

Latest updates of the SolEdge-HDG code

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OUTLINE

1. The physical models
2. Features
3. The geometries
4. 2D simulations
5. h-adaptivity
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The physical model

The equations considered are:

- Continuity equation

$$\partial_t n + \nabla \cdot (n u \mathbf{b}) - \nabla \cdot (D \nabla_{\perp} n) = \hat{S}_n. \quad (1)$$

- Momentum equation

$$\partial_t (m_i n u) + \nabla \cdot (m_i n u^2 \mathbf{b}) + \nabla_{\parallel} (k_b n (T_e + T_i)) - \nabla \cdot (\mu \nabla_{\perp} (m_i n u)) = \hat{S}_{\Gamma}. \quad (2)$$

- Total ions energy equation

$$\begin{aligned} & \partial_t \left(\frac{3}{2} k_b n T_i + \frac{1}{2} m_i n u^2 \right) + \nabla \cdot \left(\left(\frac{5}{2} k_b n T_i + \frac{1}{2} m_i n u^2 \right) u \mathbf{b} \right) - n u e E_{\parallel} + \\ & - \nabla \cdot \left(\frac{3}{2} k_b (T_i D \nabla_{\perp} n + n \chi_i \nabla_{\perp} T_i) \right) - \nabla \cdot \left(-\frac{1}{2} m_i u^2 D \nabla_{\perp} n + \frac{1}{2} m_i \mu n \nabla_{\perp} u^2 \right) + \\ & - \nabla \cdot (k_{\parallel i} T_i^{5/2} \nabla_{\parallel} T_i \mathbf{b}) + \frac{3}{2} \frac{k_b n}{\hat{\tau}_{ie}} (T_e - T_i) = \hat{S}_{E_i}. \end{aligned} \quad (3)$$

- Total electrons energy equation

$$\begin{aligned} & \partial_t \left(\frac{3}{2} k_b n T_e \right) + \nabla \cdot \left(\frac{5}{2} k_b n T_e u \mathbf{b} \right) + n u e E_{\parallel} - \nabla \cdot \left(\frac{3}{2} k_b (T_e D \nabla_{\perp} n + n \chi_e \nabla_{\perp} T_e) \right) + \\ & - \nabla \cdot (k_{\parallel e} T_e^{5/2} \nabla_{\parallel} T_e \mathbf{b}) - \frac{3}{2} \frac{k_b n}{\hat{\tau}_{ie}} (T_e - T_i) = \hat{S}_{E_e}. \end{aligned} \quad (4)$$

The neutral models

- Diffusive neutrals $\rightarrow N_n$ model

$$\partial_t n_n - \nabla \cdot (D_{n_n} \nabla n_n) = S_{n_n}$$

$$D_{n_n} = \frac{eT_i[eV]}{m_i n (\langle \sigma v_{cx} \rangle + \langle \sigma v_{iz} \rangle)}$$

- Neutral particle conservation + parallel momentum $\rightarrow N_n \Gamma_{n_n}$ model

$$\begin{cases} \partial_t n_n + \nabla \cdot (n_n u_n \mathbf{b} - D_{n_n} \nabla n_n) = S_{n_n} \\ \partial_t (n_n u_n) + \nabla \cdot (n_n u_n^2 \mathbf{b} - \eta \nabla (u_n \mathbf{b})) + \nabla_{\parallel} (n_n k_b T_n) = S_{\Gamma_{n_n}} \end{cases} \quad \eta = \frac{n_n k_b T_n}{m_i n \langle \sigma v \rangle_{cx}}$$

Conservative form of the physical model

$$\begin{cases} \mathcal{Q} - \nabla U = 0 \\ \partial_t \mathbf{U} + (\mathbf{u}_\perp \cdot \nabla) \mathbf{U} + \nabla \cdot \mathcal{F} - \nabla \cdot (D_f \mathcal{Q}) + \nabla \cdot (D_f \mathcal{Q} \mathbf{b} \otimes \mathbf{b}) - \nabla \cdot \mathcal{F}_t + \mathbf{f}_{E\parallel} + \mathbf{f}_{EX} - \mathbf{g} = \mathbf{s} \end{cases}$$

where the vector of conservative variable \mathbf{U} and its gradient \mathcal{Q} are defined as:

