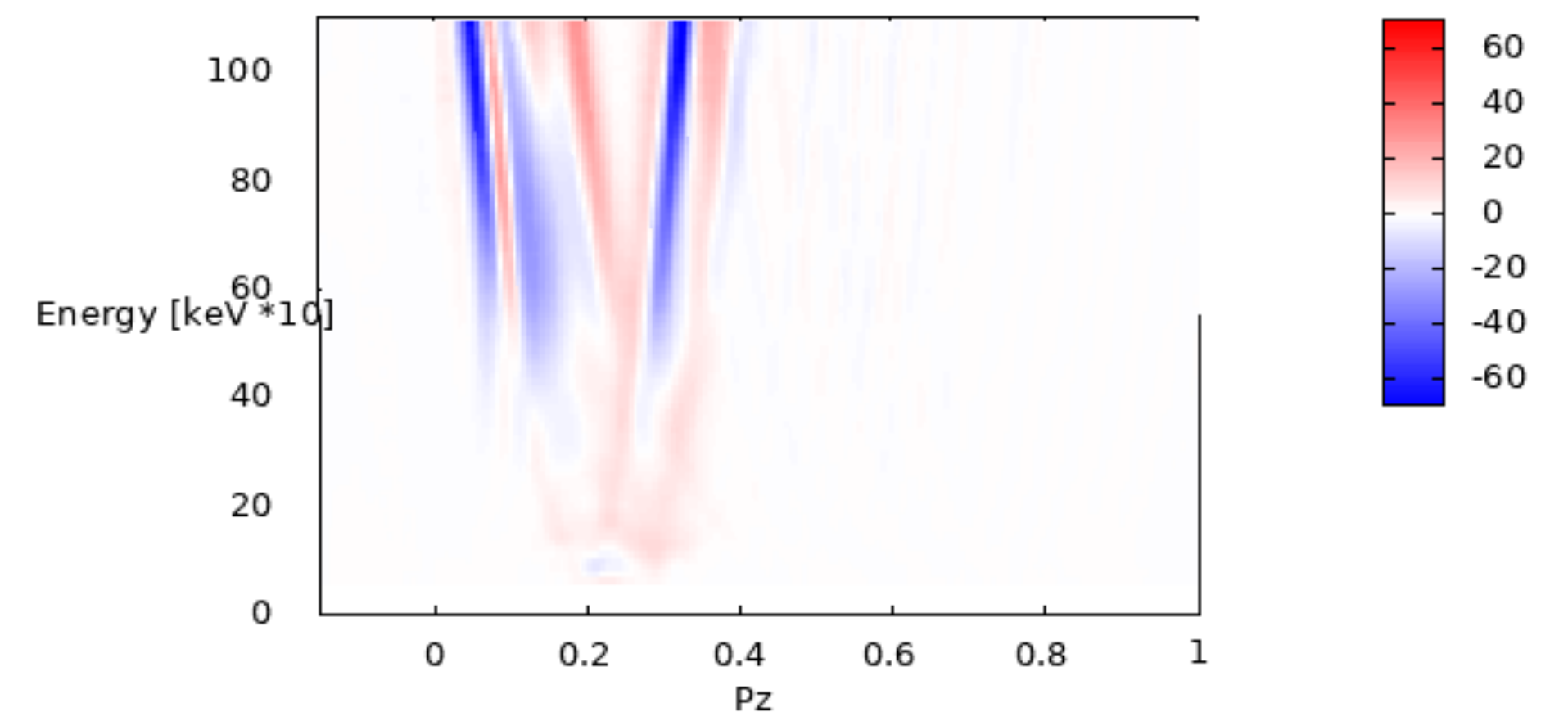
dPz (Pz,E), Lamda=0



dPz (Pz,E), Lamda=504



dPz (Pz,E), Lamda=504



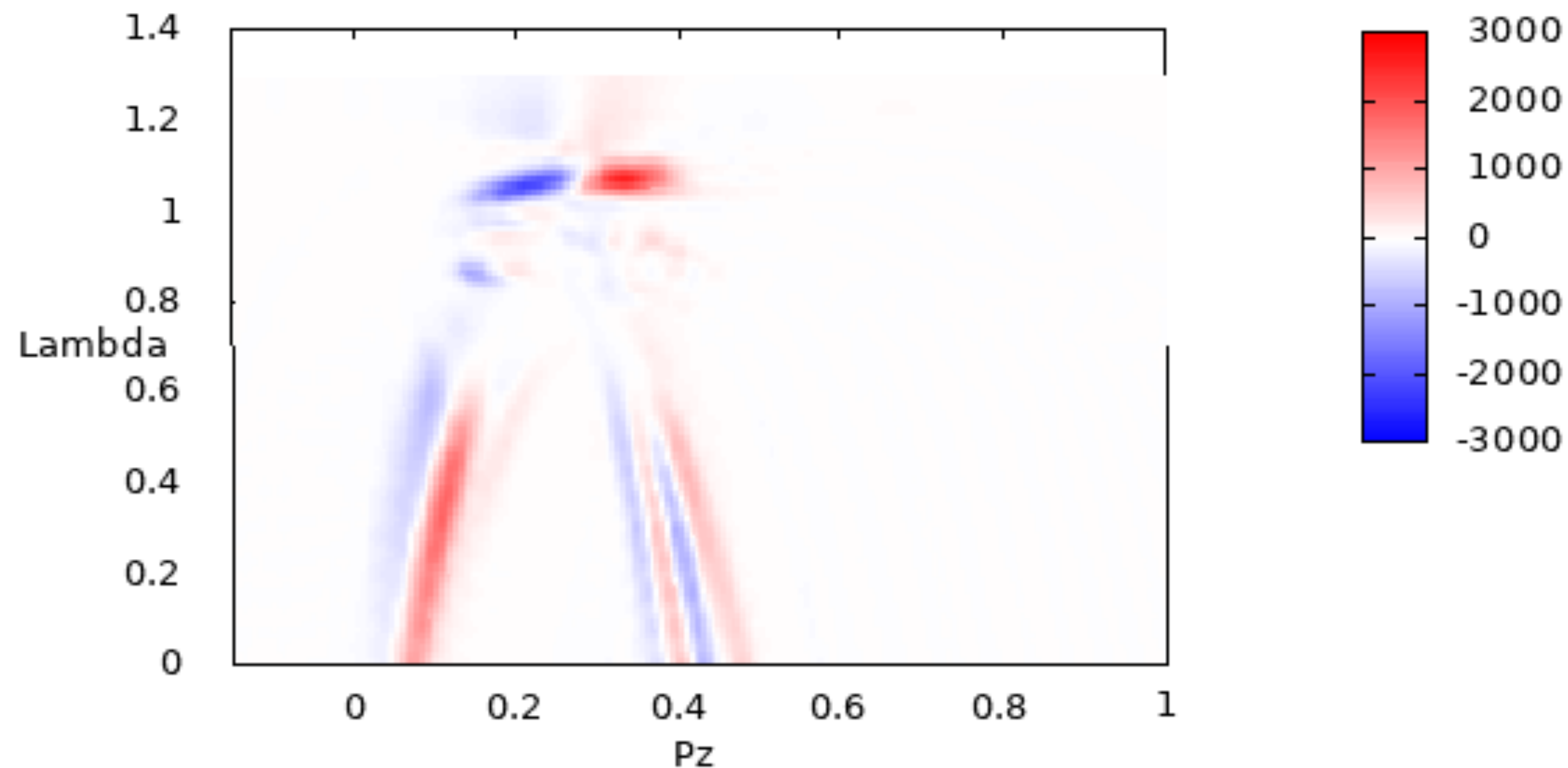


# ORB5- ATEP PSZS comparison: ,EP' eigenfunctions, combination of n=18,n=19 modes Pz- $\Lambda$ slices



n=18(even inner)  $\delta B/B=2.0e-4$   
n=18 (even outer)  $\delta B/B=2.0e-4$   
n=19  $\delta B/B=1.0e-3$

dPz (Pz,Lambda), energy=1000000





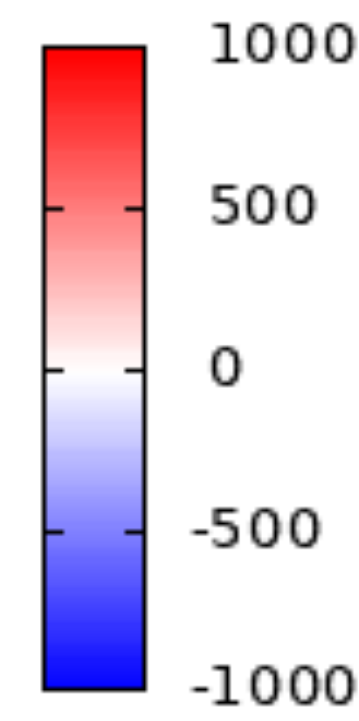
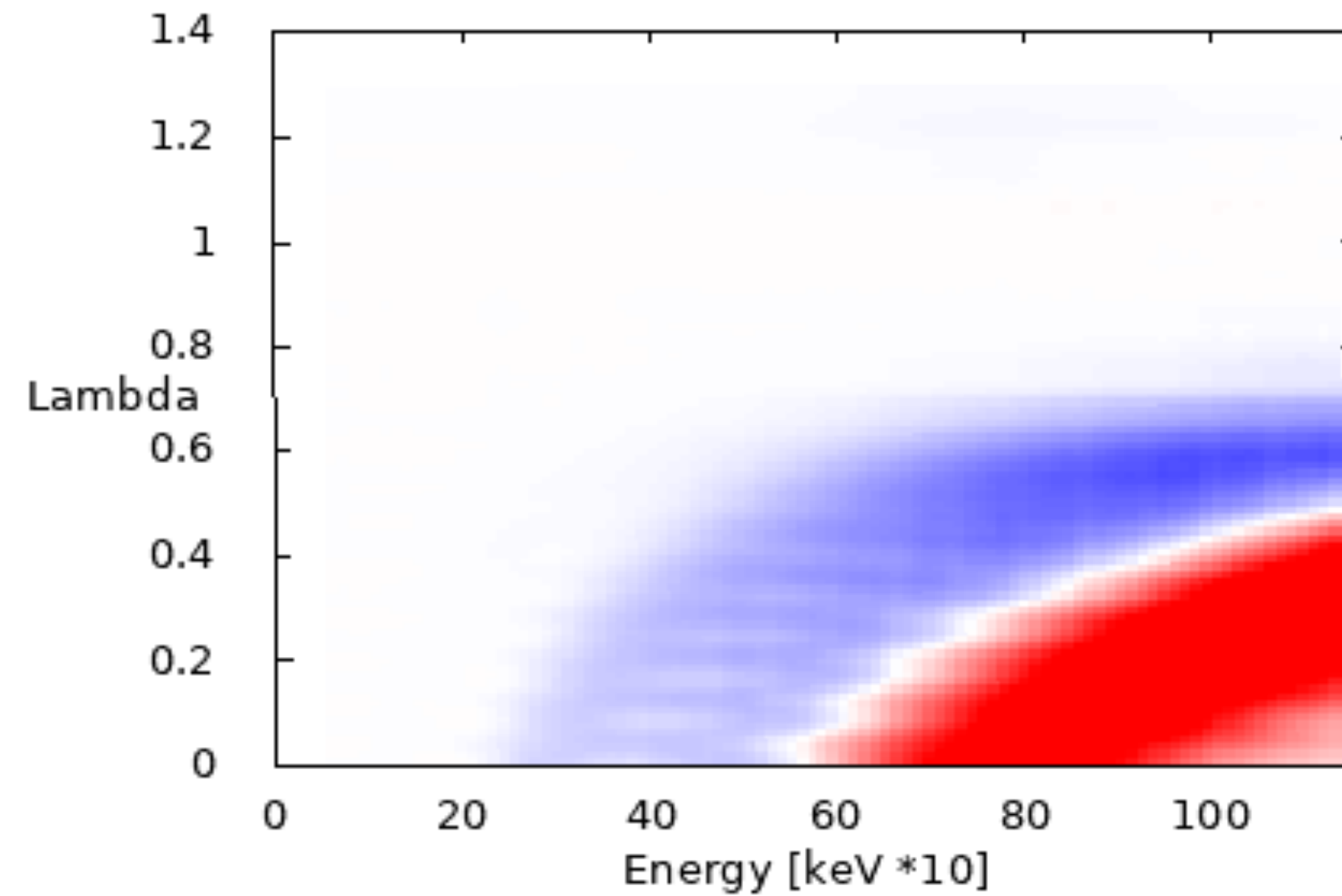


