

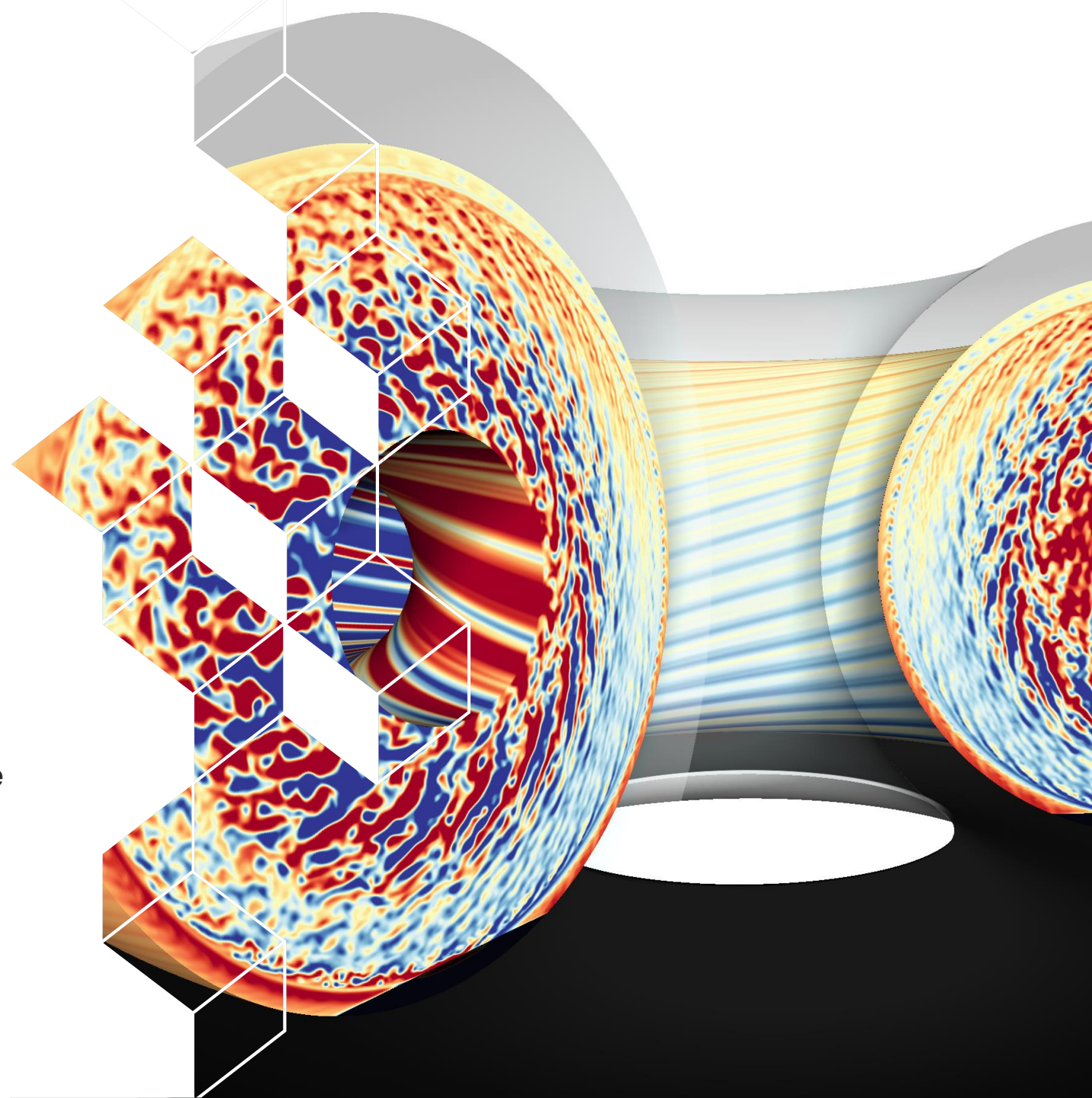


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Towards a better edge description in gyrokinetic simulations: plasma-wall and plasma-neutral interaction

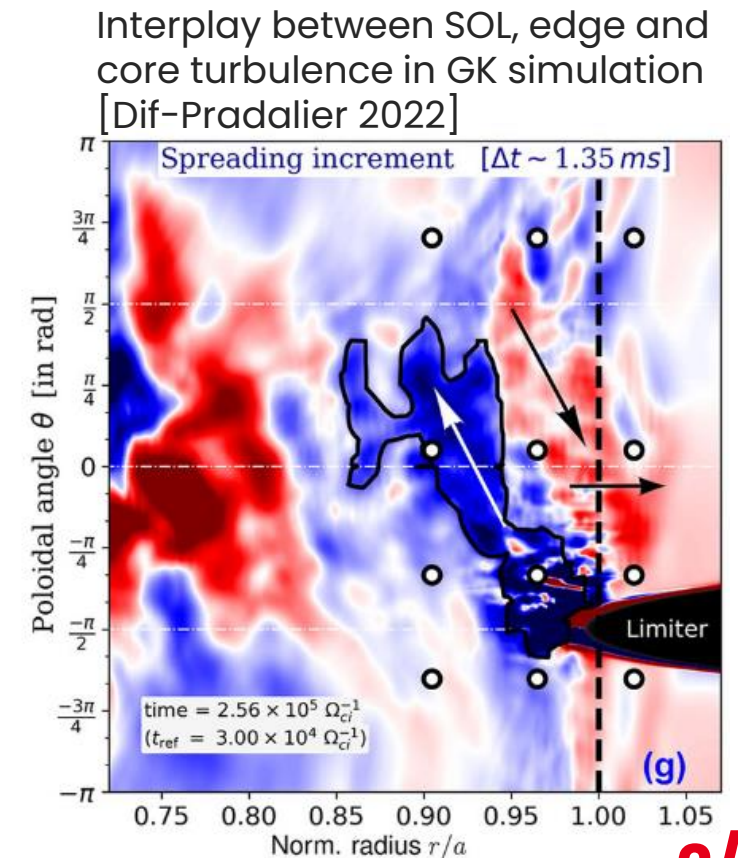
Y. Munsch, G. Dif-Pradalier, Y. Sarazin and the Gysela team

TSVV4 annual meeting – 17th October 2024



Motivation: Scrape-Off Layer conditions influence turbulence in edge plasmas

- Turbulence: main mechanism that degrades confinement in tokamaks [Wootton 1990]
- Turbulence can be regulated by ExB sheared flows in edge. Sheared flows are related to transport barrier formation [Diamond 2005] [Wagner 1982]
 - Importance of correct edge description
- Plasma-wall interaction influences SOL & edge conditions
 - Interplay between SOL, edge & core [Dif-Pradalier 2022]
 - SOL radial electric field $E_r \propto -\nabla T_e/e \rightarrow$ **sheath** [Stangeby]
 - Recycling of 99% of incoming plasma particles at wall \rightarrow **plasma-neutral interaction**
- Goal: include plasma-wall & plasma neutral interaction within gyrokinetic turbulent simulations



