



Multi Regions-of-Interest in REFMUL3

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EUROfusion



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TÉCNICO
LISBOA

Model and numerics

Solve for Maxwell's curl equations + constitutive relation (current density)

$$\nabla \times \mathbf{H} = \varepsilon_0 \frac{\partial \mathbf{E}}{\partial t} + \sigma \mathbf{E} + \mathbf{J}$$

$$\nabla \times \mathbf{E} = -\mu_0 \frac{\partial \mathbf{H}}{\partial t} - \sigma^* \mathbf{H}$$

$$\frac{\partial \mathbf{J}}{\partial t} = \varepsilon_0 \omega_p^2 \mathbf{E} + \vec{\omega}_c \times \mathbf{J}$$

using the Finite Difference Time Domain (FDTD) method in Cartesian meshes

REFMUL3 code

3D full-wave C code: hybrid OpenMP/MPI (3D) + OpenMP target offload (GPU)

K.S. Yee, *IEEE Trans Antennas Propag* **14** (1966) 302
L. Xu and N. Yuan *IEEE Antennas Wirel Propag Lett* **5** (2006) 335

F. Silva, S. Heuraux and T. Ribeiro *Proc. IRW13* (2017)
F. Silva, S. Heuraux, T. Ribeiro et al. *Fus Eng Des* **202** (2024) 114354

Motivation

What are regions-of-interest (ROI)?

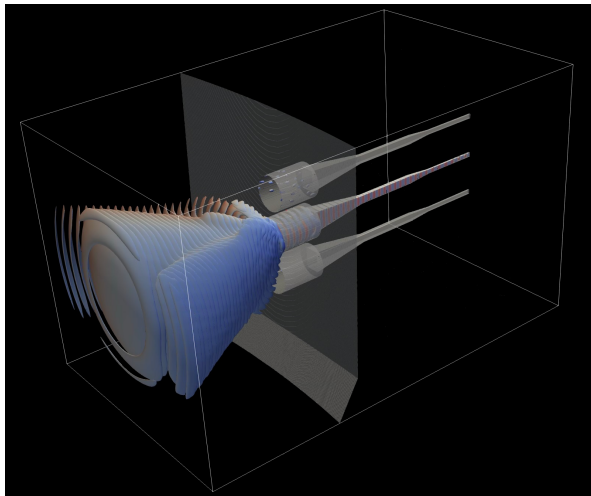
- wherever waves propagate!

Why do we need to consider them?

- wave-free volumes are currently computed
 - outside the vessel
 - inside metallic structures

Avoid:

Waste of resources!



Outline

REFMUL3 code

- Model and numerics

Motivation

Multi regions-of-interest (ROI) in 2D

- How to proceed?

- Non-matching subdomains

- Generalizations in 2D

Multi ROI: towards 3D

- Non-contiguous memory access

Summary & outlook

Outline



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How to proceed?