$$\mathbf{U} = \begin{bmatrix} U_1 \\ U_2 \\ U_3 \\ U_4 \\ U_5 \end{bmatrix} = \begin{bmatrix} n \\ nu \\ nE_i \\ nE_e \\ n_n \end{bmatrix} \quad \mathcal{Q} = \nabla \mathbf{U} = \begin{bmatrix} U_{1,x} & U_{1,y} \\ U_{2,x} & U_{2,y} \\ U_{3,x} & U_{3,y} \\ U_{4,x} & U_{4,y} \\ U_{5,x} & U_{5,y} \end{bmatrix} = \begin{bmatrix} \nabla U_1^T \\ \nabla U_2^T \\ \nabla U_3^T \\ \nabla U_4^T \\ \nabla U_5^T \end{bmatrix} .$$

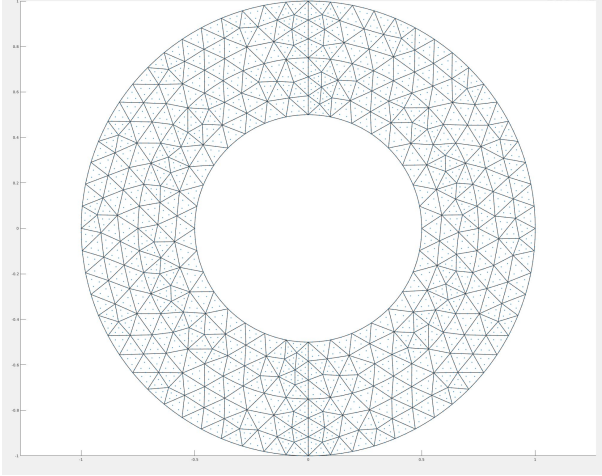
SolEdge-HDG features:

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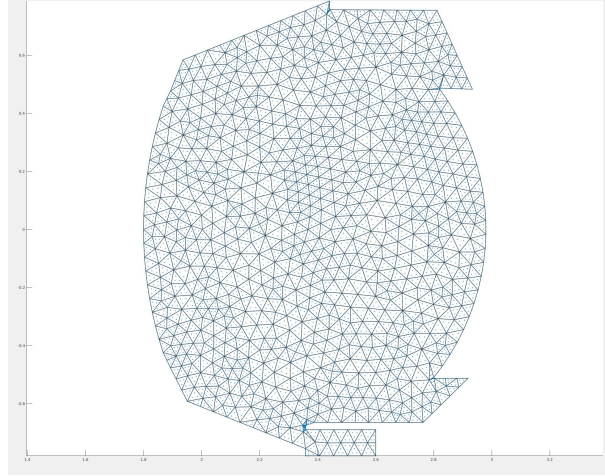
1. Fully **implicit time** scheme
2. **2 plasma models + 2 neutral models** (nGamma, nGammaTiTe, nGammaTiTeNeutrals) + **1 turbulent k-ε model**
3. **Solvers:**
 - a. **Direct:** PASTIX/PETSc (always works)
 - b. **Iterative:** PETSc/PSBLAS (only works for 2D dt < 1e-5, condition # too high)
4. **Dimensions:**
 - a. 2D: always works, robust
 - b. 3D: only works for Circular Limiter case or very simple WEST coarse meshes (condition # too high)
5. Handling **any type of geometry**, from CORE to WALL.
6. Handling of **Ohmic Heating** and **Puff + ad hoc additional heating**
7. Handling **variable magnetic equilibrium**
8. **h-adaptivity**
9. **Speed** and **parallelizability:**
 - a. **OPENMP** example: 20 threads, 28k elements p4 triangles, 5 equations, 1M nDoF, 1 minute per matrix inversion. 2h for D = 26 → 1 m2/s simulation.
 - b. **OPENMPI** example: 24 processes, 6 threads/proc, 36k elements p6 quadrangles, 6 equations, 10M nDof, 50s per inversion, 72h for ramp up ITER discharge.

