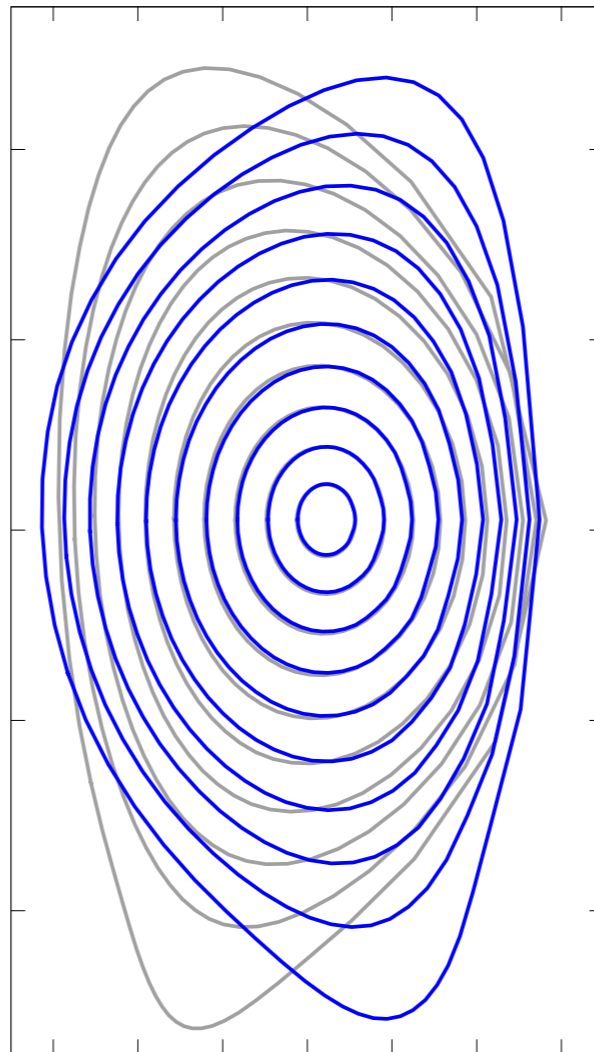


# Gyrokinetic calculations for a negative triangularity DEMO



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KDII#8 Final Meeting  
01 July 2020

# Motivation

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- Negative  $\delta$  potentially has the following benefits:
  - Improves confinement
  - Increases the L-H power threshold, thereby keeping the plasma in L-mode and avoiding ELMs

# Objectives

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- Compare the positive and negative  $\delta$  DEMO equilibria using local nonlinear GENE gyrokinetic simulations with kinetic electrons
  - Distinguish the effect of plasma profiles and magnetic geometry
  - Investigate profile stiffness
  - Do so at several minor radii (i.e.  $\rho_{tor} = 0.62, 0.72, 0.82$ )

# Error in chease calculation of input equilibria :(

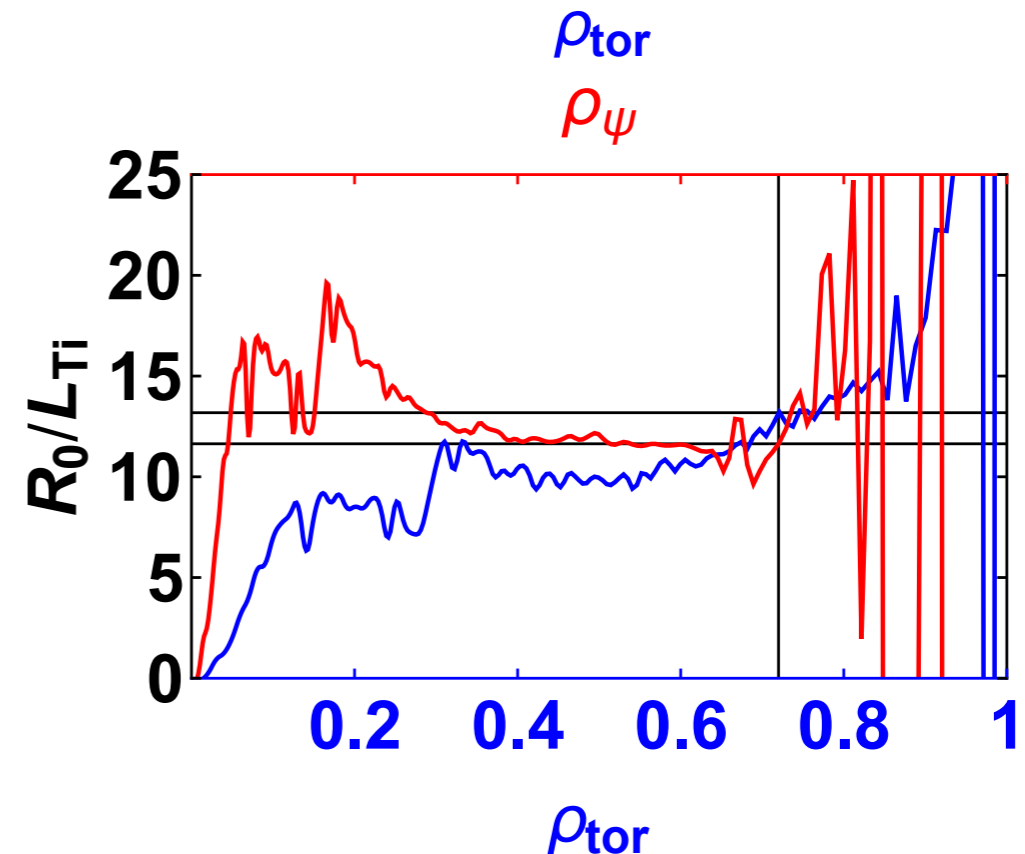
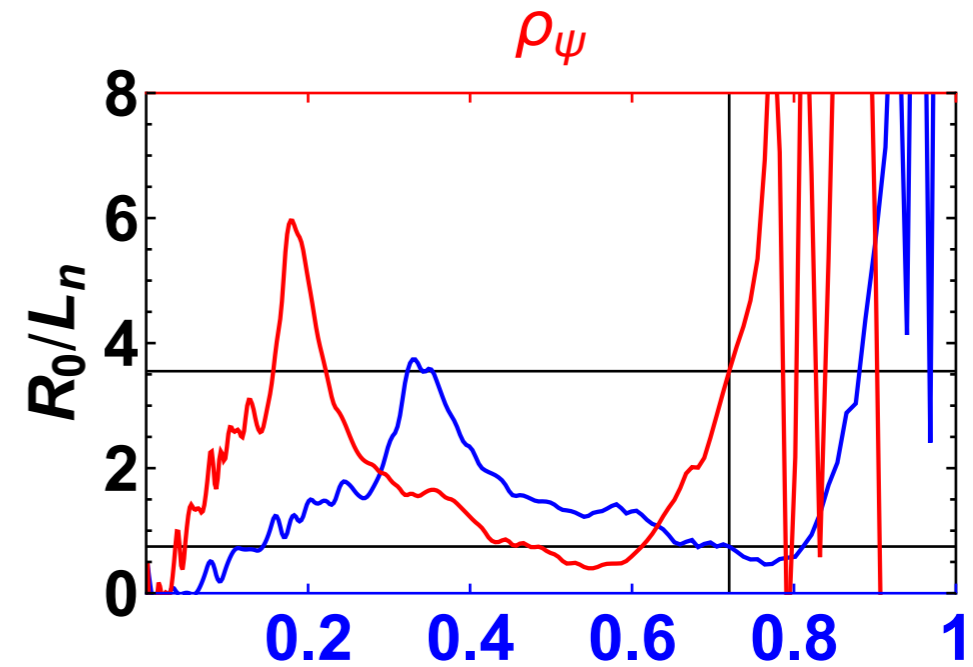
- Past simulations used the magnetic equilibria at  $\rho_{tor} = 0.72$ , but the plasma profiles at  $\rho_{\psi} = 0.72$

- Errors are:

► Should be  $R_0/L_n \approx 0.7$ , not 3.5

- Should be  $R_0/L_{Ts} \approx 13$ , not 11

- Should be  $T_i/T_e \approx 1.0$ , not 1.1



# Error in chease calculation of input equilibria :(

- Past simulations used the magnetic equilibria at  $\rho_{tor}$  plasma profiles

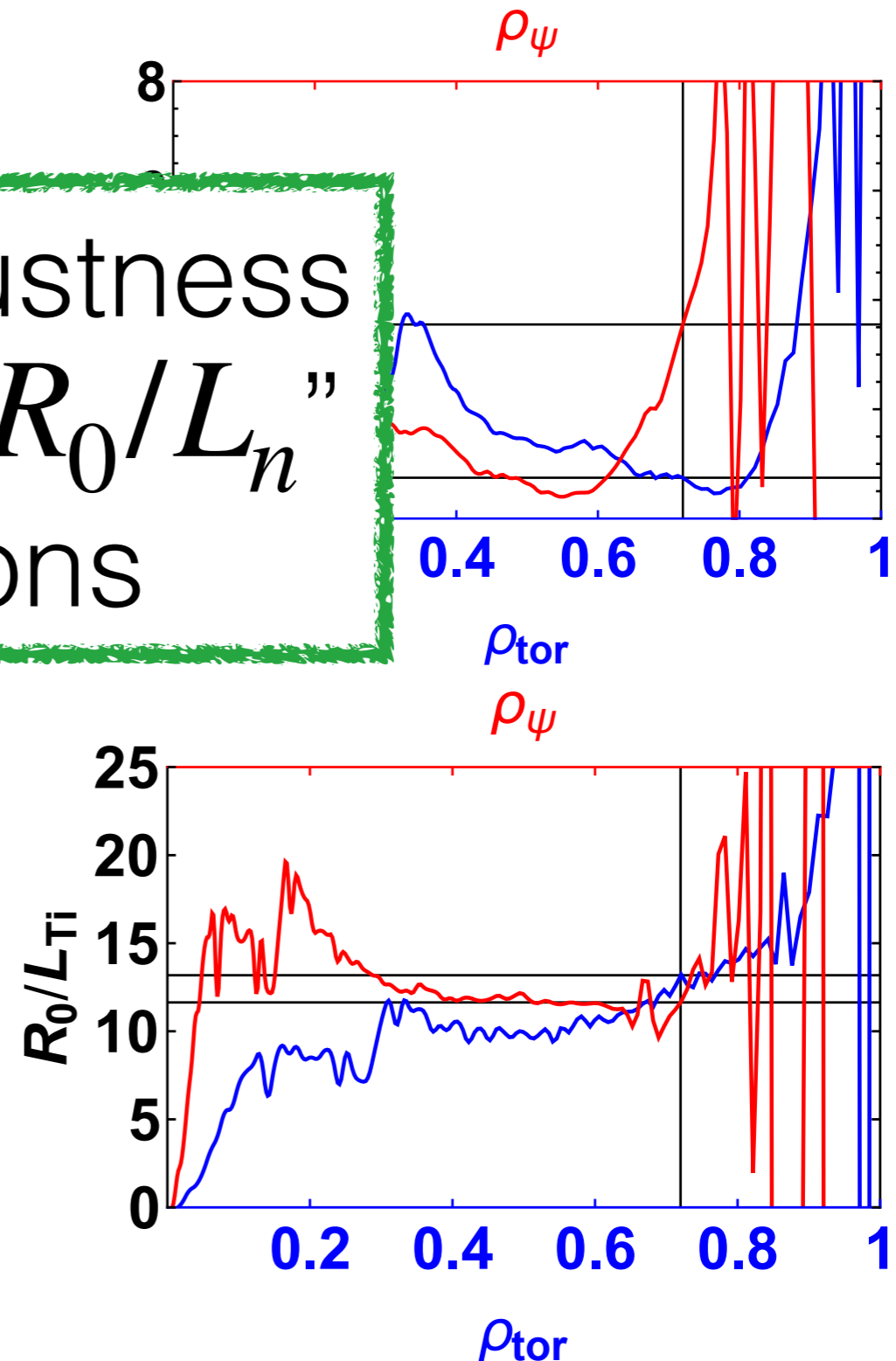
Explore robustness using “high  $R_0/L_n$ ” simulations

- Errors are:

► Should be  $R_0/L_n \approx 0.7$ , not 3.5

- Should be  $R_0/L_{Ts} \approx 13$ , not 11

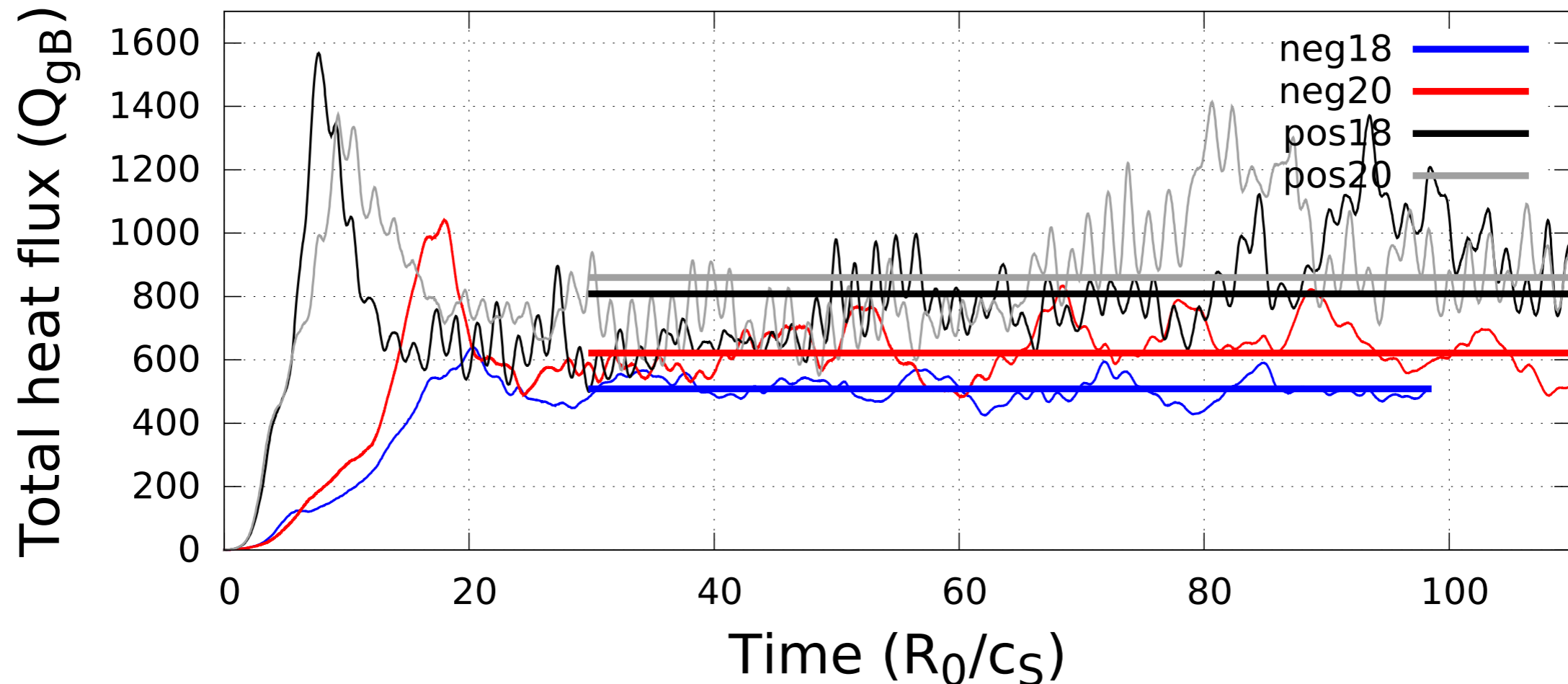
- Should be  $T_i/T_e \approx 1.0$ , not 1.1



# All sorts of results

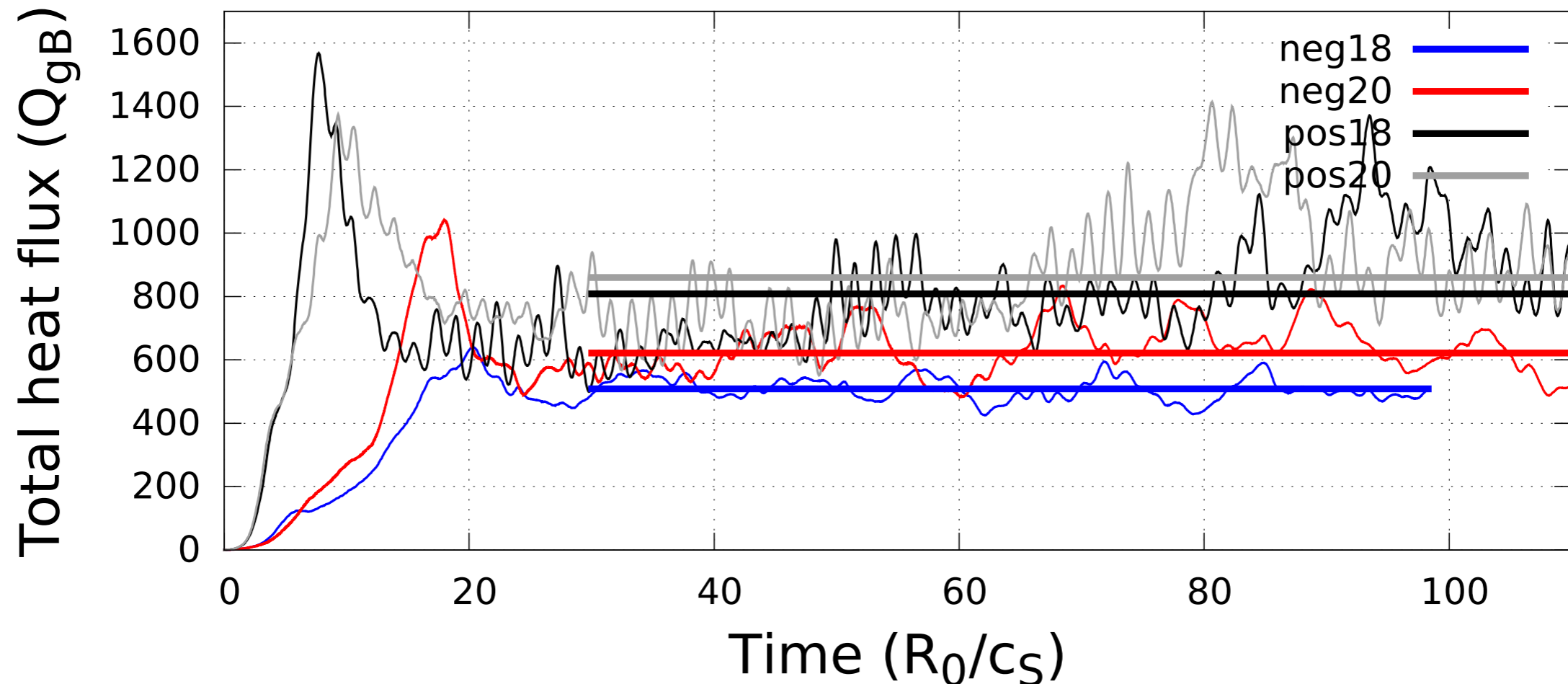
Type	Nominal								High $R_0/L_n$			
	$\rho_{tor}$	0.62		0.72				0.82		0.72		
$I_p$	18MA		18MA		20MA		18MA		18MA		20MA	
$\delta$	pos	neg	pos	neg	pos	neg	pos	neg	pos	neg	pos	neg

# High $R_0/L_n$ , $\rho_{tor} = .72$ : examining past results



- Prior results showed a strong oscillation arising from the zonal flows

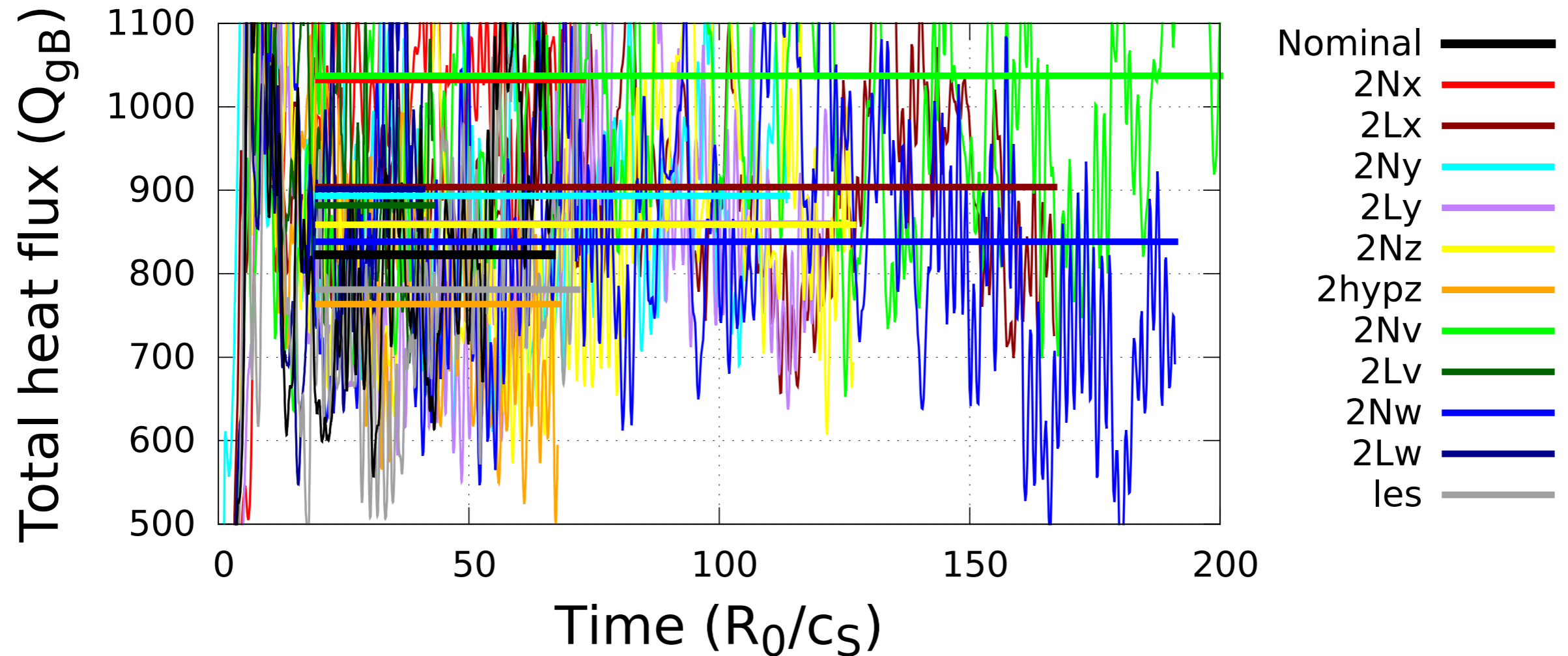
# High $R_0/L_n$ , $\rho_{tor} = .72$ : examining past results