# ORB5- ATEP PSZS comparison: ,EP' eigenfunctions, combination of n=18,n=19 modes E- $\Lambda$ slices, co-passing



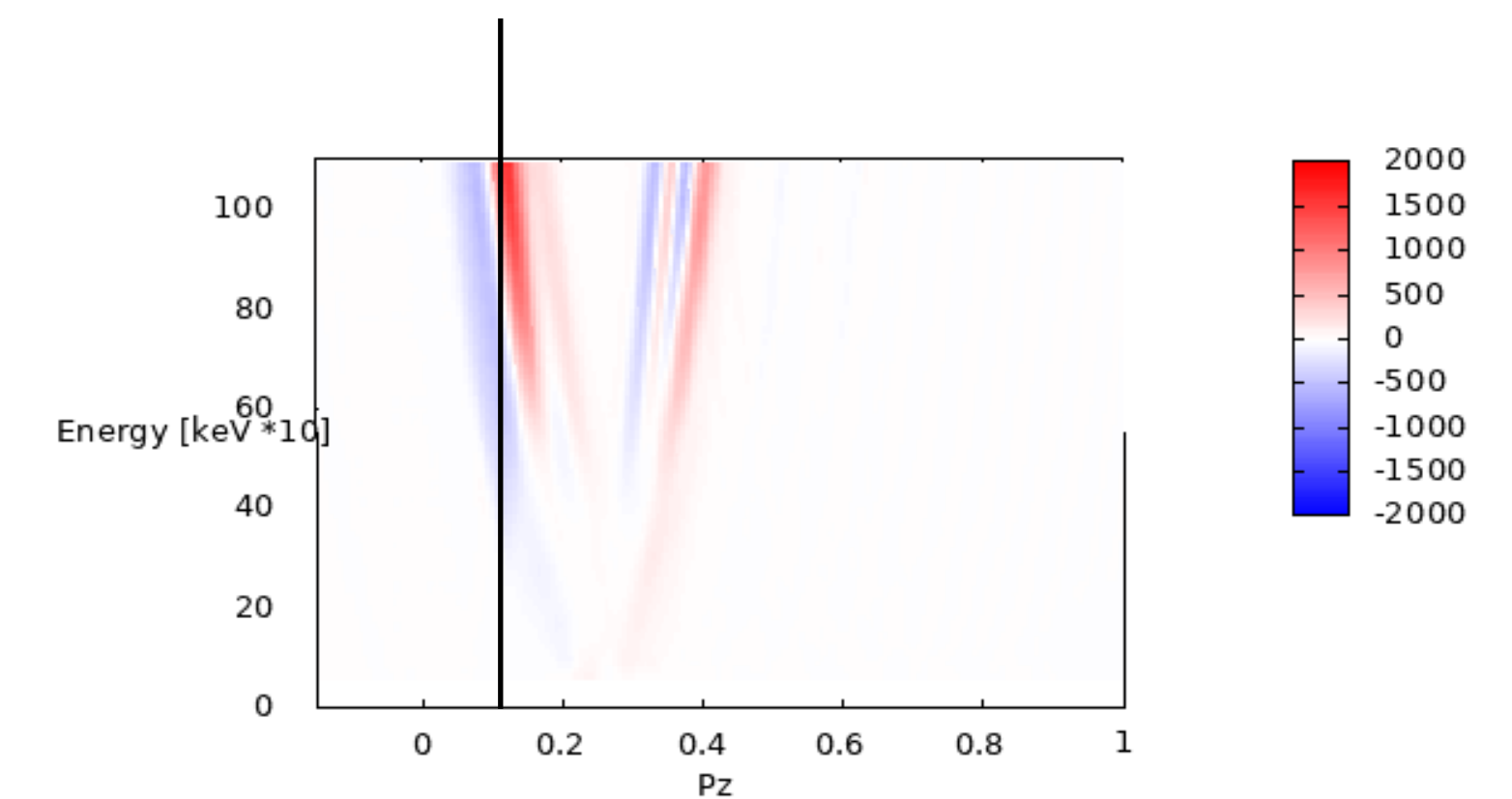
n=18(odd)  $\delta B/B=2.0e-4$   
n=18 (even)  $\delta B/B=2.0e-4$   
n=19  $\delta B/B=1.0e-3$

dPz (Pz,Lambda), Pz=101



← cut

dPz (Pz,E), Lamda=409







as expected: PSZS structures differ at different amplitudes,  
especially at large amplitudes, when stochasticity limit is crossed  $\sim \delta B/B=1.0e-3$



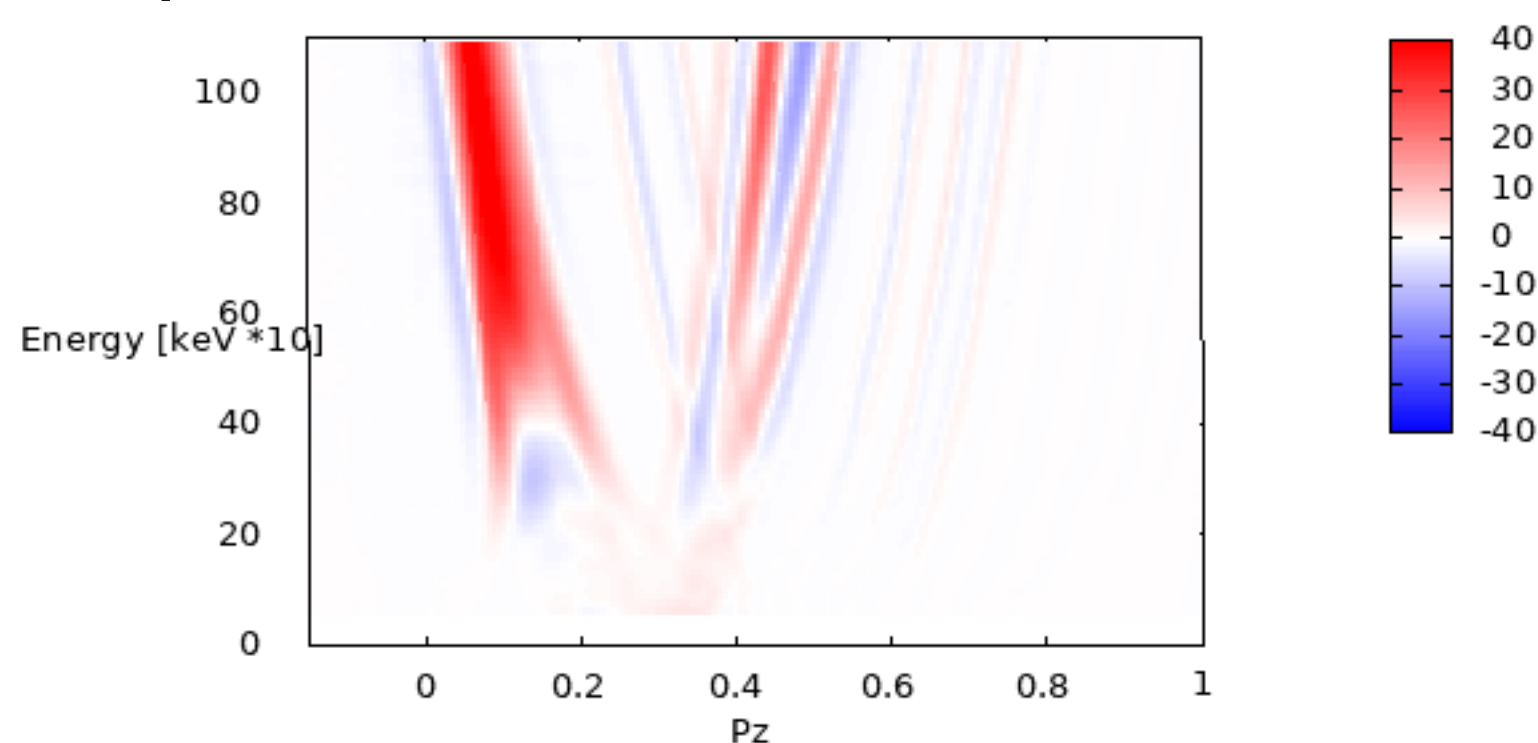
n=18(odd)  $\delta B/B=1.0e-5$   
n=18 (even)  $\delta B/B=4.0e-5$   
n=19  $\delta B/B=5.0e-5$

n=18(odd)  $\delta B/B=1.0e-4$   
n=18 (even)  $\delta B/B=4.0e-4$   
n=19  $\delta B/B=5.0e-4$