Geometries

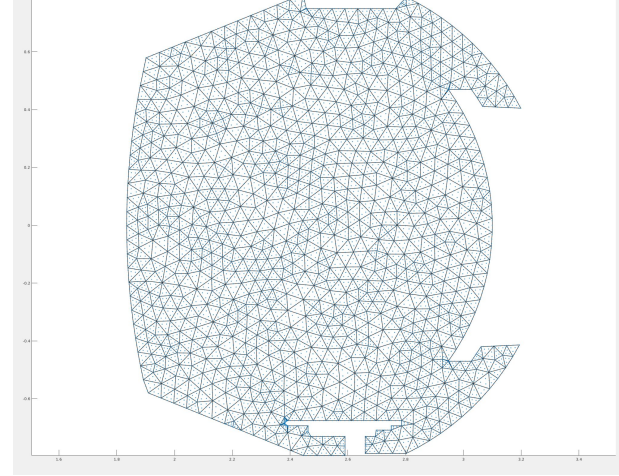
Circular Limiter case P4



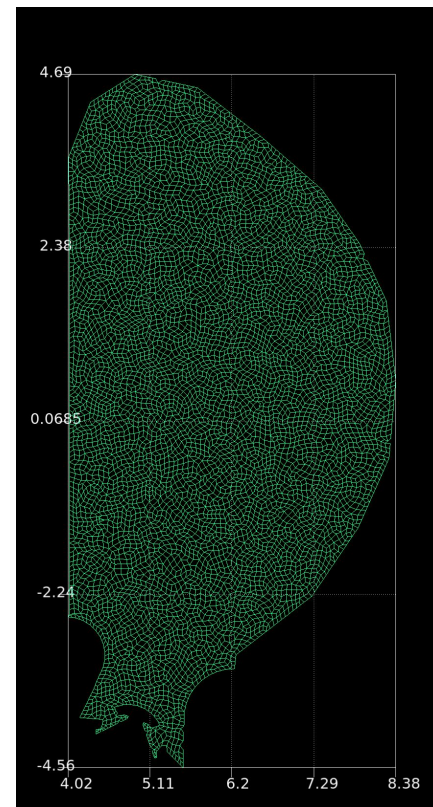
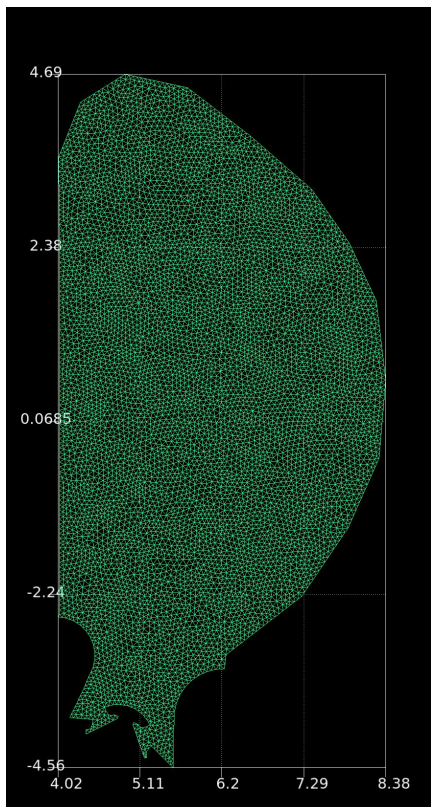
WEST divertor case P4