Non-matching subdomains

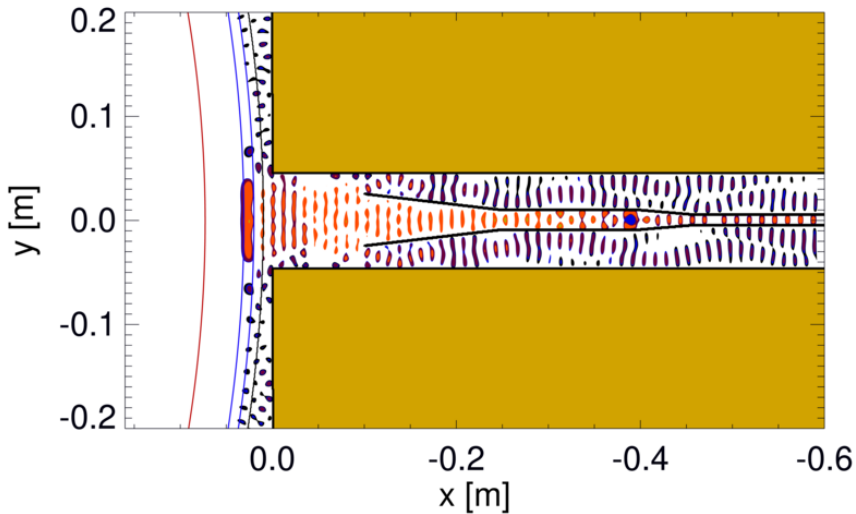
Generalizations in 2D

Multi ROI: towards 3D

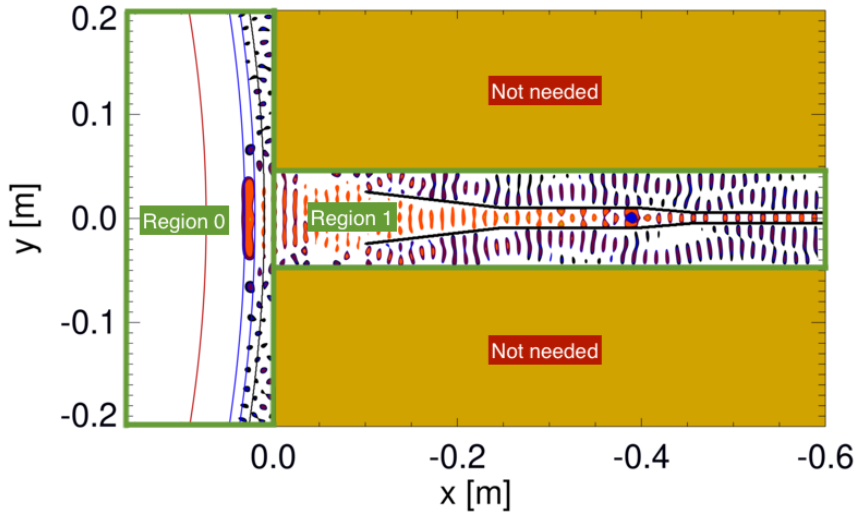
Non-contiguous memory access

Summary & outlook

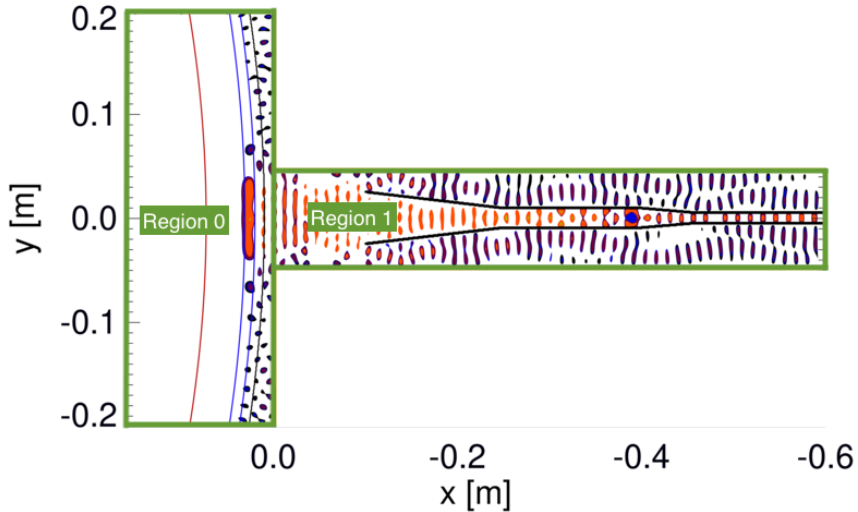
Example in 2D (simpler to illustrate)



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Example in 2D (simpler to illustrate)



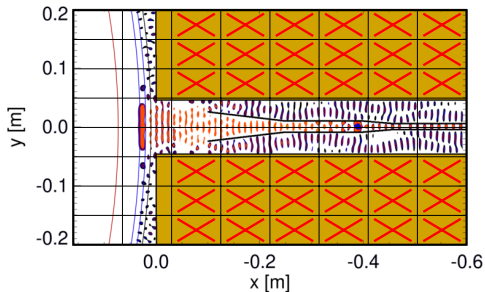
How to proceed?