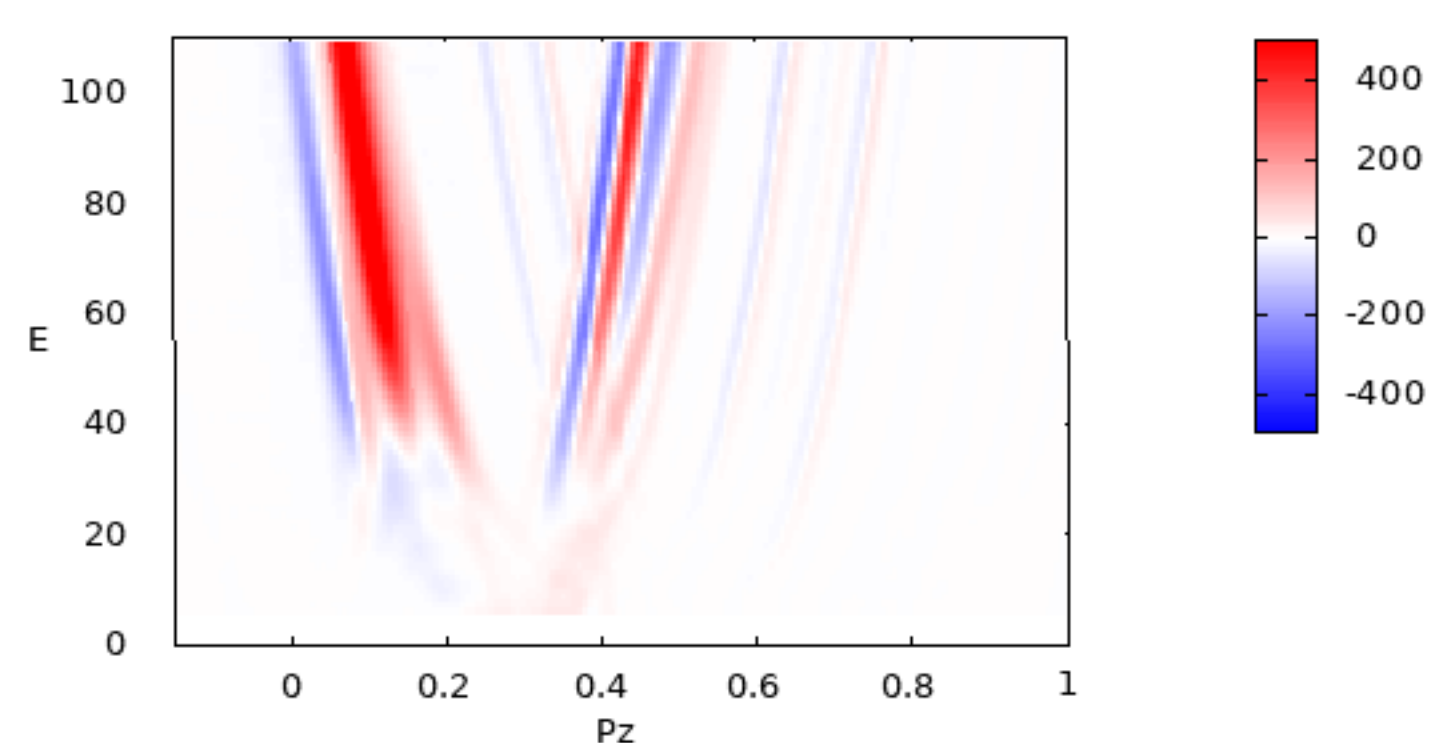
n=18(odd)  $\delta B/B=1.0e-3$   
n=18 (even)  $\delta B/B=4.0e-3$   
n=19  $\delta B/B=5.0e-3$