Outline

1. Plasma-neutral interaction

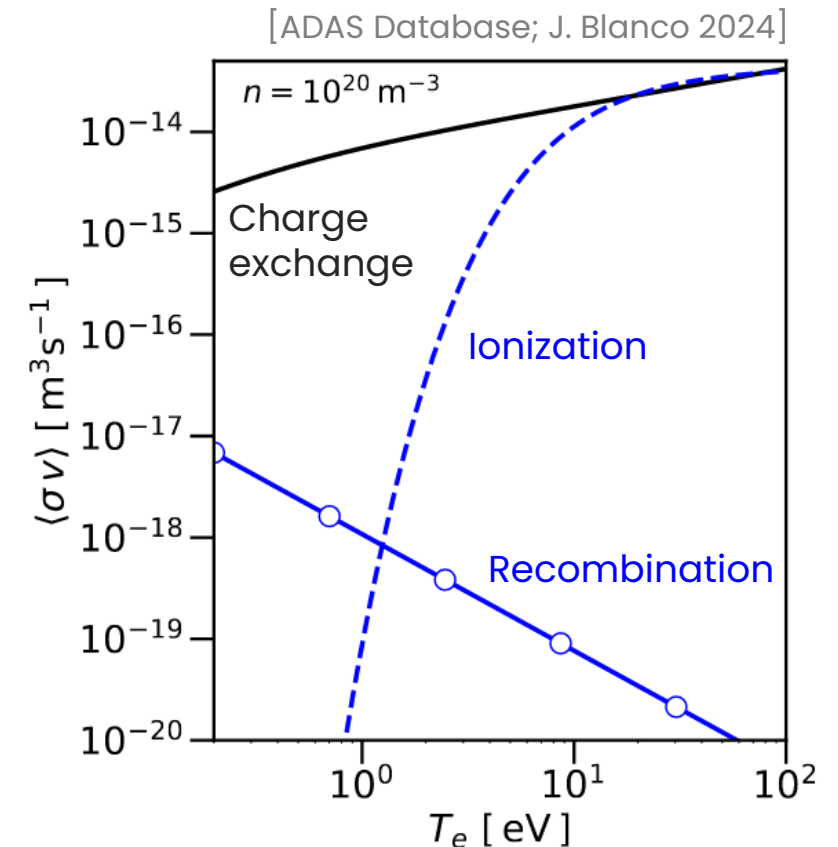
- coupling of a **fluid neutral model** with **kinetic plasma** description
- proof of principle in VOICE code (1D-1V kinetic Vlasov + Poisson)
- Follow-up: integration in gyrokinetic GYSELA framework (PhD starting in November)

2. Plasma-wall interaction in gyrokinetics: two subgrid sheath models

- **Axisymmetric limiter**
- **Non-axisymmetric limiter**
- Implementation in 5D (3D-3V) gyrokinetic code GYSELA

Plasma-neutral interaction reactions, and integration within (gyro) kinetic framework

- Fluid neutrals within gyrokinetic code: reduced computational time compared to kinetic neutrals
 - Validity of fluid model: neutral mean free path $\lambda_{\text{mfp}} \ll L$ system length ($K_n = \lambda_{\text{mfp}}/L \ll 1$)
 - Plasma-neutral interaction in VOICE (1D-1V Vlasov-Poisson) prior to GK code GYSELA
- Plasma-neutral interaction physics
 - Considered reactions: **charge-exchange, ionization & recombination**
 - Reaction rates from ADAS database + polynomial fit



A fluid model for neutrals with an advective-diffusive transport term (“pressure-diffusion” model) [Horsten 2017] [Uytven 2022] [Quadri 2023]

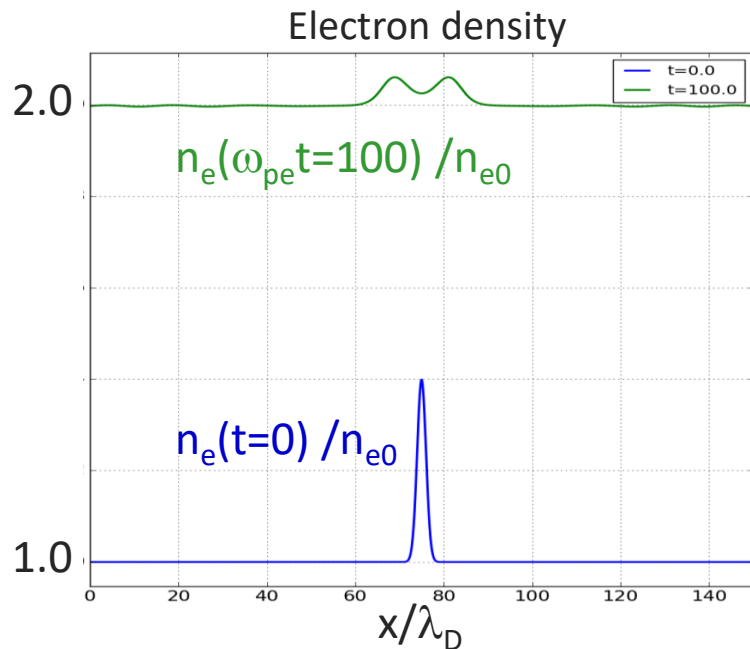
- Pressure-diffusive model for neutrals (convective-diffusive transport)
 - No energy balance eq. solved for neutral $T_N = T_i$
 - Closure on pressure gradient $\nabla p_N = \underbrace{(n_N \langle \sigma v \rangle_{cx} + n_e \langle \sigma v \rangle_r) m_i n_i \mathbf{u}_i - (n_i \langle \sigma v \rangle_{cx} + n_e \langle \sigma v \rangle_i) m_N \mathbf{\Gamma}_N}_{\text{Momentum source term (charge exch, ion. \& recomb.)}}$
 - Leads to $\mathbf{\Gamma}_N = n_{N,eq} \mathbf{u}_i - D_{N,p} \nabla p_N$ with $n_{N,eq} = \frac{n_i n_e \langle \sigma v \rangle_r + n_N n_i \langle \sigma v \rangle_{cx}}{n_i \langle \sigma v \rangle_{cx} + n_e \langle \sigma v \rangle_i}$ and $D_{N,p} = \frac{1}{m_N (n_i \langle \sigma v \rangle_{cx} + n_e \langle \sigma v \rangle_i)}$
 - Eq. solved: neutral **particle balance** $\partial n_N + \nabla \cdot \mathbf{\Gamma}_N = S_{N,n} = n_i n_e \langle \sigma v \rangle_r - n_N n_e \langle \sigma v \rangle_i$
- Coupling to Vlasov equation (kinetic plasma)
 - Key point: "1 neutral \leftrightarrow 1 ion + 1 electron" $\rightarrow \frac{DF_s}{Dt} = \dots + S_N$ with $\int dv S_N = -S_{N,n}$
 - S_N pure source of density constructed using basis of Hermite polynomials [Sarazin 2011]

Proof of principle in 1D-1V Voice code, next: extension to GYSELA

Simulation settings

- $\lambda_{\text{mfp}} = v_{T_N} / n_0 \langle \sigma v \rangle_{\text{CX}} \approx 10^4 \lambda_D \rightarrow$ reaction rates artificially increased to that $\lambda_{\text{mfp}} \approx \lambda_D$ (keeping the **ratio between rates unchanged**)
- Temperature ≈ 10 eV \rightarrow ionization & charge exchange dominate
- $t=0$: localized bump of ions & electrons (\rightarrow Langmuir waves) + constant n_N