- Prior results showed a strong oscillation arising from the zonal flows
- Appears to be the GAM



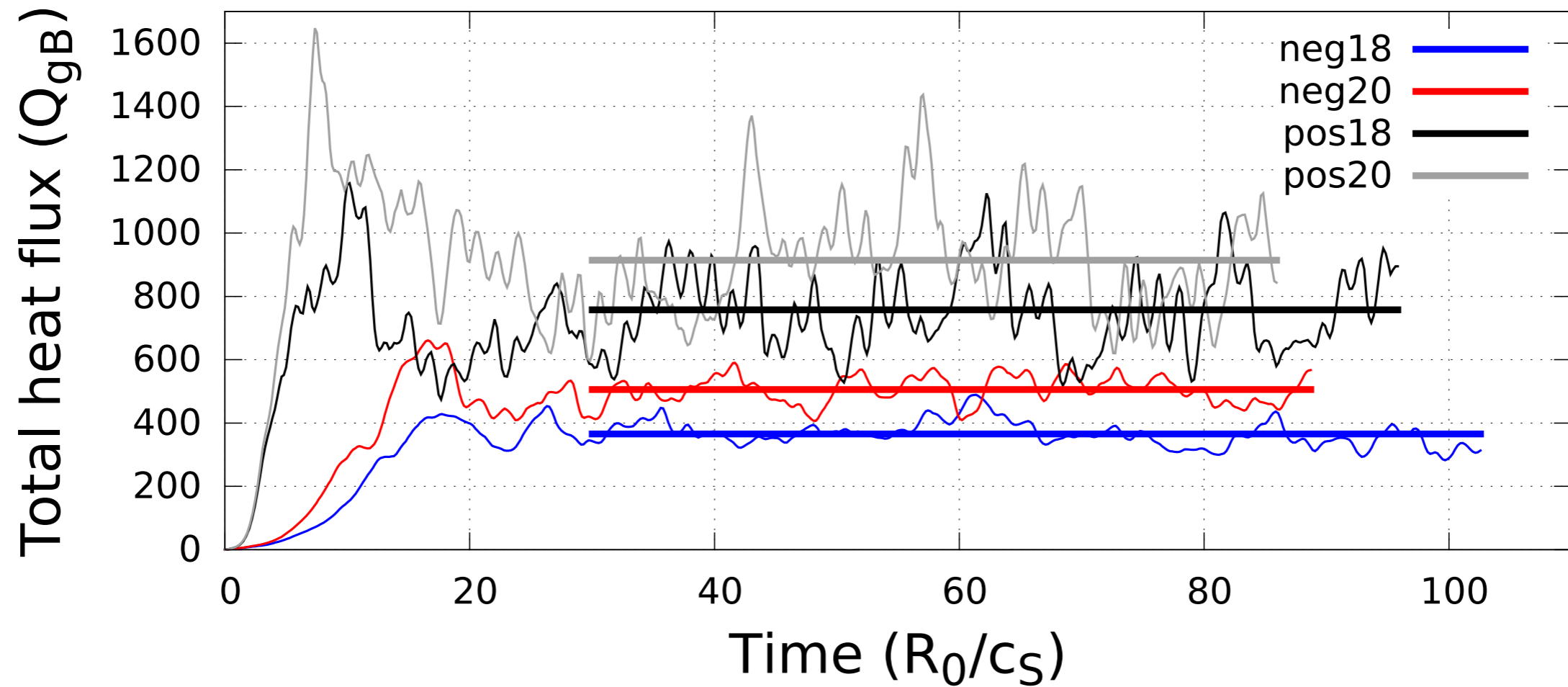
# High $R_0/L_n$ , $\rho_{tor} = .72$ : resolution study



- Found two under-resolved parameters:  $N_x$  and, surprisingly,  $N_{v||}$
- Increasing  $N_{v||}$  reduces the amplitude of the GAM

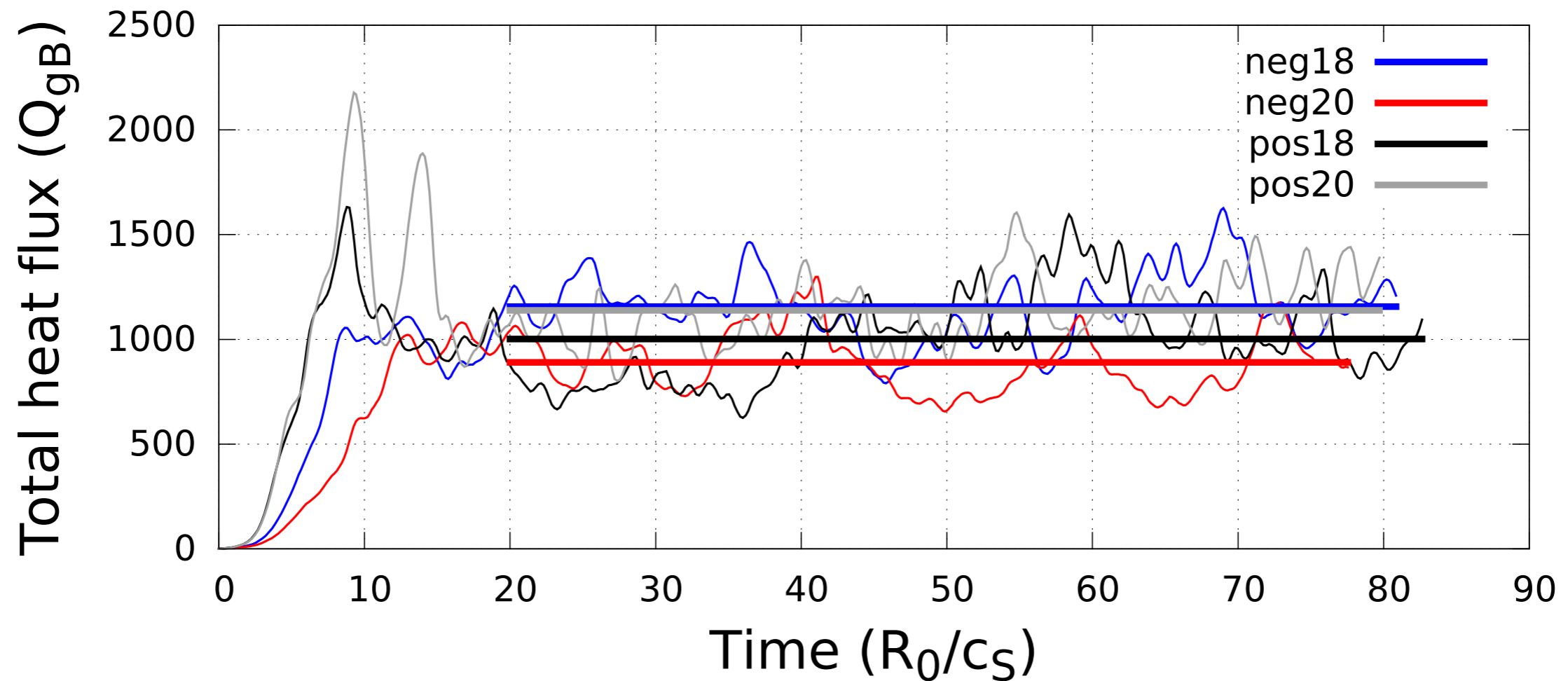
# Main results

# High $R_0/L_n$ , $\rho_{tor} = .72$ : final results



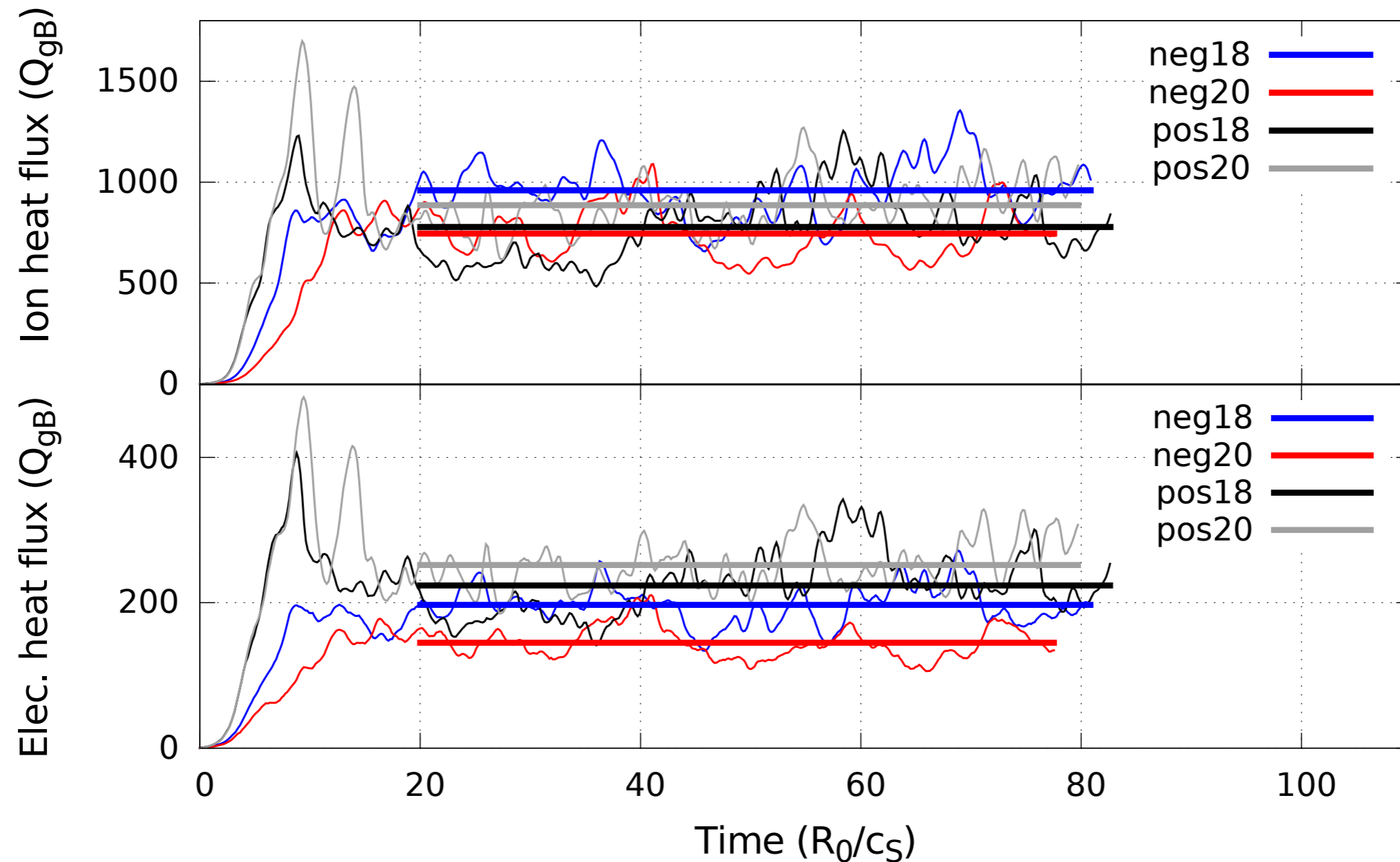
- Similar results as last year

# Nominal, $\rho_{tor} = .72$ : final results



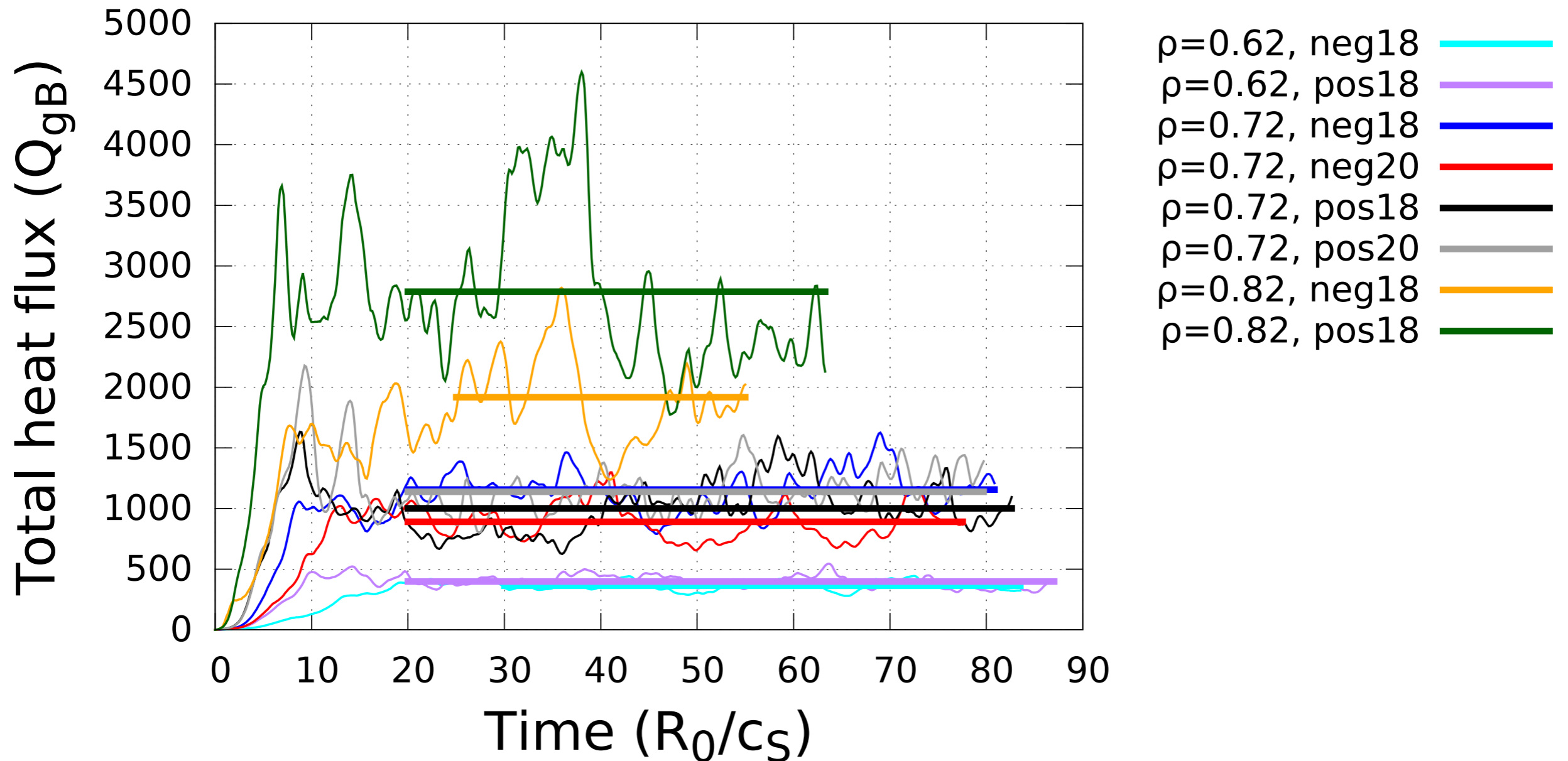
- Somewhat higher values than the high  $R_0/L_n$  cases
- Total heat fluxes are similar between all cases

# Nominal, $\rho_{tor} = .72$ : final results



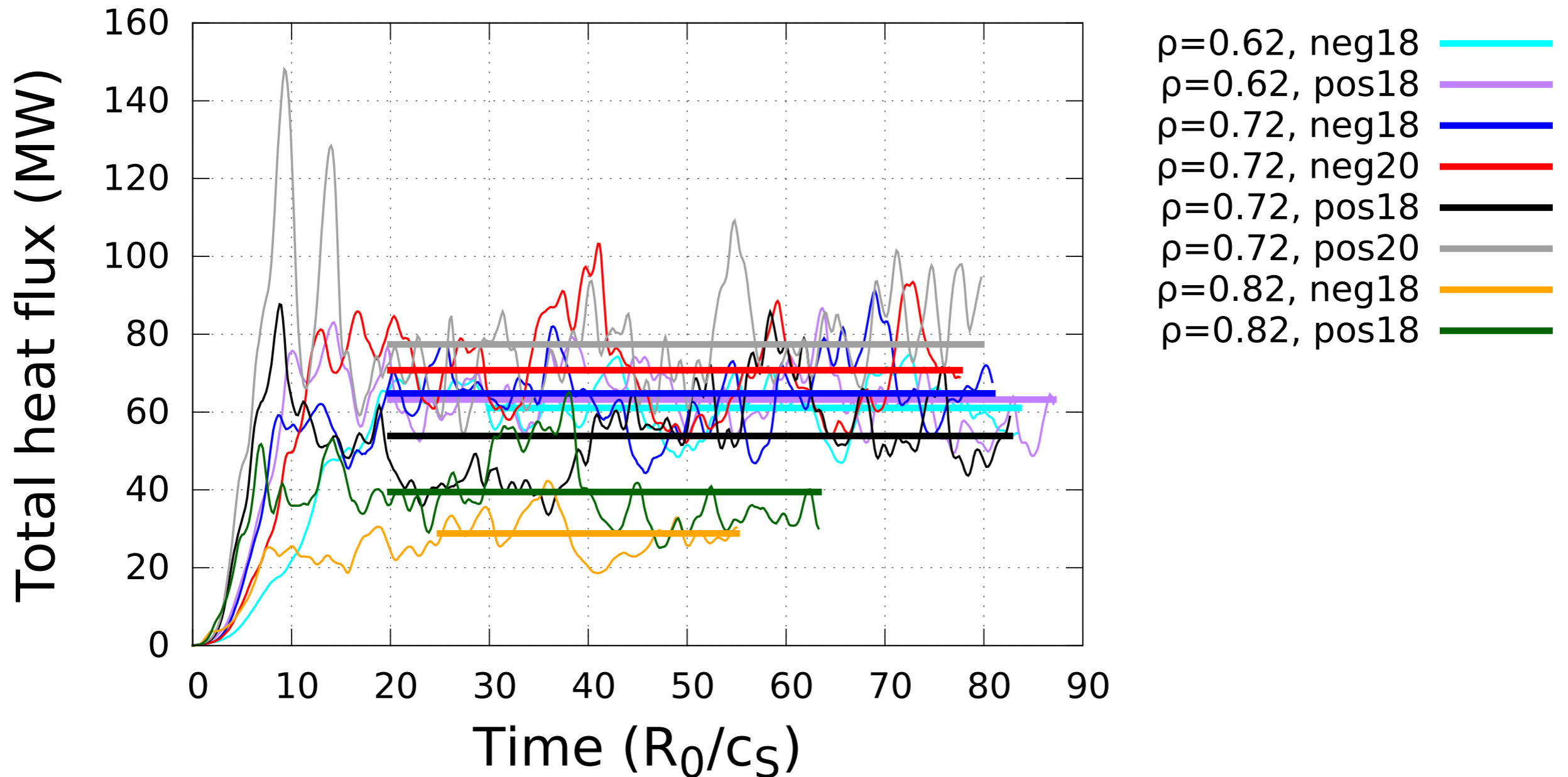
- The ion heat flux is dominant in these simulations, but **the electron heat flux is reduced by negative triangularity**

# Nominal, $\rho_{tor} = .62, .72, .82$ : final results



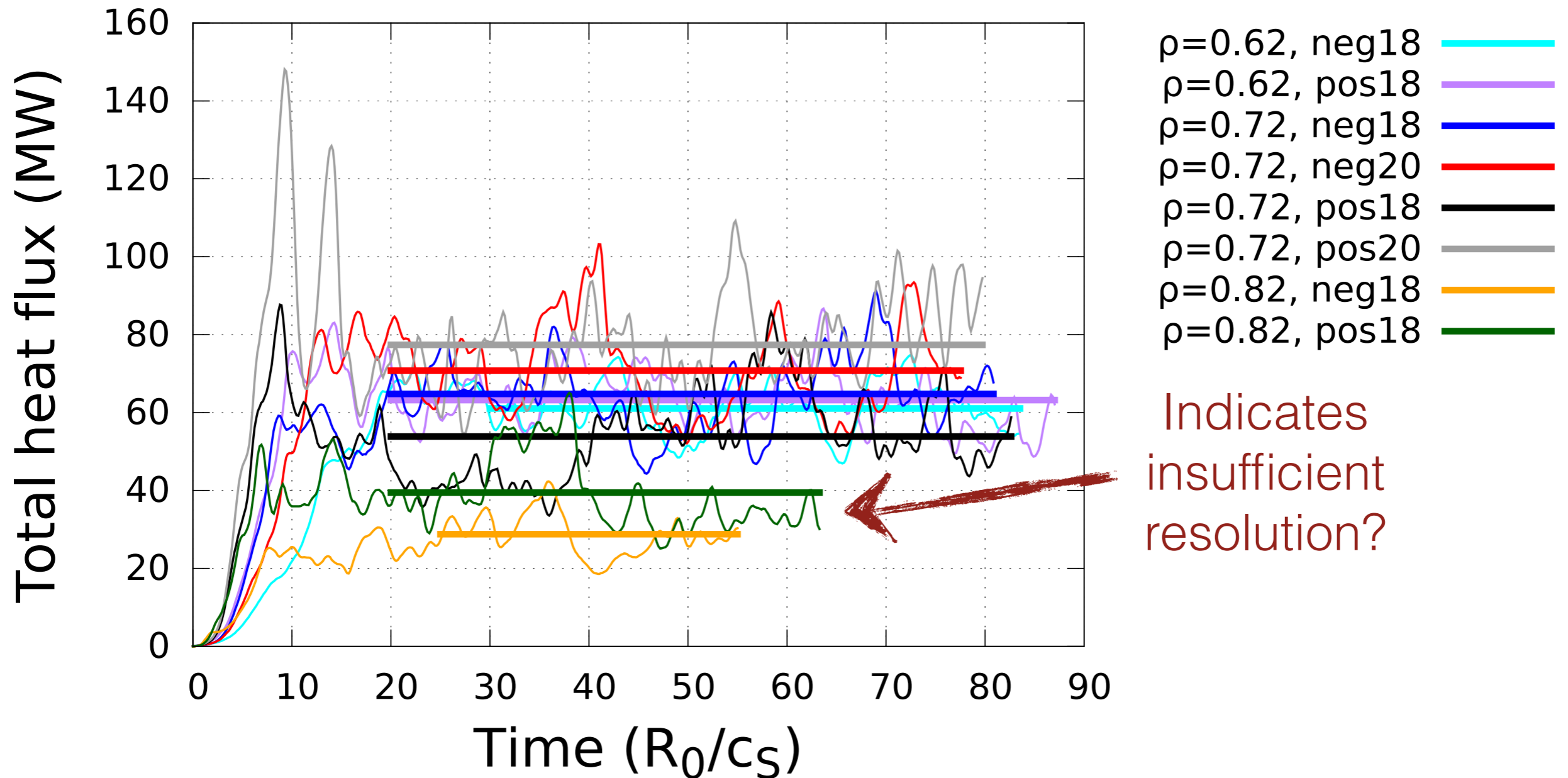
- Heat flux increases with radius in gyroBohm units