A) Remove void subdomains

- Preprocess the decomposition
- Find/remove empty subdomains
- **Caution:** MPI Cartesian topology
- **Issue:** low granularities (e.g. GPUs)

B) Define regions-of-interest (ROI)

- Global virtual space
- More effective
- Same grid-resolution for all ROIs
- **Challenge:** non-matching subdomains



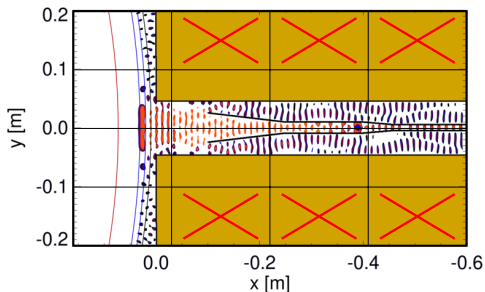
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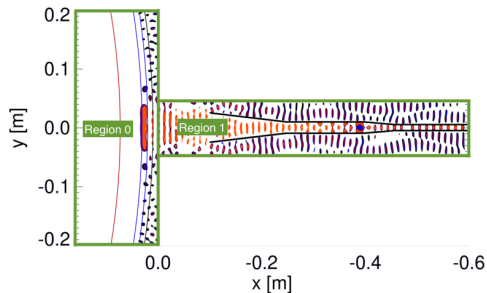
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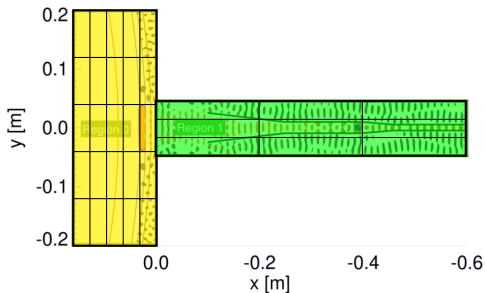
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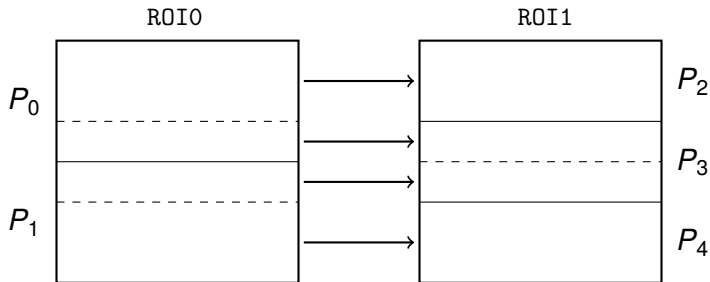
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Summary & outlook

Starting point: non-matching subdomains

2D data sent from left to right, 1D domain decomposition (inspired in [1])



Beyond simple point-to-point communication

Each MPI task sends different messages to multiple MPI tasks

[1] *Using Advanced MPI: Modern Features of the Message-Passing* (2014) by W. Gropp, T. Hoefler, R. Thakur and E. Lusk

MPI collective communication function: MPI_Alltoallv()

```
1 int MPI_Alltoallv(  
2     void *sendbuf, int *sendcnts, int *senddispls, MPI_Datatype sendtype,  
3     void *recvbuf, int *recvcnts, int *recvdispls, MPI_Datatype recvtype,  
4     MPI_Comm comm);
```

Parameters

- `sendbuf`: pointer to the send buffer containing the data to be sent.
- `sendcnts`: integer array (of length group size) specifying the number of elements to send to each task.
- `senddispls`: integer array (of length group size) specifying the displacement of first element relative to `sendbuf`.
- `sendtype`: data type of send buffer elements (handle).
- `recvbuf`: address of receive buffer (choice).
- `recvcnts`: integer array (of length group size) specifying the number of elements to receive from each task.
- `recvdispls`: integer array (of length group size) specifying the displacement of first relative to `recvbuf`.
- `recvtype`: data type of receive buffer elements (handle).
- `comm`: communicator (handle).

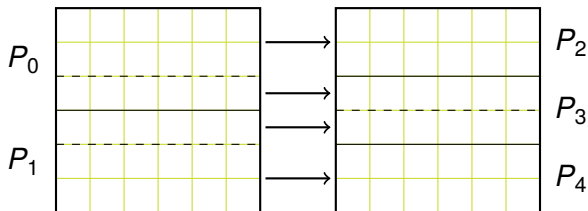
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Parameters

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- `recvtype`: data type of receive buffer elements (handle).
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Communication **send** patterns: 6x6 grid