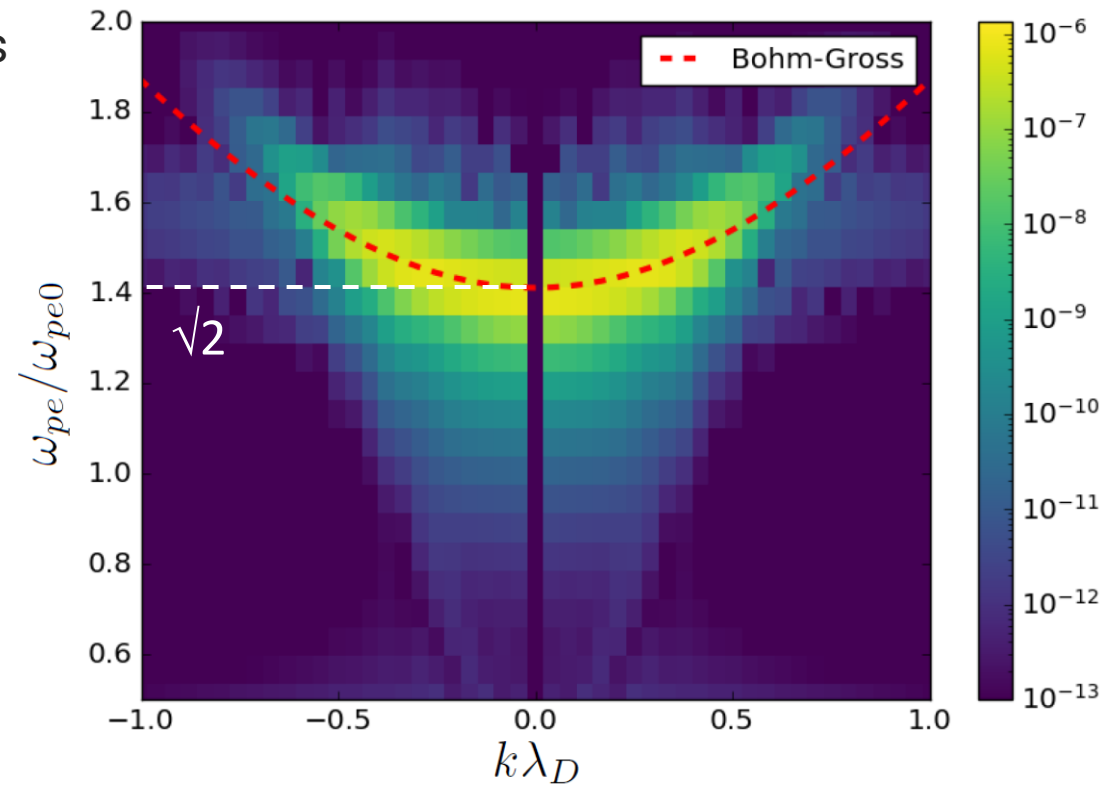
Ionization of neutrals \rightarrow higher freq. Langmuir waves



Bohm Gross:

$$\omega \approx \omega_{pe} (1 + 3(k\lambda_D)^2)^{1/2}$$

$$\text{with } \omega_{pe} = \sqrt{\frac{e^2 n_e}{\epsilon_0 m_e}}$$



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Describing plasma-wall interaction in the gyrokinetic framework requires a subgrid model

- Debye sheath: subgrid for gyrokinetics and is **positively charged**

	Debye sheath	Gyrokinetic plasma
Scale	$\lambda_D \approx 1 \mu\text{m}$	$\rho_i \approx 50 \mu\text{m}$
Frequency	$\omega_{pe} \approx 200 \text{ GHz}$	$\Omega_{ci} \approx 100 \text{ MHz}$

With typical SOL density & temperature $n_0 \approx 10^{19} \text{ m}^{-3}$ $T_0 \approx 30 \text{ eV}$

- Directly resolving Debye sheath in a gyrokinetic code not possible \rightarrow subgrid model
- Critical feature: plasma-wall interaction **ensures quasineutrality** on spatial scales $L \gg \lambda_D$ and time scales $\tau \gg \omega_{pe}^{-1}$
- Goal: retrieve this feature in gyrokinetic framework using **subgrid sheath model**

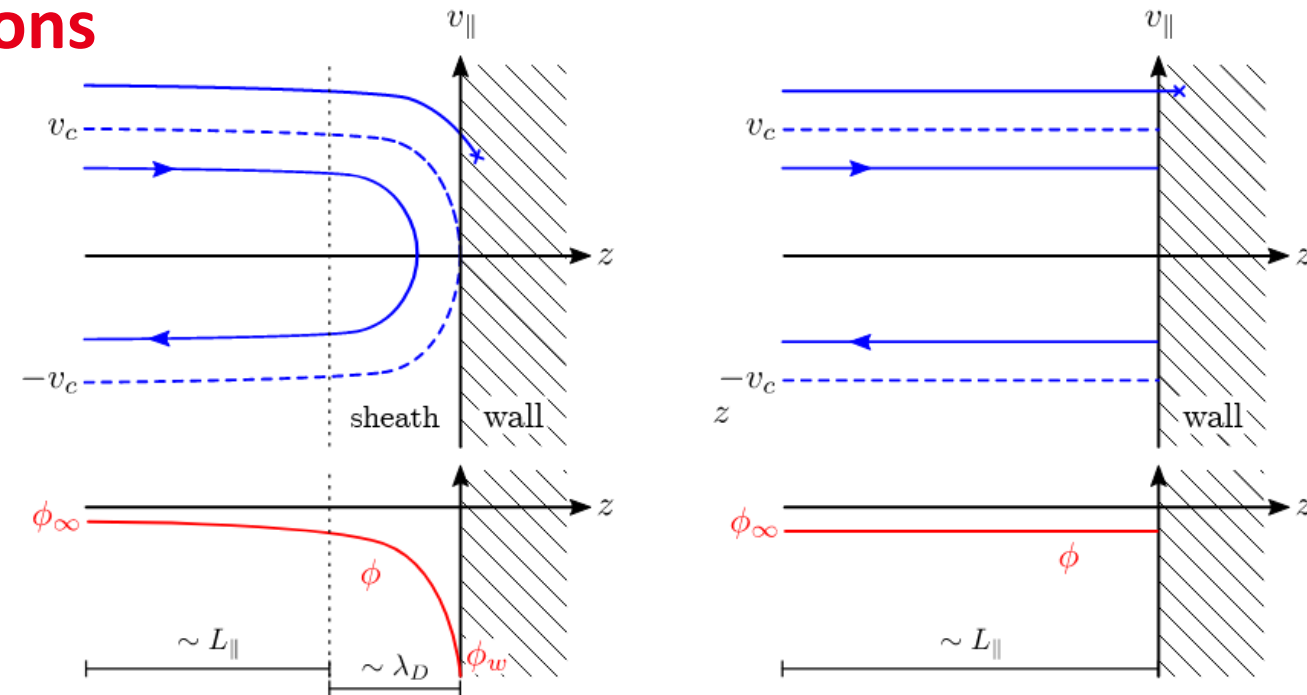
Subgrid sheath model components: absorption of ions & fast electrons, reflection of slow electrons

- Description in simplified (z, v_{\parallel}) phase space
- Fast electrons $v_{\parallel} > v_c$ and ions: **absorbed**
- Slow electrons $v_{\parallel} < v_c$ **reflected**

- Key elements of a subgrid sheath model:

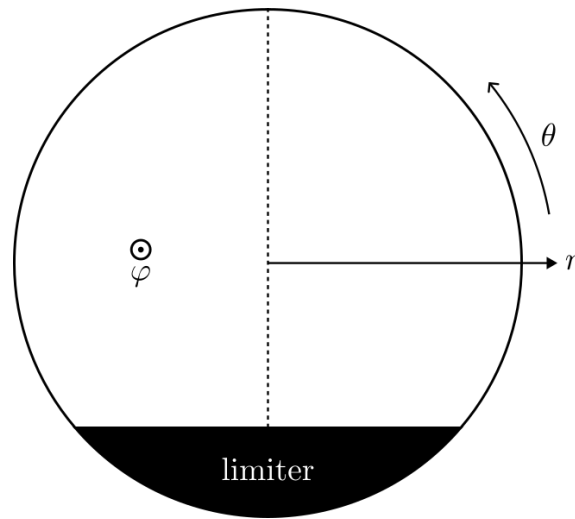
1. Absorption of ions & fast electrons
2. Reflection of slow electrons \rightarrow dependent of numerical scheme
3. Definition of cutoff velocity $v_c \rightarrow$ *logical, conducting, flux-averaged* sheath models

- Next slides: description of two subgrid sheath models valid for *backward semi-Lagrangian* schemes (GYSELA framework)

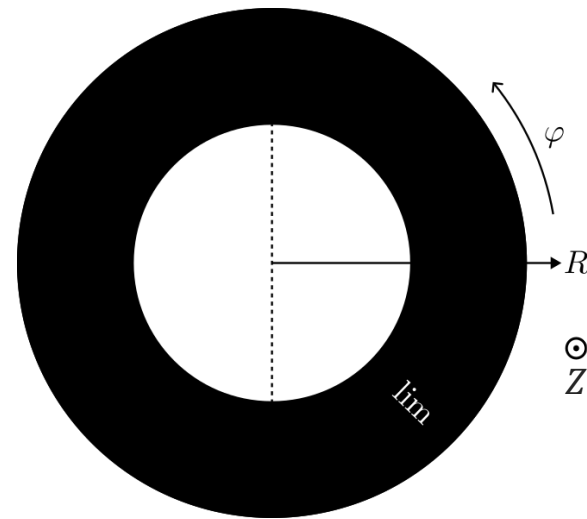


1.