# Nominal, $\rho_{tor} = .62, .72, .82$ : final results



- Heat flux increases with radius in gyroBohm units, but not in MW

# Nominal, $\rho_{tor} = .62, .72, .82$ : final results

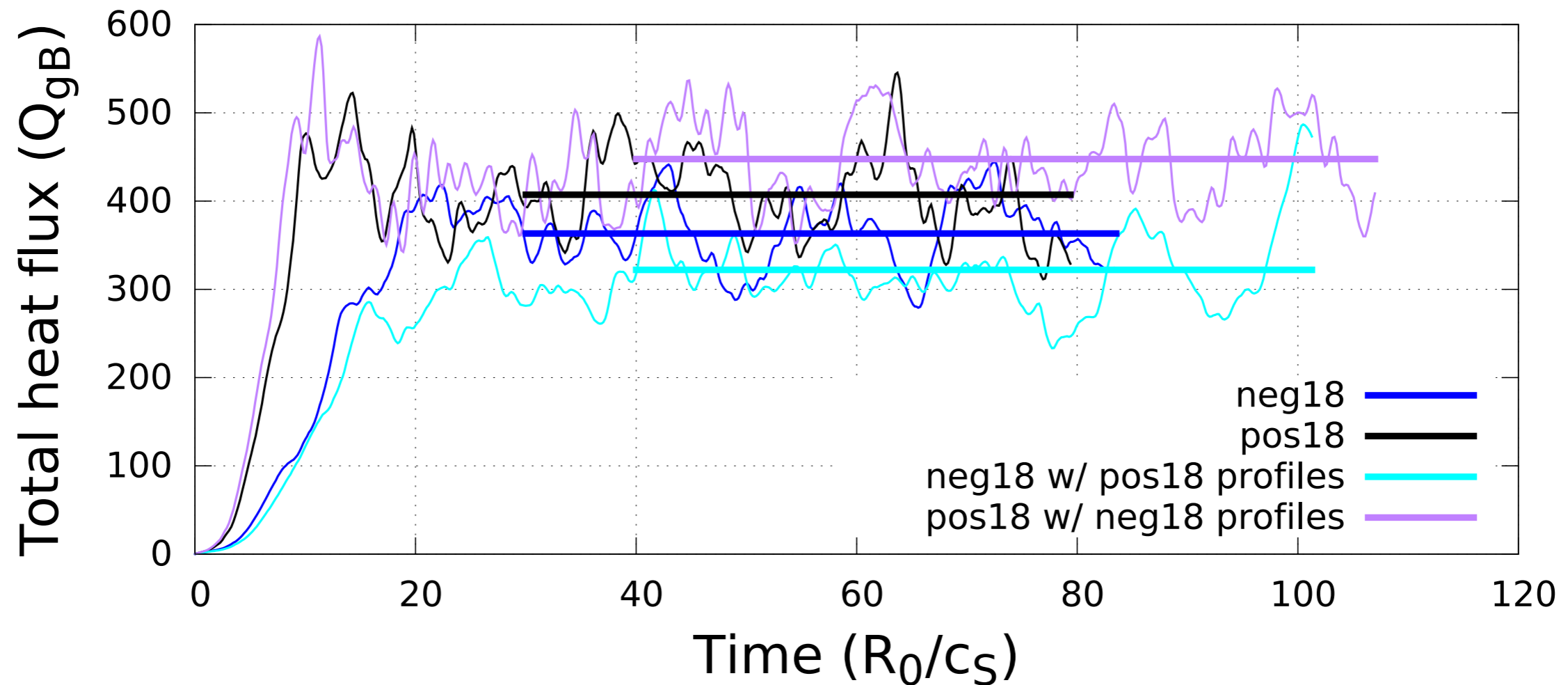


- Heat flux increases with radius in gyroBohm units, but not in MW



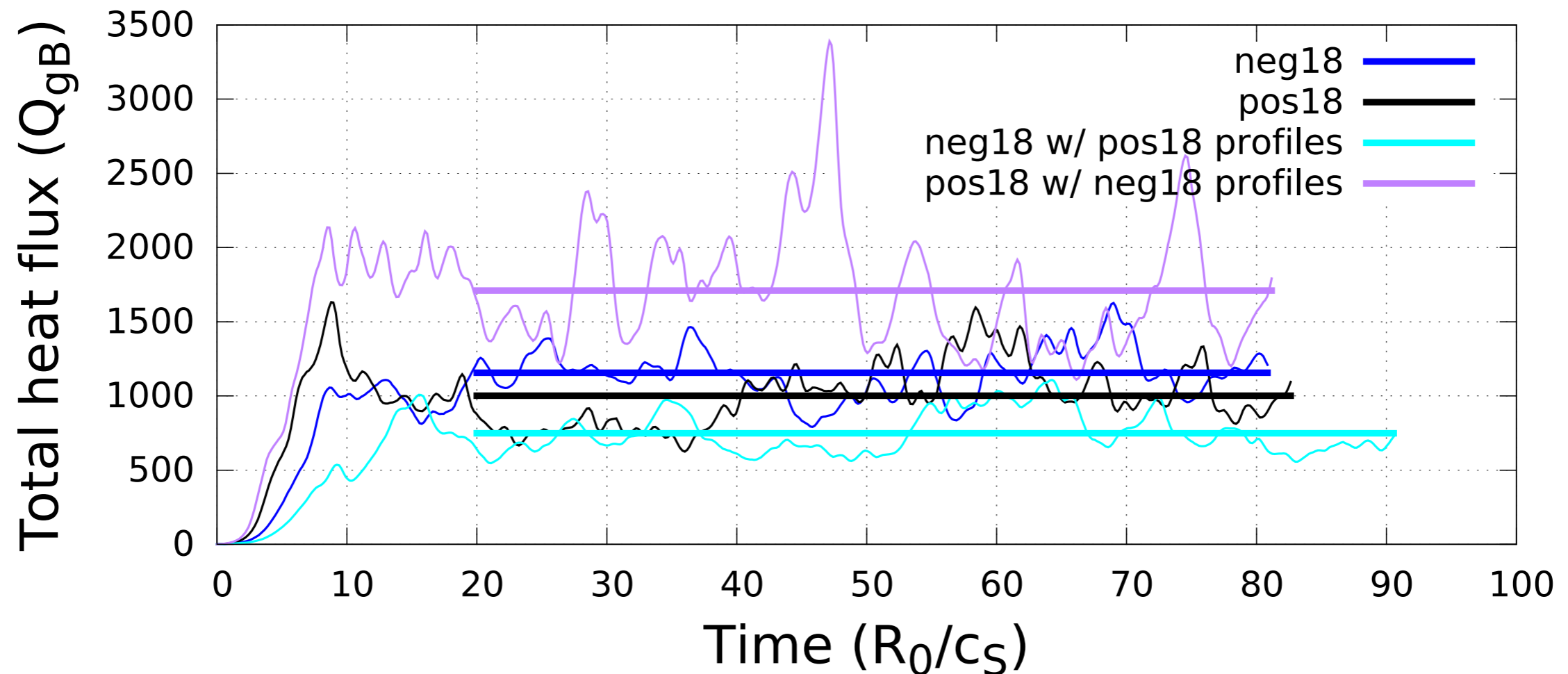
# Swapping plasma profiles

# Nominal, $\rho_{tor} = .62$ : swapping plasma profiles



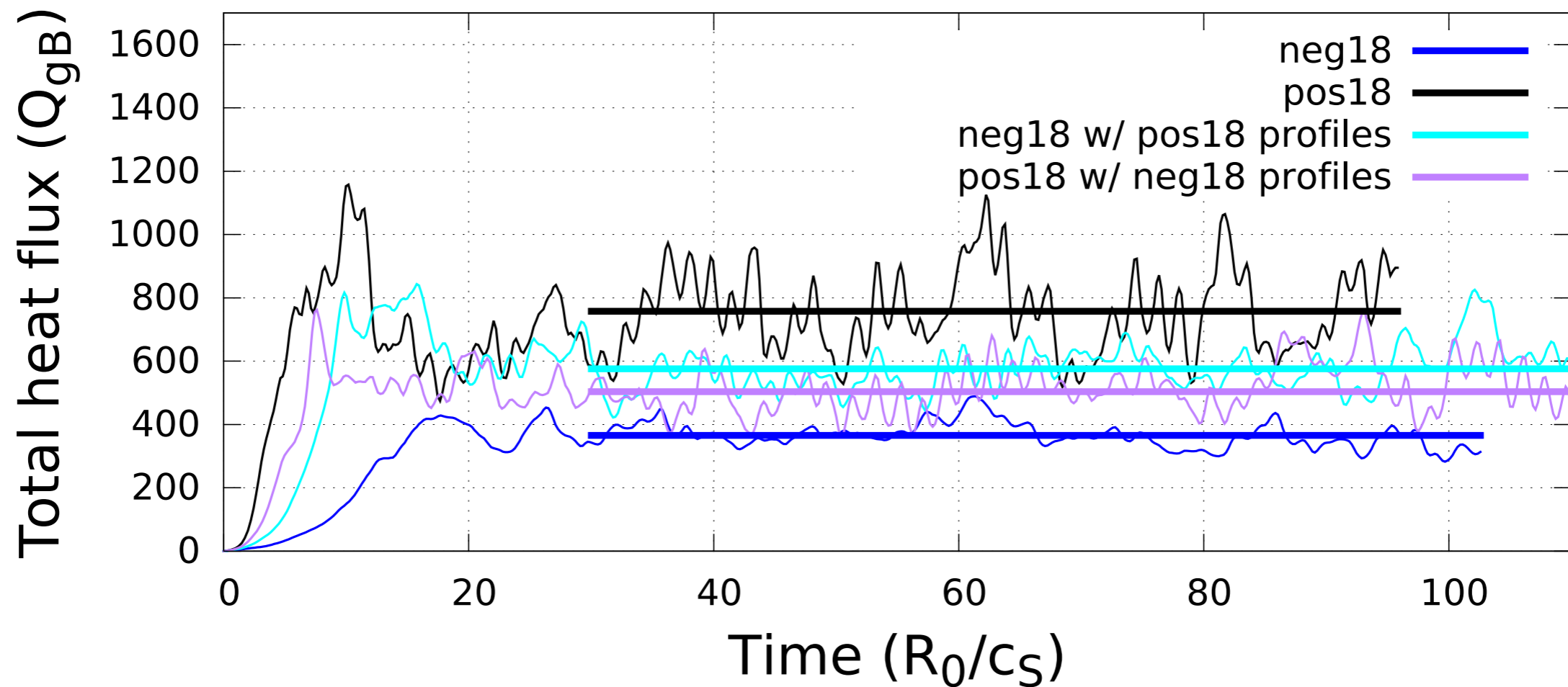
- Negative  $\delta$  magnetic geometry is stabilizing (holding profiles constant)
- Changes the heat flux by roughly 20%

# Nominal, $\rho_{tor} = .72$ : swapping plasma profiles



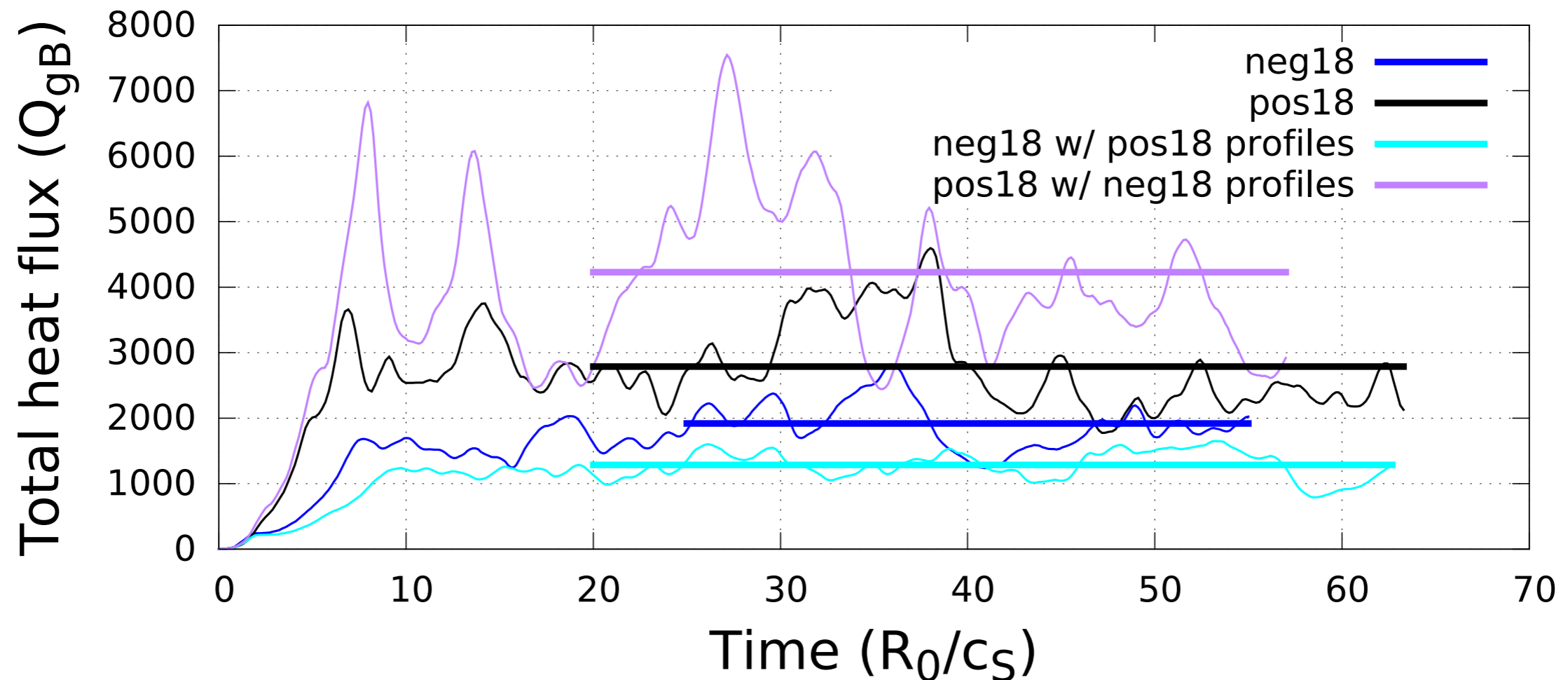
- Negative  $\delta$  magnetic geometry is stabilizing (holding profiles constant)
- Changes the heat flux by roughly 40%

# High $R_0/L_n$ , $\rho_{tor} = .72$ : swapping plasma profiles



- Negative  $\delta$  magnetic geometry is stabilizing (holding profiles constant)
- Changes the heat flux by roughly 30%

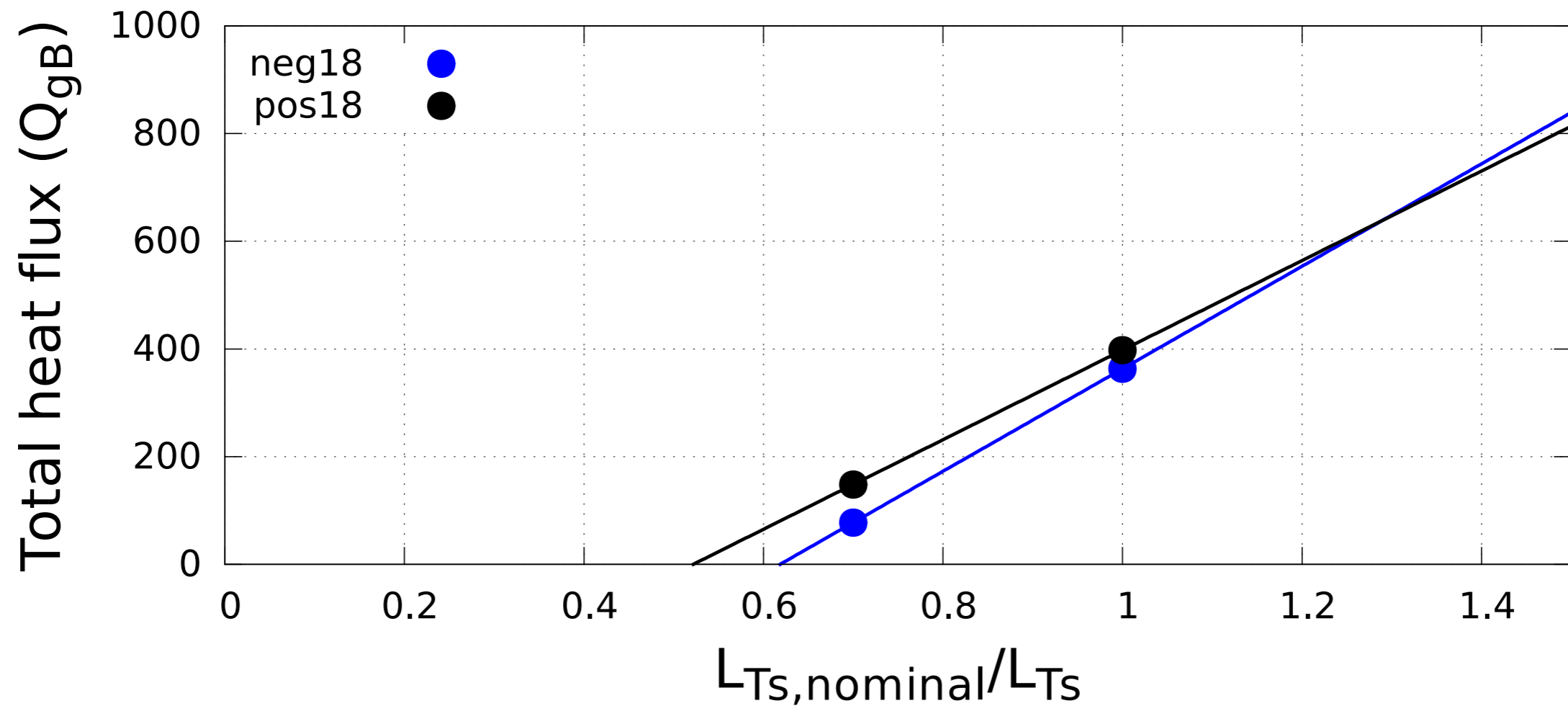
# Nominal, $\rho_{tor} = .82$ : swapping plasma profiles



- Negative  $\delta$  magnetic geometry is stabilizing (holding profiles constant)
- Changes the heat flux by roughly 65%