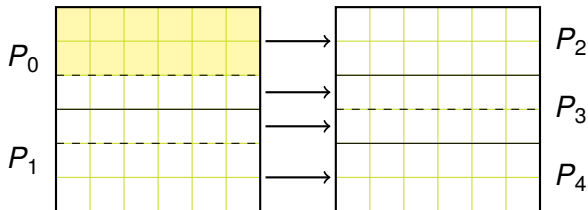
`sendcnts[ntasks]`

task	0	1	2	3	4
0					
1					
2					
3					
4					

`senddispls[ntasks]`

task	0	1	2	3	4
0					
1					
2					
3					
4					

Communication **send** patterns: 6x6 grid



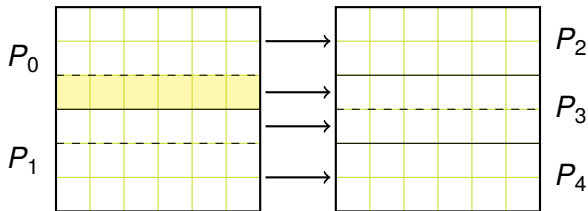
`sendcnts[ntasks]`

task	0	1	2	3	4
0	0	0	12		
1					
2					
3					
4					

`sendispls[ntasks]`

task	0	1	2	3	4
0	0	0	0		
1					
2					
3					
4					

Communication **send** patterns: 6x6 grid



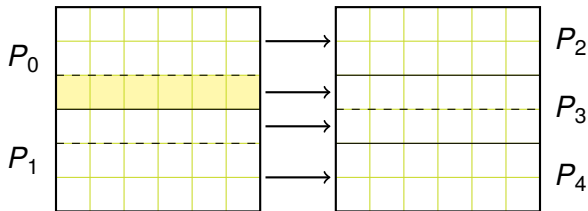
`sendcnts[ntasks]`

task	0	1	2	3	4
0	0	0	12	6	
1					
2					
3					
4					

`sendispls[ntasks]`

task	0	1	2	3	4
0	0	0	0	12	
1					
2					
3					
4					

Communication **send** patterns: 6x6 grid



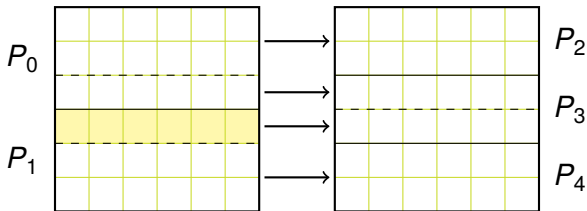
`sendcnts[ntasks]`

task	0	1	2	3	4
0	0	0	12	6	0
1					
2					
3					
4					

`sendispls[ntasks]`

task	0	1	2	3	4
0	0	0	0	12	0
1					
2					
3					
4					

Communication **send** patterns: 6x6 grid



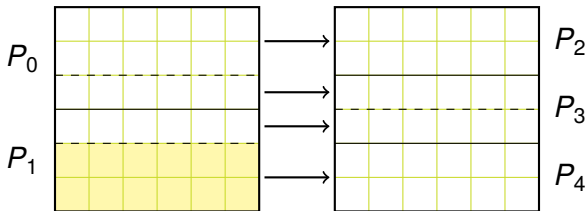
`sendcnts[ntasks]`

task	0	1	2	3	4
0	0	0	12	6	0
1	0	0	0	6	
2					
3					
4					

`sendispls[ntasks]`

task	0	1	2	3	4
0	0	0	0	12	0
1	0	0	0	0	
2					
3					
4					

Communication **send** patterns: 6x6 grid



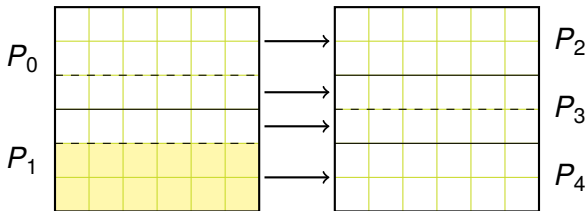
`sendcnts[ntasks]`

task	0	1	2	3	4
0	0	0	12	6	0
1	0	0	0	6	12
2					
3					
4					

`sendispls[ntasks]`

task	0	1	2	3	4
0	0	0	0	12	0
1	0	0	0	0	6
2					
3					
4					

Communication **send** patterns: 6x6 grid