Axisymmetric limiter with immersed boundary conditions & flux-averaged cutoff velocity



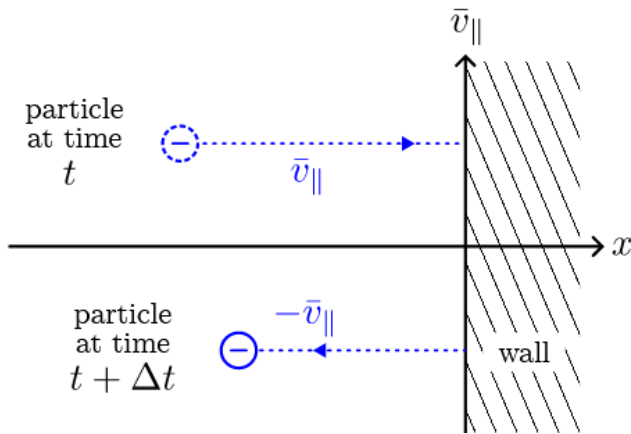
Poloidal
plane



View from
above

Implementation of electrons reflection depends on numerical scheme

- Lagrangian scheme

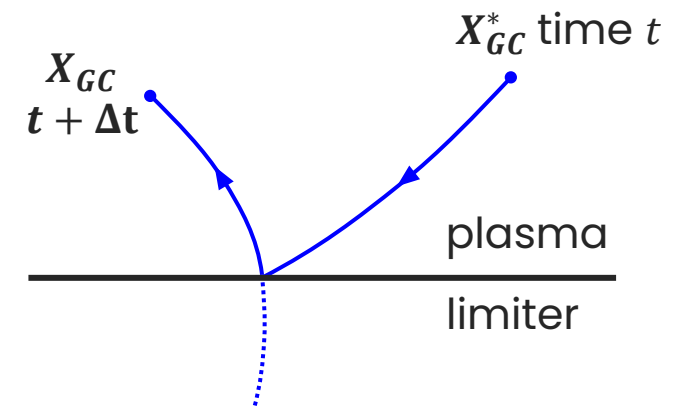


- Backward semi-Lagrangian scheme: characteristics traced back in time to update distribution function

$$F_e(\mathbf{X}_{GC}, t + \Delta t) = F_e(\mathbf{X}_{GC}^*, t)$$

$$\frac{d\mathbf{X}_{GC}}{dt} = v_{\parallel} + v_{\perp}$$

- Reflection of slow electrons: flip characteristics on wall limiter surface

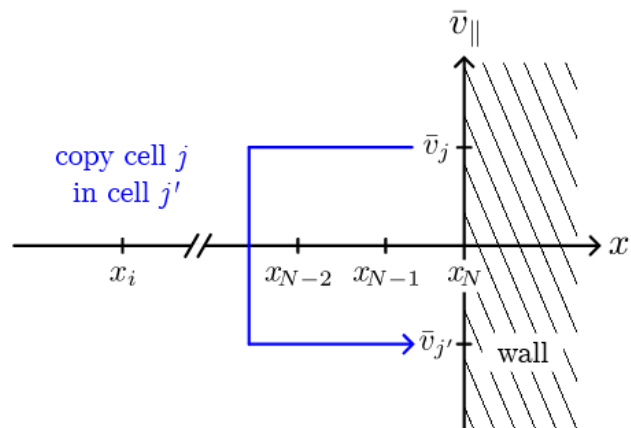


- Absorption of fast electrons

$$F_e(t + \Delta t, \mathbf{X}_{GC}) = 0$$

for each fast electron that intercepts the wall

- Eulerian scheme



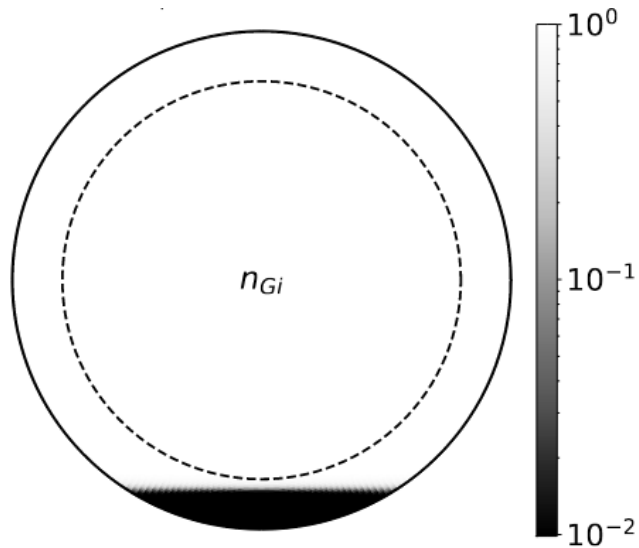
Immersed boundary conditions for ion absorption

- Limiter **immersed** in simulation domain $\frac{DF_i}{Dt} = \mathcal{C} + \mathcal{S} + \mathcal{S}_{\text{lim}}, \quad \mathcal{S}_{\text{lim}}(F_i) = -\nu \mathcal{M}_{\text{lim}} (F_i - F_{\text{lim}}).$

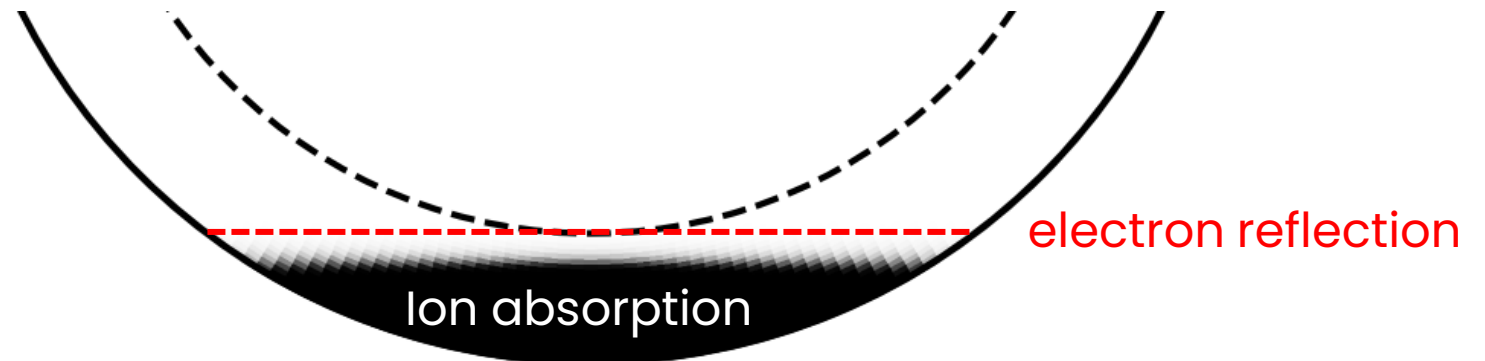
F_{lim} : maxwellian of very low density