dPz (Pz,E), Lamda=0

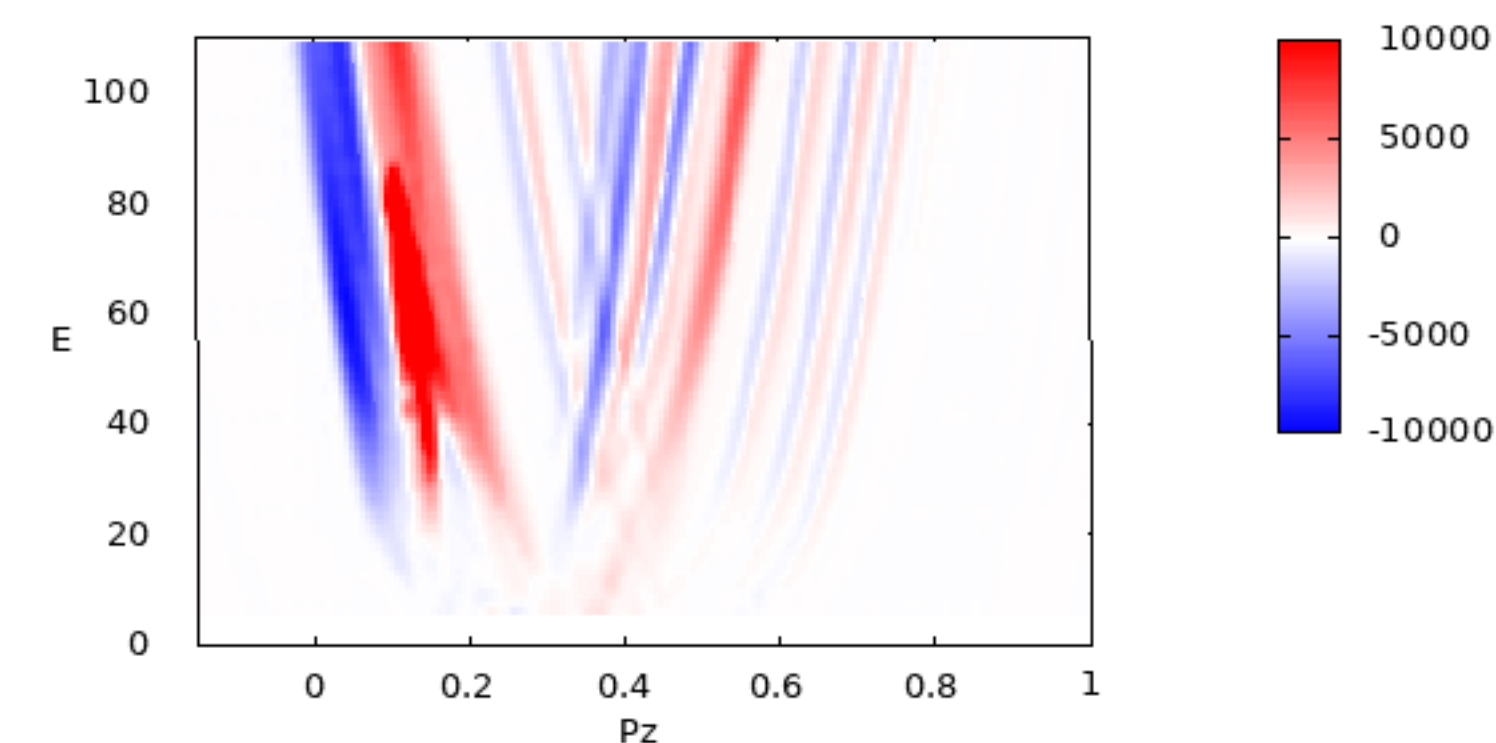
$\Lambda=\mu B/E=0.0$



dPz (Pz,E), Lamda=0

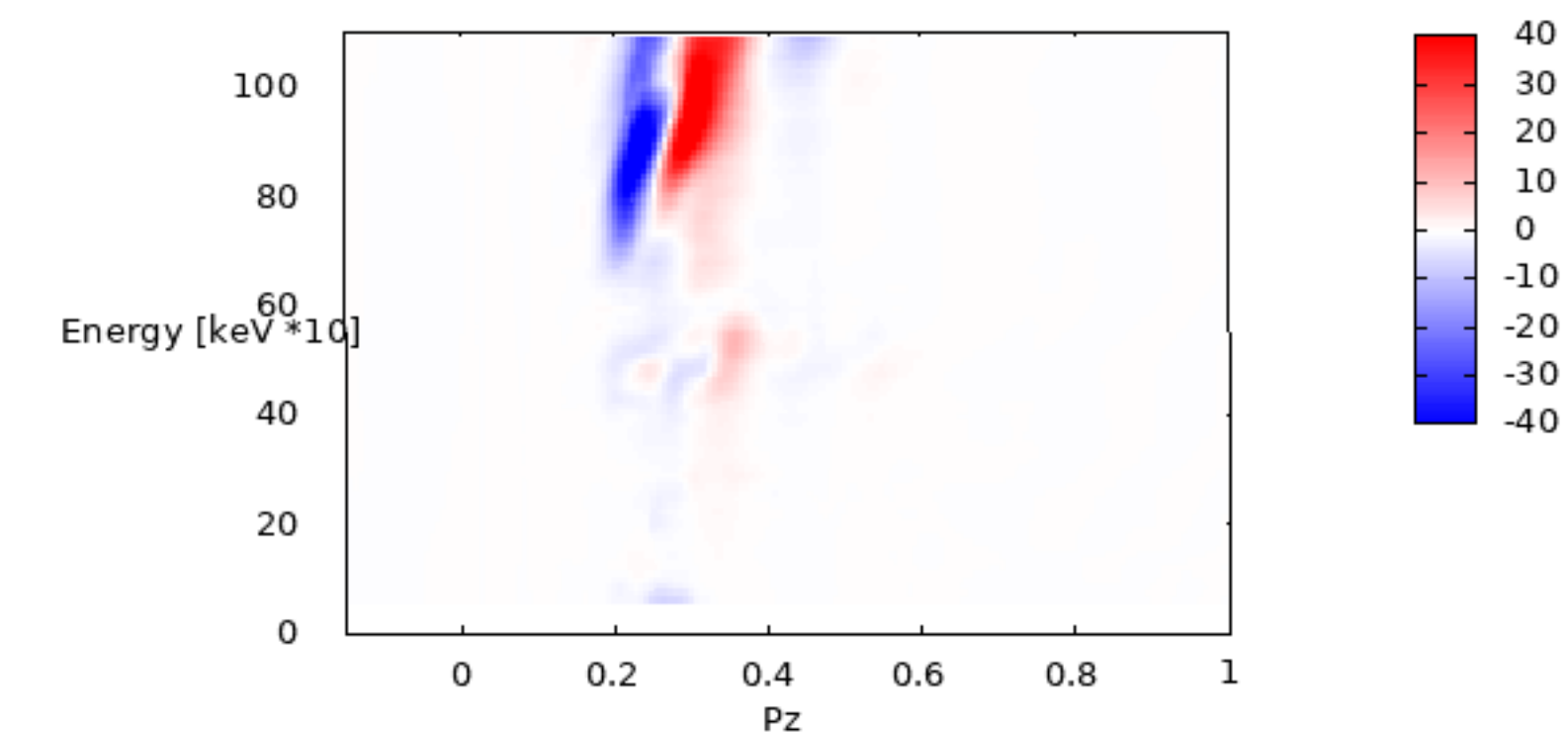


dPz (Pz,E), Lamda=0

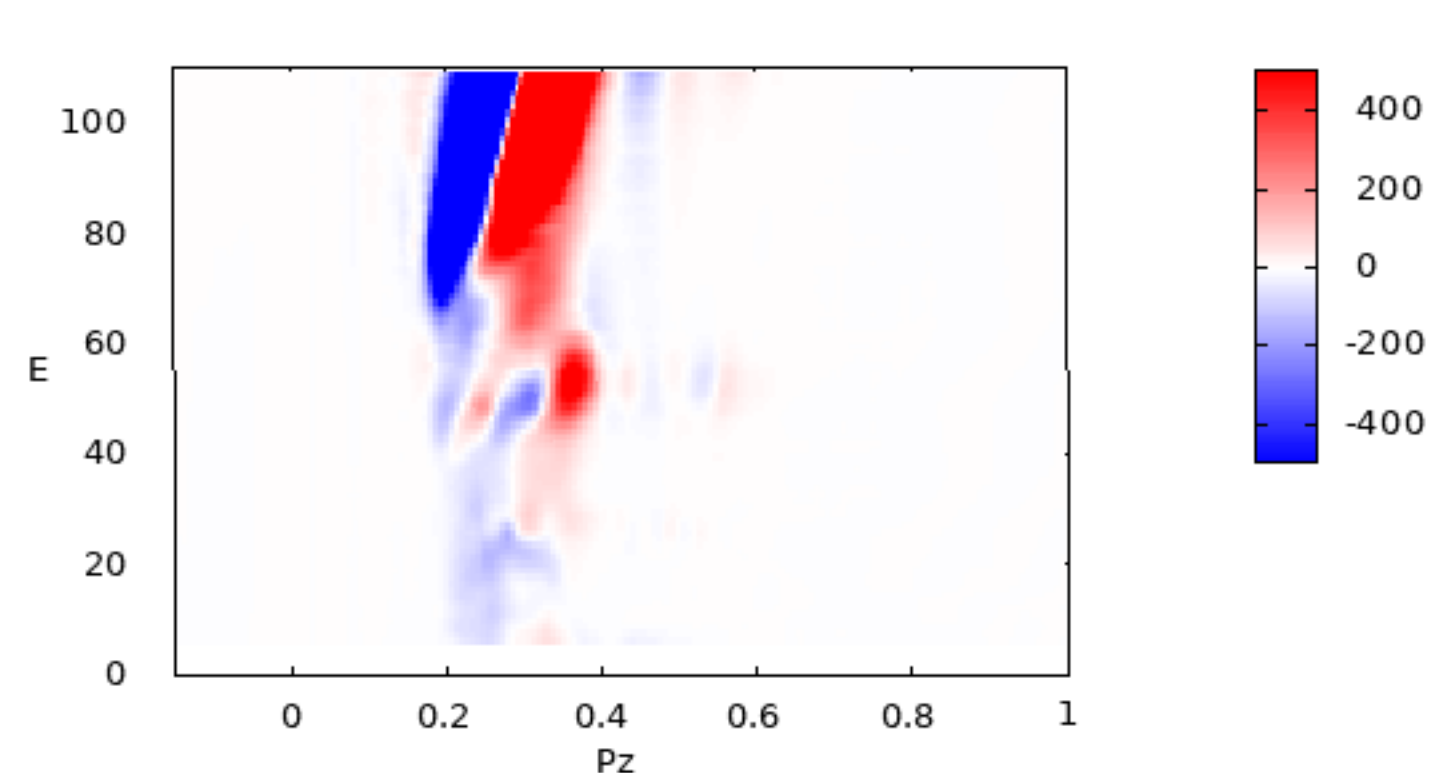


dPz (Pz,E), Lamda=1103

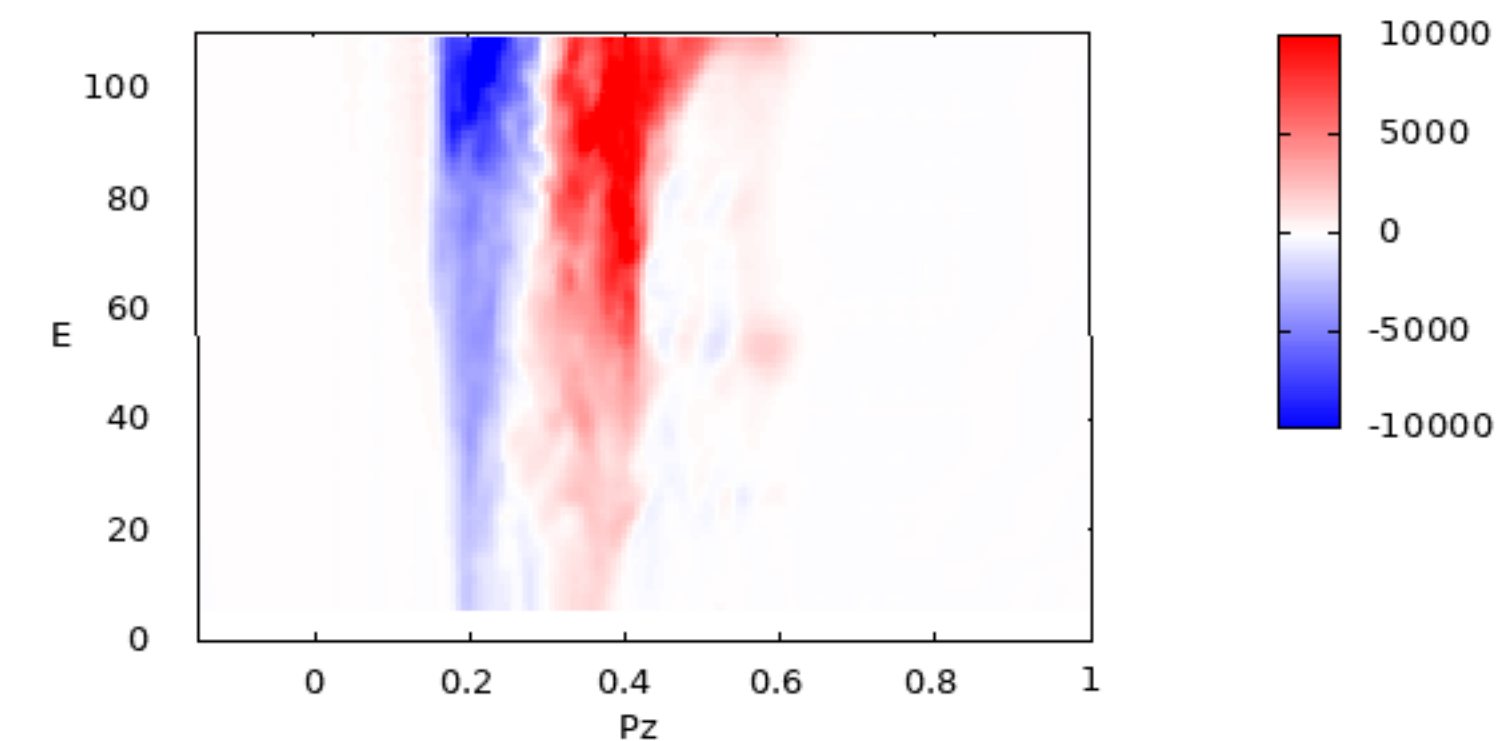
$\Lambda=\mu B/E=1.1$  - trapped



dPz (Pz,E), Lamda=1103



dPz (Pz,E), Lamda=1103



- **comparison of ORB5 and ATEP PSZS starts to be satisfying - most differences understood in detail**
- **multi-mode cases create complex PSZS structures that are not additive - difficult to imagine a simpler model that would capture these effects...**