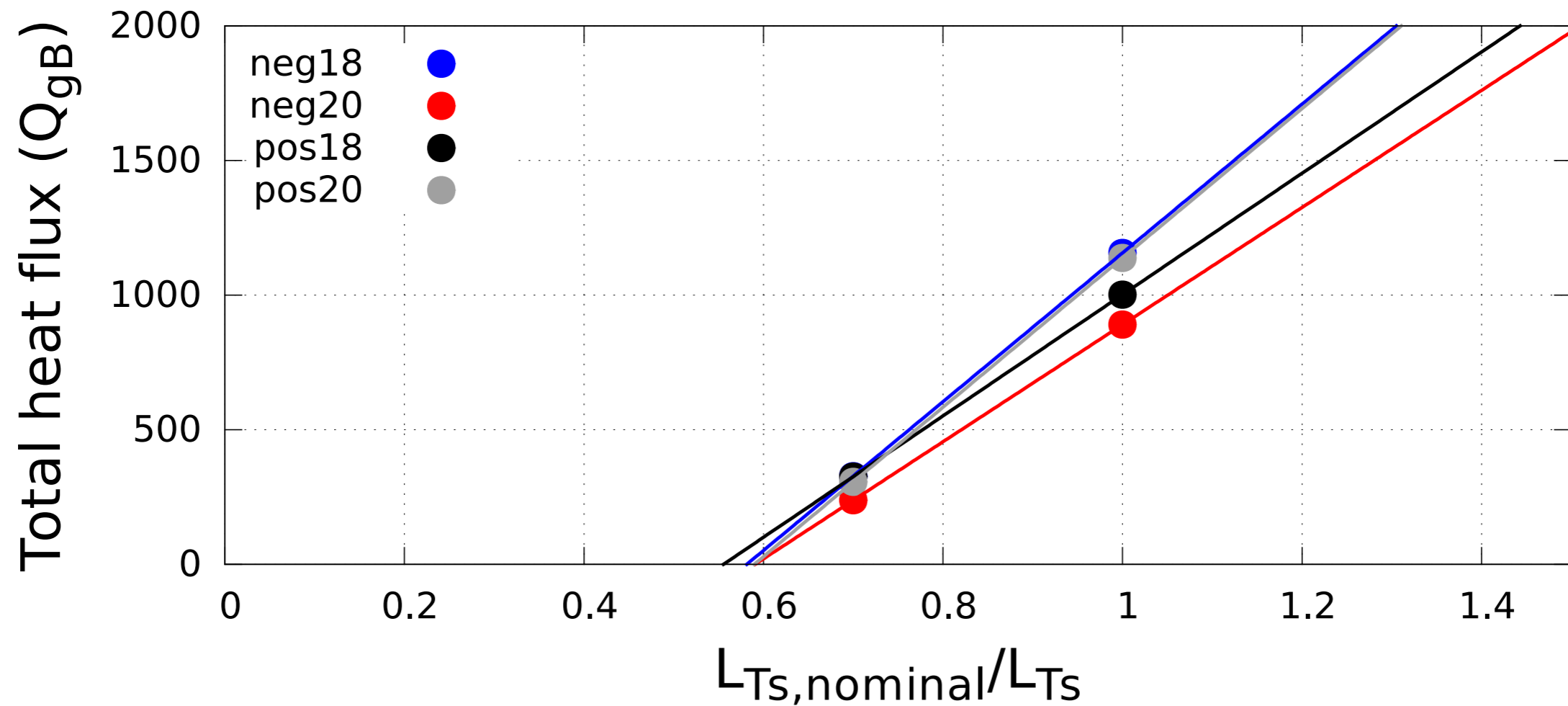
# Investigating profile stiffness

# Nominal, $\rho_{tor} = .62$ : profile stiffness



- Triangularity has little effect on stiffness
- Similar critical gradients

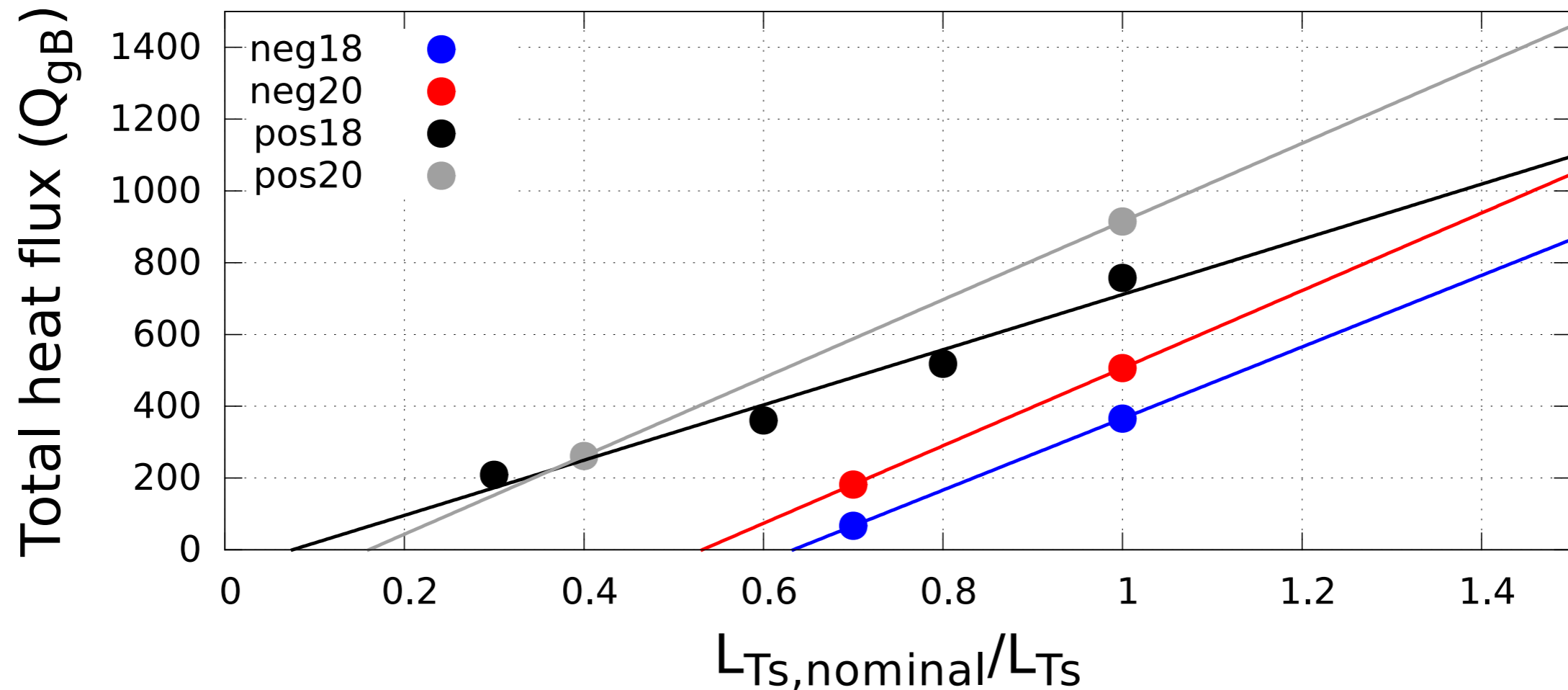
# Nominal, $\rho_{tor} = .72$ : profile stiffness



- Triangularity has little effect on stiffness
- Similar critical gradients

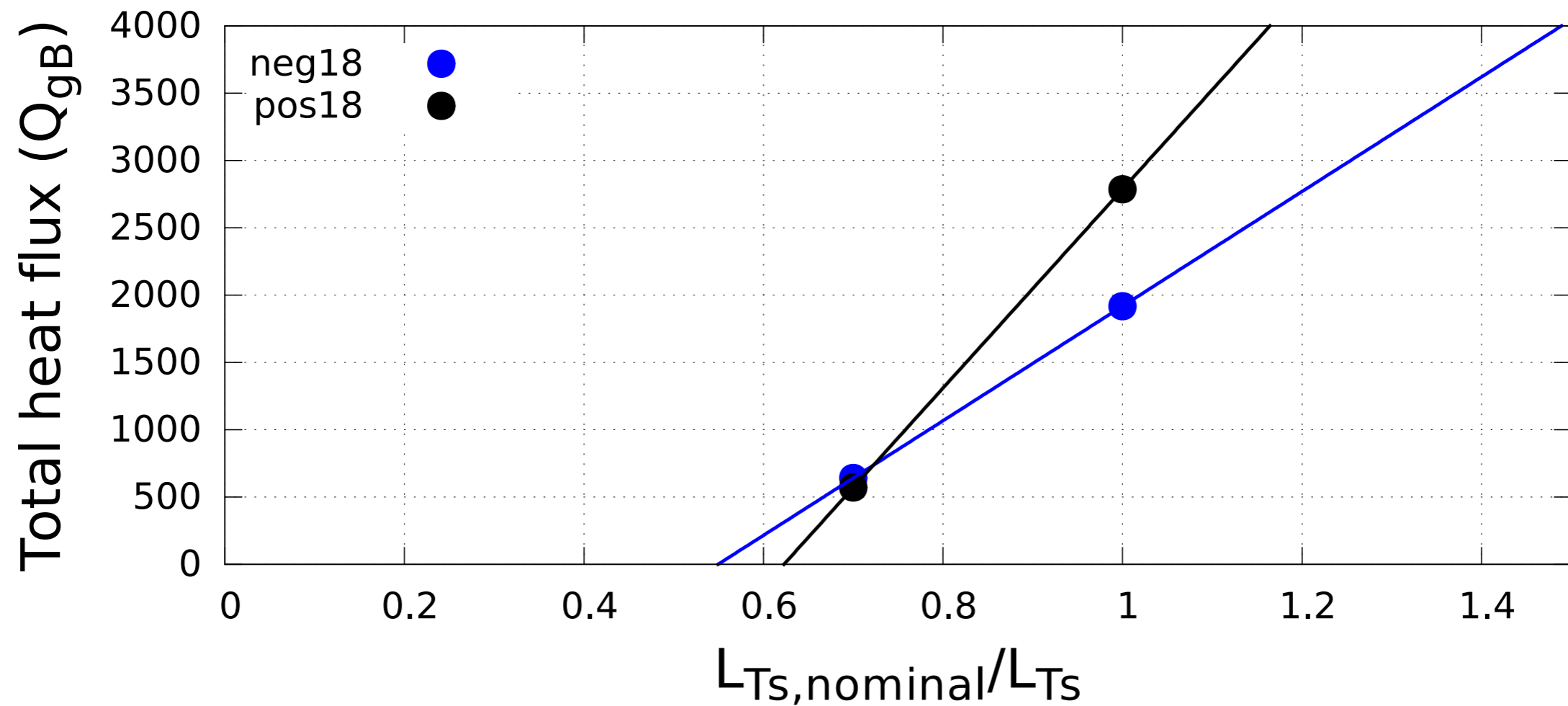


# High $R_0/L_n$ , $\rho_{tor} = .72$ : profile stiffness



- Negative  $\delta$  is slightly more stiff than positive  $\delta$
- Different critical gradient, but remember these profiles are inconsistent

# Nominal, $\rho_{tor} = .82$ : profile stiffness



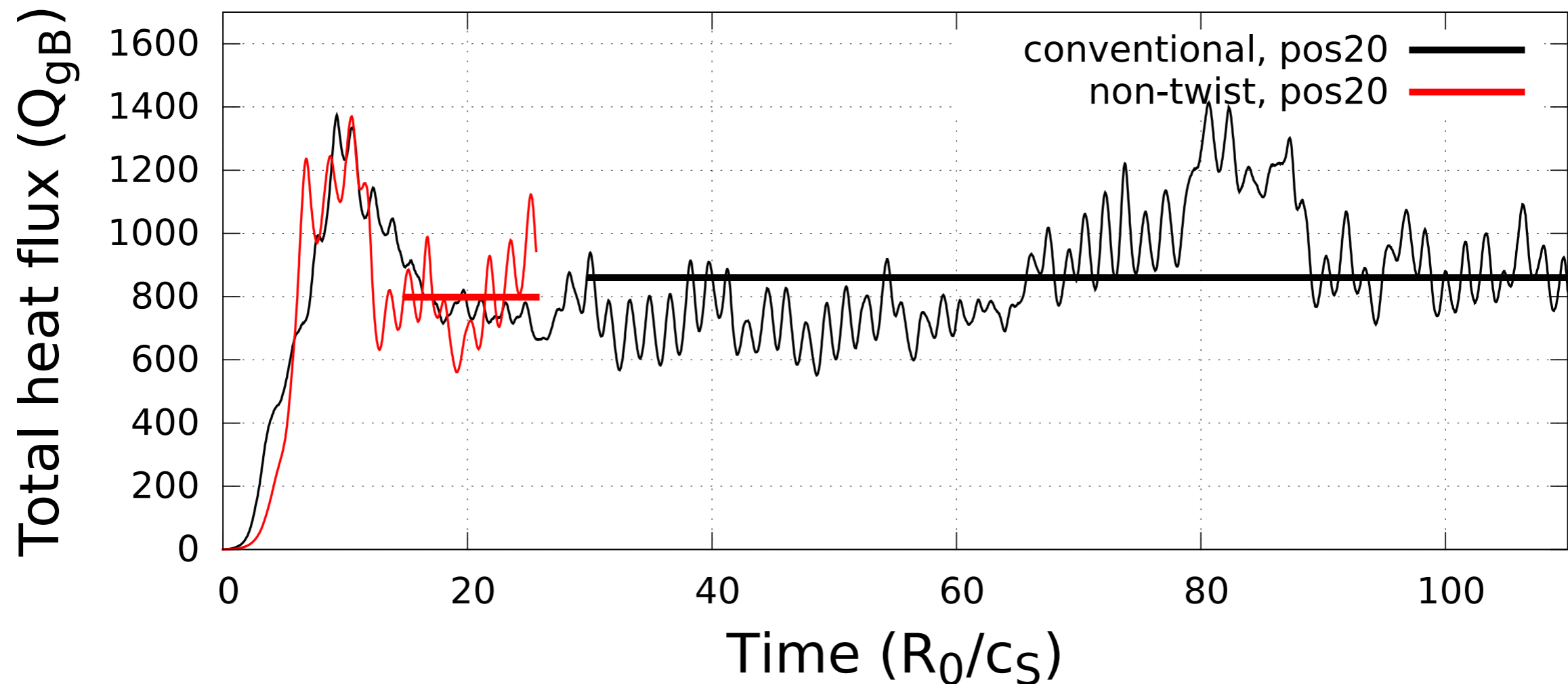
- Indicates that positive  $\delta$  is somewhat more stiff
- Similar critical gradients

# Takeaways

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- These simulations indicate that (in order of robustness):
  1. negative  $\delta$  lowers the fraction of heat transported by electrons
  2. negative  $\delta$  reduces heat transport at constant plasma profiles
  3. both the plasma profiles and the magnetic geometry have a significant impact on the heat flux, which seems to increase with minor radial location
  4. positive vs. negative  $\delta$  has minimal effect on profile stiffness

# Future work

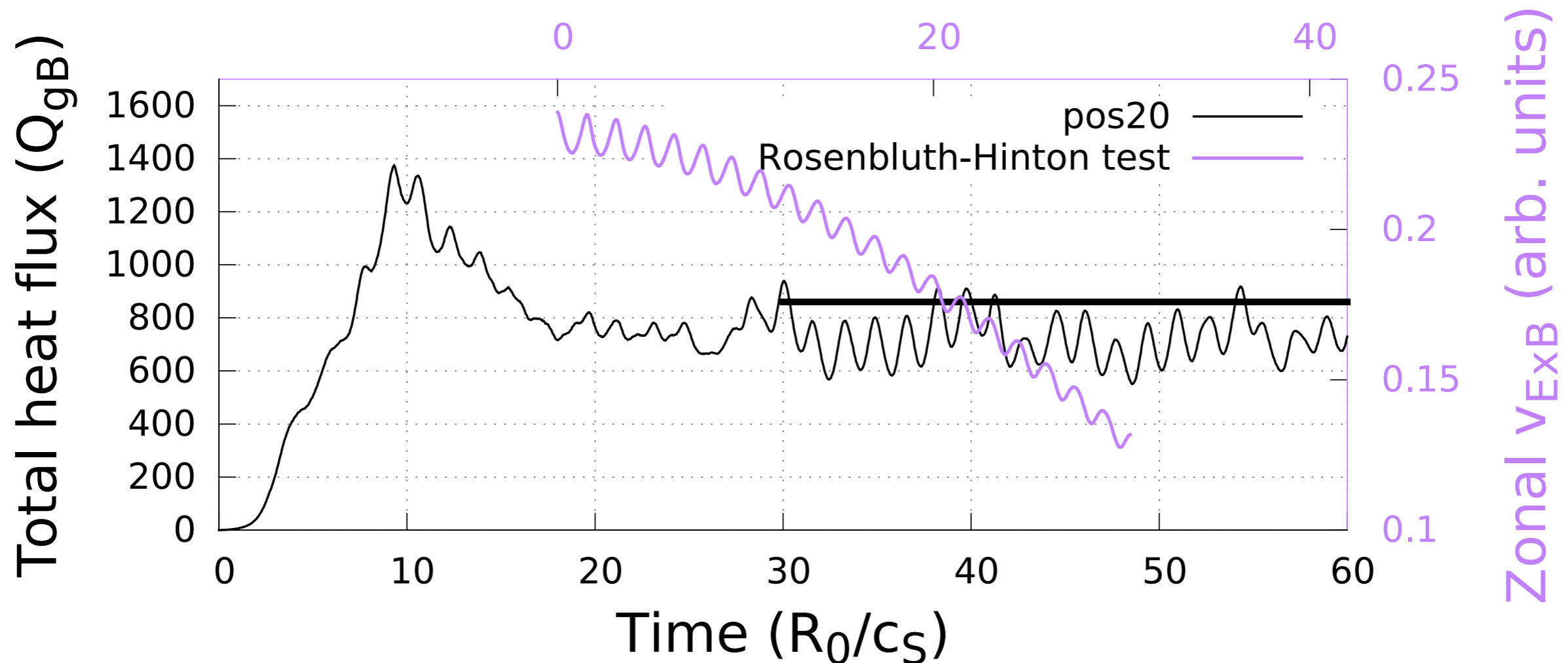


- Test if new type of simulation domain can make high  $\hat{s}$  simulations cheaper
- Swap individual geometric coefficients to determine which are important

Thank you!

# High $R_0/L_n$ , $\rho_{tor} = .72$ : examining past results

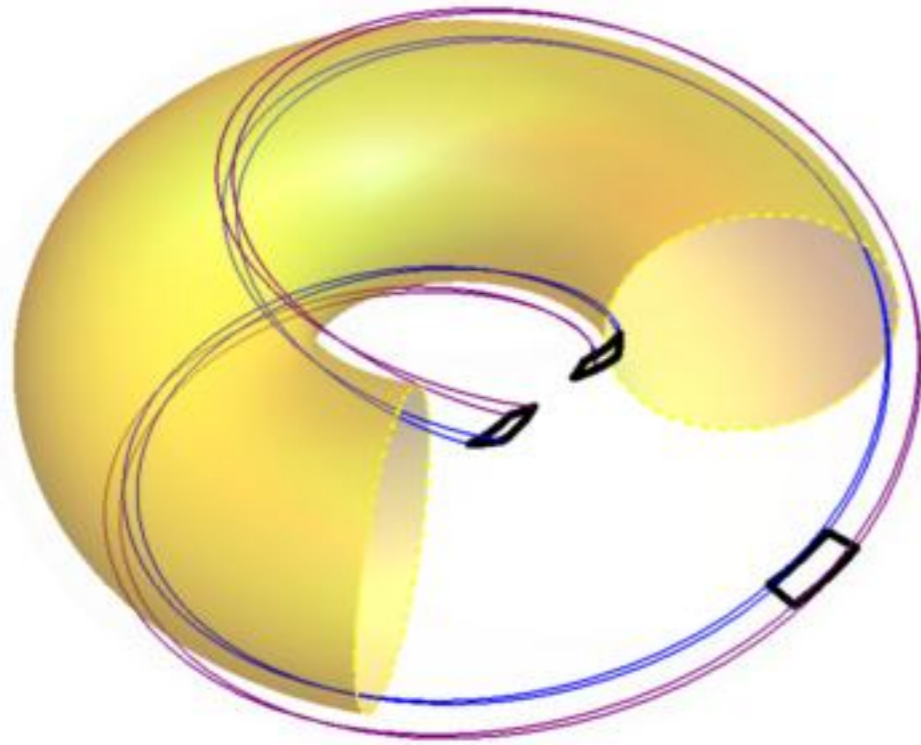
Sugama and Watanabe, *J. Plasma Phys.* **72** (2006).



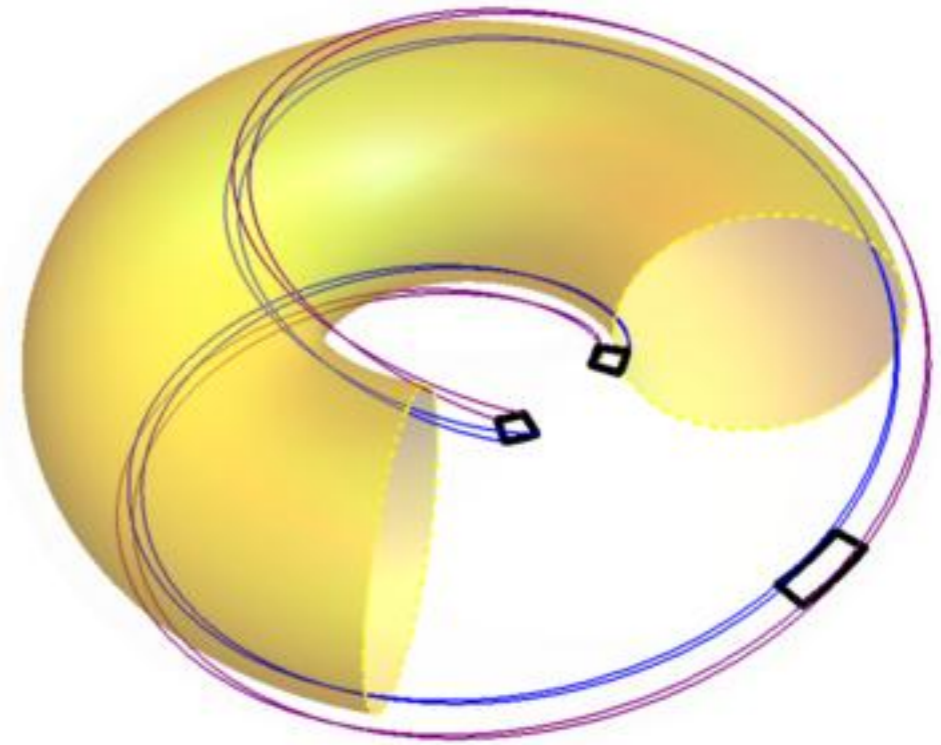
- Appears to be the GAM, as the frequency matches a Rosenbluth-Hinton test and is close to simple theoretical predictions

# Non-twisting flux tube to move outwards

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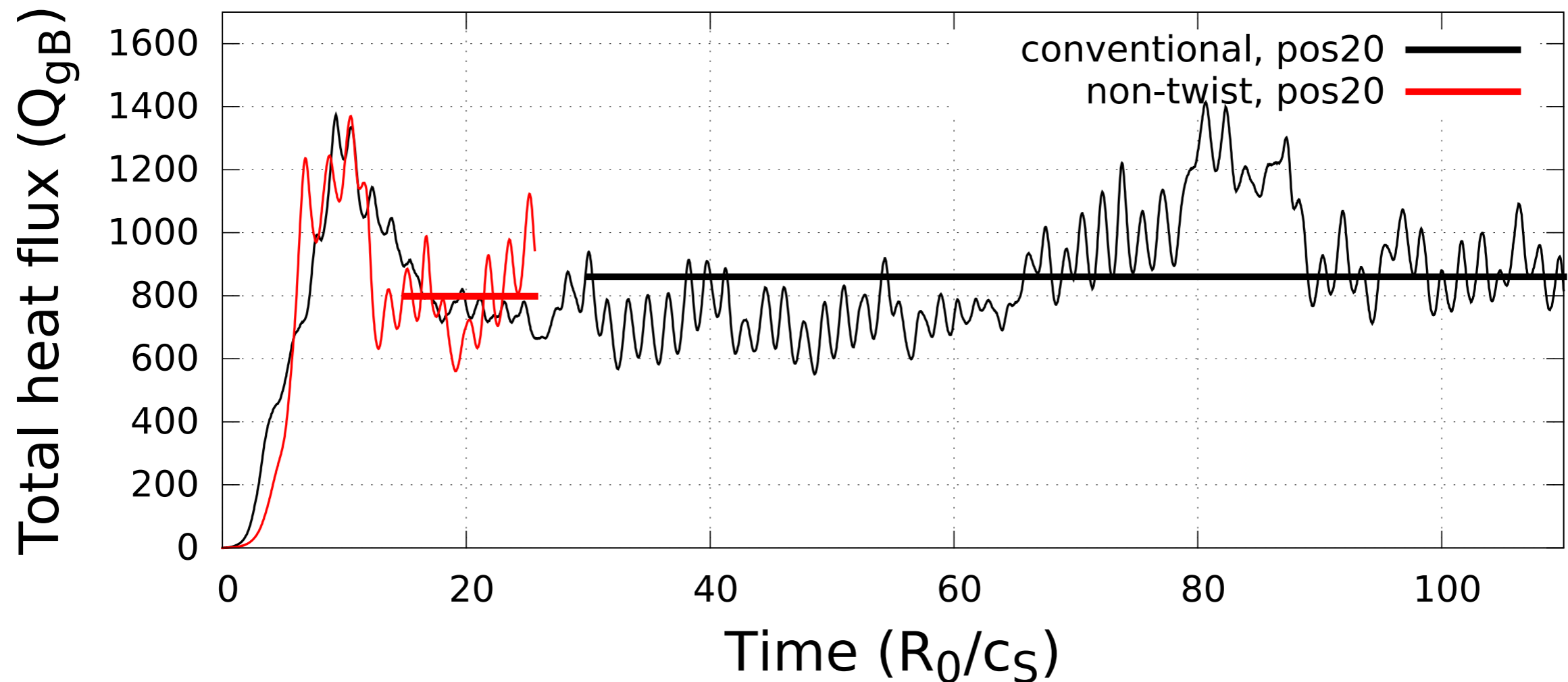
Conventional