M_{lim} : limiter mask (=1 in limiter, 0 in plasma, smooth transition)

- Example of uniform ion density profile with limiter



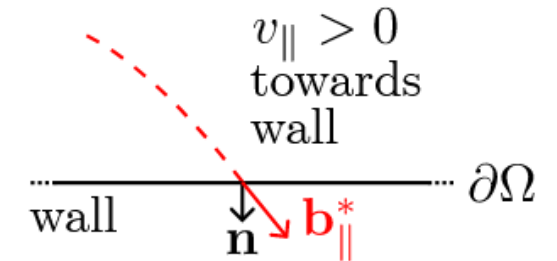
- Ion absorption & electron reflection do not coincide due to penalization



- Shift necessary for computing fluxes (next slide)

Flux-averaged sheath ensures plasma quasineutrality by matching ion & electron gyrocenter fluxes *on spatial average over limiter*

- Logical sheath: v_c such that $\Gamma_{GC} = \Gamma_e$ at **every position** on limiter surface
- Conducting sheath: $v_c = \sqrt{2e(\phi - \phi_w)/m_e}$ with ϕ_w limiter bias
- Flux averaged sheath model : definition of cutoff velocity v_c such that



Limiter ion gyrocenter flux $\langle \Gamma_{GC,i} \rangle_{lim}$

$$\int_{\partial\Omega} d^2S \int_{-\infty}^{+\infty} dv_{||} \int_0^{+\infty} d\mu J_v J_0 F_i(\mathbf{x}, v_{||}, \mu) (v_{||} \mathbf{b}_{||}^* + \mathbf{v}_E + \mathbf{v}_D) \cdot \mathbf{n}$$

Spatial average over limiter surface

Normal vector to limiter surface

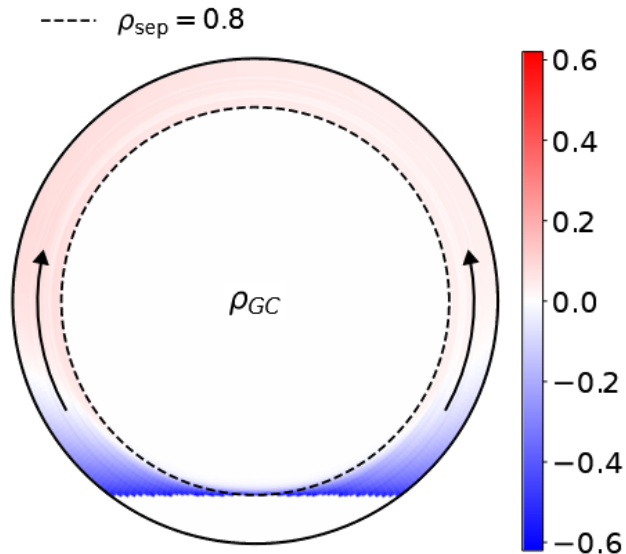
Limiter partial electron flux $\langle \Gamma_e \rangle_{lim}$

$$= \int_{\partial\Omega} d^2S \int_{-v_c}^{+\infty} d\bar{v}_{||} \int_0^{+\infty} d\mu J_v F_e(\mathbf{x}, \bar{v}_{||}, \mu) (\bar{v}_{||} \mathbf{b}_{||}^* + \mathbf{v}_E + \mathbf{v}_D) \cdot \mathbf{n},$$

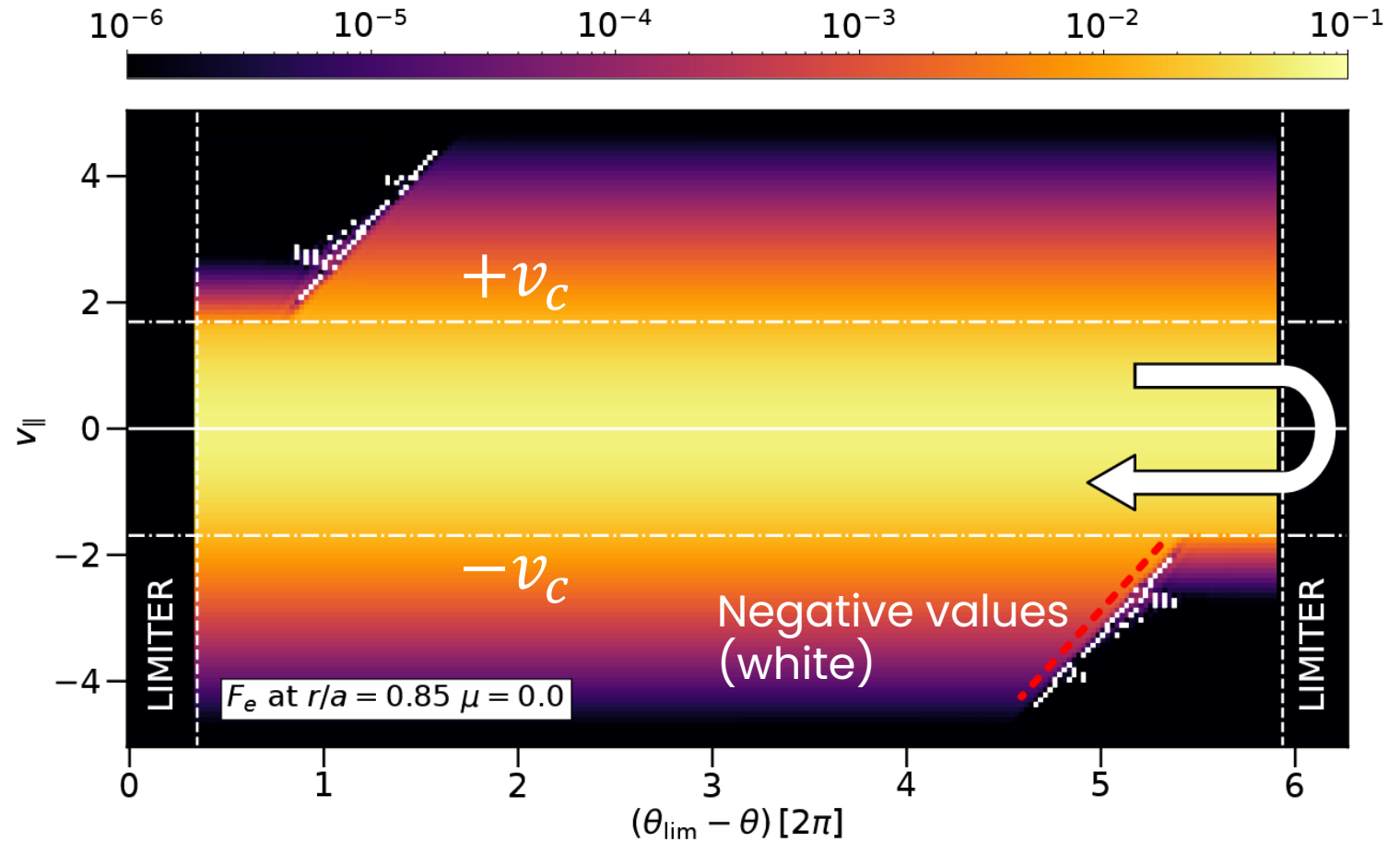
$v_{||} \in [-\infty; -v_c]$ electrons are absorbed in limiter
 → no contribution to electron flux (?)