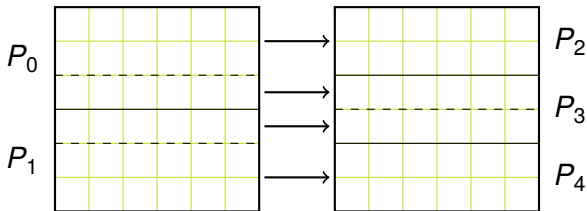
`sendcnts[ntasks]`

task	0	1	2	3	4
0	0	0	12	6	0
1	0	0	0	6	12
2	0	0	0	0	0
3	0	0	0	0	0
4	0	0	0	0	0

`sendispls[ntasks]`

task	0	1	2	3	4
0	0	0	0	12	0
1	0	0	0	0	6
2	0	0	0	0	0
3	0	0	0	0	0
4	0	0	0	0	0

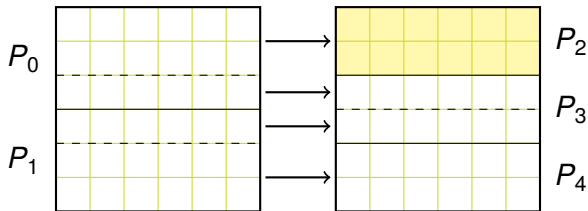
Communication **receive** patterns: 6x6 grid



recvcnts[ntasks]					
task	0	1	2	3	4
0					
1					
2					
3					
4					

recvdispls[ntasks]					
task	0	1	2	3	4
0					
1					
2					
3					
4					

Communication receive patterns: 6x6 grid



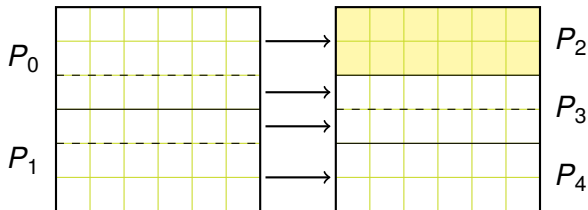
recvcnts[ntasks]

task	0	1	2	3	4
0	0	0	0	0	0
1	0	0	0	0	0
2	12				
3					
4					

recvdispls[ntasks]

task	0	1	2	3	4
0	0	0	0	0	0
1	0	0	0	0	0
2	0				
3					
4					

Communication receive patterns: 6x6 grid



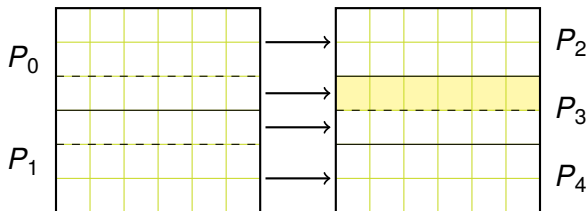
recvcnts[ntasks]

task	0	1	2	3	4
0	0	0	0	0	0
1	0	0	0	0	0
2	12	0	0	0	0
3					
4					

recvdispls[ntasks]

task	0	1	2	3	4
0	0	0	0	0	0
1	0	0	0	0	0
2	0	0	0	0	0
3					
4					

Communication receive patterns: 6x6 grid



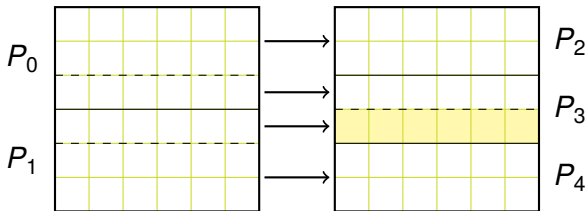
recvcnts[ntasks]

task	0	1	2	3	4
0	0	0	0	0	0
1	0	0	0	0	0
2	12	0	0	0	0
3	6				
4					

recvdispls[ntasks]

task	0	1	2	3	4
0	0	0	0	0	0
1	0	0	0	0	0
2	0	0	0	0	0
3	0				
4					

Communication receive patterns: 6x6 grid



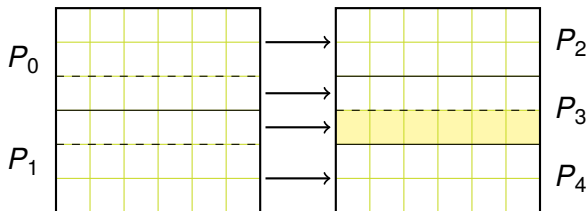
recvcnts[ntasks]

task	0	1	2	3	4
0	0	0	0	0	0
1	0	0	0	0	0
2	12	0	0	0	0
3	6	6			
4					

recvdispls[ntasks]