WEST divertor case P4

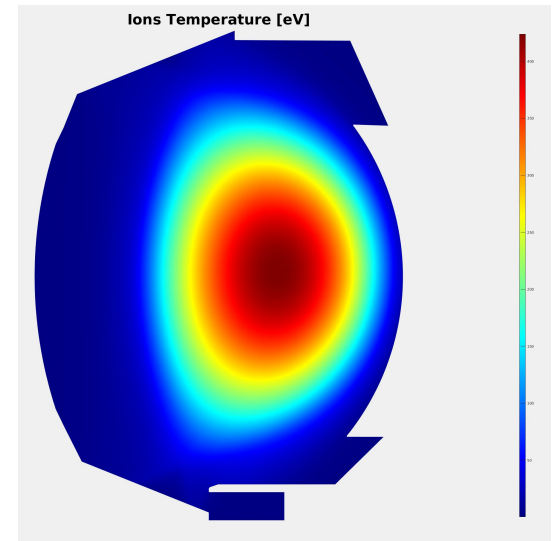
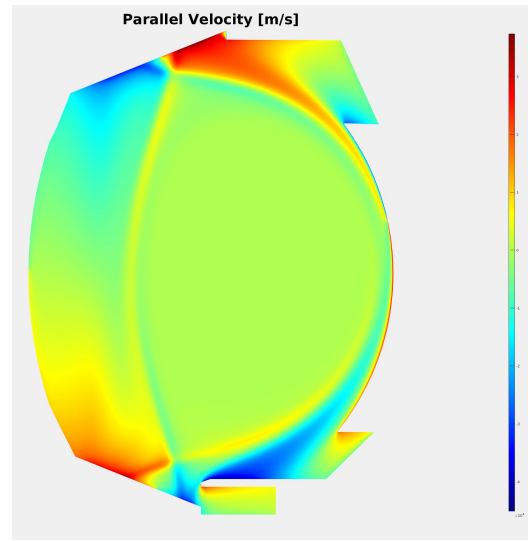
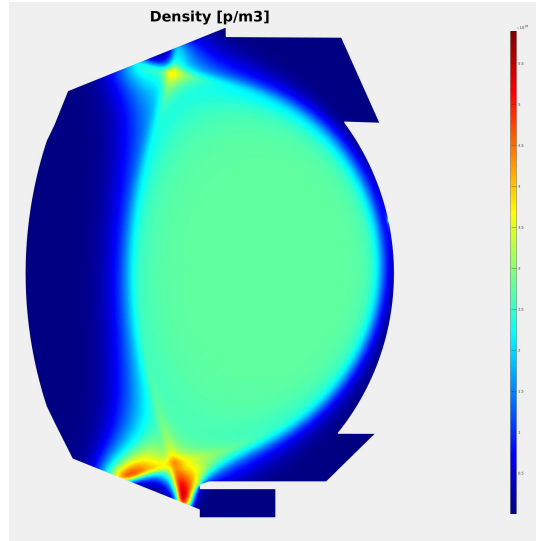


Geometries: ITER triangles and quadrangles

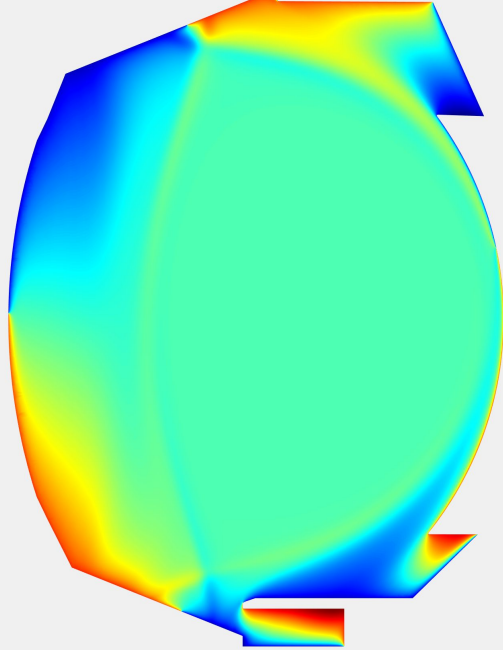


2D WEST simulations

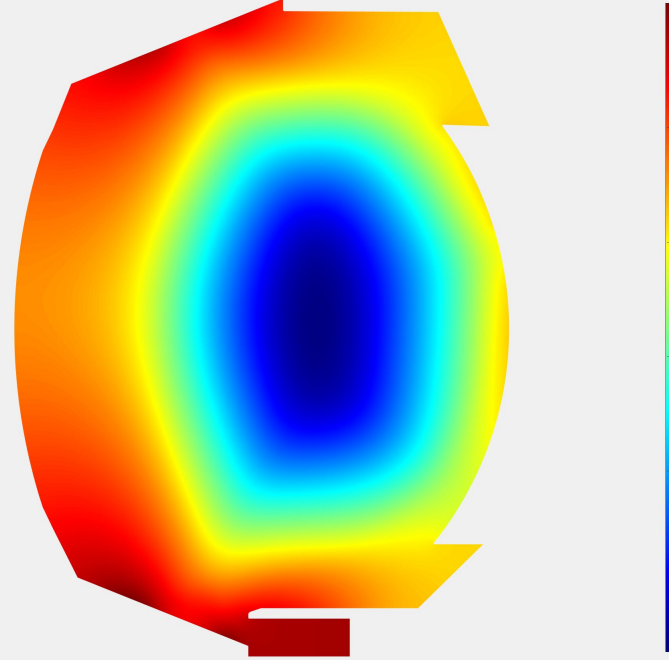
SolEdge-HDG is a robust code for 2D simulations. Here is an example of a 2D steady state WEST simulation with NGammaTiTe with diffusive neutrals model at 1 m2/s:



Mach

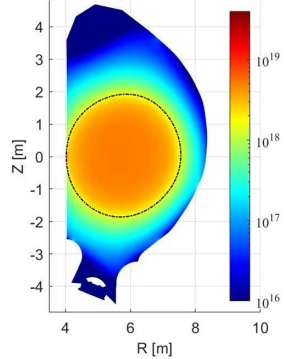


Log10 Neutral density [p/m3]

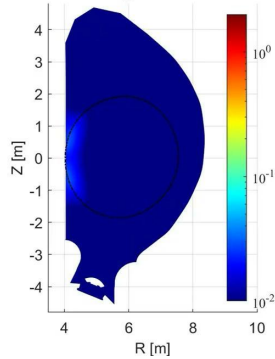


2D ITER ramp up discharge phase

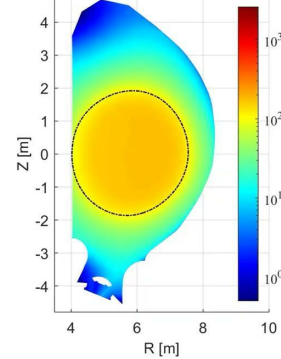
#135011 n_p [m⁻³] t = 0.050 s



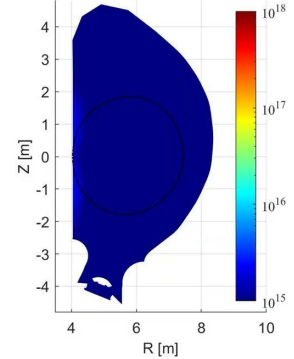
#135011 P_n [Pa] t = 0.050 s



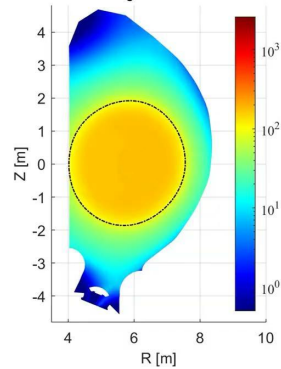
#135011 T_i [eV] t = 0.050 s



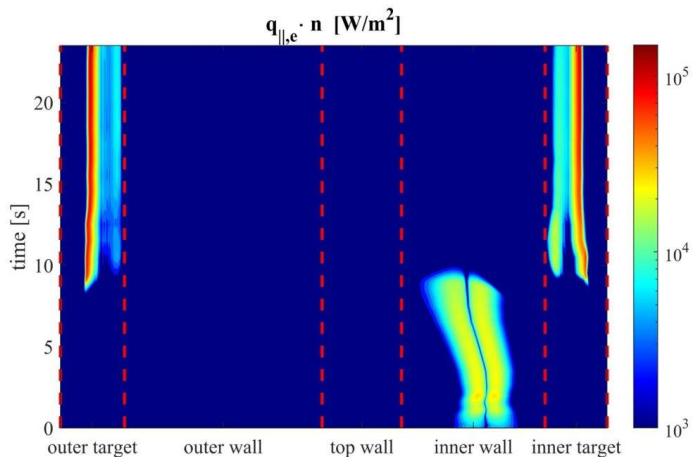
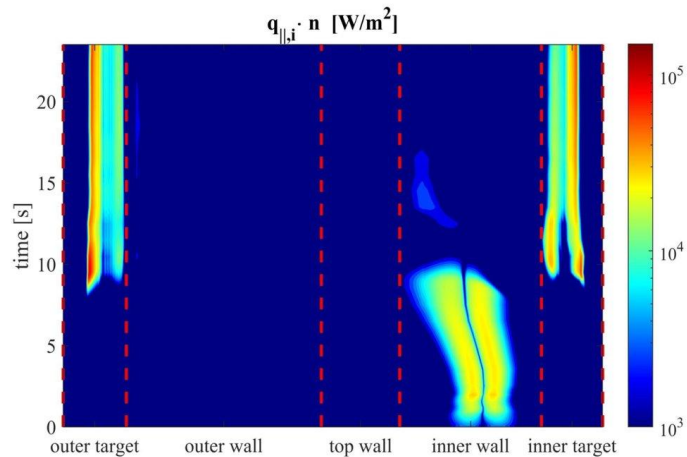
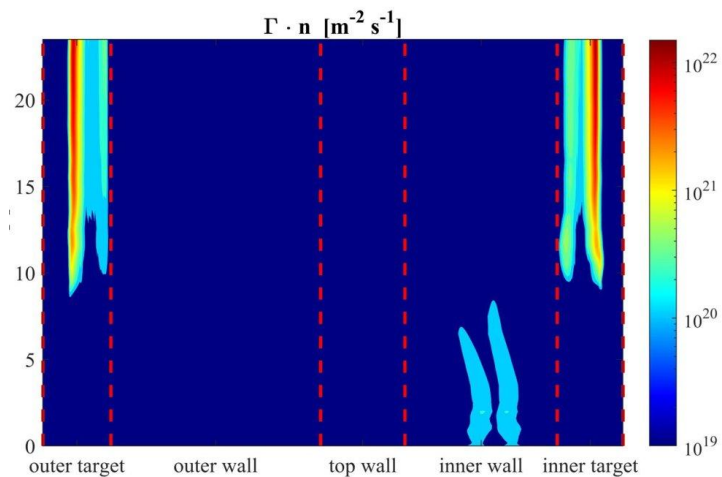
#135011 n_n [m⁻³] t = 0.000 s