Absorption of ions and fast electrons & reflection of slow electrons work as expected

- Fast electron depletion propagates in SOL
- Depletion of ions visible close to limiter
- Large charge density when QN is not solved



Electron distribution function in SOL (no QN, fixed v_c , no collisions)

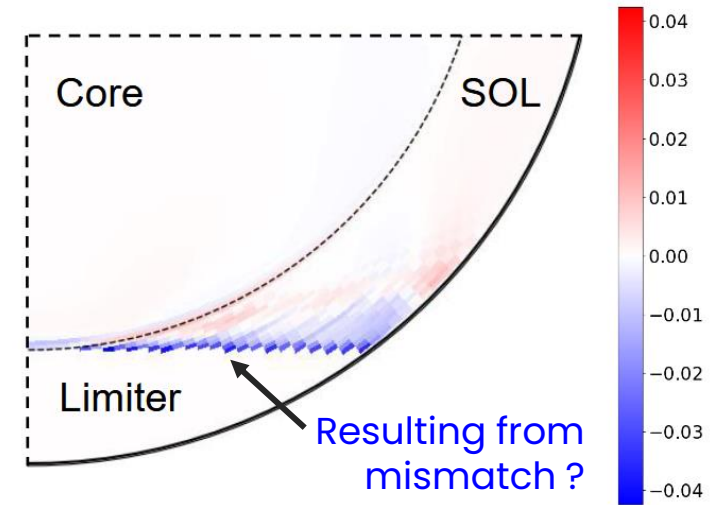
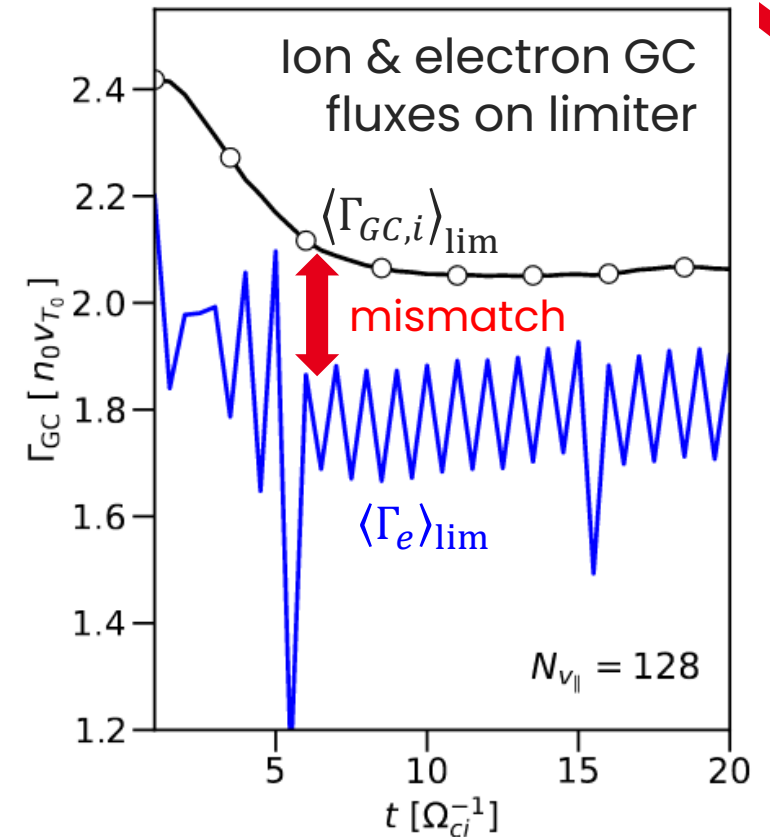


Electron & ion fluxes on limiter surface do not match: limiter surface is negatively charged

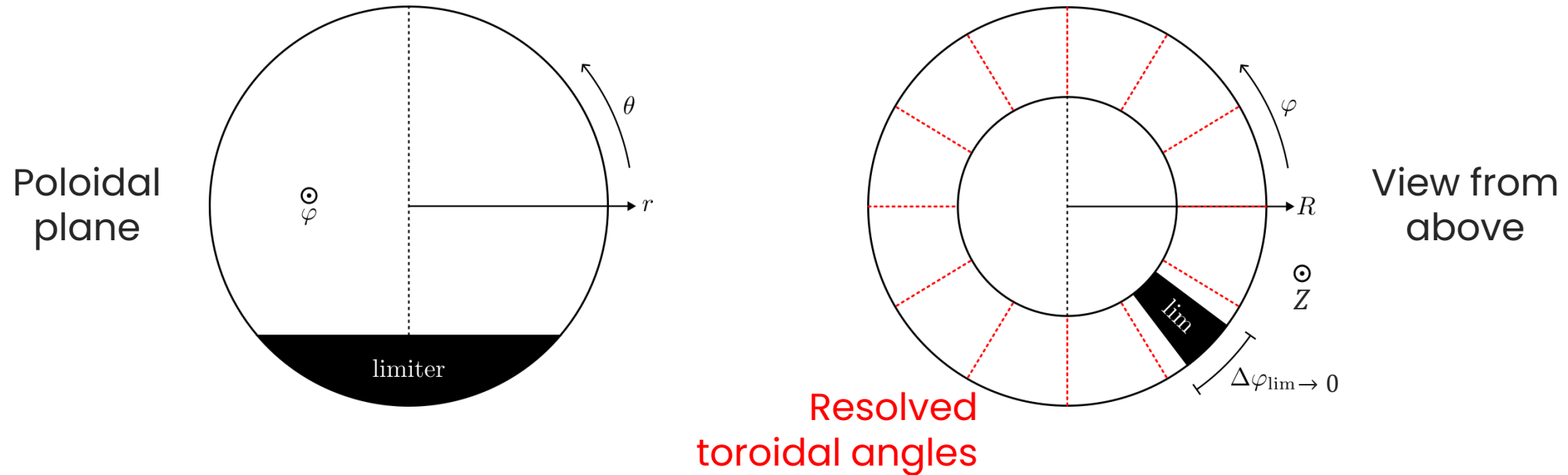
- Eventually leads to quasineutrality & simulation breakdown on very short timescales $t \approx 100 \Omega_{ci}^{-1} \ll t_{\text{turb}}$.
- Independent of discretization
- Flux mismatch possible origins:
 - Limiter immersed in domain (QN solver)
 - $v_{\parallel} \in [-\infty; -v_c]$ electrons actually contribute to electron flux

$$\begin{aligned} \langle \Gamma_{GC,i} \rangle_{\text{lim}} &= \int_{\partial\Omega} d^2S \int_{-v_c}^{+\infty} d\bar{v}_{\parallel} \int_0^{+\infty} d\mu J_v F_e(\mathbf{x}, \bar{v}_{\parallel}, \mu) (\bar{v}_{\parallel} \mathbf{b}_{\parallel}^* + \mathbf{v}_E + \mathbf{v}_D) \cdot \mathbf{n}, \\ &+ \int_{\partial\Omega} d^2S \int_{-v_c}^{+\infty} d\bar{v}_{\parallel} \int_{-\infty}^{-v_c} d\mu J_v F_e(\mathbf{x}, \bar{v}_{\parallel}, \mu) (\bar{v}_{\parallel} \mathbf{b}_{\parallel}^* + \mathbf{v}_E + \mathbf{v}_D) \cdot \mathbf{n}, \end{aligned}$$

(to be checked in simulations)