- **amplitude dependence of PSZS with fixed amplitude ratios found**
- **simple resonances are well represented by ATEP- resolution: 128-256 radial points are necessary**
- **higher order resonances are reliably found - confirmation of zonal and orbit averaging procedures**
- **IMAS framework is now robust for handling PSZS data (HDF5)**
- **runtime for (256x96x96): about 30mins with 64 processes - speed up easily possible; parallel collect of IDSs is demanding part**

**started to implement analytical distribution functions - C. di Troia [NF 2021]**

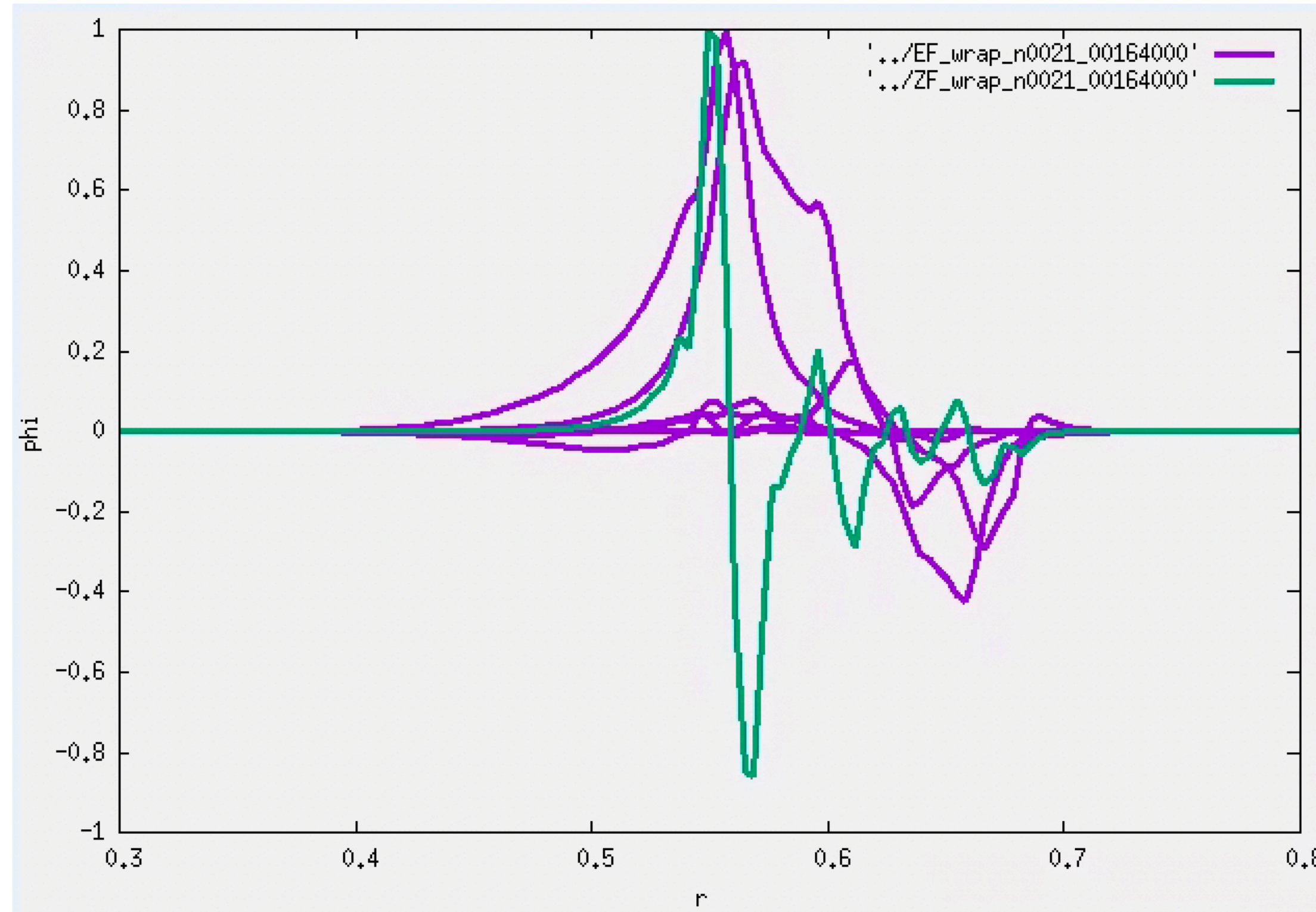
**quantitative benchmark will be possible then**