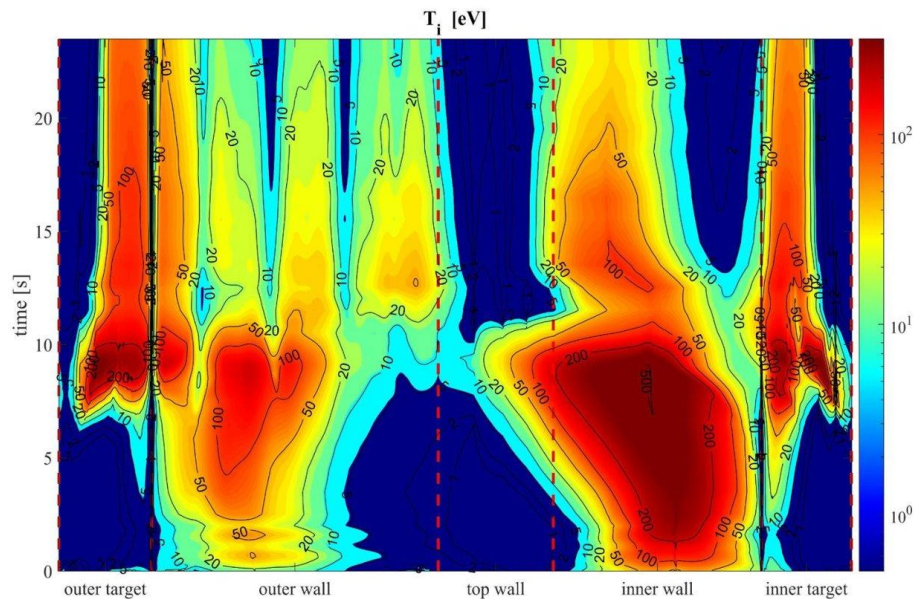
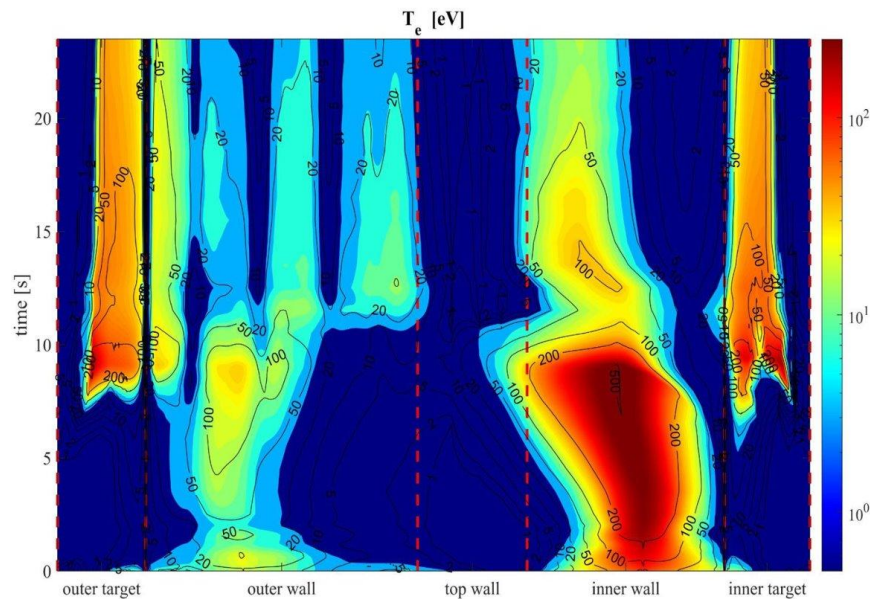
#135011 T_e [eV] t = 0.050 s