task	0	1	2	3	4
0	0	0	0	0	0
1	0	0	0	0	0
2	0	0	0	0	0
3	0	6			
4					

Communication receive patterns: 6x6 grid



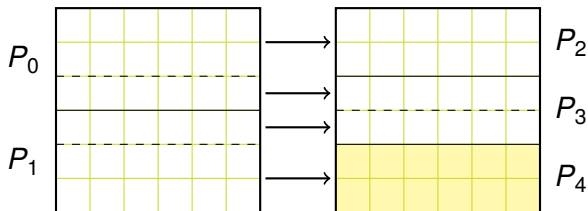
recvcnts[ntasks]

task	0	1	2	3	4
0	0	0	0	0	0
1	0	0	0	0	0
2	12	0	0	0	0
3	6	6	0	0	0
4					

recvdispls[ntasks]

task	0	1	2	3	4
0	0	0	0	0	0
1	0	0	0	0	0
2	0	0	0	0	0
3	0	6	0	0	0
4					

Communication receive patterns: 6x6 grid



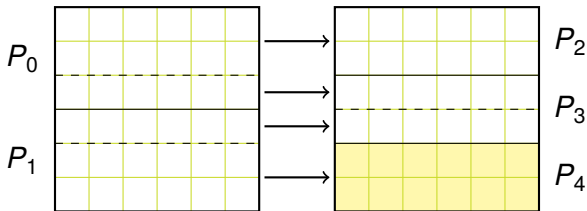
recvcnts[ntasks]

task	0	1	2	3	4
0	0	0	0	0	0
1	0	0	0	0	0
2	12	0	0	0	0
3	6	6	0	0	0
4	0	12			

recvdispls[ntasks]

task	0	1	2	3	4
0	0	0	0	0	0
1	0	0	0	0	0
2	0	0	0	0	0
3	0	6	0	0	0
4	0	0			

Communication receive patterns: 6x6 grid



recvcnts[ntasks]

task	0	1	2	3	4
0	0	0	0	0	0
1	0	0	0	0	0
2	12	0	0	0	0
3	6	6	0	0	0
4	0	12	0	0	0

recvdispls[ntasks]

task	0	1	2	3	4
0	0	0	0	0	0
1	0	0	0	0	0
2	0	0	0	0	0
3	0	6	0	0	0
4	0	0	0	0	0

Compute arguments for MPI_Alltoallv()

```
1  /* loop ranks in remote ROI only, since there are no local ROI exchanges */
2  for (int iRank = myRankF[color_rm]; iRank < myRankL[color_rm]; iRank++) {
3      if (color == color_here) {
4          jF_rm = calc_jF(iRank - myRankF[color_rm], nRanks_ROI[color_rm], Ni, Nj);
5          jL_rm = calc_jL(iRank - myRankF[color_rm], nRanks_ROI[color_rm], Ni, Nj);
6          if (jF <= jL_rm && jL >= jF_rm) {
7              commcounts[iRank] = ( min(jL, jL_rm) - max(jF, jF_rm) + 1) * Ni;
8              commispls[iRank] = displs;
9              displs += commcounts[iRank];}
10         else {
11             commcounts[iRank] = 0;
12             commdispls[iRank] = 0;}
13     } else { /* color == color_rm */
14         commcounts[iRank] = 0;
15         commdispls[iRank] = 0;}
16 }
```

Computing ***counts** & ***displs** is easier than using point-to-point communication

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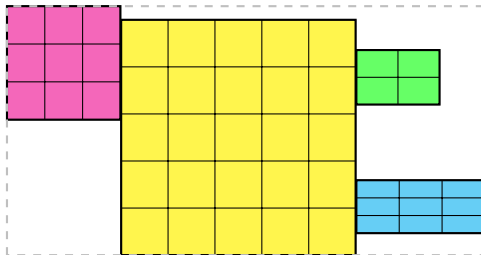
Generalizations in 2D

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Summary & outlook

Generalizations in 2D



- **2D domain decomposition:** adjust computation of counts & displs
- **Exchange of ghost-layers:** communication buffers become 1D
- **MPI communicators & groups:** subset of MPI tasks in each ROI interface
- **> 2 ROIs:** global virtual space (not allocated) as reference frame

General 2D domain decomposed multi-ROI configurations: **implemented and tested**