Z. Qiu [NF 2017]

$$\delta\psi_Z = -\frac{1}{B_0} \frac{k_{\theta,0}}{\omega_0} \frac{\partial}{\partial r} \left( |\hat{A}_0|^2 \sum_m |\Phi_0|^2 \right). \quad (23)$$

to be improved, benchmarked with ORB5  
and use force/beat-driven scalings (or  
spontaneously generated) for saturation  
[Juvert]



101006 TAE, n=21 and related ZFZS (model)

for calculating PSZS response including ZFZS:

using implementation of neoclassical radial E-field in HAGIS by A. Bergman [PoP 2001]

next slides: ad-hoc scaling of  $\Phi_z$  (note 1kV peak value for  $\Phi_z$  gives for this ITER case peak  $E_r \sim 25\text{kV/m}$ )

[Zonca, FEC 2023]

$$\Delta_1 = \frac{\text{propagator } (\omega_G + i\partial_t - l\omega_b - \Delta_1 - \Delta_2)^{-1}}{-ie^{-il\vartheta_c} \left[ e^{iQ_z} (\delta\dot{\theta}_z \partial_\theta + \delta\dot{\mathcal{E}}_z \partial_\varepsilon) \right] e^{il\vartheta_c}}$$

shearing

$$\Delta_2 = \frac{\sum_{l'} e^{-il'\vartheta_c} \left[ e^{iQ_G} (\delta\dot{\theta}_G \partial_\theta + \delta\dot{\mathcal{E}}_G \partial_\varepsilon)^* \right] e^{il'\vartheta_c} \frac{1}{(\omega_{GI} - l'\omega_b)}}}{\times e^{-il'\vartheta_c} \left[ e^{iQ_G} (\delta\dot{\theta}_G \partial_\theta + \delta\dot{\mathcal{E}}_G \partial_\varepsilon) \right] e^{il'\vartheta_c}}$$

resonance broadening & frequency shift



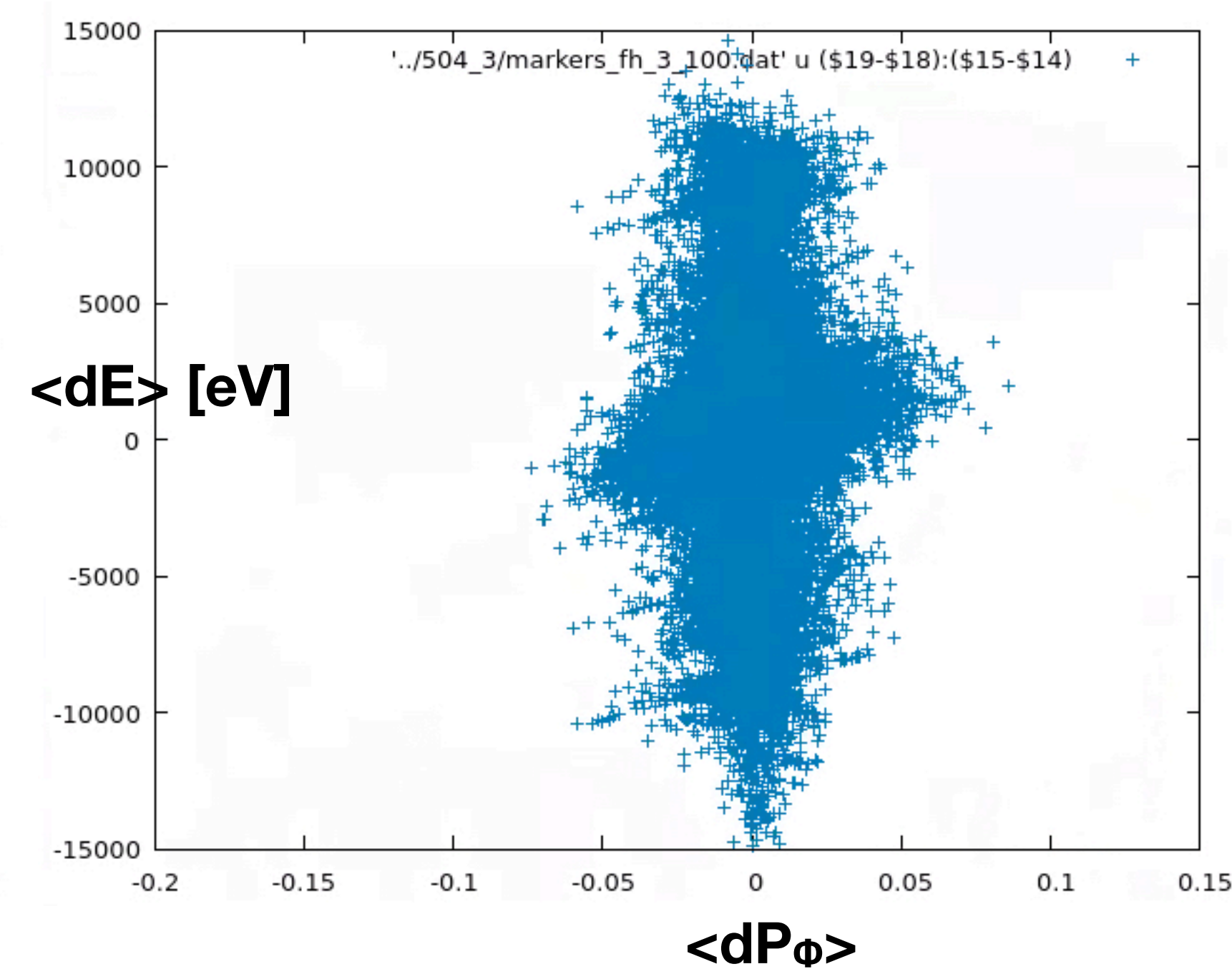
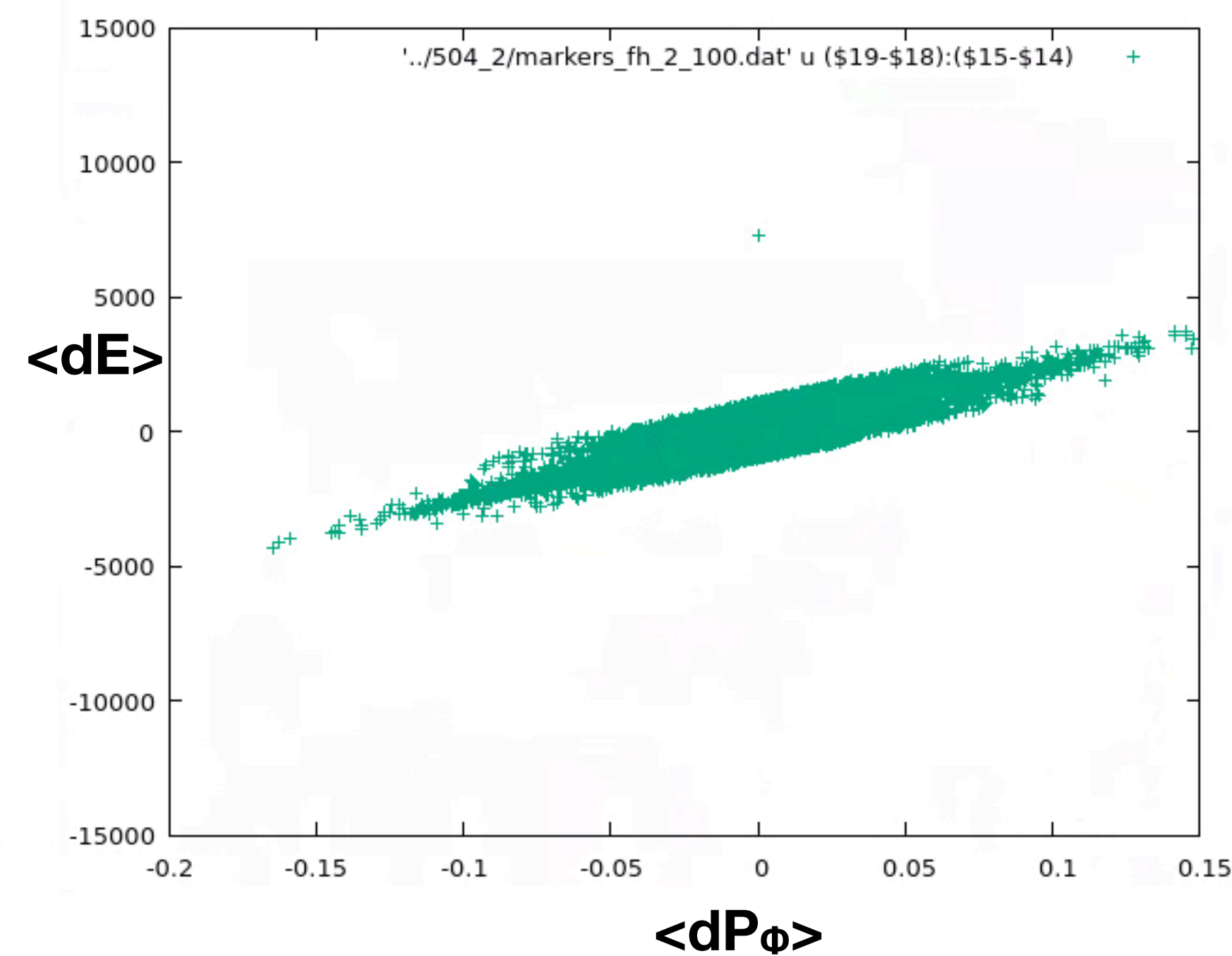
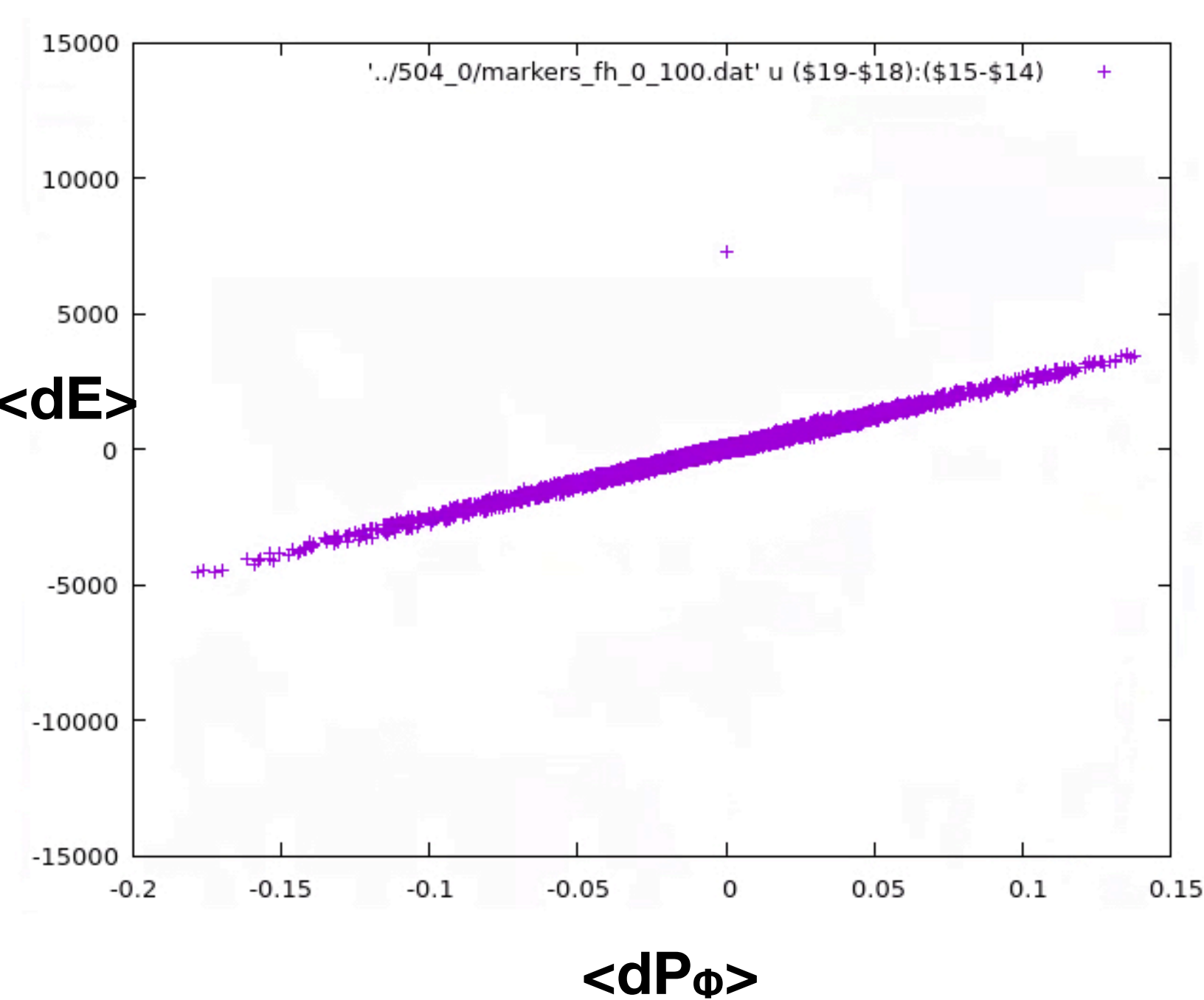
single wave conservation:  $n dE - \omega dP_\phi = 0$