Spatio-Temporal Map of plasma quantities at wall coordinates: General Overview



Spatio-Temporal Map of plasma quantities at wall coordinates: General Overview



h-Adaptivity

SolEdge-HDG has recently been equipped with **h-adaptivity**:

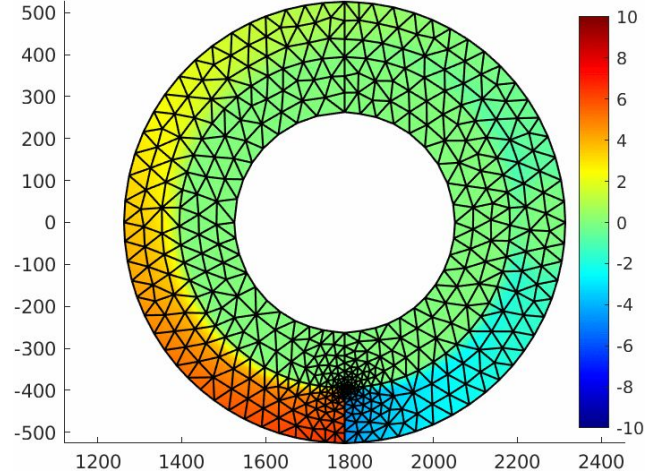
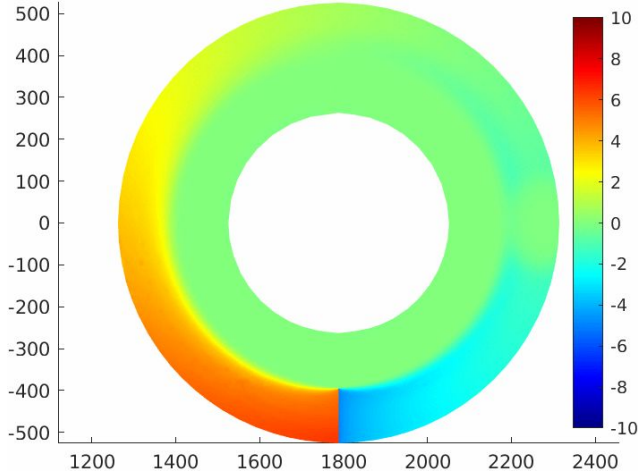
1. the mesh is **locally refined** where and when spurious oscillations are detected on the physical variables and/or their gradient (**error indicator**)
2. the mesh is **locally refined** in order to achieve a input value of relative difference between the physical variables of the solution at order p and its projection at order $p + 1$ (**error estimator**)

This allows to to:

1. **create meshes** of any given number of elements just by changing the input relative difference of the estimator
2. **refine only where is needed** in order to avoid costly overrefinement (more robust, fast and computationally cheaper) and save user time

Results on h-adaptivity: circular case

The first tests were made on the **NGamma** model, starting with a steady state solution and adding a gaussian density “**blob**” close to the separatrix. The system is then left evolve in time. Refinement is performed either every **t time steps** or when the **NR scheme diverges**.



Steady state work flow:

Before adaptivity:

- do a few time steps to initialize
- start steady state simulation at $D = 26 \text{ m}^2/\text{s}$
- simulation crashes
- manually create a new mesh
- repeat n times
- convergence to desired D

With adaptivity:

- do a few time steps to initialize
- start steady state simulation at $D = 26 \text{ m}^2/\text{s}$
- let adaptivity handle the crashes and the remeshing
- convergence to desired D

Results on h-adaptivity: WEST case, reducing diffusion (D)