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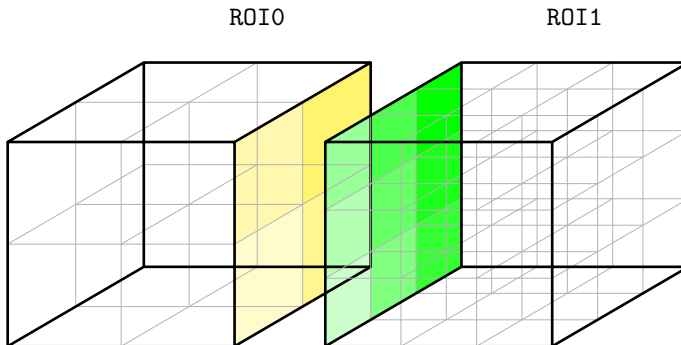
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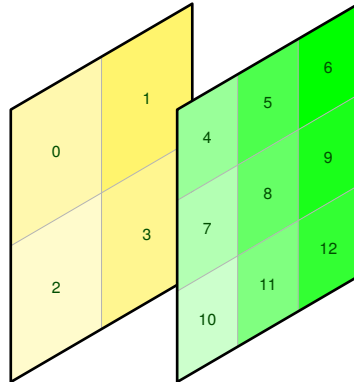
Important difference:

Communication buffers between 3D ROIs are 2D faces decomposed in 2D

Interface communication



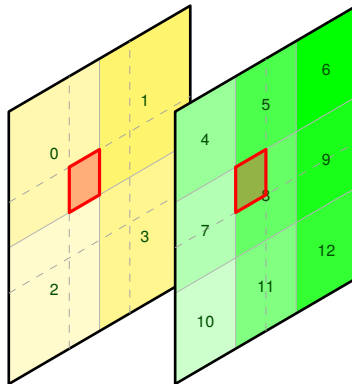
2D communication buffers



Interface communication

2D communication buffers

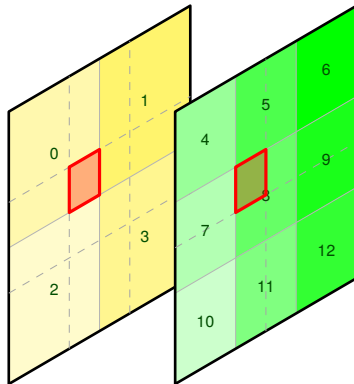
- Exchanged data: subsets of 2D data
- Memory access pattern is **non-contiguous!**



Interface communication

2D communication buffers

- Exchanged data: subsets of 2D data
- Memory access pattern is **non-contiguous!**
- Arrays of counts and displs + `MPI_Alltoallv()`: **not enough**
- Further concepts required, e.g. **blocksize** and **stride**



Non-contiguous memory access

How can we generalize our algorithm?

(0, 4)	(0, 5)	(1, 5)	(1, 6)
(0, 7)	(0, 8)	(1, 8)	(1, 9)
(2, 7)	(2, 8)	(3, 8)	(3, 9)
(2, 10)	(2, 11)	(3, 11)	(3, 12)

superposition of interface communication buffers and data layout

Solution:

Use most general `MPI_Alltoallw()` call together with **MPI derived data types**

MPI derived data types + MPI_Alltoallw() (ongoing)

```
1 int MPI_Alltoallw(  
2     void *sendbuf, int *sendcnts, int *senddispls, MPI_Datatype *sendtype,  
3     void *recvbuf, int *recvcnts, int *recvdispls, MPI_Datatype *recvtype,  
4     MPI_Comm comm);
```

Strategy

- Compute **counts** and **displs** as before (using Cartesian topology)
- Use this information to create **array of MPI derived data types** (DDT)
- Each DDT describes **memory access pattern** to communication buffers
- Call **MPI_Alltoallw()** (not v!) using array of DDTs as argument

Note:

Already implemented for 2D multi-ROI case, **extension to 3D ongoing...**

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Multi regions-of-interest

- Same grid-resolution for all ROIs
- **Non-matching** interface subdomains
- Communication algorithm **devised**
- **Tailored all-to-all** communication + **memory access patterns**
- General multi-ROI 2D configuration: **implemented**
- Extension to 3D ongoing: **should be finished soon...**

Outlook

- Deployment to REFMUL3: **left for future work**