broken in presence of E-field - transport matrix is not strictly diagonal

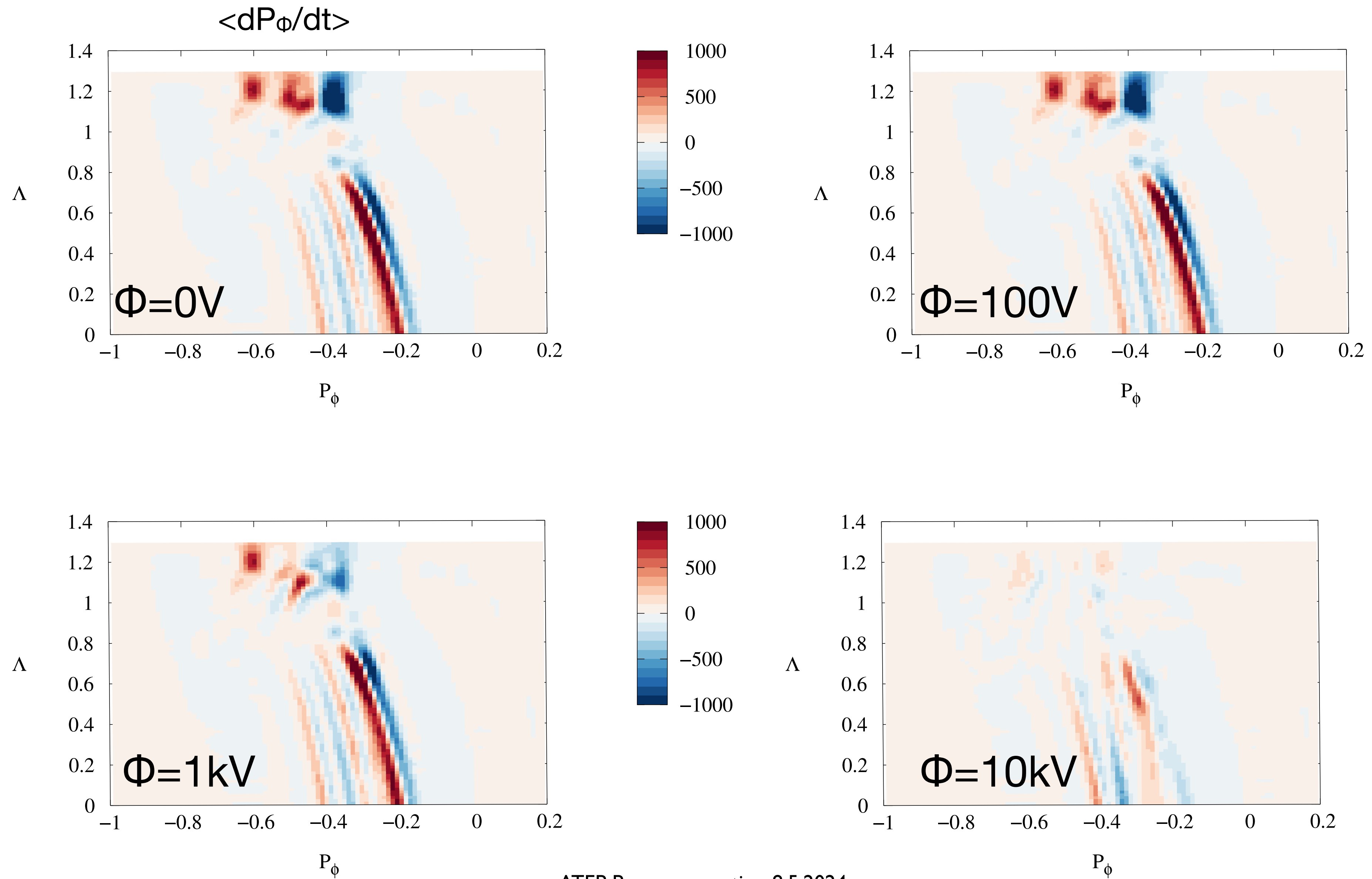
$\Phi=0V$

$\Phi=1kV$

$\Phi=10kV$

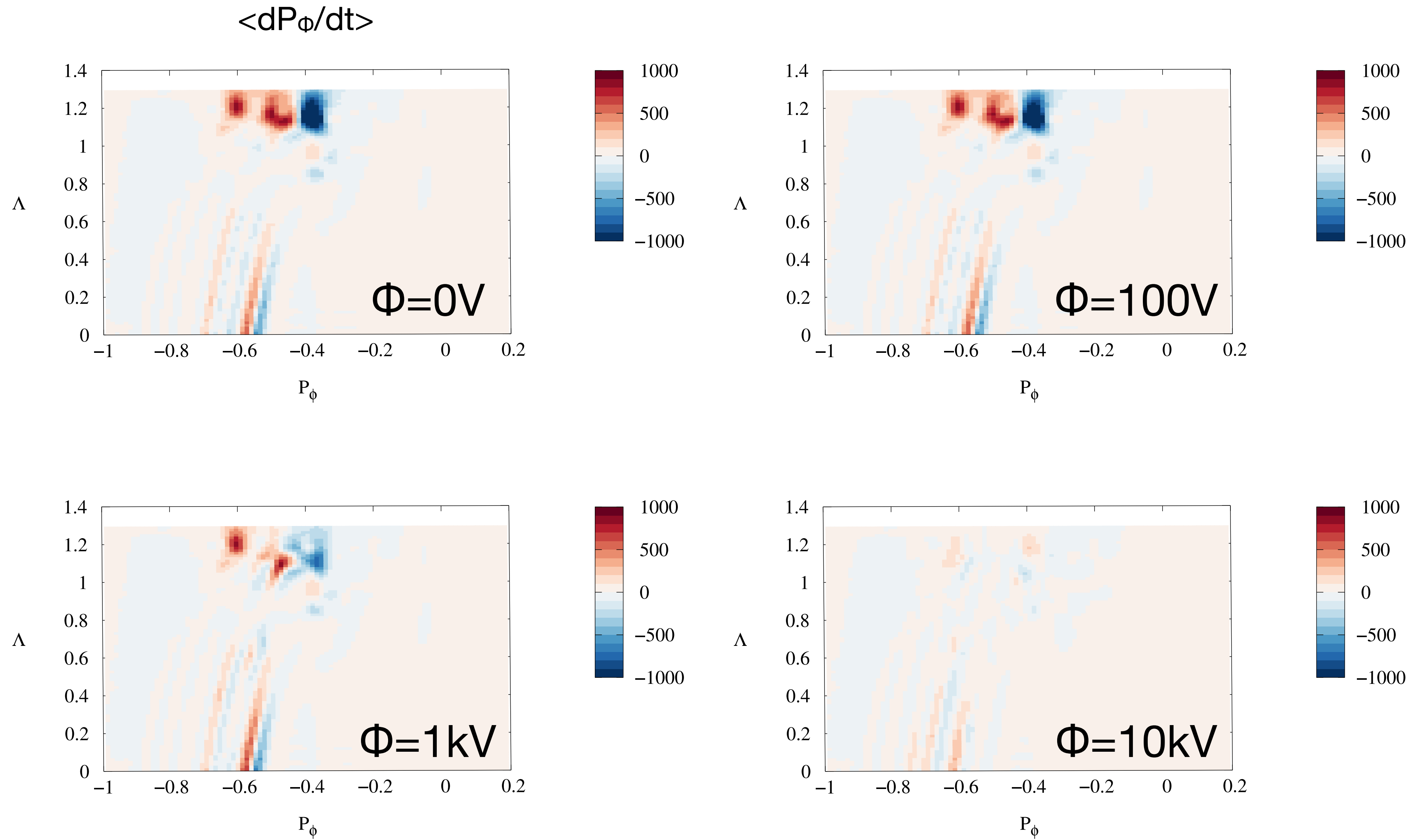


# 750keV co-passing+trapped ions ( $dB/B_{TAE}=1.0e-3$ )



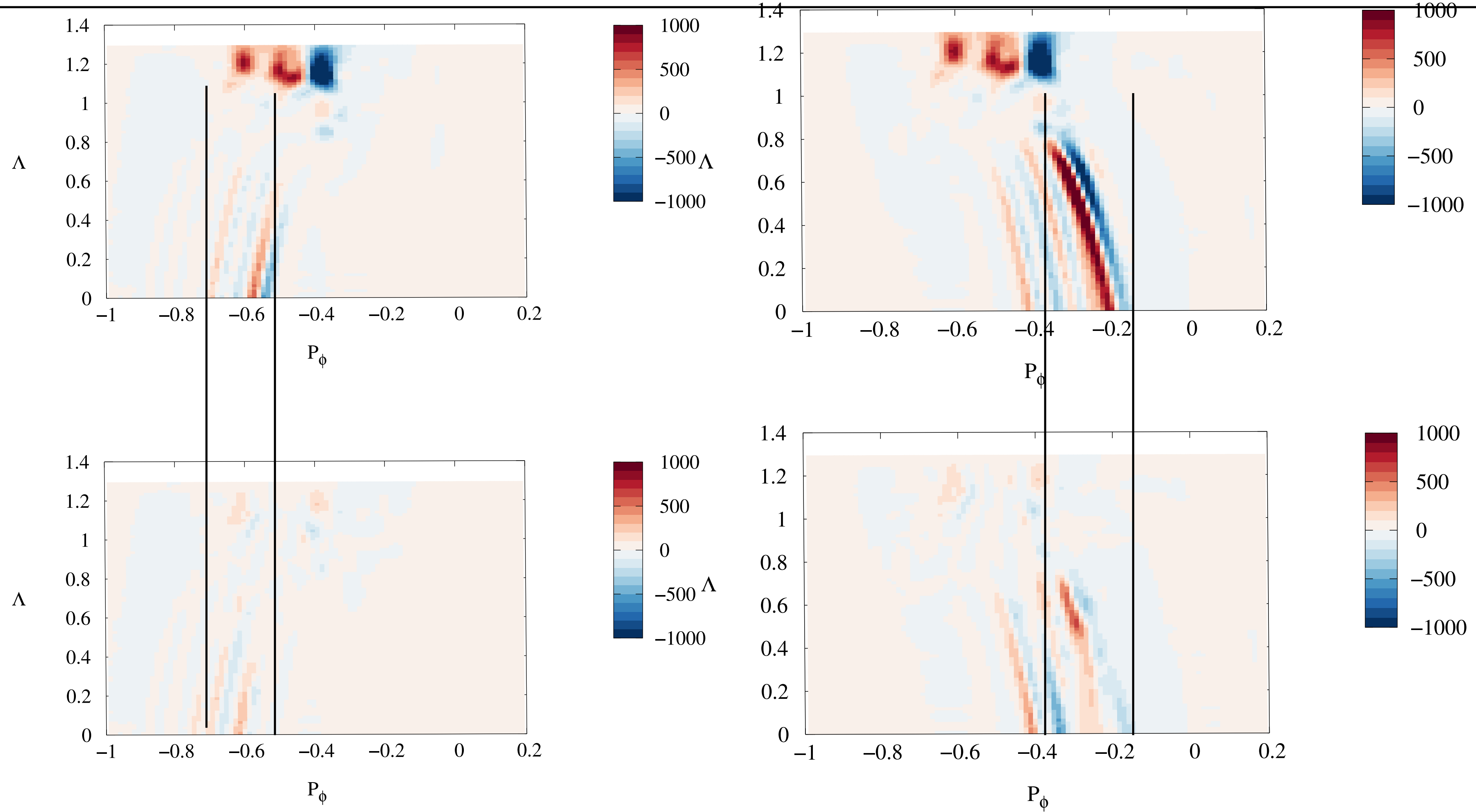


# 750keV counter-passing+trapped ions



# 0 vs 10kV: counter passing

# 0 vs 10kV co-passing



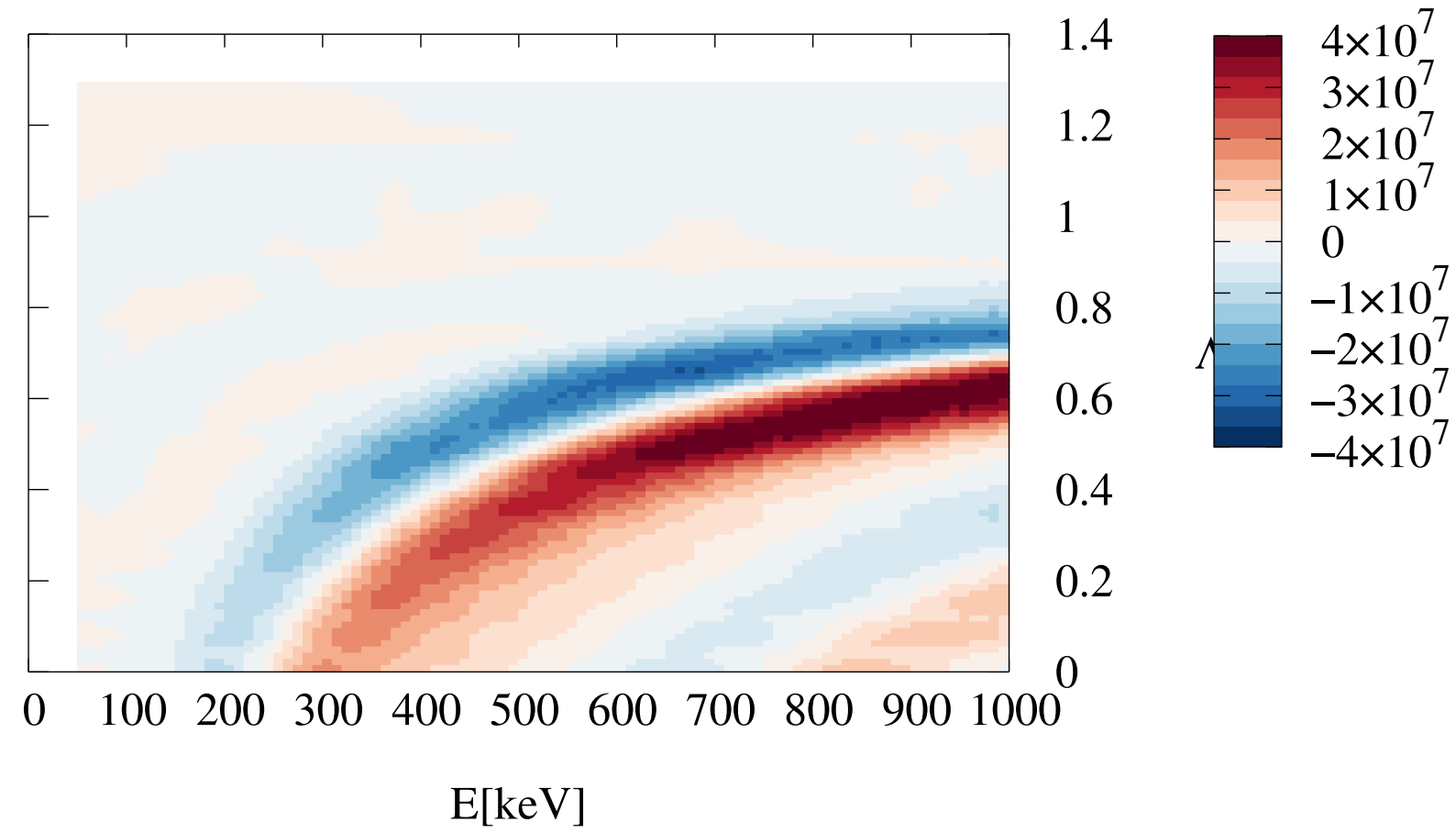
shift and broadening of resonances observed