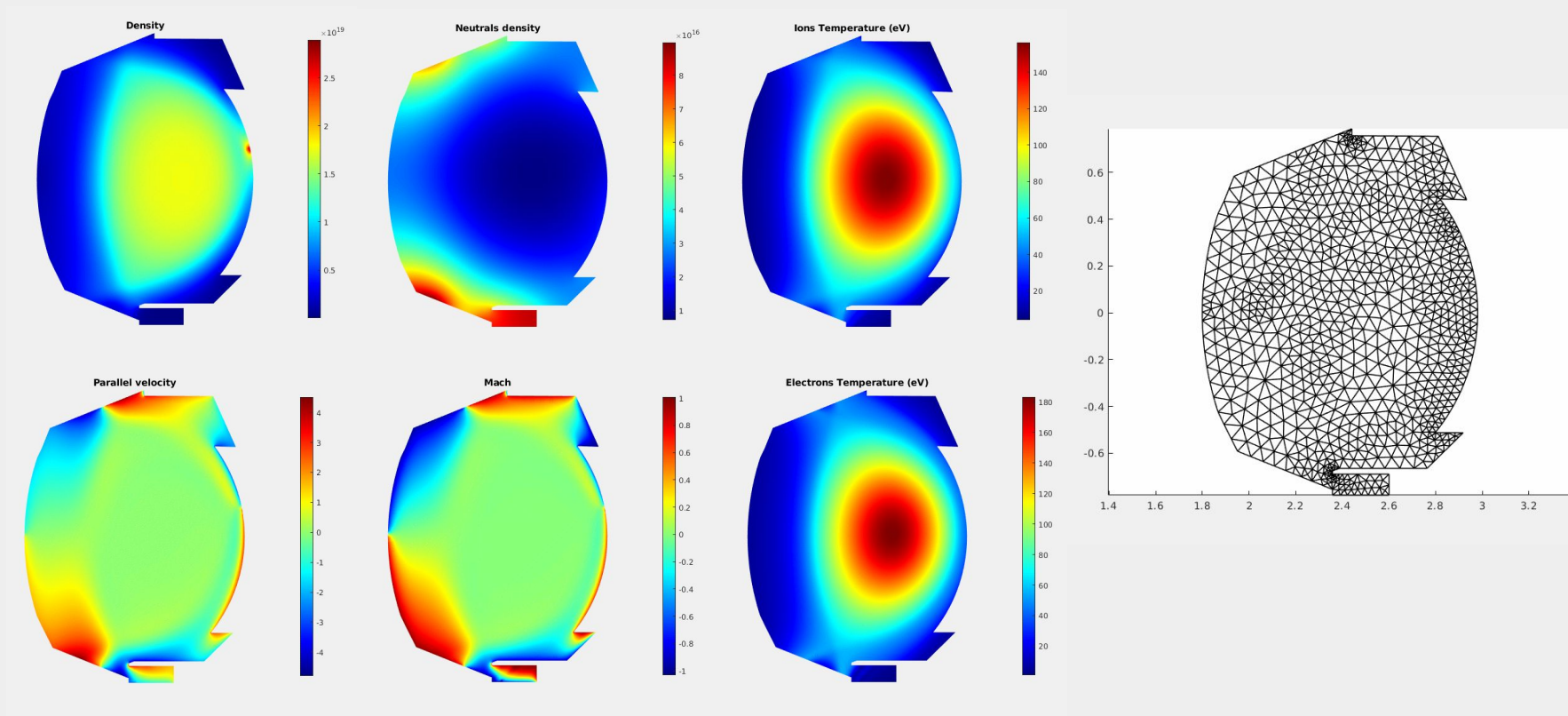
Model: **NGammaTiTe** with **diffusive neutrals**.

The simulation is started at **D = 26** m²/s and then **progressively reduced** till **D ~ 0.37** m²/s.

Adaptivity is called every time diffusion is reduced and in case of divergence of NR scheme.

The **error estimator** is based on the **Mach** number while the **error indicator** is based on **all physical variables**.

Results on h-adaptivity: WEST case



Conclusions

SolEdge-HDG is a **robust, fast** and highly **parallelizable** high order code that allows to compute **steady** or **transient** simulations on **any geometry** and **magnetic field** configuration.

The **fully implicit** scheme allows **fast steady state simulations**.

So far, for practical uses, only the **2D** version is **performant**, problems with the condition number hinder the possibility to use the 3D version.

The newly implemented **h-adaptivity** is a valuable tool to improve code **robustness, speed, precision** and save user and machine **time** and **resources**.

Thank you for your attention

Questions:

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