Non-twisting

- Domain follows a central field line, but allows magnetic shear to move field lines through the periodic domain
- Should enable more efficient numerical treatment of large magnetic shear

# Non-twisting flux tube benchmark

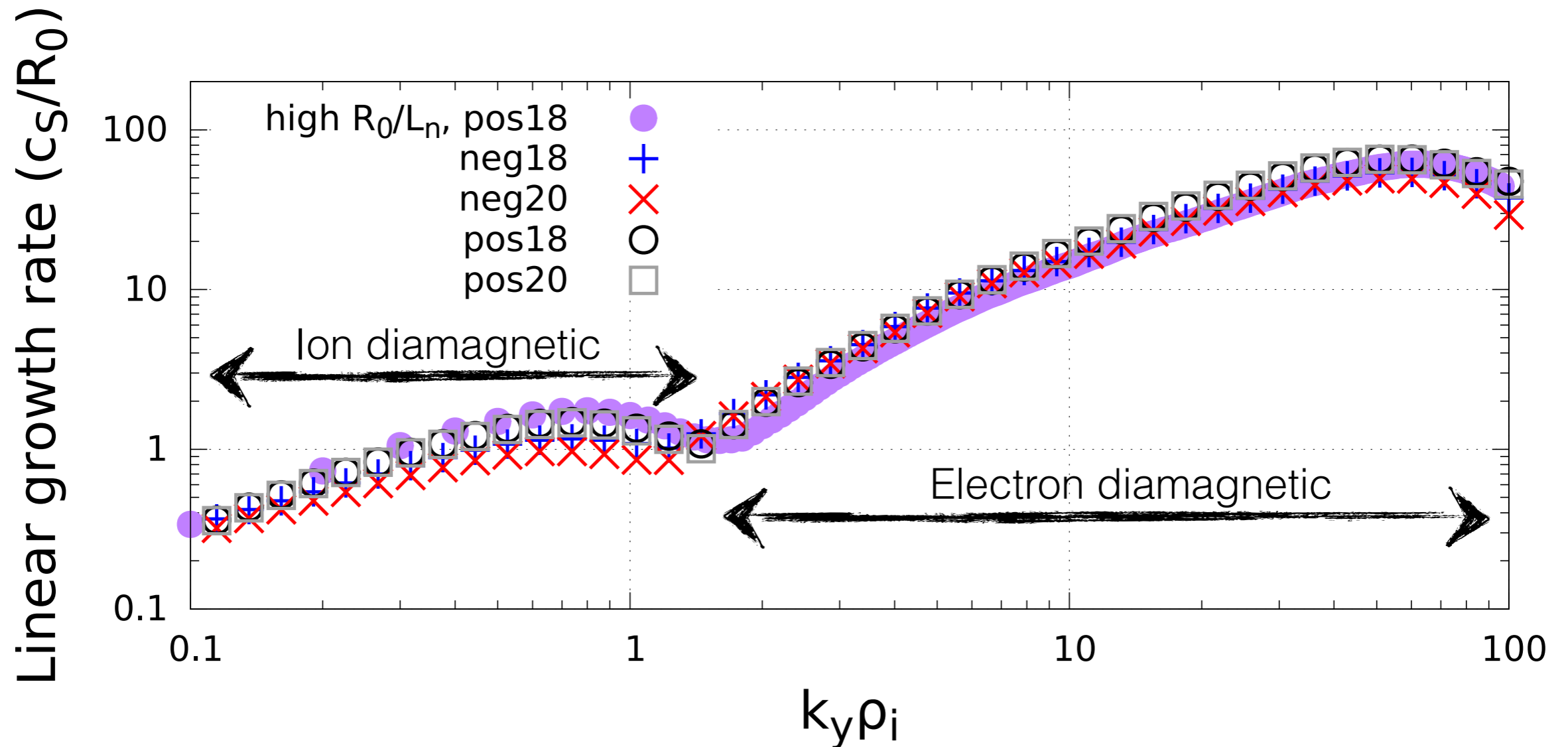


- Benchmarked using full nonlinear DEMO geometry and kinetic electrons
- Next perform radial resolution study to determine computational savings



# Nominal: Linear spectrum with kinetic electrons

Staebler et al. *Nucl. Fusion* **57** (2017).

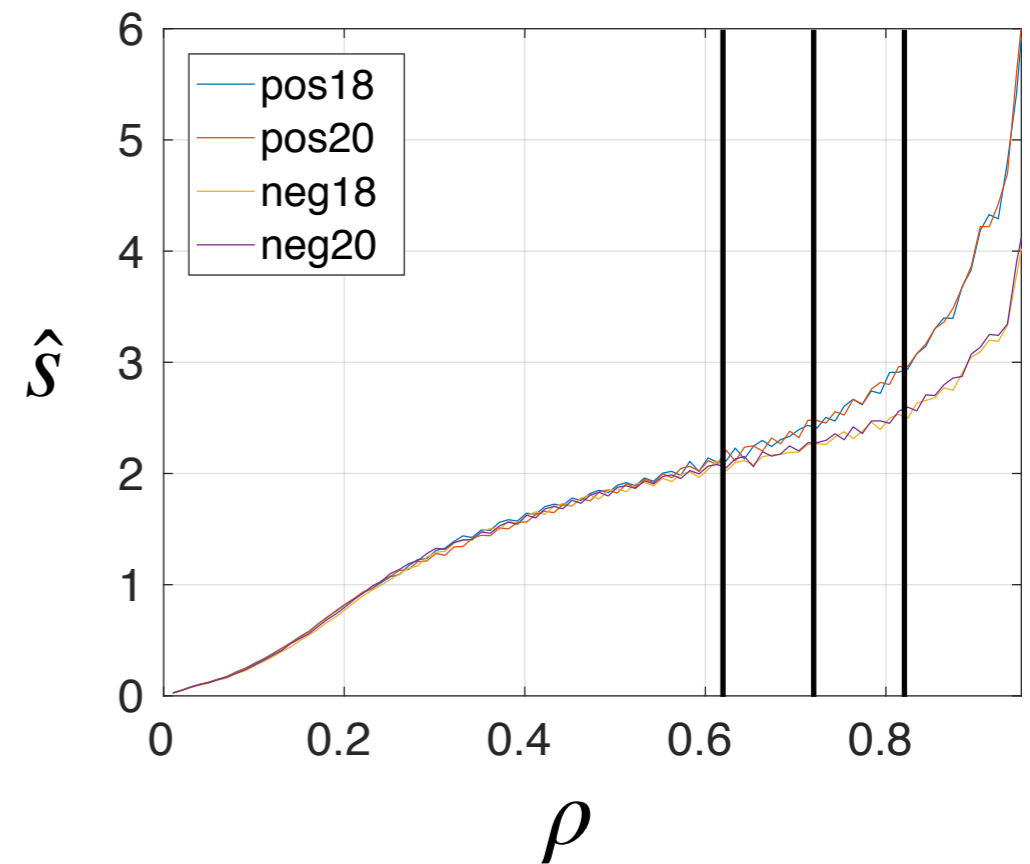


- Like the high  $R_0/L_n$  case: comparing  $\gamma/k_y \Big|_{ITG} \approx 2.0$  with  $\gamma/k_y \Big|_{ETG} \approx 1.3$ , suggests that multi-scale interactions are marginal

# Simulate flux surfaces at $\rho = \{0.62, 0.72, 0.82\}$

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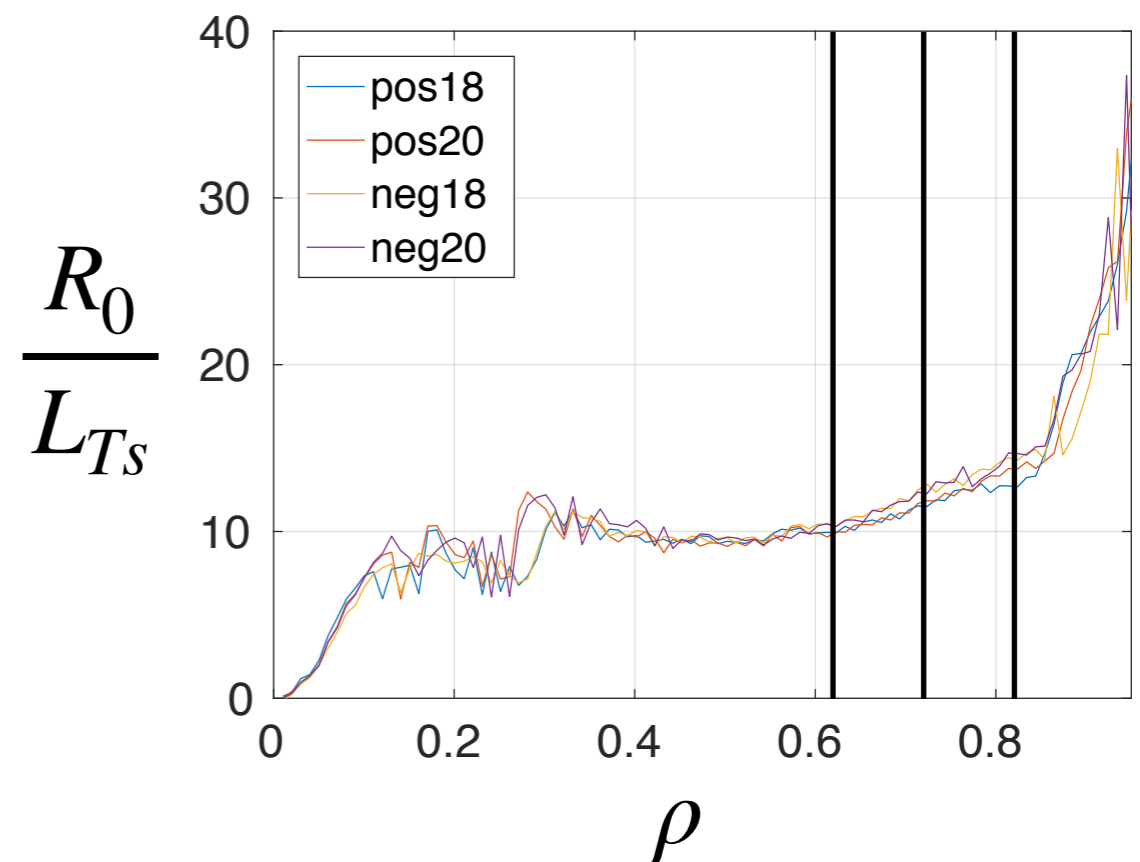
- Simulations near the edge are difficult due to:
  - Large values of magnetic shear



# Simulate flux surfaces at $\rho = \{0.62, 0.72, 0.82\}$

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- Simulations near the edge are difficult due to:
  - Large values of magnetic shear
  - Large logarithmic gradients



# Simulate flux surfaces at $\rho = \{0.62, 0.72, 0.82\}$

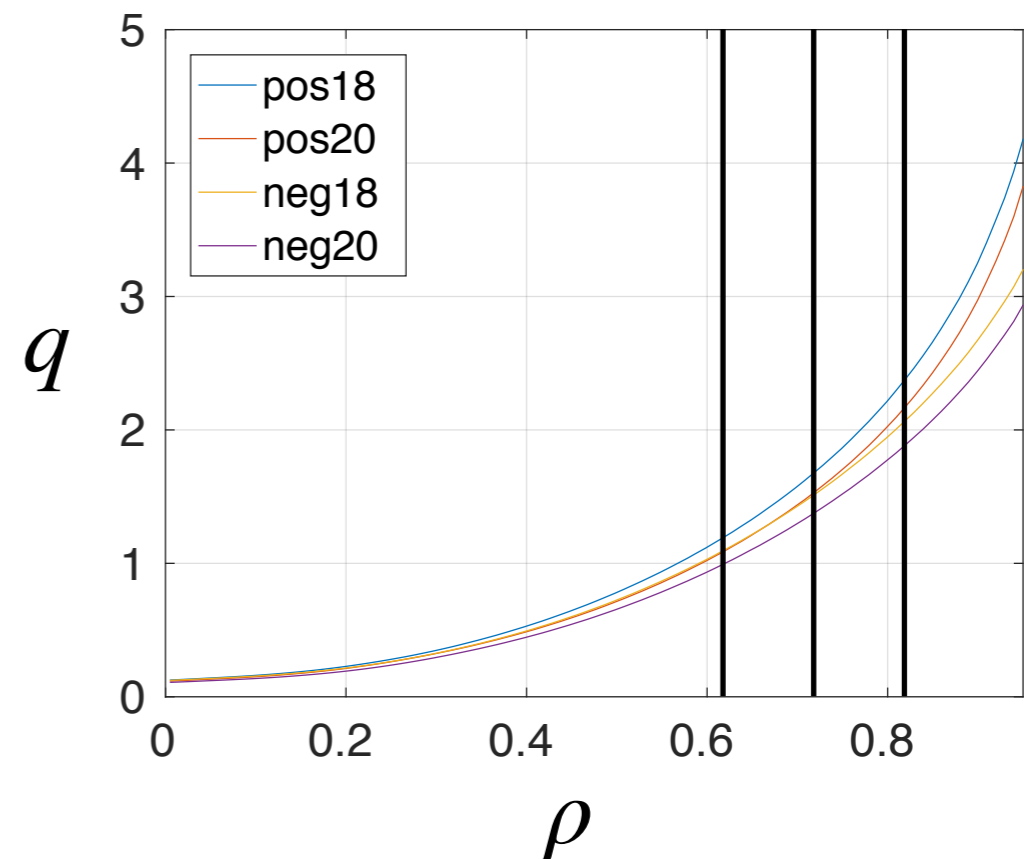
---

- Simulations near the edge are difficult due to:

- Large values of magnetic shear
- Large logarithmic gradients

- Simulations in the core are problematic because:

- Sawtooth inversion radius at  $\rho \approx 0.6$



# Simulate flux surfaces at $\rho = \{0.62, 0.72, 0.82\}$

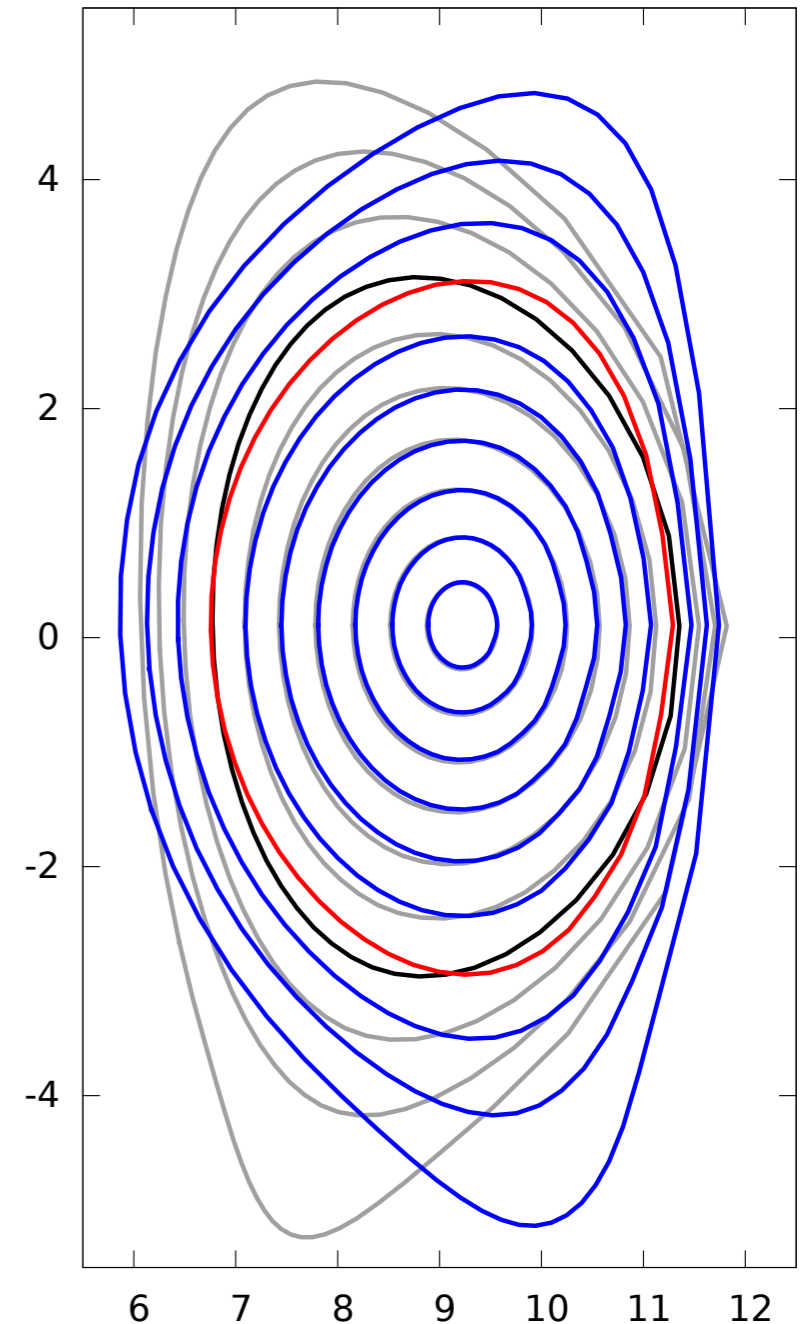
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- Simulations near the edge are difficult due to:

- Large values of magnetic shear
- Large logarithmic gradients

- Simulations in the core are problematic because:

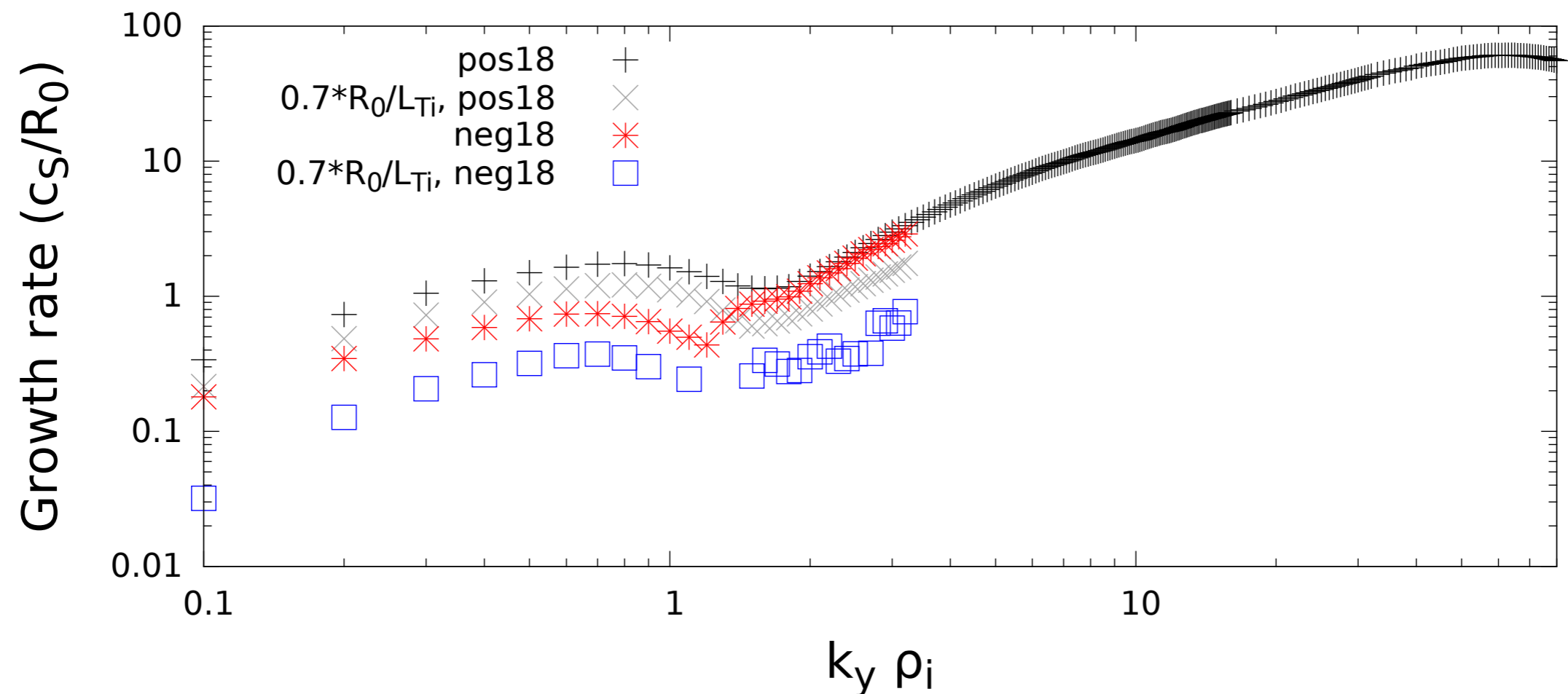
- Sawtooth inversion radius at  $\rho \approx 0.6$
- Impact of triangularity is weaker



# Last year: Linear results with kinetic electrons

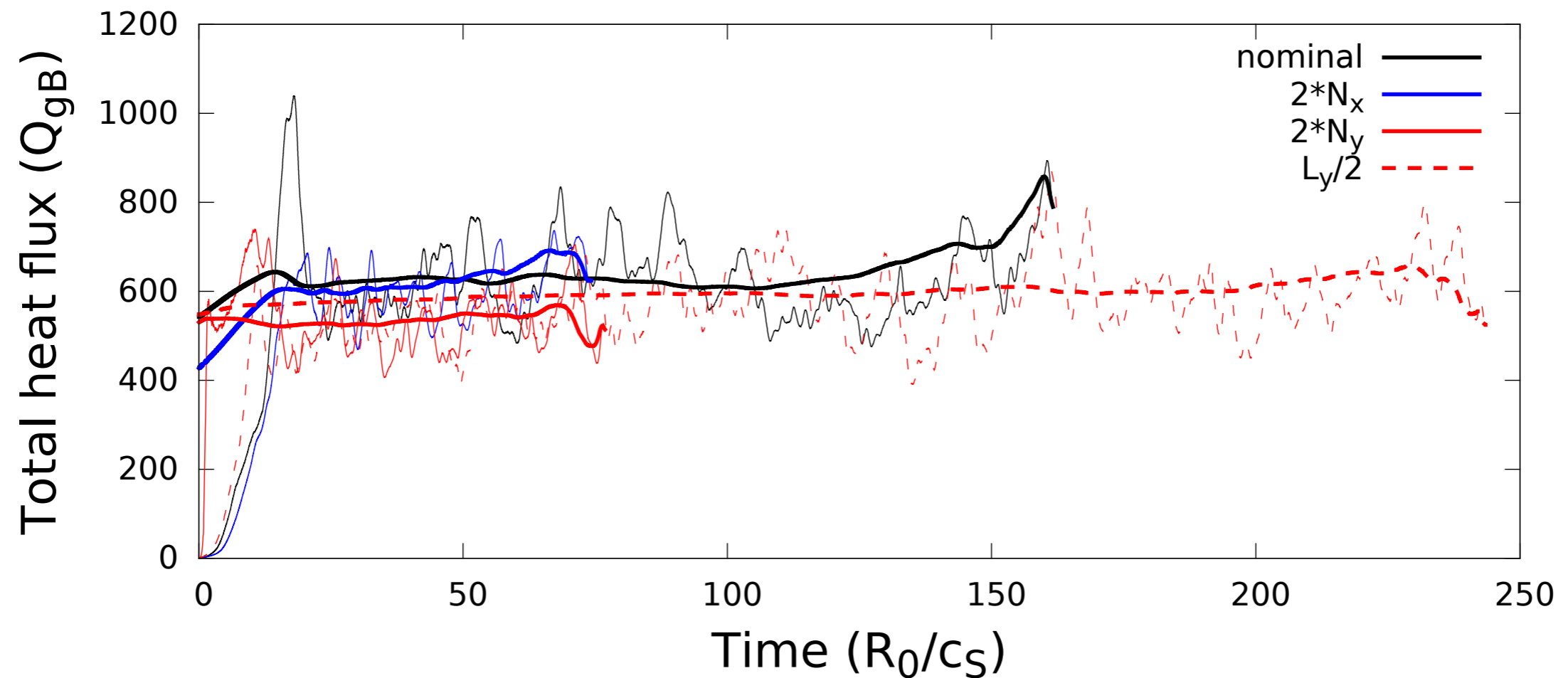
Staebler et al. *Nucl. Fusion* **57** (2017).