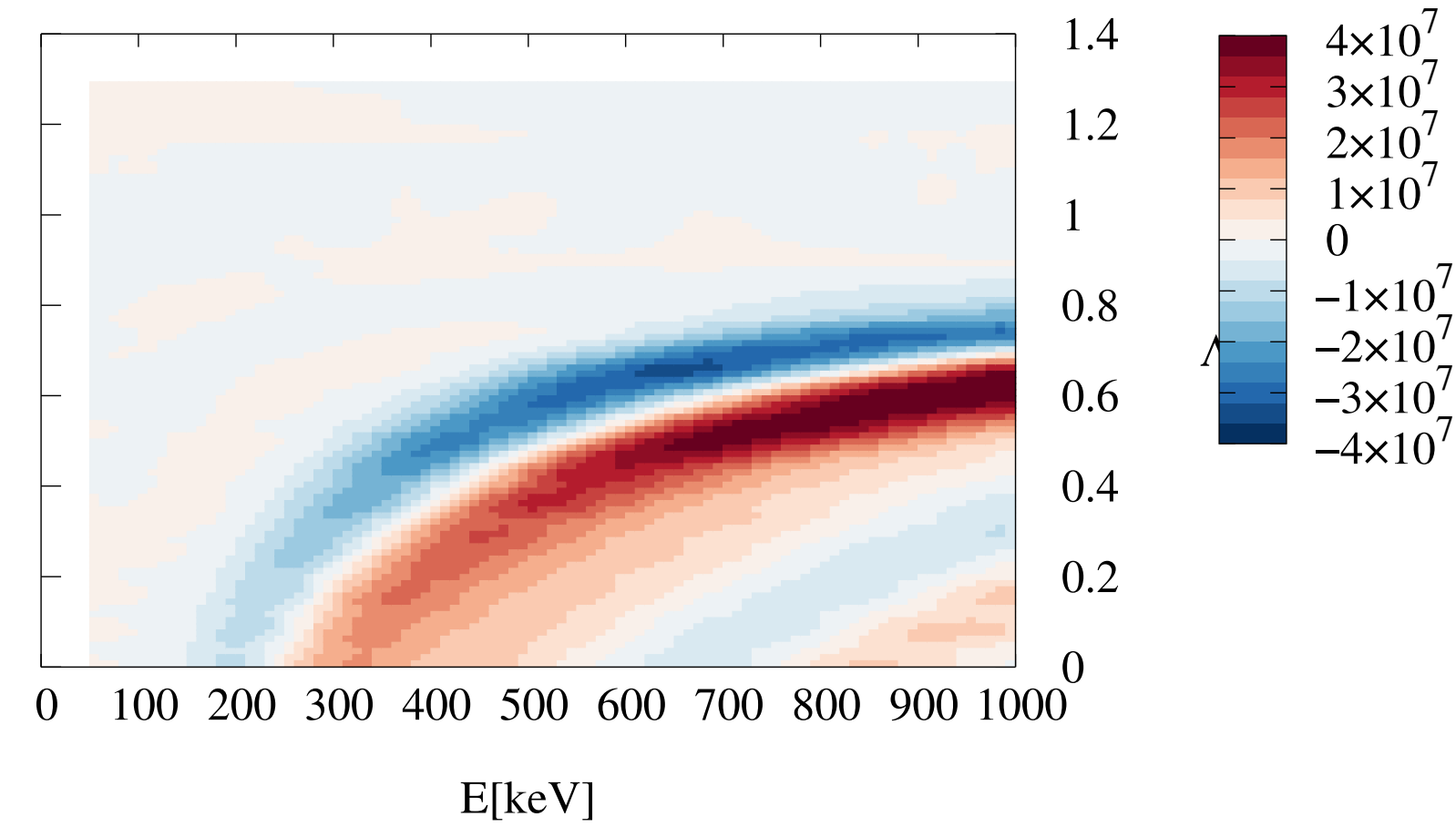
# co-passing+trapped ions, $P_z = -0.29$



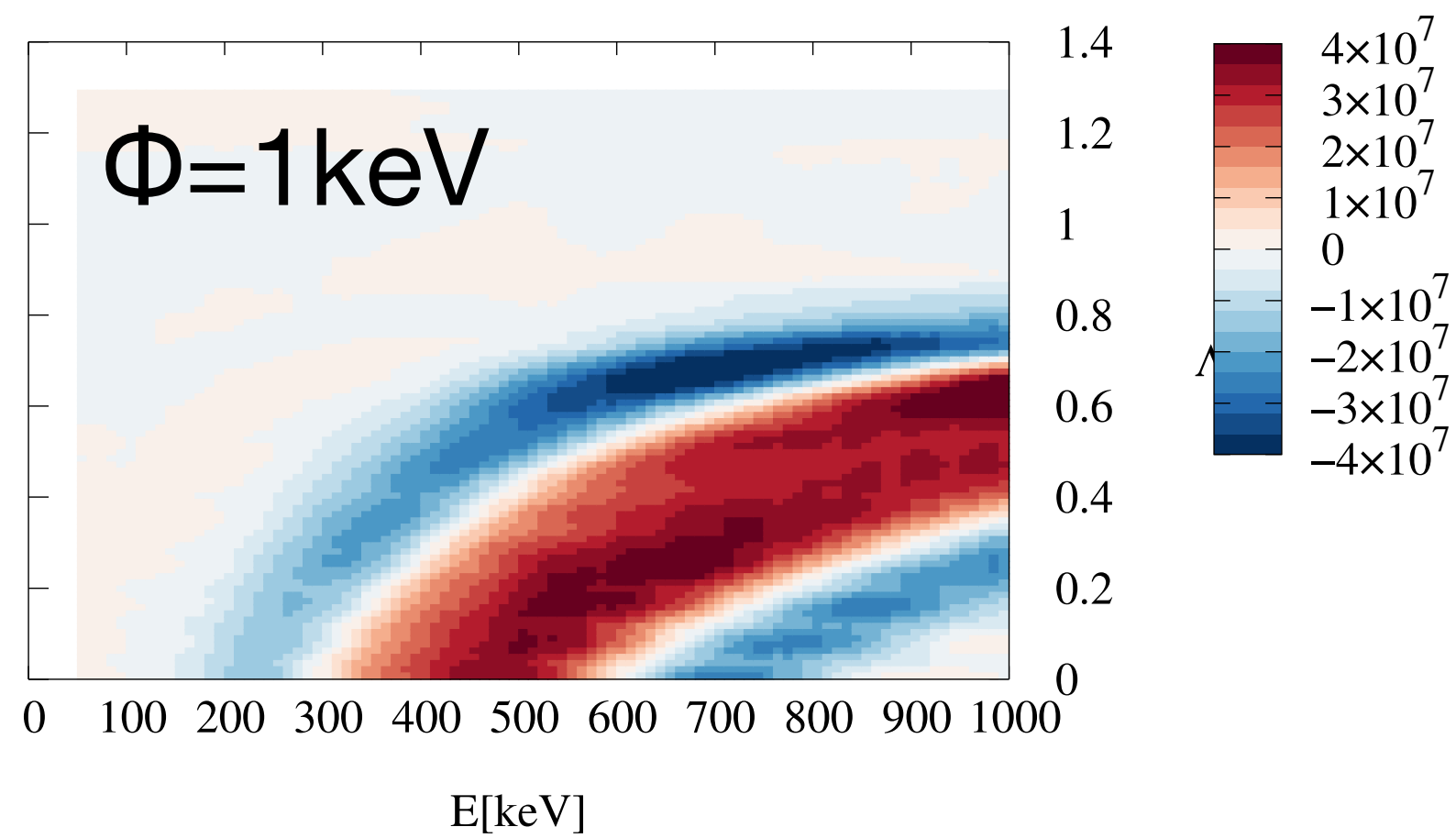
$\Phi = 0V$   $\langle dE/dt \rangle$



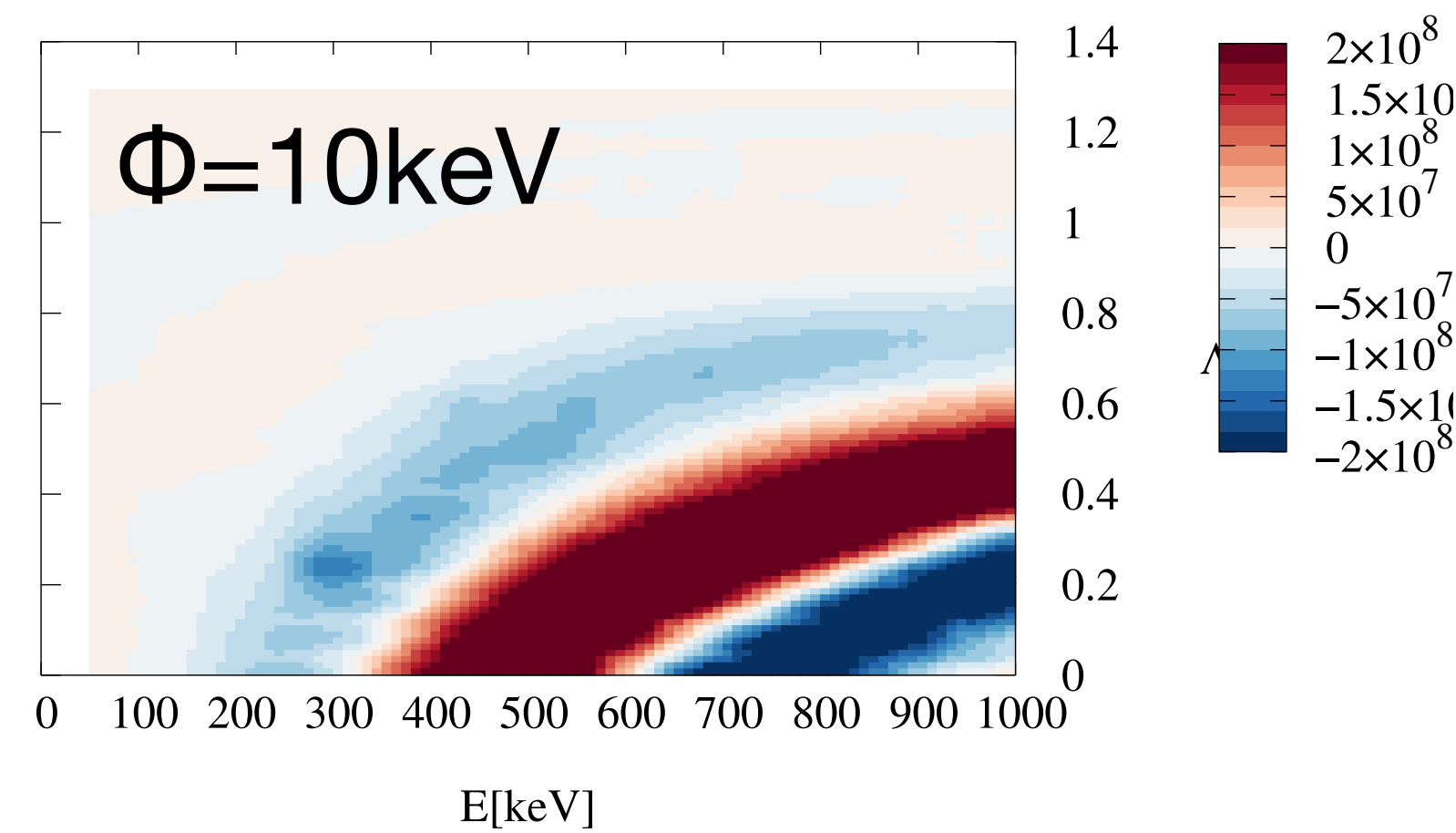
$\Phi = 100V$



$\Phi = 1keV$



$\Phi = 10keV$





## discussion/outlook

- **PSZS formulation gives detail insight into non-linear saturation physics - and can be used to set up a practical reduced model**
- **ready to add ZF evolution to QL model - extend energy balance equation**
- **quantitative studies needed for qualification of reduced model: radial mode structures and saturation amplitude ORB5 scans [Juvert, yesterday]**
- **including higher non-linear harmonics ( $2*n$ ) has been technically prepared**
- **investigate other ZF generation processes (spontaneous excitation)**
- **investigate compatibility with existing transport models: modification of TGLF quenching rule?**