2. Infinitely-thin toroidal limiter without penalization & with conducting cutoff velocity



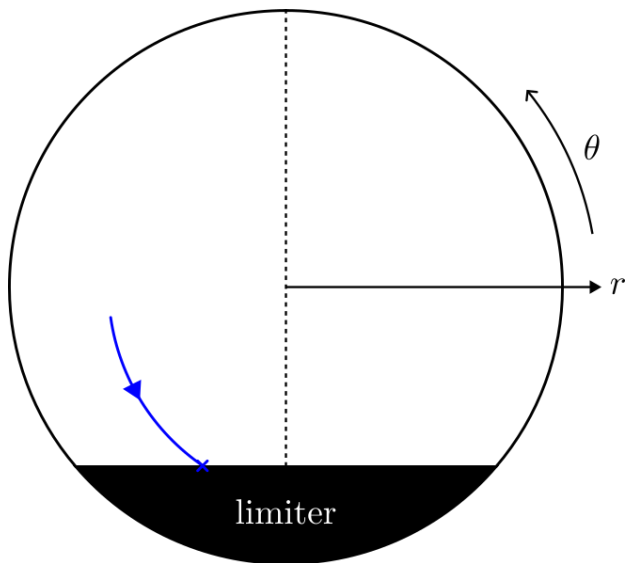
- Unknowns: **Penalization**, **Backward semi-Lagrangian** scheme, **flux-averaged** cutoff velocity
 - Limiter located between two adjacted toroidal positions → not immersed in simulation
 - Cutoff velocity computed with conducting sheath model $v_c = \sqrt{2e\phi/m_e}$

The thin toroidal limiter: a simple boundary condition embedded within toroidal advection step

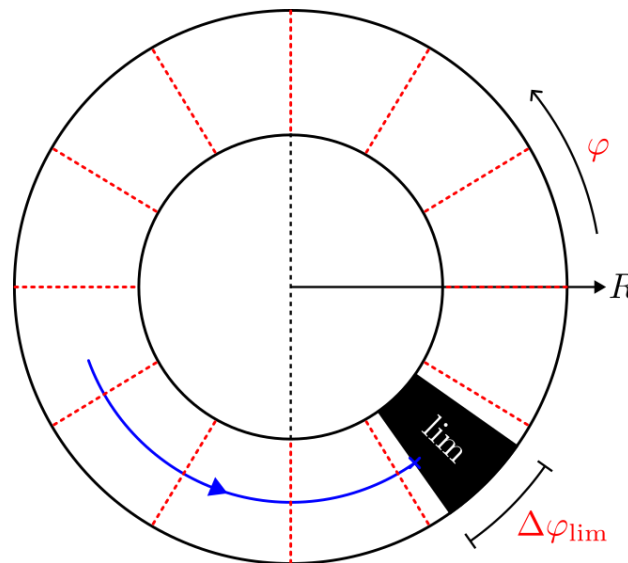
- Strang splitting of gyrokinetic equation

$$\frac{\partial F_s}{\partial t} + \frac{d\mathbf{x}}{dt} \cdot \nabla_{\mathbf{x}} F_s + \frac{dv_{\parallel}}{dt} \nabla_{v_{\parallel}} F_s = \mathcal{S}(F_s) + \mathcal{C}(F_s).$$

- | | |
|---|-------------|
| <ol style="list-style-type: none"> v_{\parallel} advection on $\Delta t/2$ φ advection on $\Delta t/2$ (r, θ) advection on Δt | + symmetric |
|---|-------------|



Particles intercept **axisymmetric** limiter during (r, θ) advection

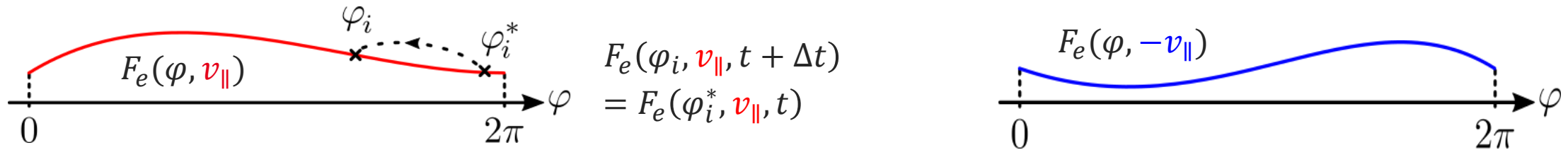


Particles intercept **thin** limiter during φ advection

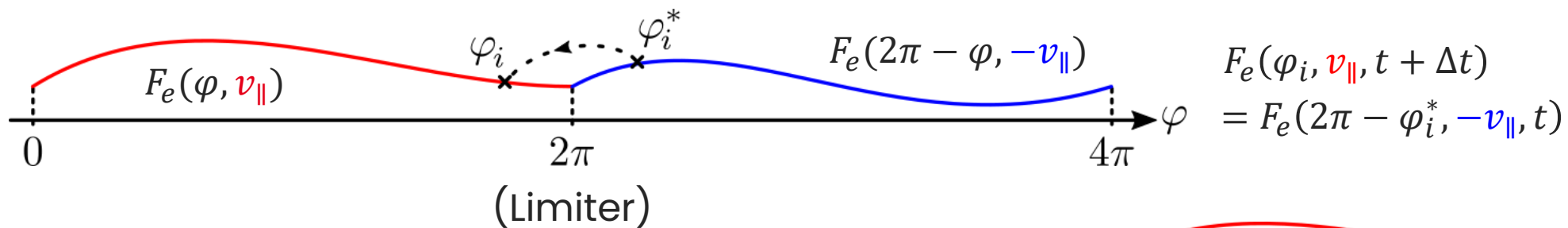
- Axisymmetric limiter is immersed in Vlasov **and** QN
- Thin limiter is located between two toroidal mesh points
- Thus thin limiter is immersed in **Vlasov only (not in QN)**

Absorptions & reflections simple and efficient within 1D toroidal advection

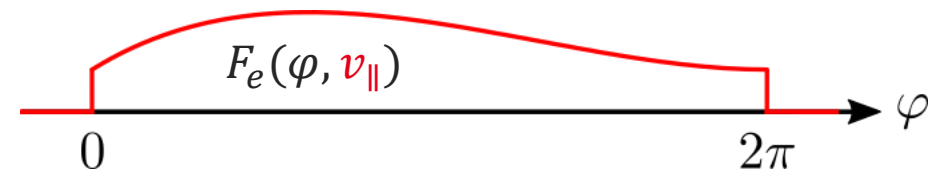
- Usual 1D toroidal advection at fixed (r, θ, μ) (periodic BC. at $\varphi = 2\pi$)



- With thin limiter: reflection on an **extended toroidal domain**



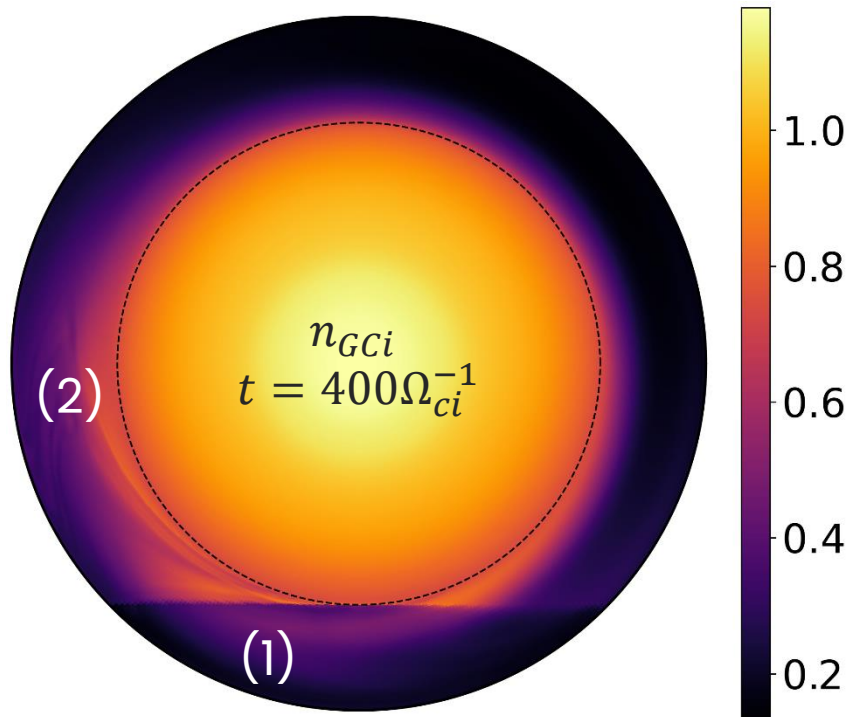
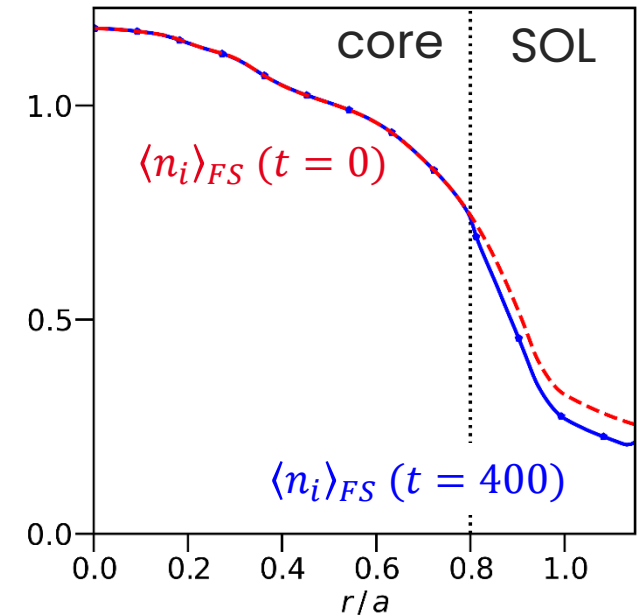
- Absorption: BC. Dirichlet at zero outside domain