- A common rule of thumb, comparing  $\gamma/k_y \Big|_{ITG} \approx 2.2$  with  $\gamma/k_y \Big|_{ETG} \approx 1.0$ , suggests that multi-scale interactions are fairly weak

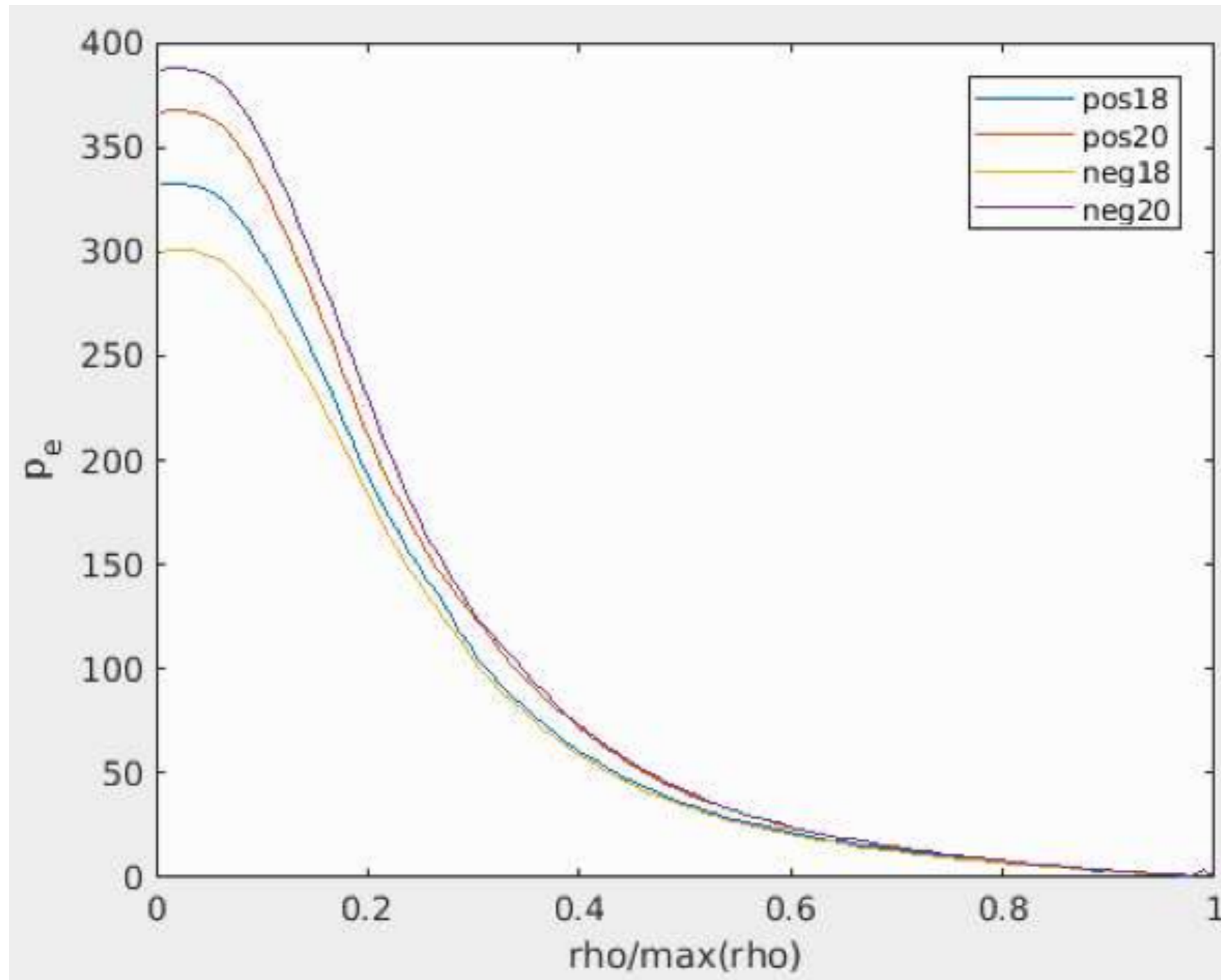


# Last year: resolution study with kinetic electrons

- Resolution study of the **neg20** case for the most concerning parameters seems satisfactory

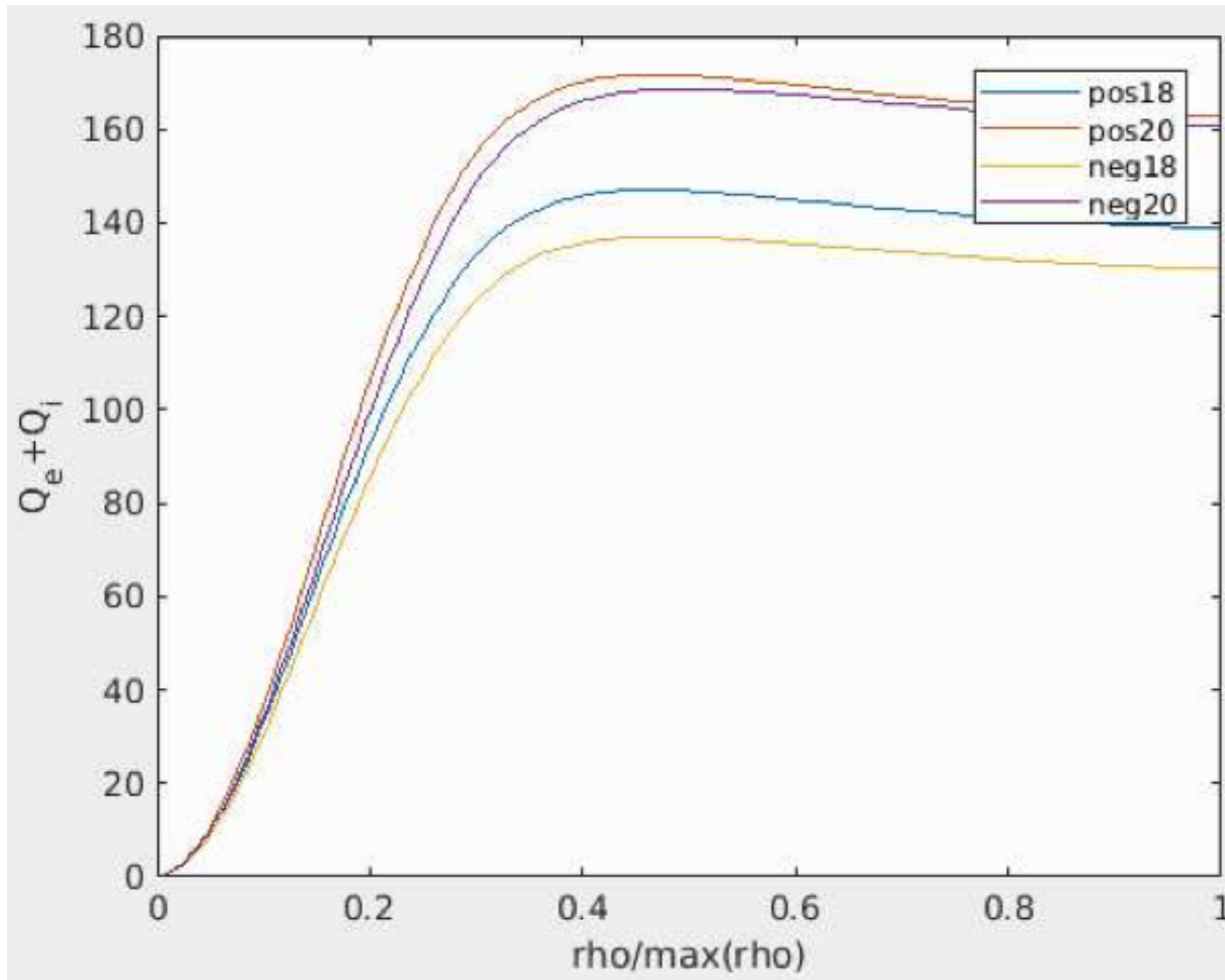


# Electron pressure profile from TGLF

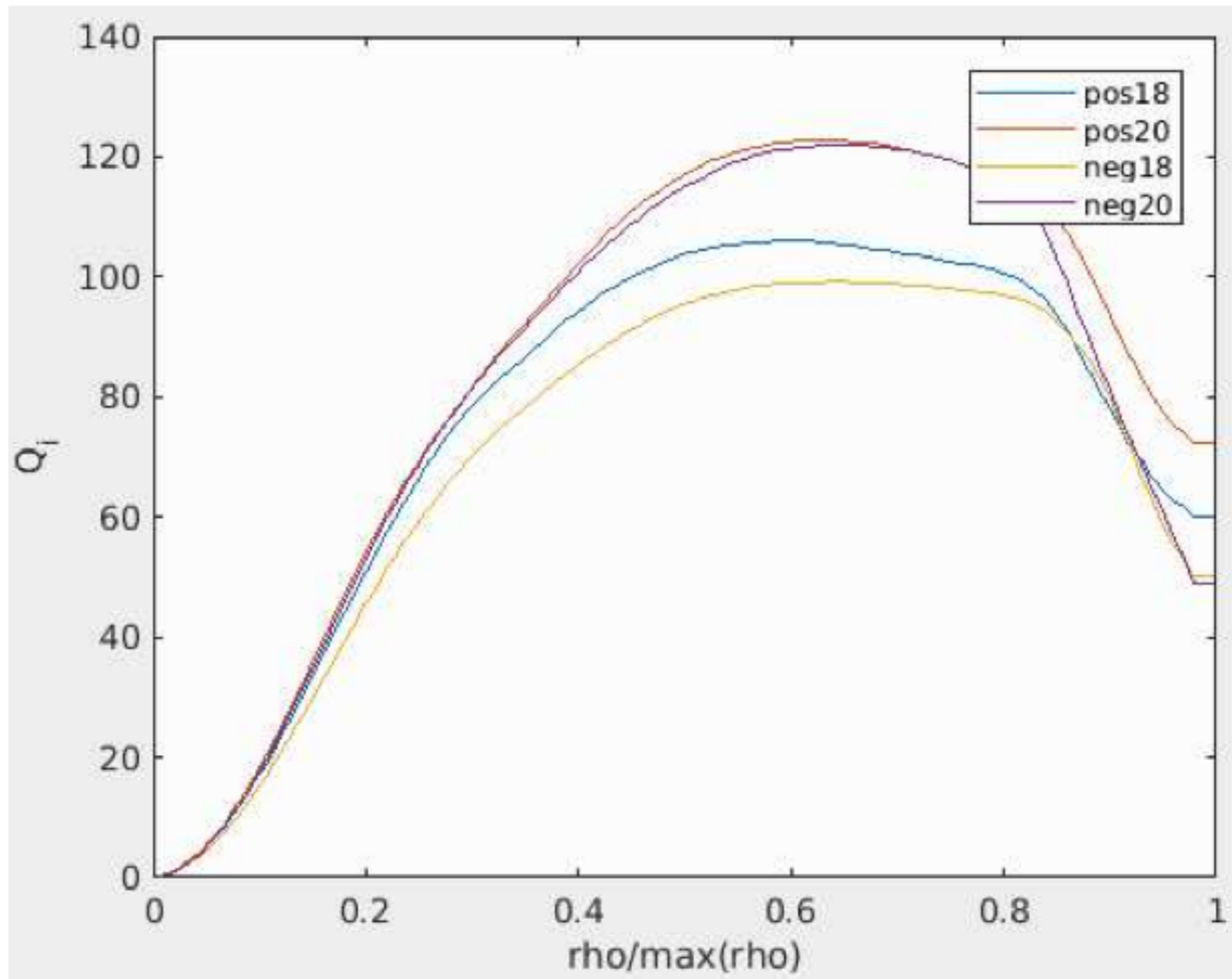




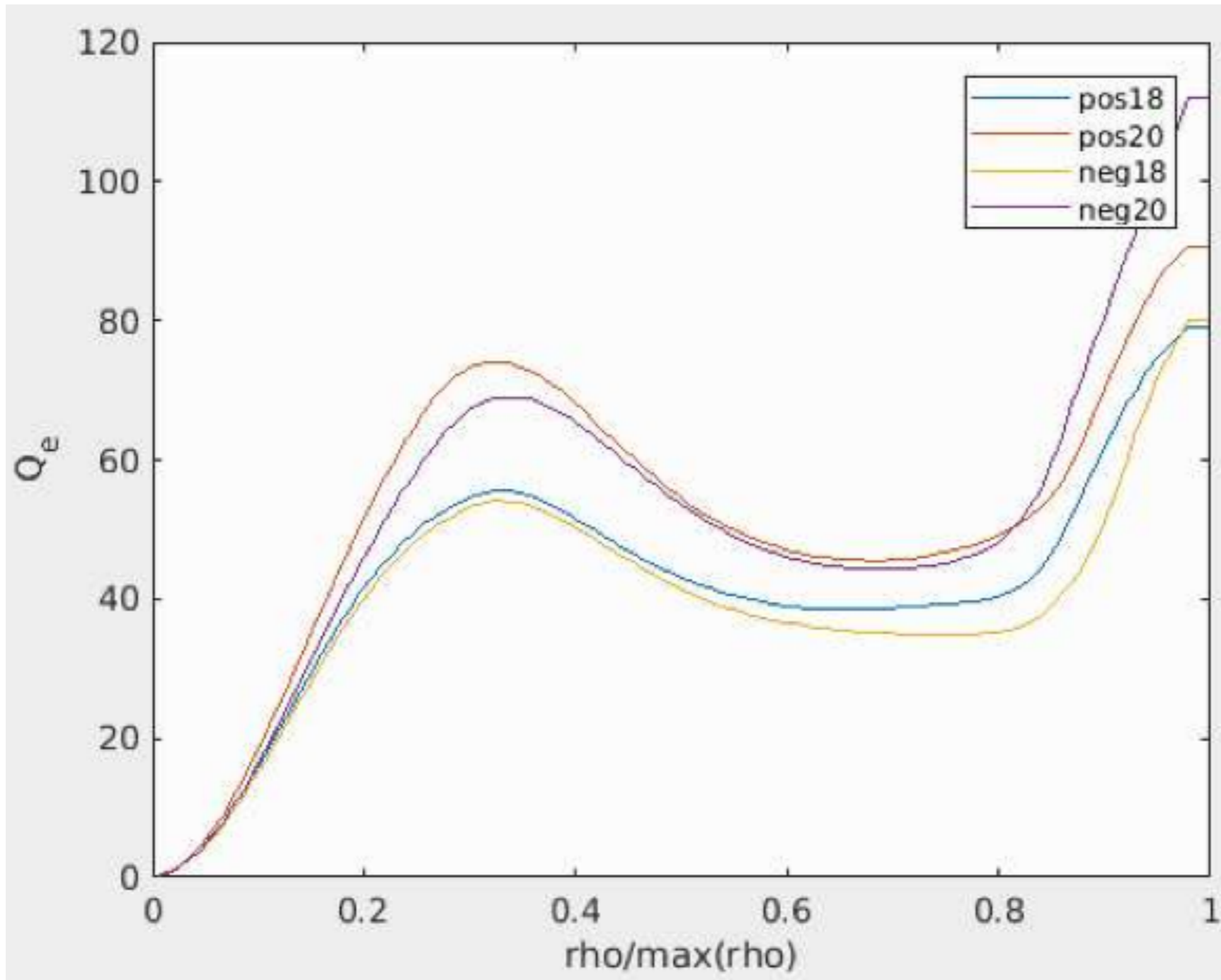
# Total heat flux from TGLF in MW



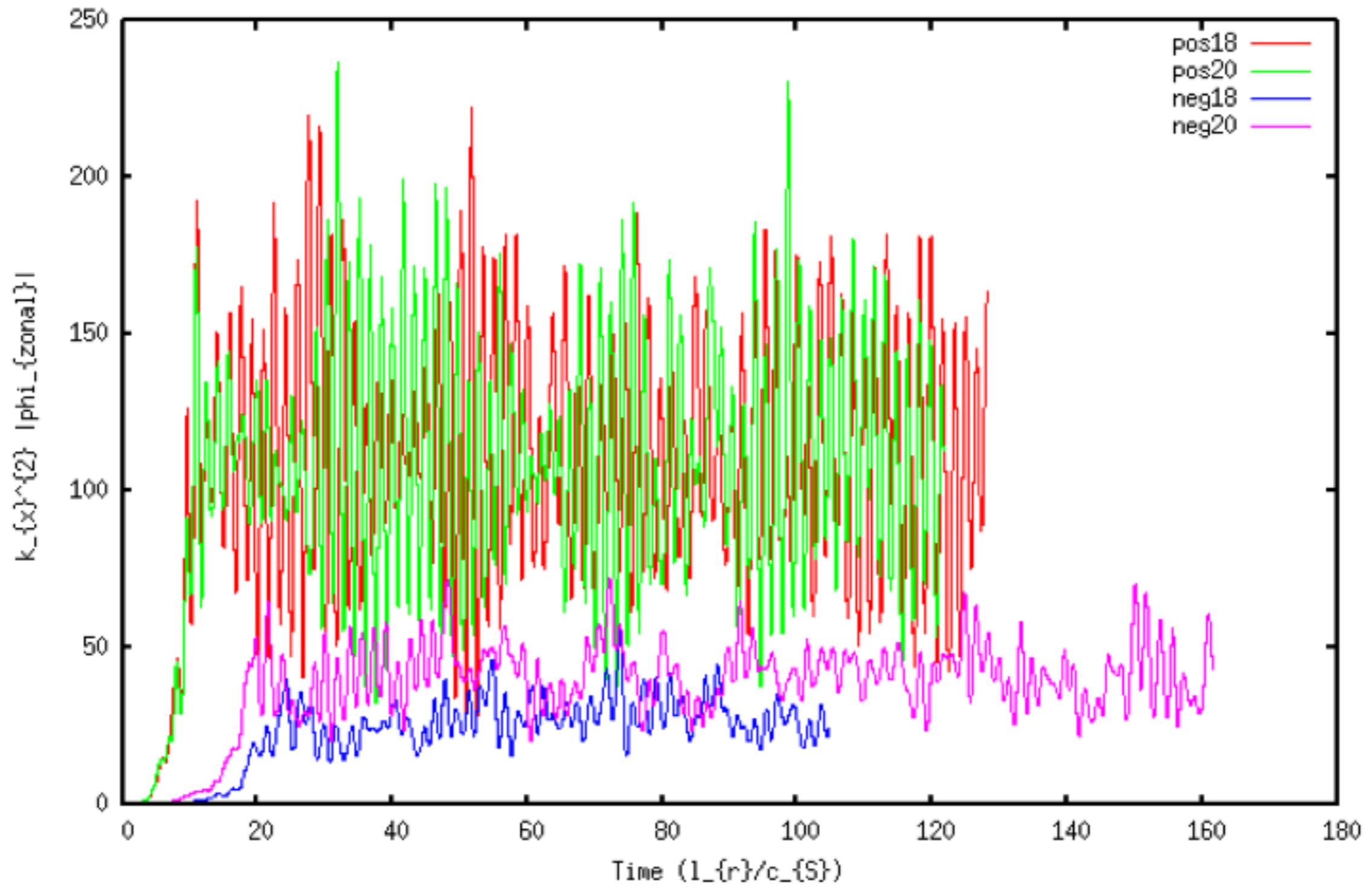
# Ion heat flux from TGLF in MW



# Electron heat flux from TGLF in MW



# Zonal oscillations from nonlinear kinetic simulations



# Input parameters for nonlinear kinetic simulations

```
! pos18
&geometry
magn_geometry = 'chease'
q0 = 1.7049163
shat = 2.3791041
geonfile = 'ogyropsi.h5'
x_def = 'arho_t'
flux_pos = 0.72000000
minor_r = 0.42802953
major_R = 1.0000000
dpdx_term= 'gradB_eq_curv'
dpdx_pm = 0.31365353E-01
norm_flux_projection = F
/

&species
name = 'ions'
omn = 3.7726245
omt = 10.384133

mass = 1.0000000
temp = 1.1012114
dens = 1.0000000
charge = 1
/

&species
name = 'electrons'
omn = 3.7726245
omt = 10.046073

mass = 0.21785000E-03
temp = 1.0000000
dens = 1.0000000
charge = -1

! pos20
&geometry
magn_geometry = 'chease'
q0 = 1.5550048
shat = 2.3914969
geonfile = 'ogyropsi.h5'
x_def = 'arho_t'
flux_pos = 0.72000000
minor_r = 0.42847416
major_R = 1.0000000
dpdx_term= 'gradB_eq_curv'
dpdx_pm = 0.33737323E-01
norm_flux_projection = F
/

&species
name = 'ions'
omn = 3.9569369
omt = 10.734664

mass = 1.0000000
temp = 1.1218137
dens = 1.0000000
charge = 1
/

&species
name = 'electrons'
omn = 3.9569369
omt = 10.514612

mass = 0.21785000E-03
temp = 1.0000000
dens = 1.0000000
charge = -1

! neg18
&geometry
magn_geometry = 'chease'
q0 = 1.5343302
shat = 2.2000282
geonfile = 'ogyropsi.h5'
x_def = 'arho_t'
flux_pos = 0.72000000
minor_r = 0.41714032
major_R = 1.0000000
dpdx_term= 'gradB_eq_curv'
dpdx_pm = 0.36014773E-01
norm_flux_projection = F
/

&species
name = 'ions'
omn = 2.7080109
omt = 8.5717145

mass = 1.0000000
temp = 1.1058137
dens = 1.0000000
charge = 1
/

&species
name = 'electrons'
omn = 2.7080109
omt = 9.9598991

mass = 0.21785000E-03
temp = 1.0000000
dens = 1.0000000
charge = -1

! neg20
&geometry
magn_geometry = 'chease'
q0 = 1.3988000
shat = 2.2103327
geonfile = 'ogyropsi.h5'
x_def = 'arho_t'
flux_pos = 0.72000000
minor_r = 0.41760834
major_R = 1.0000000
dpdx_term= 'gradB_eq_curv'
dpdx_pm = 0.39377451E-01
norm_flux_projection = F
/

&species
name = 'ions'
omn = 2.9316145
omt = 9.9035116

mass = 1.0000000
temp = 1.1116355
dens = 1.0000000
charge = 1
/

&species
name = 'electrons'
omn = 2.9316145
omt = 9.9796884

mass = 0.21785000E-03
temp = 1.0000000
dens = 1.0000000
charge = -1
```