- Simple implementation: no computation of interception point for reflection

Thin toroidal limiter leads to a depletion of SOL density at early simulation times

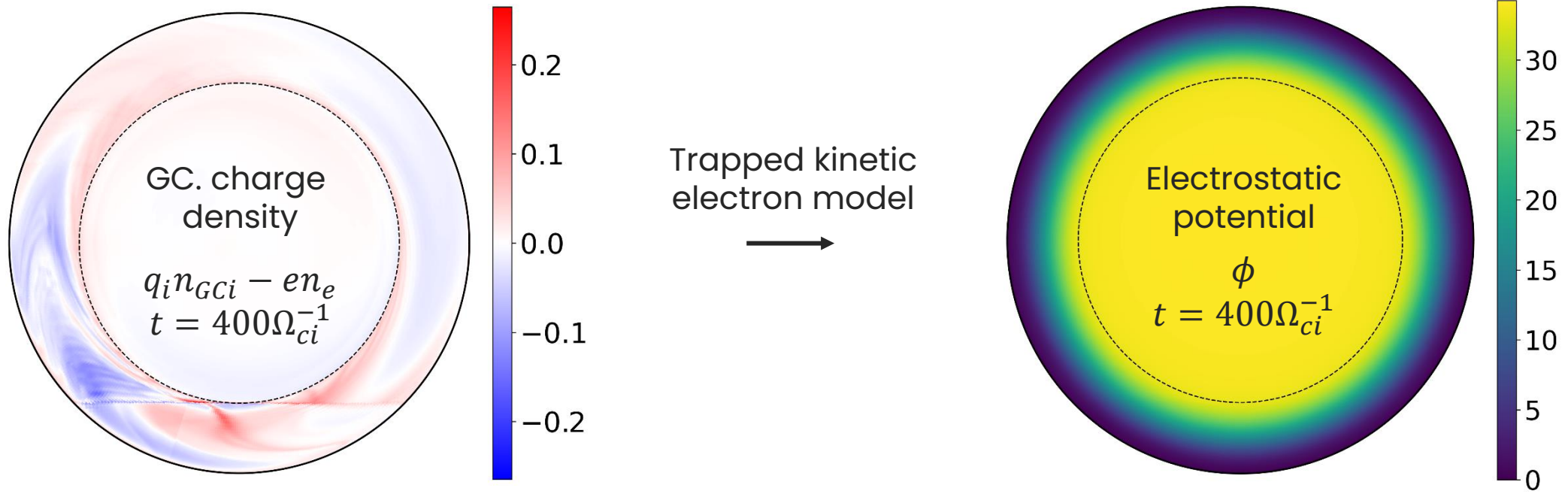
- Thin lim. allows for reaching longer simulation times $t \approx 2000 \Omega_{ci}^{-1}$
 - vs. $t \approx 100 \Omega_{ci}^{-1}$ for axisymmetric lim.
 - WIP: reach turbulent times $t > 100,000 \Omega_{ci}^{-1}$



- (1) Ion density non-vanishing in « limiter » domain \rightarrow different physics than with axi. lim ?
- (2) Complex reorganization features \rightarrow need for overcoming initial transient $t > 2000 \Omega_{ci}^{-1}$

Possible necessity of adapting the quasineutrality model for overcoming initial transient

$$-\nabla_{\perp} \cdot \left(\frac{m_i \bar{n}_{\text{eq},i}}{e Z_i B^2} \nabla_{\perp} \phi \right) + \langle n_e^{\text{pass.}} \rangle_{\text{FS}} \frac{e(\phi - \langle \phi \rangle_{\text{FS}})}{\langle T_e \rangle_{\text{FS}}} = Z_i n_{\text{GI}} - n_e^{\text{trap.}} - \langle n_e^{\text{pass.}} \rangle_{\text{FS}}$$



- Large (spurious?) GC charge density at early times
 - $\phi \approx \langle \phi \rangle_{\text{FS}} \gg 1$ in simulation
 - $\langle \phi \rangle_{\text{FS}}$ can't balance large charges with poloidal dependency
- BC for QN solver : $\phi = 0$ at $r = r_{\text{max}} \rightarrow v_c = 0$ absorption of all electrons in lim

Concluding remarks & perspectives

1. Plasma-neutral interaction

- Pressure-diffusion fluid model for neutrals
- Coupling to kinetic plasma description with moment approach for source
- Proof of principle simulation in 1D-1V Voice code
- Next: fluid model to be added in GK code GYSELA

2. Plasma-wall interaction

- Description of two subgrid sheath models valid in gyrokinetic framework
- Long (turbulent) simulation time not reached at the moment
- Axisymmetric limiter: assess the origin of ion & electron flux mismatch
- Thin toroidal limiter: overcome initial reorganization (QN BC modification)



Backup slides

Coupling fluid neutral & kinetic plasma neutral with Hermite polynomials

- Neutral-plasma coupling via **source term** in Vlasov equation $\frac{DF_S}{Dt} = C(F_S) + S(F_S) + S_N(F_S, n_N, x, v)$
 - S_N = particle source only, no momentum/energy injection
 - Constraint: ensure "1 neutral \leftrightarrow 1 ion + 1 electron" balance

- Construction of S_N by projection on Hermite polynomials [Sarazin 2011]

$$S_N(F_S, n_N, x, v) = \sum_{h=0}^{+\infty} c_h(n_N, F_S) H_h\left(\frac{v_s}{\sqrt{2T_N}}\right) \exp\left(-\frac{v_s^2}{2T_N}\right) = c_0 \left(\frac{3}{2} - \frac{v_s^2}{2T_N}\right) \exp\left(-\frac{v_s^2}{2T_N}\right) \quad \text{Pure density source}$$

- With $c_0 = \frac{S_{n,N}}{\sqrt{2\pi T_N}}$ and $S_{n,N} = n_N n_e \langle \sigma v \rangle_i - (n_i n_e \langle \sigma v \rangle_r)$

- Number of particles (plasma + neutrals) conserved $\left\{ \begin{array}{l} \partial_t n_N + \nabla \cdot \Gamma_N = -S_{N,n} \\ \frac{DF_S}{Dt} = \dots + S_N(F_S, n_N, x, v) \text{ and } \int dv S_N = S_{N,n} \end{array} \right.$