omt/omn = 2.75

omt/omn = 2.71

omt/omn = 3.16

omt/omn = 3.38

# Input parameters for nonlinear adiabatic sims.

```
pos18
&geometry
magn_geometry = 'chease'
q0 = 1.7049163
shat = 2.3791041
geon_dir = '.'
geomfile = 'ogyropsi.h5'
x_def = 'arho_t'
flux_pos = 0.72000000
minor_r = 0.42802953
major_R = 1.0000000
dpdx_term= 'gradB_eq_curv'
dpdx_pm = 0.31365353E-01
norm_flux_projection = F
/

&species
name = 'ions'
omn = 5.5182257
omt = 14.977186

mass = 1.0000000
temp = 1.0000000
dens = 1.0000000
charge = 1
```

omt/omn = 2.71

```
pos20
&geometry
magn_geometry = 'chease'
q0 = 1.5550048
shat = 2.3914969
geon_dir = '.'
geomfile = 'ogyropsi.h5'
x_def = 'arho_t'
flux_pos = 0.72000000
minor_r = 0.42847416
major_R = 1.0000000
dpdx_term= 'gradB_eq_curv'
dpdx_pm = 0.33737323E-01
norm_flux_projection = F
/

&species
name = 'ions'
omn = 5.0452291
omt = 13.214426

mass = 1.0000000
temp = 1.0000000
dens = 1.0000000
charge = 1
```

omt/omn = 2.62

```
neg18
&geometry
magn_geometry = 'chease'
q0 = 1.5343302
shat = 2.2000282
geon_dir = '.'
geomfile = 'ogyropsi.h5'
x_def = 'arho_t'
flux_pos = 0.72000000
minor_r = 0.41714032
major_R = 1.0000000
dpdx_term= 'gradB_eq_curv'
dpdx_pm = 0.36014773E-01
norm_flux_projection = F
/

&species
name = 'ions'
omn = 3.4580024
omt = 11.342345

mass = 1.0000000
temp = 1.0000000
dens = 1.0000000
charge = 1
```

omt/omn = 3.28

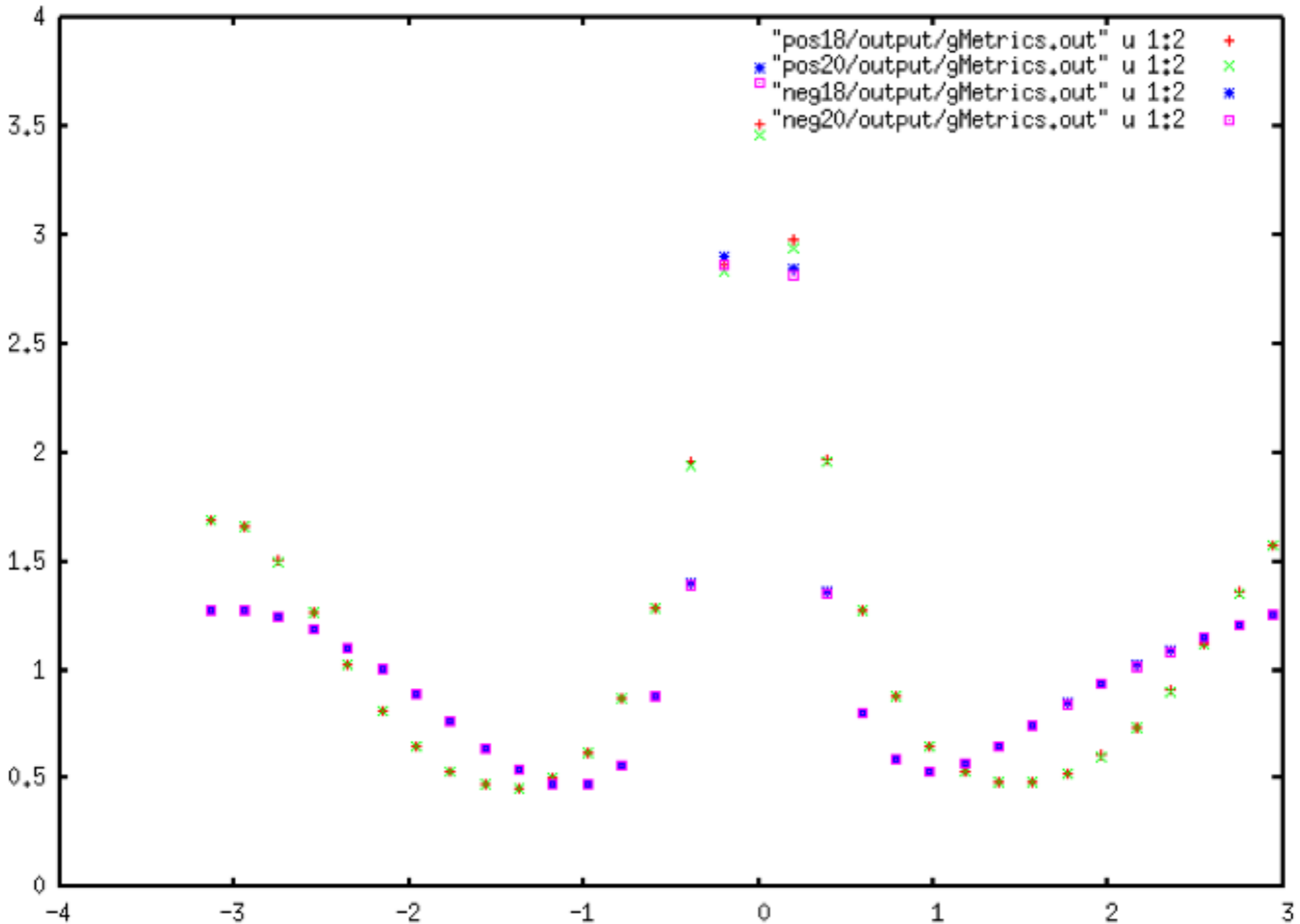
```
neg20
&geometry
magn_geometry = 'chease'
q0 = 1.3988000
shat = 2.2103327
geon_dir = '.'
geomfile = 'ogyropsi.h5'
x_def = 'arho_t'
flux_pos = 0.72000000
minor_r = 0.41760834
major_R = 1.0000000
dpdx_term= 'gradB_eq_curv'
dpdx_pm = 0.39377451E-01
norm_flux_projection = F
/

&species
name = 'ions'
omn = 3.7474076
omt = 13.374003

mass = 1.0000000
temp = 1.0000000
dens = 1.0000000
charge = 1
```

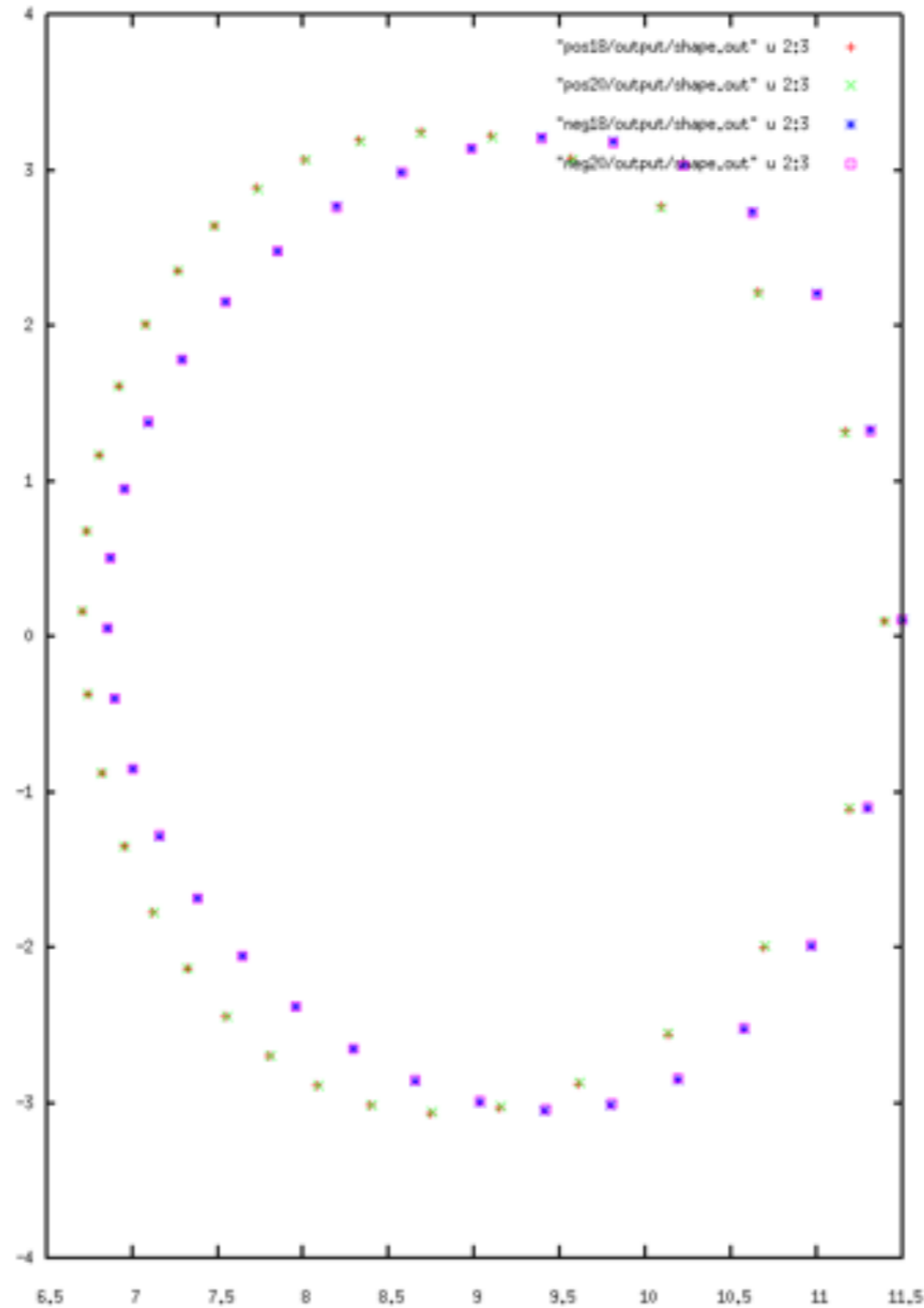
omt/omn = 3.57

$\left| \vec{\nabla} \rho \right|^2$  as a function of poloidal angle



# Flux surface shape in the poloidal plane

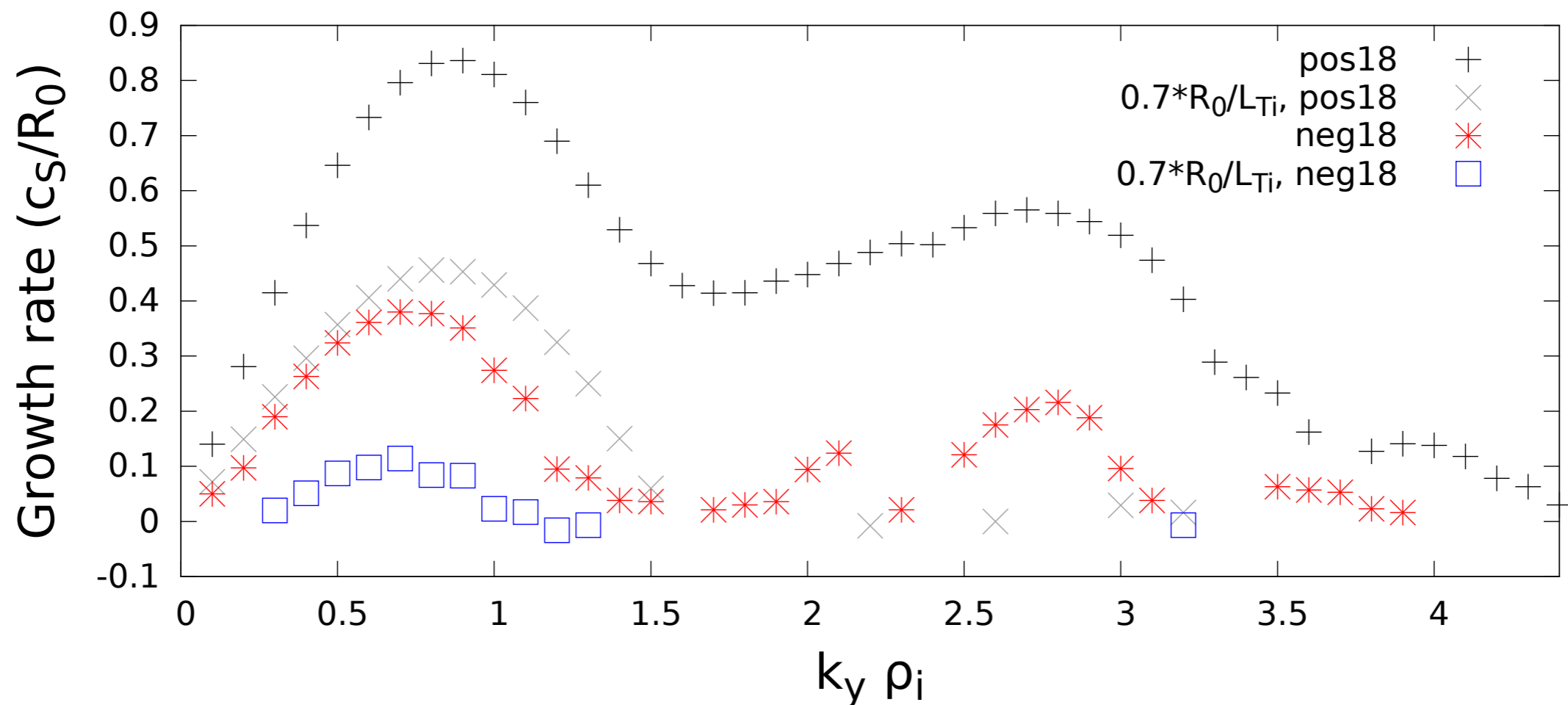
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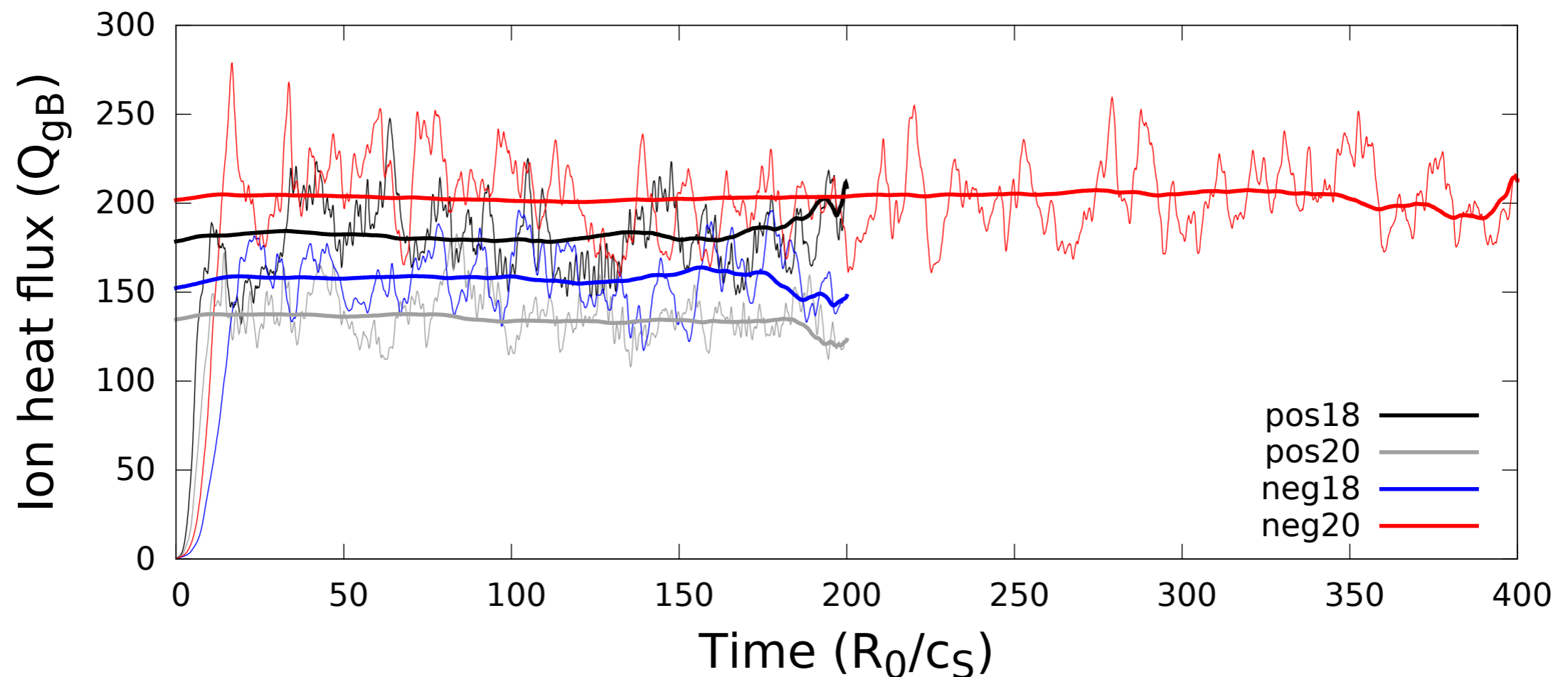
# Linear results with adiabatic electrons

- Found a fairly broad spectrum of unstable modes
- Critical gradient for negative  $\delta$  is maybe a bit larger



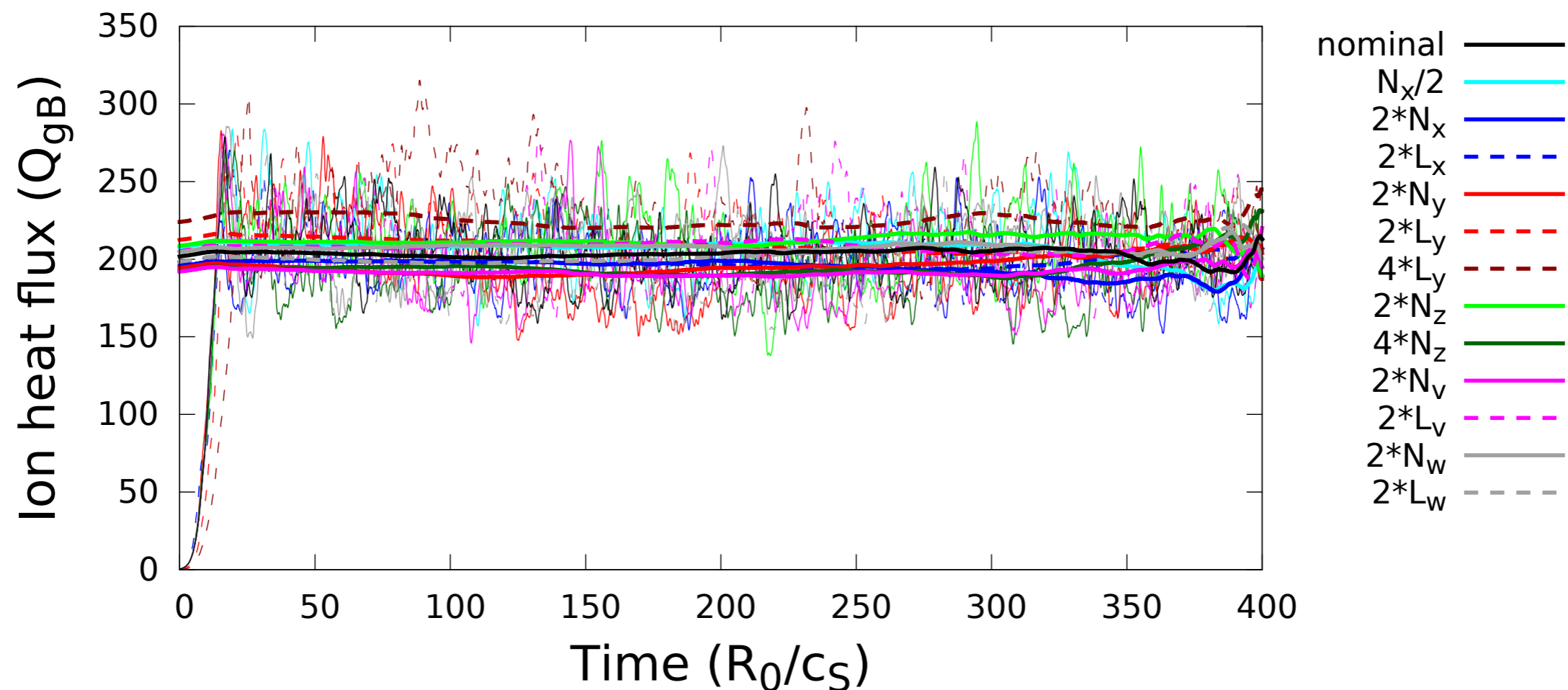
# Nonlinear results with adiabatic electrons

- Results are mixed, but indicates that negative  $\delta$  **increases** energy transport
- Main purpose is to find most strongly driven case for resolution study



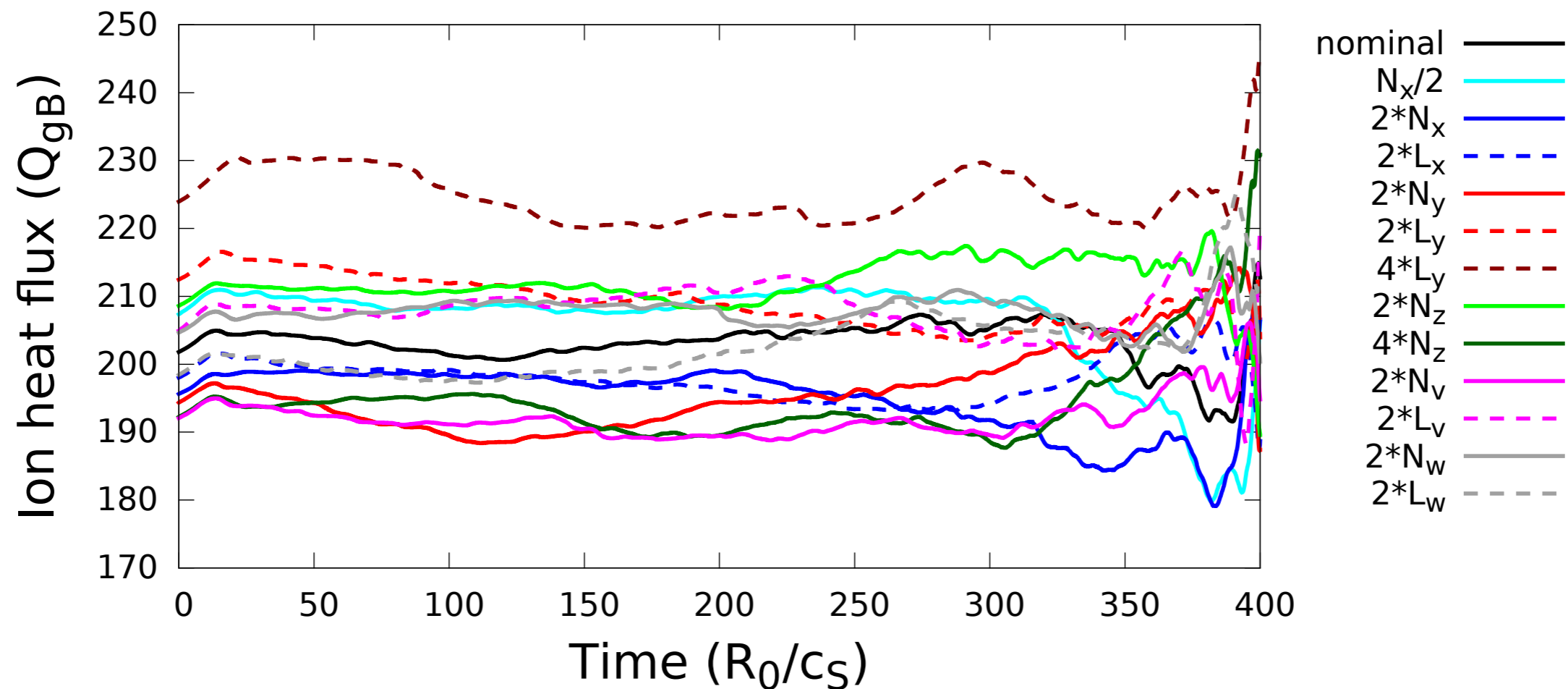
# Nonlinear resolution study with adiabatic electrons

- Resolution study of the **neg20** case indicates that  $L_y$  should be doubled and  $N_x$  can be halved



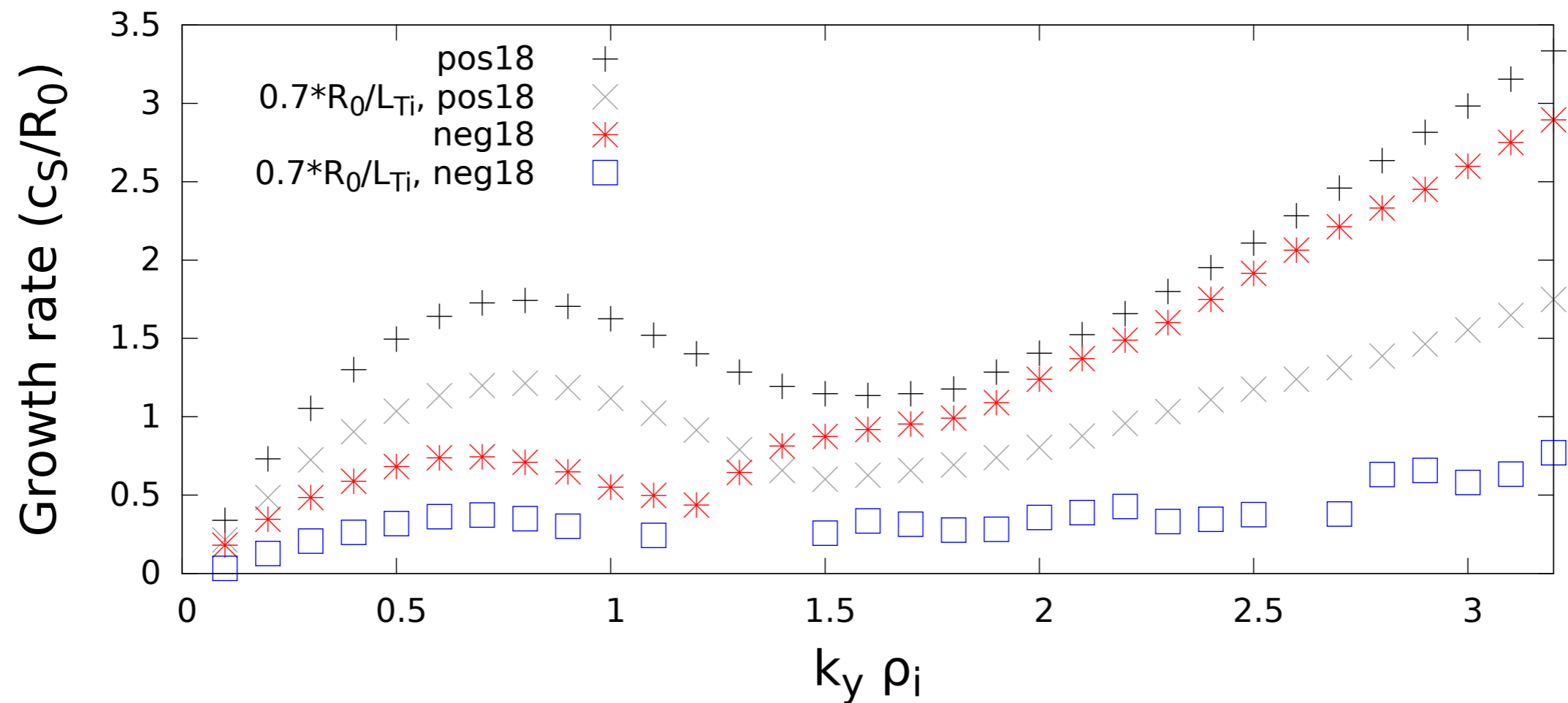
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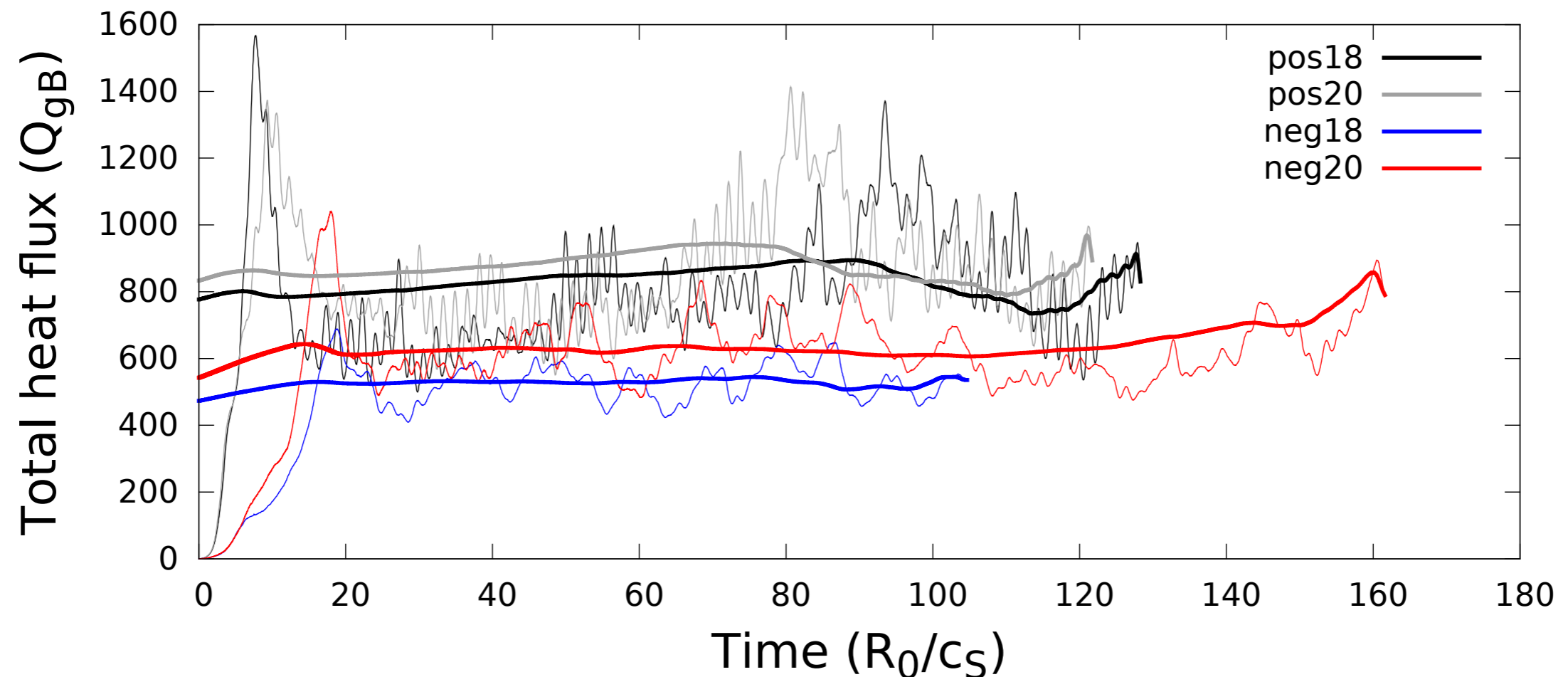
# Linear results with kinetic electrons

- See surprising divergence with small scale turbulence (concerning!)
- Again, critical gradient for negative  $\delta$  is maybe a bit larger



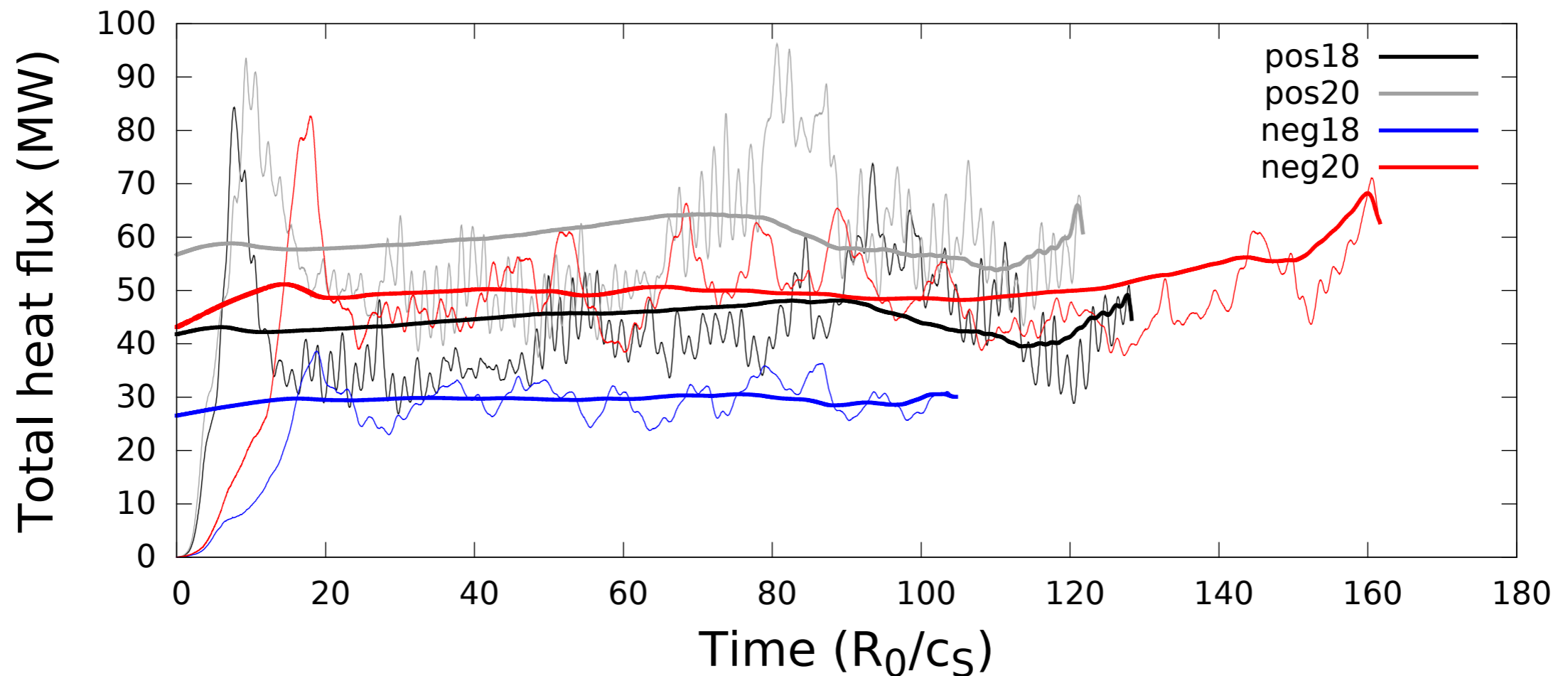
# Nonlinear results with kinetic electrons

- Negative  $\delta$  cases have lower total heat flux
- Positive  $\delta$  cases exhibit an unusual oscillation from the zonal flows



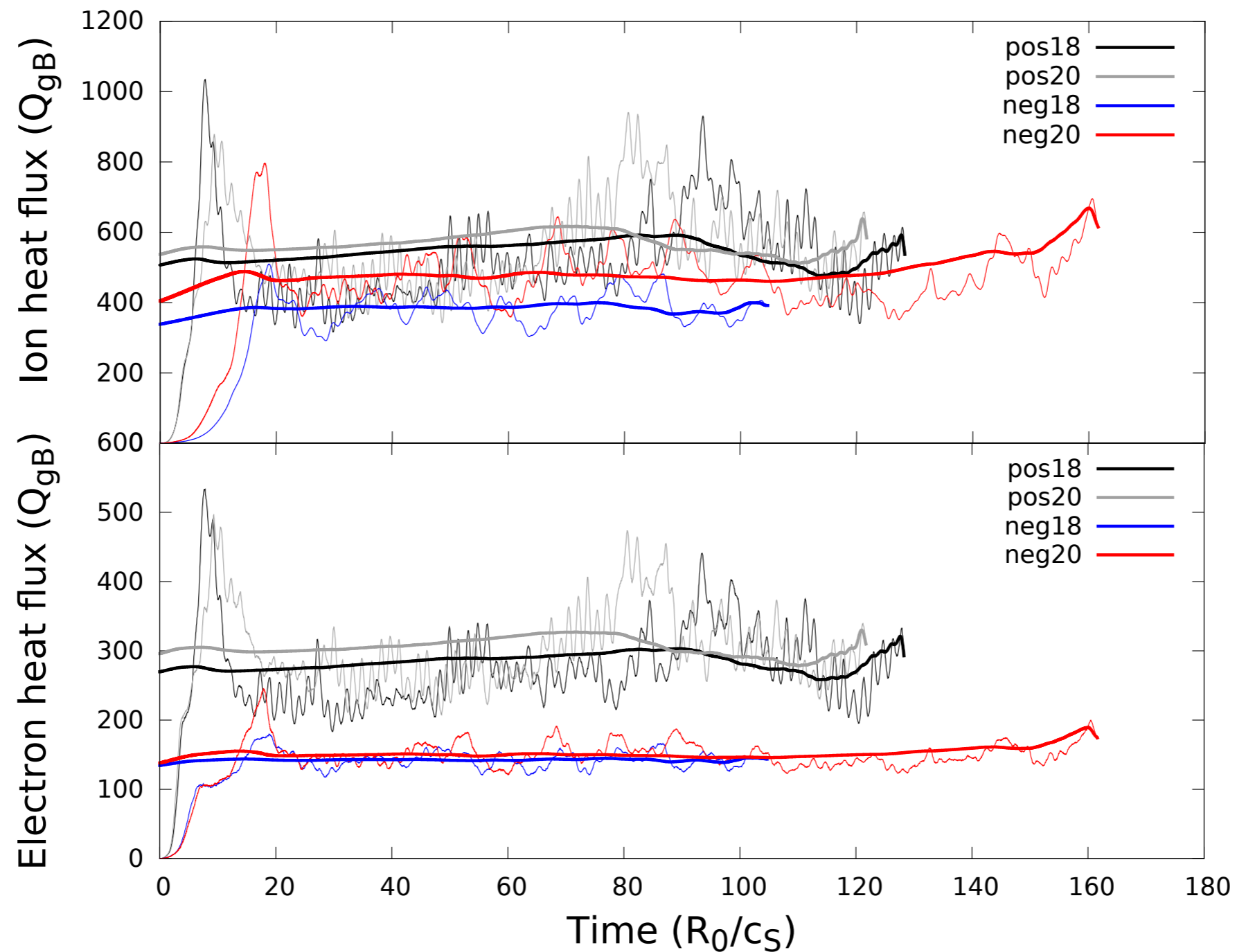
# Nonlinear results with kinetic electrons

- Same trends hold true for required heating power (i.e. adjusting for differences in surface area, temperature, and density)



# Nonlinear results with kinetic electrons

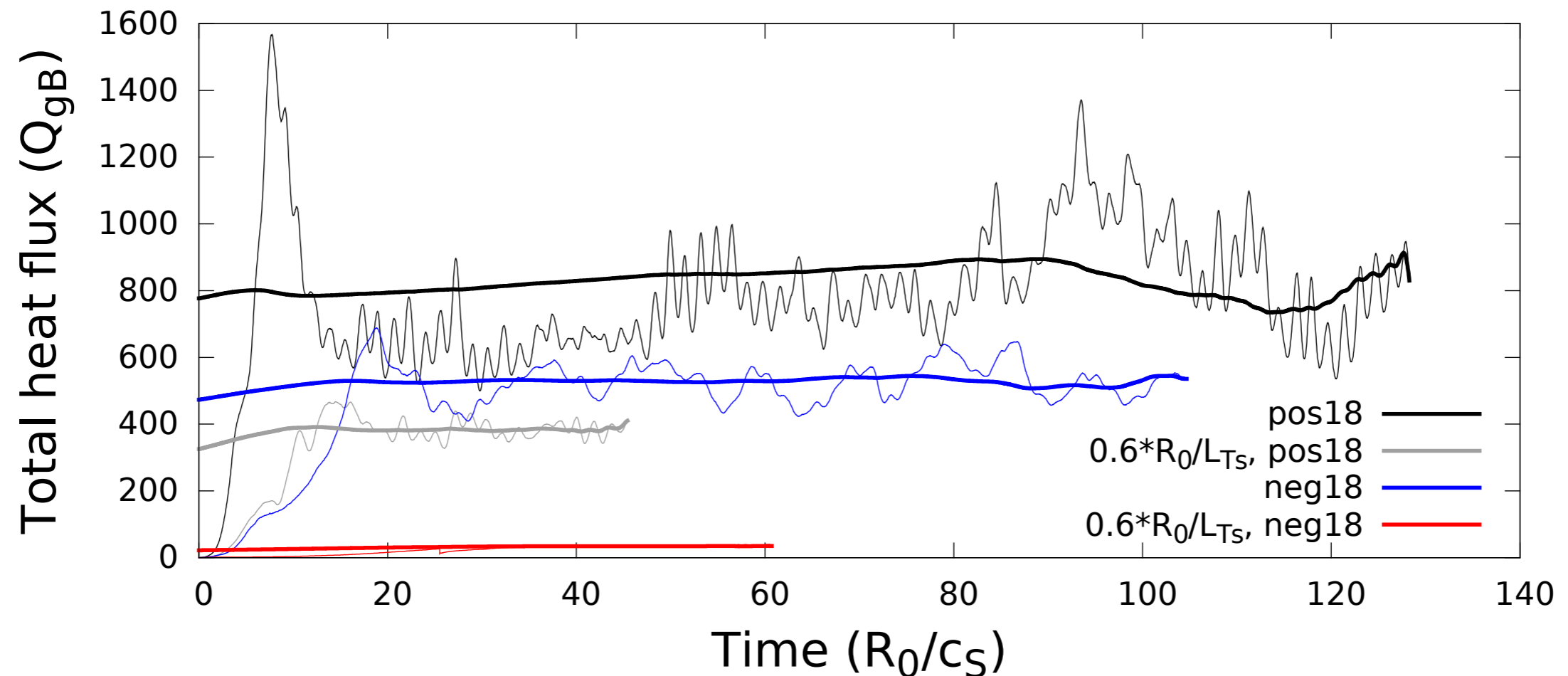
- Electron heat flux is more strongly affected by reversing  $\delta$





# Nonlinear stiffness study with kinetic electrons

- Negative  $\delta$  has a higher critical gradient



# Nonlinear stiffness study with kinetic electrons

- Negative  $\delta$  has a higher critical gradient

